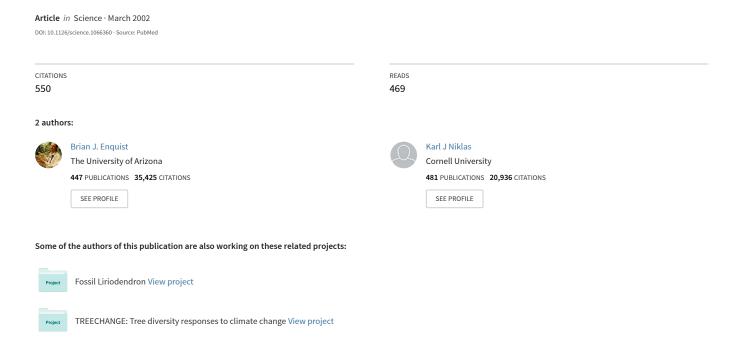
### Global Allocation Rules for Patterns of Biomass Partitioning in Seed Plants



## Global Allocation Rules for Patterns of Biomass Partitioning in Seed Plants

Brian J. Enquist<sup>1,2\*</sup> and Karl J. Niklas<sup>3</sup>

A general allometric model has been derived to predict intraspecific and interspecific scaling relationships among seed plant leaf, stem, and root biomass. Analysis of a large compendium of standing organ biomass sampled across a broad sampling of taxa inhabiting diverse ecological habitats supports the relations predicted by the model and defines the boundary conditions for above- and below-ground biomass partitioning. These canonical biomass relations are insensitive to phyletic affiliation (conifers versus angiosperms) and variation in averaged local environmental conditions. The model thus identifies and defines the limits that have guided the diversification of seed plant biomass allocation strategies.

Despite its importance to ecology, global climate research, and evolutionary and ecological theory, the general principles underlying how plant metabolic production is allocated to above- and below-ground biomass remain unclear (1-6). Indeed, there are few large data sets with which to evaluate patterns of standing biomass within and across the broad spectrum of vascular plant species (2, 7). The resulting uncertainty severely limits the accuracy of models for many ecologically and evolutionarily important phenomena across taxonomically diverse communities (8-11). Thus, although quantitative assessments of biomass allocation patterns are central to biology, theoretical or empirical assessments of these patterns remain contentious (2, 8, 10, 11).

Nonetheless, the scaling relations among standing leaf, stem, and root (below-ground) biomass  $(M_{\rm I}, M_{\rm S}, \text{ and } M_{\rm R}, \text{ respectively})$  can be derived analytically by first noting that the amount of resource used per individual plant,  $\dot{R}_0$ , approximates metabolic demand and gross photosynthesis (B) (12-14). Because B is predicted to scale proportionally to total  $M_{\rm L}$  ( $\dot{R}_{\rm O} \propto$  $B \propto M_{\rm I}$ ), theory predicts that the surface areas over which resources are exchanged with the environment (e.g., leaf surface area, which correlates with  $M_{\rm I}$ ) are proportional to the 3/4 power of the total plant biomass  $(M_T)$  (12–14). Thus,  $B \propto M_{\rm L} \propto \dot{M}_{\rm T}^{3/4}$  and  $M_{\rm L} \propto \dot{D}_{\rm S}^2$ , where  $D_{\perp}$  is stem diameter. Empirical studies confirm that plant metabolic rate scales as the 3/4 power of  $M_{\rm T}$  (which equals the sum of  $M_{\rm L}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$ ) and that metabolic rates scale isometrically with respect to  $M_{\rm L}$  (7, 12, 13, 15). Here, we extend this theory (16) on the basis of three assumptions: (i) Stem and root bulk tissue densities are approximately constant during ontogeny (13), (ii) the effective hydraulic cross-sectional areas of stems and roots are equivalent (owing to the conservation of water mass flowing through a plant) (17, 18), and (iii) stem length scales roughly isometrically with respect to root length  $(L_{\rm R})$ . If valid, these three basic assumptions corroborate the predictions that standing  $M_{\rm L}$  will scale as the 3/4 power of  $M_{\rm S}$ and as the 3/4 power of  $M_{\rm R}$  and that standing  $M_{\rm S}$  and  $M_{\rm R}$  will scale isometrically with respect to each other (  $M_{\rm L} \propto M_{\rm S}^{-3/4} \propto M_{\rm R}^{-3/4}$  and  $M_{\rm S} \propto$  $M_{\rm p}$ ). It also follows that above-ground biomass  $(M_{\wedge})$  will scale in a nearly isometric manner with respect to  $M_{\rm R}$  (i.e.,  $M_{\rm L}+M_{\rm S} \varpropto M_{\rm R})$  across and within clades and different habitats.

These predictions were tested against data

gathered from a variety of sources for standing  $M_{\rm I}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$  per plant across monocot, dicot, and conifer species differing by ~nine orders of magnitude in total body mass (19–21) [see supplemental data (22)]. Regression analyses (21) of these data show that all observed scaling exponents  $(\alpha_{RMA})$  comply remarkably well with those predicted by the model (Table 1). For example,  $M_{\rm L}$  scales across species as the 1.99 power [95% confidence interval (CI) =  $1.90 \le \alpha_{\rm RMA} \le 2.07$ ] of  $D_{\rm S}$  (Fig. 1) and does not differ significantly between angiosperm and conifer species (Table 1). Likewise, comparisons between angiosperm and conifer species reveal no statistically significant variation in the scaling exponents for standing  $M_{\rm I}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$ , whereas the relation between  $M_{\rm A}$  and  $M_{\rm R}$  is nearly isometric for mature individuals, as predicted (i.e.,  $M_A = 3.88 M_R^{1.02}$ ) (Fig. 2). Within the larger size ranges, statistical outliers are remarkably absent from all bivariant plots even when data from arborescent palm species, which lack a branched growth habit, are included (Figs. 1 and 2). However, our theory predicts a nonlinear log-log relation between  $M_{\rm A}$  and  $M_{\rm R}$ for plants less than 1 year old (16). This is not evident in our data for juvenile plants (i.e., less than 1 year old), which are best approximated by a linear log-log curve (Fig. 2). We attribute the departure of these data from theoretical expectations to the influence of nutrients provided by endosperm or megagametophyte tissues on the biomass partitioning pattern attending seedling establishment. Such a "maternal resource compartment" is expected to favor  $M_{\rm R}$  as opposed to  $M_{\rm A}$  (specifically leaf) accumulation.

The effect of plant size on the numerical values of scaling exponents was insignificant above the threshold of 1-year-old plants. When the data in the large size ranges were sorted into

**Table 1.** Statistical comparisons among standing  $M_{\rm L}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$  relations across seed plants and within angiosperm and conifer data sets. Scaling exponents and allometric constants are for reduced major axis regression ( $\alpha_{\rm RMA} \pm {\rm SE}$  and  $\beta_{\rm RMA} \pm {\rm SE}$ ) of  $\log_{10}$ -transformed data (original units in kg of dry weight per plant). In all cases, P < 0.0001.

$lpha_{RMA}$ ± SE				$eta_{\sf RMA} \pm {\sf SE}$			
Y <sub>1</sub> versus Y <sub>2</sub>	Predicted	Observed	95% CI	Observed	r²	n	F
Across all data sets							
$M_{\rm L}$ versus $M_{\rm S}$ $M_{\rm L}$ versus $M_{\rm R}$ $M_{\rm S}$ versus $M_{\rm R}$	0.75 0.75 1.00	$0.75 \pm 0.008$ $0.79 \pm 0.016$ $1.09 \pm 0.009$	0.73-0.76 0.76-0.82 1.05-1.13	$\begin{array}{c} 0.12 \pm 0.012 \\ 0.41 \pm 0.016 \\ 2.59 \pm 0.012 \end{array}$	0.910 0.861 0.971	661 338 366	8,425 2,439 13,621
Angiosperm interspecific data sets							
$M_{\rm L}$ versus $M_{\rm S}$ $M_{\rm L}$ versus $M_{\rm R}$ $M_{\rm S}$ versus $M_{\rm R}$	0.75 0.75 1.00	$0.73 \pm 0.008$ $0.76 \pm 0.015$ $1.10 \pm 0.012$	0.71-0.74 0.74-0.79 1.08-1.12	$0.13 \pm 0.075$ $0.30 \pm 0.019$ $2.61 \pm 0.017$	0.924 0.920 0.977	622 217 221	7,537 2,466 9,129
Conifer interspecific data sets							
$M_{\rm L}$ versus $M_{\rm S}$ $M_{\rm L}$ versus $M_{\rm R}$ $M_{\rm S}$ versus $M_{\rm R}$	0.75 0.75 1.00	$\begin{array}{c} 0.78 \pm 0.015 \\ 0.86 \pm 0.029 \\ 1.10 \pm 0.019 \end{array}$	0.74-0.81 0.79-0.92 1.06-1.14	$\begin{array}{c} 0.34 \pm 0.074 \\ 0.76 \pm 0.035 \\ 2.73 \pm 0.022 \end{array}$	0.863 0.802 0.951	350 172 171	2,198 689 3,282
Mean exponent of intraspecific datasets							
$M_{\rm R}$ versus $M_{\rm A}$	~1.00	$0.98 \pm 0.11$	0.885-1.09	-	_	_	32

<sup>&</sup>lt;sup>1</sup>Department of Ecology and Evolutionary Biology, University of Arizona, Tucson, AZ 87519, USA. <sup>2</sup>Center for Applied Biodiversity Science, Conservation International, 1919 M Street N.W., Suite 600, Washington, DC 20036, USA. <sup>3</sup>Department of Plant Biology, Cornell University, Ithaca, NY 14853, USA.

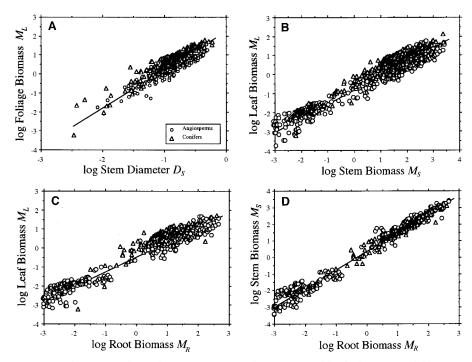
<sup>\*</sup>To whom correspondence should be addressed. E-mail: benguist@u.arizona.edu

different size ranges, separate regression analyses failed to detect statistically significant differences in the scaling exponents for  $M_{\rm L}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$  relations. For example, regression of  $M_{\rm L}$  versus  $+3 < \log_{10} M_{\rm R} < -0.5$  obtained a scaling exponent of 0.77  $\pm$  0.02 (95% CI = 0.74 to 0.81,  $r^2=0.783$ , n=337, F=1208, P<0.0001), whereas regression of  $M_{\rm L}$  versus  $-0.5 \leq \log_{10} M_{\rm R} < +3$  obtained a scaling exponent of 0.79  $\pm$  0.04 (95% CI = 0.68 to 0.89,  $r^2=0.539$ , n=183, F=211.3, P<0.0001). Slight deviations were observed for allocation exponents involving  $M_{\rm R}$  (Table 1). This is likely due to increased error in sampling the smallest roots from large trees.

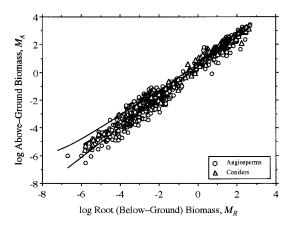
Compilations of intraspecific variation in  $M_{\rm A}$  and  $M_{\rm R}$  during ontogeny provide strong additional support for our theory. Across 61 species of woody tree and large shrub species, the average scaling exponent for  $M_{\rm L}$  versus basal stem diameter scales is 2.17 (95% CI = 2.01 to 2.32, mode = 2.06, n = 61). This numerical value is essentially indistinguishable from that predicted or observed within or across our data sets. Furthermore, as predicted, the average intraspecific exponent for the scaling of root and shoot biomass  $(M_A)$  during ontogeny across 32 independent studies including 26 species of herbaceous and woody plant species is  $0.98~(95\%~CI=1.09 \leq \alpha_{RMA} \leq 0.885).$  These exponents also agree with data reported for a limited number of studies treating individual species or individual community samples of comparable geographic scale (2), although it is evident from our theory that a maternal compartment can influence shoot-to-root ratios for especially small, juvenile plants.

The scaling exponents predicted by the model also appear to be insensitive to ecological factors known to influence local community composition, abundance, and average plant size. For example, whereas average  $M_{\rm T}$ per community is inversely proportional to the number of plants per ha,  $M_T \propto N^{-4/3}$  or N $\propto M_{\rm T}^{-3/4}$  in accordance with allometric theory (12), the scaling exponents for biomass allocation do not vary across diverse communities differing by over five orders of magnitude in average plant size (Fig. 3). Despite the residual variation in organ and  $M_{\rm T}$  attributable to plants grown under stressful conditions [e.g., drought, light deprivation, or elevated ultraviolet-B (UV-B levels)], statistical outliers are once again comparatively rare.

The ability to predict the absolute amounts of  $M_{\rm L}$ ,  $M_{\rm S}$ , or  $M_{\rm R}$  at the level of both the individual plant or an entire community is limited, because significant variation exists in the numerical values of allometric "constants" across species. For example, although both angiosperm and gymnosperm  $M_{\rm L}$  scales as the 3/4 power of  $M_{\rm S}$  (Table 1), the corresponding allometric constants ( $\beta_{\rm RMA}$  values = the y intercepts) significantly differ from each other (i.e., 0.13  $\pm$  0.075 and 0.34  $\pm$  0.074, respectively)



**Fig. 1.**  $D_{\rm S}$  and  $M_{\rm L}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$  relations for average plants from worldwide data sets. Solid lines are reduced major axis regression curves of log-transformed data. Angiosperm and conifer species are denoted by circles and triangles, respectively. (**A**)  $M_{\rm L}$  versus  $D_{\rm S}$  (trunk diameter at breast height). (**B**)  $M_{\rm L}$  versus  $M_{\rm S}$ . (**C**)  $M_{\rm L}$  versus  $M_{\rm R}$  ( $r^2=0.861$ , n=338, F=2439, P<0.0001). (**D**)  $M_{\rm S}$  versus  $M_{\rm R}$ . See Table 1 for additional statistics. Note, the relatively larger spread in (B) and (C) is due to differences between Angiosperms and Gymnosperms.

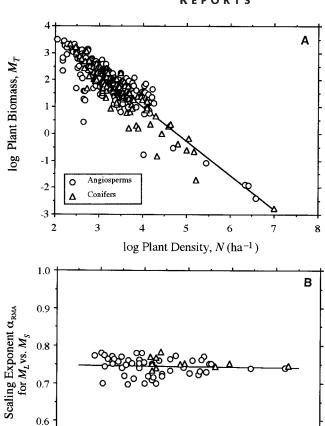


**Fig. 2.**  $M_{\rm A}$  versus  $M_{\rm R}$ . Angiosperm and conifer species are denoted by circles and triangles, respectively. Log-log nonlinear curve denotes predicted values of  $M_{\rm A}$  based on theory [i.e.,  $M_{\rm S}+M_{\rm L}=(\beta_{12}/\beta_{13})M_{\rm R}+(M_{\rm R}/\beta_{13})^{3/4}]$  (16), with empirical values of  $M_{\rm R}$  with  $\beta_{12}=8.33$  and  $\beta_{13}=2.44$ ; the log-log linear curve denotes the best statistical fit of actual data.

(Table 1). Thus, for equivalent  $M_{\rm S}$ , conifers have, on average, 2.6 times more  $M_{\rm L}$  than do angiosperms. This observation resonates with the fact that conifers typically retain three cohorts of leaves that have less well-developed aerenchymatous mesophyll as compared with angiosperm leaves. Yet, even though conifer wood tends to be less dense than angiosperm wood, angiosperms and gymnosperms do not differ in the allometric relation between total  $M_{\rm R}$  and  $M_{\rm A}$  nor with the scaling of plant density and  $M_{\rm A}$  (Figs. 2 and 3).

Plant biologists have long held the opinion that much idiosyncratic and site-specific variation exists in biomass allocation both within and across plant taxa, especially during ontogeny (23). Taxon and site-specific variation in biomass allocation is well known in response to differential selection for adaptations to different environmental conditions (e.g., species adapted to arid and hot conditions tend to have reduced  $M_{\rm L}$  with respect to  $M_{\rm S}$  or  $M_{\rm R}$ ) (23, 24). Nevertheless, when viewed across a large range of plant sizes, the about 10-fold variation in biomass allocation shown in Figs. 1 through 3 is slight as compared with the striking invariance observed (and predicted) for the scaling exponents of  $M_L$ ,  $M_S$ , and  $M_R$  across an impressive  $\sim$ nine orders of magnitude of  $M_{\rm T}$  across diverse communities differing in latitude and elevation. Traditionally, this variation has been indexed by ratios (e.g., stem:leaf, root:shoot, etc.). How-

Fig. 3. Effects of plant density (number of plants per ha, N) on individual plant  $M_{\tau}$  and the scaling exponent (slope of reduced major axis regression curve,  $\alpha_{\rm RMA}$ ) for the relation between individual plant  $M_{\rm L}$  and  $M_{\rm S.}$  Data were taken from Cannell data sets (19, 20). Angiosperm and conifer species are denoted by circles and triangles, respectively. (A)  $M_{\rm T}$  is inversely proportional to N,  $M_T \propto$ N - 1.33 (95% CI  $-1.41 \le \alpha_{RMA} \le -1.26;$  $r^2 = 0.787, n = 298, F =$ 1096, P < 0.0001). (B) Numerical value of scaling exponent for the relation between  $M_1$  and  $M_2$ (Fig. 1B) does not vary significantly as a function of N  $(r^2 = 0.0002, n =$ 64, F = 0.017, P =0.817).



ever, ratios fail to capture the actual functional relations characterizing biomass allocation among organ types. In contrast, our model and empirical findings quantitatively define the numerical limits on plant allocation strategies, which incidentally accord well with the observation that  $M_A$  and  $M_B$  are not significantly correlated with site age, absolute latitude, elevation, or number of species within the community. Furthermore, expressing allocation in terms of functional allometric relation provides a baseline by which to assess residual variation. For example, residual variation in biomass allocation between roots and shoots is significantly, although very weakly, correlated with plant height (P < 0.0001,  $r^2 =$ 0.058, n = 271) and local productivity (P = $0.007, r^2 = 0.04, n = 178$ ).

0.5

2

Our model provides strong bridges to more detailed biometric analyses of individual plants within and across communities (10, 25). Furthermore, in conjunction with the allometric relation predicted by a growing body of allometric theory (12–15, 26), a general allometric framework directly pertains to developing quantitative models for global climate as well as a variety of other important ecological and evolutionary phenomena including the approximate boundary conditions for difficult-to-mea-

sure  $M_{\rm R}$  (I–I0). Also, by identifying fundamental biomass partitioning rules, the model helps to identify the biophysical constraints acting on allocation tradeoffs in plant biology that potentially extend into the fossil record when seed plants first evolved. Allometric theory therefore holds great promise as a powerful quantitative tool with which to predict past and present-day plant structure-function relation at the level of the individual, community, or entire ecosystem (26).

log Plant Density,  $N(ha^{-1})$ 

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- 16. Noting that  $B = \beta_1$ ,  $M_T^{3/4} = \beta_1 (M_L + M_S + M_R)^{3/4}$ , and  $B = \beta_2 M_L$ , where  $\beta_1$  and  $\beta_2$  include units of years<sup>-1</sup>, we obtain  $M_L = \beta_3 (M_L + M_S + M_R)^{3/4}$ , where  $\beta_3 = \beta_1/\beta_2$ . Because, for any species,  $M_S =$  $\beta_4 \rho_S D_S^2 L_S$  and  $M_R = \beta_5 \rho_R D_R^2 L_R$ , where  $\rho$  is stem or root tissue bulk density, L is organ length, and  $D_R$  is root diameter, and because  $\beta_4 p_s$  and  $\beta_5 p_R$  are constant (i.e., denoted by  $\beta_6$  and  $\beta_7$ , respectively), we also see that  $M_L = \beta_3 (M_L + \beta_6 D_s^2 L_s + \beta_7 D_R^2 L_R)^{3/4}$ . This relation can be solved for  $M_L$  by imposing a minimum "cost" constraint so that that the total volume of water absorbed and transported by roots through stems per unit time is conserved such that  $D_n$ is proportional to  $D_s^2$  (17, 18, 27). Thus,  $M_1 \propto \beta_8 D_s^2$  and  $M_{\rm L} \propto \beta_9 D_{\rm R}^{\ 2}$ , where  $\beta_8$  and  $\beta_9$  are additional allometric constants reflecting the proportional allocation to root and shoot biomass. These scaling relations give  $M_L = \beta_3[1+(\beta_6/\beta_9)\ L_S+(\beta_7/\beta_9)L_R]^{3/4}(M_L)^{3/4}$  and thus  $M_L = \beta_3^{\ 4}[1+(\beta_6/\beta_9)L_S+(\beta_7/\beta_9)L_R]^3$ . Allometric theory predicts that many biological lengths (such as root and shoot length) scale as  $M^{1/4}(L_s \propto M^{1/4})$  and  $L_R$  and  $L_S$   $\propto M^{1/4}$ ) (12–15). Therefore, it is expected that  $L_R$  and  $L_S$ scale isometrically to each other (i.e.,  $L_R$ It therefore follows that  $M_L = \beta_3^4 [(1/L_s) + (\beta_6/L_s)]$  $(\beta_8) + (\beta_7 \beta_{10}/\beta_9)^{3} L_s^{3}$ . Furthermore, because  $1/L_s$ > 0 with increasing growth in size, we find that  $M_L \sim \beta_3^4 [(\beta_6/\beta_8) + (\beta_7\beta_{10}/\beta_9)]^3 L_S^3 = \beta_{11}L_S^3$  $M_L = \beta_3 \{(\beta_6/\beta_8) + (\beta_7\beta_7)^{1/3}\beta_7\} L_S^2 = \beta_{11}L_S^2$ . Therefore, our model predicts that  $M_S = ((\beta_6/\beta_8\beta_{11}^{-1/3}), M_L M_L^{-1/3} = \beta_{12}M_L^{4/3}, M_R = (\beta_7\beta_{10}/\beta_9\beta_{11}^{-1/3}), M_L M_L^{1/3} = \beta_{13}M_L^{4/3}, and M_S = (\beta_{12}/\beta_{13})M_R$ . The reciprocal of  $L_S$  appears in our derivations  $(1/L_s)$ . This term approaches zero with increasing plant size but will affect the values of scaling exponents with  $M_s$  for very small plants. Thus, deviations in the predicted values of exponents are expected for plants smaller than those measured in this study. It also follows that the total  $M_A$  is a complex allometry equaling the sum of both the shoot and leaf biomass,  $M_A = M_S +$  $M_{\rm L}=(\beta_{12}/\beta_{13})M_{\rm R}+(M_{\rm R}/\beta_{13})^{3/4}.$  Thus, once an individual plant becomes photosynthetically selfsufficient and exhausts its maternal compartment contributing to early seedling development (i.e., angiosperm endosperm or conifer megagametophyte nutrients),  $\dot{M}_{\rm A}$  is predicted to scale nearly isometrically with respect to M<sub>R</sub>
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between 1991 and 2001 (22). These data were from

plants grown under a variety of natural field and exper-

imental conditions (e.g., elevated UV-B or CO<sub>2</sub> levels and

drought). Only two criteria were used to select data:

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- Data (i) had to have small variance (as gauged by reported SE) and (ii) had to be reported in units of kg of dry weight per plant. A total of 385 species are represented in the complete data set (including arborescent monocots, dicots, and conifers). Data for the intraspecific scaling of plant organ biomass were collected by B.J.E. primarily from the agricultural and forestry literature (25. 27. 28).
- 21. M<sub>L</sub>, M<sub>S</sub>, and M<sub>R</sub> were each computed for an average plant from each community or experimental manipulation with the quotient of total plant biomass per site or treatment and plant density. Model type II (reduced major axis) regression analyses were then used to determine scaling exponents and allometric constants (regression slopes and y intercepts designated as α<sub>RMA</sub> and β<sub>RMA</sub>, respectively), because functional rather than predictive relation were sought among variables that were
- biologically interdependent and subject to unknown measurement error (7). Because many authors failed to report all of the necessary parameters required to assess  $M_{\rm L}$ ,  $M_{\rm S}$ , and  $M_{\rm R}$ , the sample size of regression analyses varies across statistical comparisons.
- Supplementary materials can be found on Science Online at www.sciencemag.org/cgi/content/full/295/ 5559/1517/DC1.
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# Enzyme Dynamics During Catalysis

Elan Zohar Eisenmesser, Daryl A. Bosco, Mikael Akke, Dorothee Kern \*

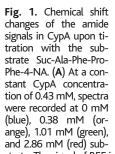
Internal protein dynamics are intimately connected to enzymatic catalysis. However, enzyme motions linked to substrate turnover remain largely unknown. We have studied dynamics of an enzyme during catalysis at atomic resolution using nuclear magnetic resonance relaxation methods. During catalytic action of the enzyme cyclophilin A, we detect conformational fluctuations of the active site that occur on a time scale of hundreds of microseconds. The rates of conformational dynamics of the enzyme strongly correlate with the microscopic rates of substrate turnover. The present results, together with available structural data, allow a prediction of the reaction trajectory.

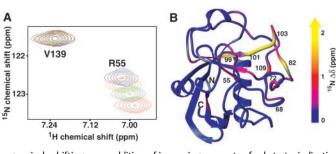
Although classical enzymology together with structural biology have provided profound insights into the chemical mechanisms of many enzymes (1), enzyme dynamics and their relation to catalytic function remain poorly characterized. Because many enzymatic reactions occur on time scales of micro- to milliseconds, it is anticipated that the conformational dynamics of the enzyme on these time scales might be linked to its catalytic action (2). Classically, enzyme reactions are studied by detecting substrate turnover. Here, we examine enzyme catalysis in a nonclassical way by characterizing motions in the enzyme during substrate turnover. Dynamics of enzymes during catalysis have previously been detected with methods such as fluorescent resonance energy transfer, atomic force microscopy, and stopped-flow fluorescence, which report on global motions of the enzyme or dynamics of particular molecular sites. In contrast, nuclear magnetic resonance (NMR) spectroscopy enables investigations of motions at many atomic sites simultaneously (3, 4). Previous NMR studies reporting on the time scales, amplitudes, and energetics of motions in proteins, have provided information on the relation between protein mobility and function (5–15). Here, we have used NMR relaxation experiments to advance these efforts by characterizing conformational exchange in an enzyme, human cyclophilin A (CypA), during catalysis

CypA is a member of the highly conserved family of cyclophilins that are found in high concentrations in many tissues. Cyclophilins are peptidyl-prolyl cis/trans isomerases that catalyze the interconversion between cis and trans conformations of X-Pro peptide bonds, where "X" denotes any amino acid. CypA operates in numerous biological

processes (16, 17). It is the receptor for the immunosuppressive drug cyclosporin A, is essential for HIV infectivity, and accelerates protein folding in vitro by catalyzing the rate-limiting cis/trans isomerization of prolyl peptide bonds (18, 19). However, its function in vivo and its molecular mechanism are still in dispute. X-ray structures of CypA in complex with different peptide ligands show cis X-Pro bonds (20, 21), except for a trans conformation in the CypA/HIV-1 capsid complex (22, 23). In each case, only one conformer was observed in the crystal, even though both isomers must bind to CypA for catalysis of cis/trans isomerization to occur.

We characterized motions in CypA during catalysis with the use of 15N spin relaxation experiments with and without the substrate Suc-Ala-Phe-Pro-Phe-4-NA (24). Longitudinal  $(R_1)$  and transverse  $(R_2)$  auto-relaxation rates, transverse cross-correlated cross-relaxation rates  $(\eta_{xy})$ , and  $\{{}^{1}H\}$ - ${}^{15}N$  nuclear Overhauser enhancements (NOE) were measured for all backbone amides in CypA (25). Though all parameters are sensitive to "fast" motions (pico- to nanoseconds), only  $R_2$  is sensitive to "slow" conformational exchange (micro- to milliseconds) (5-8). A progressive substrateinduced shift for several CypA amide resonances (Fig. 1) indicates catalysis-linked motions. It shows (i) that these amides experience different magnetic environments in free CypA (E) and in CypA bound to substrate (ES) and (ii) that the





strate. The signal of R55 is progressively shifting upon addition of increasing amounts of substrate, indicating fast conformational exchange during catalysis. The observed chemical shifts are population-weighted averages of E and ES, and thus shift towards the position of the ES complex with increasing amounts of substrate. In contrast, the signal of V139 is not affected by catalysis. (B) The chemical shift differences between free CypA and in the presence of 2.86 mM substrate were mapped onto the structure (1RMH) (21) with the use of a continuous color scale.

<sup>&</sup>lt;sup>1</sup>Department of Biochemistry, Brandeis University, Waltham, MA 02454, USA. <sup>2</sup>Department of Biophysical Chemistry, Lund University, Post Office Box 124, SE-221 00 Lund. Sweden.

<sup>\*</sup>To whom correspondence should be addressed. E-mail: dkern@brandeis.edu