

### Homework 3 – Solutions

Problems (not review questions) : 5.18, 5.19, 5.27, 5.38, 5.39, 5.44, 5.45

5.18 A particular MOSFET for which  $V_m = 0.5$  V and  $k'_n(W/L) = 1.6$  mA/V<sup>2</sup> is to be operated in the saturation region. If  $i_D$  is to be 50  $\mu$ A, find the required  $v_{GS}$  and the minimum required  $v_{DS}$ . Repeat for  $i_D = 200$   $\mu$ A.

$$\mathbf{5.18} \quad V_m = 0.5 \text{ V}, \quad k_n = 1.6 \text{ mA/V}^2$$

$$I_D = 0.05 = \frac{1}{2} \times 1.6 \times V_{OV}^2$$

$$\Rightarrow V_{OV} = 0.25 \text{ V and } V_{DS} \geq 0.25 \text{ V}$$

$$V_{GS} = 0.5 + 0.25 = 0.75 \text{ V}$$

$$I_D = 0.2 = \frac{1}{2} \times 1.6 \times V_{OV}^2$$

$$\Rightarrow V_{OV} = 0.5 \text{ V and } V_{DS} \geq 0.5 \text{ V}$$

$$V_{GS} = 0.5 + 0.5 = 1 \text{ V}$$

5.19 A particular  $n$ -channel MOSFET is measured to have a drain current of 0.4 mA at  $V_{GS} = V_{DS} = 1$  V and of 0.1 mA at  $V_{GS} = V_{DS} = 0.8$  V. What are the values of  $k_n$  and  $V_t$  for this device?

**5.19** For  $V_{GS} = V_{DS} = 1$  V, the MOSFET is operating in saturation,

$$I_D = \frac{1}{2} k_n (V_{GS} - V_t)^2$$

$$0.4 = \frac{1}{2} k_n (1 - V_t)^2 \quad (1)$$

$$0.1 = \frac{1}{2} k_n (0.8 - V_t)^2 \quad (2)$$

Dividing Eq. (1) by Eq. (2) and taking square roots gives

$$2 = \frac{1 - V_t}{0.8 - V_t}$$

$$\Rightarrow V_t = 0.6 \text{ V}$$

Substituting in Eq. (1), we have

$$0.4 = \frac{1}{2} k_n \times 0.4^2$$

$$\Rightarrow k_n = 5 \text{ mA/V}^2$$

\*5.27 The table above lists 10 different cases labeled (a) to (j) for operating an NMOS transistor with  $V_t = 1$  V. In each case the voltages at the source, gate, and drain (relative to the circuit ground) are specified. You are required to complete the table entries. Note that if you encounter a case for which  $v_{DS}$  is negative, you should exchange the drain and source before solving the problem. You can do this because the MOSFET is a symmetric device.

$$\mathbf{5.27} \quad V_{DS} = V_D - V_S \quad V_{GS} = V_G - V_S$$

$$V_{OV} = V_{GS} - V_t = V_{GS} - 1.0$$

According to Table 5.1, three regions are possible.

Case	$V_S$	$V_G$	$V_D$	$V_{GS}$	$V_{OV}$	$V_{DS}$	Region of operation
a	+1.0	+1.0	+2.0	0	-1.0	+1.0	Cutoff
b	+1.0	+2.5	+2.0	+1.5	+0.5	+1.0	Sat.
c	+1.0	+2.5	+1.5	+1.5	+0.5	+0.5	Sat.
d	+1.0	+1.5	0	+0.5	-0.5	-1.0	Sat.*
e	0	+2.5	1.0	+2.5	+1.5	+1.0	Triode
f	+1.0	+1.0	+1.0	0	-1.0	0	Cutoff
g	-1.0	0	0	+1.0	0	+1.0	Sat.
h	-1.5	0	0	+1.5	+0.5	+1.5	Sat.
i	-1.0	0	+1.0	+1.0	0	+2.0	Sat.
j	+0.5	+2.0	+0.5	+1.5	+0.5	0	Triode

\* With the source and drain interchanged.

5.38 A PMOS transistor has  $k'_p(W/L) = 100 \mu\text{A}/\text{V}^2$ ,  $V_t = -1.0 \text{ V}$ , and  $\lambda = -0.02 \text{ V}^{-1}$ . The gate is connected to ground and the source to  $+5 \text{ V}$ . Find the drain current for  $v_D = +4 \text{ V}$ ,  $+2 \text{ V}$ ,  $+1 \text{ V}$ ,  $0 \text{ V}$ , and  $-5 \text{ V}$ .

5.38

$$k_p = k'_p \left( \frac{W}{L} \right) = 100 \mu\text{A}/\text{V}^2$$

$$V_{tp} = -1 \text{ V} \quad \lambda = -0.02 \text{ V}^{-1}$$

$$V_G = 0, \quad V_S = +5 \text{ V} \Rightarrow V_{SG} = 5 \text{ V}$$

$$|V_{OV}| = V_{SG} - |V_{tp}| = 5 - 1 = 4$$

• For  $v_D = +4 \text{ V}$ ,  $v_{SD} = 1 \text{ V} < |V_{OV}| \Rightarrow$  triode-region operation,

$$\begin{aligned} i_D &= k_p \left[ v_{SD} |V_{OV}| - \frac{1}{2} v_{SD}^2 \right] \\ &= 100 \left( 1 \times 4 - \frac{1}{2} \times 1 \right) = 350 \mu\text{A} \end{aligned}$$

• For  $v_D = +2 \text{ V}$ ,  $v_{SD} = 3 \text{ V} < |V_{OV}| \Rightarrow$  triode-region operation,

$$\begin{aligned} i_D &= k_p \left[ v_{SD} |V_{OV}| - \frac{1}{2} v_{SD}^2 \right] \\ &= 100 \left( 3 \times 4 - \frac{1}{2} \times 9 \right) = 750 \mu\text{A} \end{aligned}$$

• For  $v_D = +1 \text{ V}$ ,  $v_{SD} = 4 \text{ V} = |V_{OV}| \Rightarrow$  saturation-mode operation,

$$\begin{aligned} i_D &= \frac{1}{2} k_p |V_{OV}|^2 (1 + |\lambda| v_{SD}) \\ &= \frac{1}{2} \times 100 \times 16 (1 + 0.02 \times 4) = 864 \mu\text{A} \end{aligned}$$

• For  $v_D = 0 \text{ V}$ ,  $v_{SD} = 5 \text{ V} > |V_{OV}| \Rightarrow$  saturation-mode operation,

$$i_D = \frac{1}{2} \times 100 \times 16 (1 + 0.02 \times 5) = 880 \mu\text{A}$$

• For  $v_D = -5 \text{ V}$ ,  $v_{SD} = 10 \text{ V} > |V_{OV}| \Rightarrow$  saturation-mode operation,

$$i_D = \frac{1}{2} \times 100 \times 16 (1 + 0.02 \times 10) = 960 \mu\text{A}$$

5.39 A  $p$ -channel transistor for which  $|V_t| = 0.8$  V and  $|V_A| = 40$  V operates in saturation with  $|v_{GS}| = 3$  V,  $|v_{DS}| = 4$  V, and  $i_D = 3$  mA. Find corresponding signed values for  $v_{GS}$ ,  $v_{SG}$ ,  $v_{DS}$ ,  $v_{SD}$ ,  $V_t$ ,  $V_A$ ,  $\lambda$ , and  $k'_p(W/L)$ .

$$\mathbf{5.39} \quad V_{tp} = 0.8 \text{ V}, \quad |V_A| = 40 \text{ V}$$

$$|v_{GS}| = 3 \text{ V}, \quad |v_{DS}| = 4 \text{ V}$$

$$i_D = 3 \text{ mA}$$

$$|V_{OV}| = |v_{GS}| - |V_{tp}| = 2.2 \text{ V}$$

$$|v_{DS}| > |V_{OV}| \Rightarrow \text{saturation mode}$$

$$v_{GS} = -3 \text{ V}$$

$$v_{SG} = +3 \text{ V}$$

$$v_{DS} = -4 \text{ V}$$

$$v_{SD} = 4 \text{ V}$$

$$V_{tp} = -0.8 \text{ V}$$

$$V_A = -40 \text{ V}$$

$$\lambda = -0.025 \text{ V}^{-1}$$

$$i_D = \frac{1}{2} k_p (v_{GS} - V_{tp})^2 (1 + \lambda v_{DS})$$

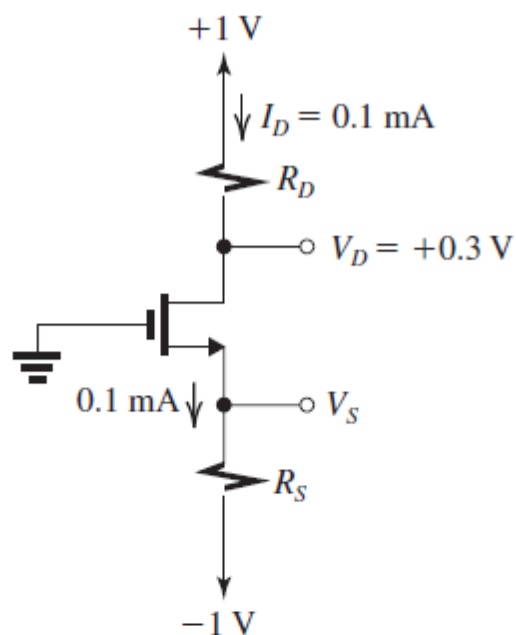
$$3 = \frac{1}{2} k_p [-3 - (-0.8)]^2 (1 - 0.025 \times -4)$$

$$\Rightarrow k_p = 1.137 \text{ mA/V}^2$$

Note: If  $\lambda$  is not specified, assume it is zero.

**D 5.44** Design the circuit of Fig. P5.44 to establish a drain current of 0.1 mA and a drain voltage of +0.3 V. The MOSFET has  $V_t = 0.5$  V,  $\mu_n C_{ox} = 400 \mu\text{A/V}^2$ ,  $L = 0.4 \mu\text{m}$ , and  $W = 5 \mu\text{m}$ . Specify the required values for  $R_S$  and  $R_D$ .

### 5.44



Since  $V_{DG} > 0$ , the MOSFET is in saturation.

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} V_{OV}^2$$

$$0.1 = \frac{1}{2} \times 0.4 \times \frac{5}{0.4} \times V_{OV}^2$$

$$\Rightarrow V_{OV} = 0.2 \text{ V}$$

$$V_{GS} = V_t + V_{OV} = 0.5 + 0.2 = 0.7$$

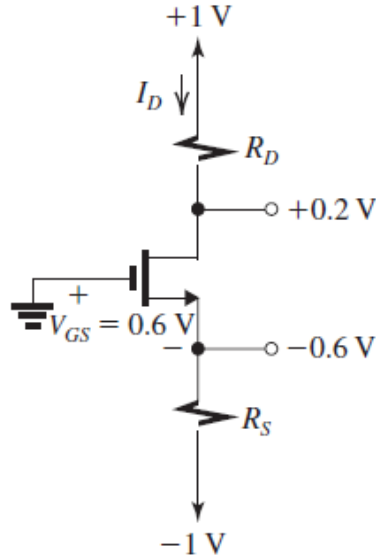
$$V_S = 0 - V_{GS} = -0.7 \text{ V}$$

$$R_S = \frac{V_S - (-1)}{I_D} = \frac{-0.7 + 1}{0.1} = 3 \text{ k}\Omega$$

$$R_D = \frac{1 - V_D}{I_D} = \frac{1 - 0.3}{0.1} = \frac{0.7}{0.1} = 7 \text{ k}\Omega$$

5.45 The NMOS transistor in the circuit of Fig. P5.44 has  $V_t = 0.4$  V and  $k_n = 4$  mA/V<sup>2</sup>. The voltages at the source and the drain are measured and found to be  $-0.6$  V and  $+0.2$  V, respectively. What current  $I_D$  is flowing, and what must the values of  $R_D$  and  $R_S$  be? What is the largest value for  $R_D$  for which  $I_D$  remains unchanged from the value found?

**5.45**



$$= \frac{1}{2} \times 4 \times (0.6 - 0.4)^2$$

$$= 0.08 \text{ mA}$$

$$R_D = \frac{1 - V_D}{I_D} = \frac{1 - 0.2}{0.08} = \frac{0.8}{0.08} = 10 \text{ k}\Omega$$

$$R_S = \frac{-0.6 - (-1)}{I_D} = \frac{-0.6 + 1}{0.08} = 5 \text{ k}\Omega$$

For  $I_D$  to remain unchanged from 0.08 mA, the MOSFET must remain in saturation. This in turn can be achieved by ensuring that  $V_D$  does not fall below  $V_G$  (which is zero) by more than  $V_t$  (0.4 V). Thus

$$1 - I_D R_{D\max} = -0.4$$

$$R_{D\max} = \frac{1.4}{0.08} = 17.5 \text{ k}\Omega$$

Since  $V_{DG} > 0$ , the MOSFET is operating in saturation. Thus

$$I_D = \frac{1}{2} k_n (V_{GS} - V_t)^2$$