

## Vector Space Proof Demonstration

*Generated by the Khwarizmi Symbolic System*

**Goal:** Prove that  $(2 \cdot (u + 0) + -1 \cdot u) = u$ .

**Proof:**

$$(2) \ (u + 0) = u \quad [VS\_Add\_Id]$$

$$(2a) \ 2 \cdot (u + 0) = 2 \cdot u \quad [VS\_Add\_Id]$$

$$(2b) \ (2 \cdot (u + 0) + -1 \cdot u) = (2 \cdot u + -1 \cdot u) \quad [VS\_Add\_Id]$$

$$(3) \ (2 \cdot u + -1 \cdot u) = (2 + -1) \cdot u \quad [VS\_Factor\_Scalar]$$

$$(4) \ (2 + -1) = 1 \quad [Scalar\_Arith]$$

$$(4a) \ (2 + -1) \cdot u = 1 \cdot u \quad [Scalar\_Arith]$$

$$(5) \ 1 \cdot u = u \quad [VS\_Scalar\_Id]$$

**Hence,**  $u = u$

*Proof log automatically generated by Khwarizmi. All transformations follow registered axioms.*