

## Vector Space Proof Demonstration

*Generated by the Khwarizmi Symbolic System*

**Goal:** Prove that  $(2 \cdot (u + 0) + -1 \cdot u) = u$

Start:  $(u + 0)$

$$(1) \quad (u + 0) = u \quad [VS\_Add\_Id]$$

$$(1a) \quad 2 \cdot (u + 0) = 2 \cdot u \quad [VS\_Add\_Id]$$

$$(1b) \quad (2 \cdot (u + 0) + -1 \cdot u) = (2 \cdot u + -1 \cdot u) \quad [VS\_Add\_Id]$$

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$$(2) \quad (2 \cdot u + -1 \cdot u) = (2 + -1) \cdot u \quad [VS\_Factor\_Scalar]$$

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$$(3) \quad (2 + -1) = 1 \quad [Scalar\_Arith]$$

$$(3a) \quad (2 + -1) \cdot u = 1 \cdot u \quad [Scalar\_Arith]$$

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$$(4) \quad 1 \cdot u = u \quad [VS\_Scalar\_Id]$$

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Final Result:  $u$

**Q.E.D.**