



FORMAL LAND

# FORMAL VERIFICATION SOLIDITY IN COQ

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ENCODE CLUB LONDON



# **FORMAL LAND**

- **Formal verification company**
- **Dedicated to Web3**
- **Tezos, Aleph Zero, Sui Foundation**
- **Since 2021**



<https://formal.land/>



# COQ-OF-SOLIDITY

A tool to verify smart contract on all possible inputs, and anticipate all vulnerabilities.

Open source:

<https://github.com/formal-land/coq-of-solidity>



# REASONS

1. **Billions** are stolen every year
2. **No police** on Web3
3. **Example:** Ethereum fork (DAO attack)



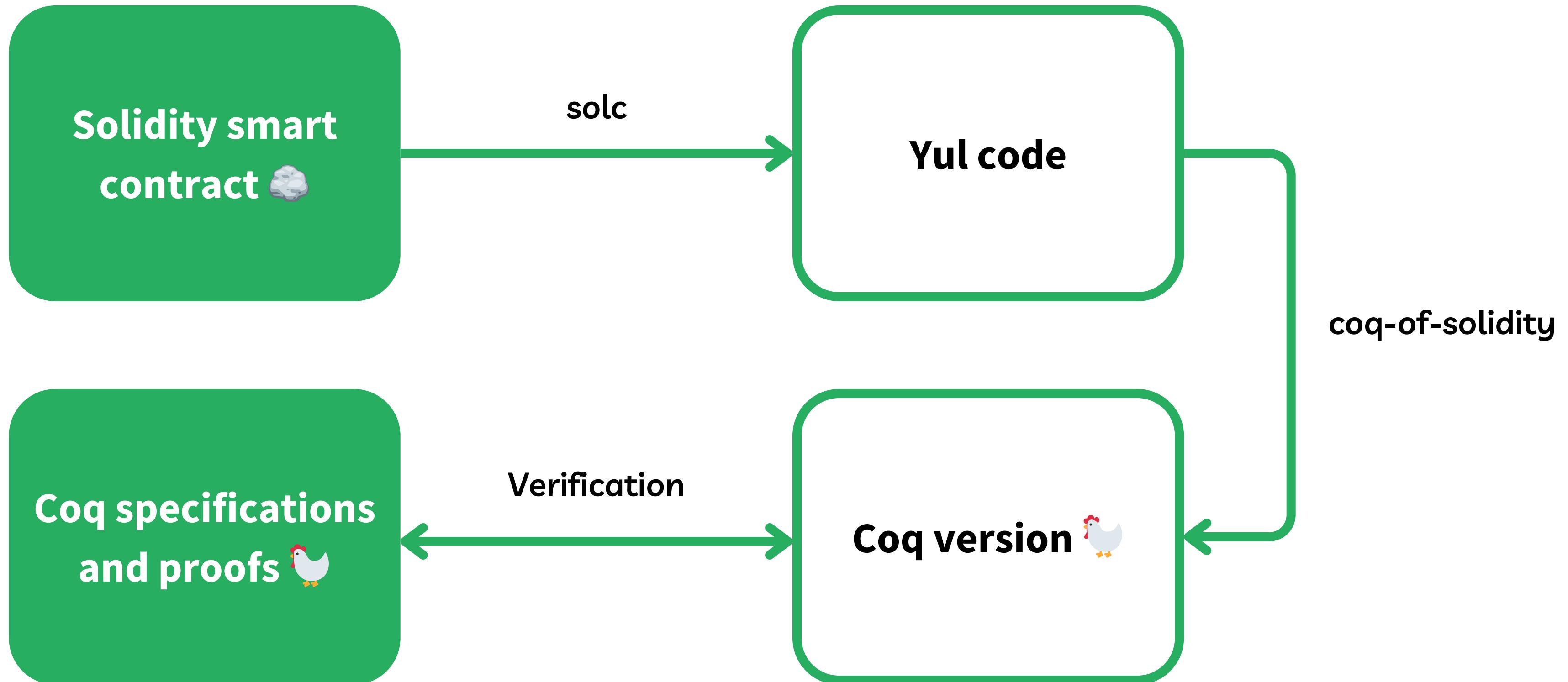
# TECHNIQUES

- Code review/Documentation
- Testing
- CI/CD
- Fuzzing/property based testing
- Modelling/Model Checking
- Symbolic Testing
- Program proof/Correct by Construction

Where we are



*Increasing effort,  
Increasing confidence*





# FORMAL VERIFICATION

- We can check **infinitely** many inputs
- In fact, we check all
- **How?**



# HOW?

- We **do not execute** the code
- We reason on **symbols**



# 0 SPECIFICATIONS

- **What do we want to verify?**
- No blocked state
- No overflows
- Optimizations are correct



**1 IF**

**if condition then**

action\_then

**else**

action\_else



## 2 LOOP

**for i = 0 to size-1 do**

action

**done**



## 3 FUNCTION

```
function foo() {  
    x = bar()  
  
    return x + 1  
}
```



## APPLICATION

- Verification of <https://smoo.th/>
- Optimized implementation of elliptic curves
- For authentication protocols
- Ongoing work



# SOURCE

```
//inlined ec_Add
T1:=shl(7, T1)//Computed value address offset.....
let T4:=mload(add(Mem, T1))//X2
mstore(add(Mem, _zzz2), mload(add(Mem, add(96, T1))))//ZZZ2

if iszero(ZZ) {
    X := T4//X2
    Y := mload(add(Mem, add(32, T1)))//Y2
    ZZ := mload(add(Mem, add(64, T1)))//ZZZ2
    ZZZ := mload(add(Mem, add(96, T1)))//ZZZ2
    continue
}
```

# COQ TRANSLATION

```
let~ usr0T1 := [[ shl ~(| 7, usr0T1 |) ]] in
let~ usr0T4 := [[ mload ~(| add ~(| usr0Mem, usr0T1 |) |) ]] in
do~ [[ mstore ~(| add ~(| usr0Mem, 2144 |), mload ~(| add ~(| usr0Mem, add ~(| 96, usr0T1 |) |) |) |) ]] in
let_state~ '(var_X_60, var_Y_80, var_ZZZ_83, var_ZZ_86) := [[
  Shallow.if_ (
    iszero ~(| var_ZZ_86 |),
    let~ var_X_60 := [[ usr0T4 ]] in
    let~ var_Y_80 := [[ mload ~(| add ~(| usr0Mem, add ~(| 32, usr0T1 |) |) |) ]] in
    let~ var_ZZ_86 := [[ mload ~(| add ~(| usr0Mem, add ~(| 64, usr0T1 |) |) |) ]] in
    let~ var_ZZZ_83 := [[ mload ~(| add ~(| usr0Mem, add ~(| 96, usr0T1 |) |) |) ]] in
    M.pure (BlockUnit.Continue, (var_X_60, var_Y_80, var_ZZZ_83, var_ZZ_86)),
    (var_X_60, var_Y_80, var_ZZZ_83, var_ZZ_86)
  )
]] default~ (var_X_60, var_Y_80, var_ZZZ_83, var_ZZ_86) in
```

# COQ PROOF

```
(1/1)
{{?codes, environment,
Some
  (make_state environment state
    [mem0; mem1; 0; mem3; mem4; mem5; mem6; mem7; mem8; mem9; 480; mem11;
     mem12; mem13; mem14; Q.(PA.X); Q.(PA.Y); Q'.(PA.X);
     Q'.(PA.Y); p; a; G.(PA.X); G.(PA.Y); G'.(PA.X);
     G'.(PA.Y); 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0];
    []])
| let~ ' zero_t_uint256_1
  := M.call Contract_91.Contract_91_deployed.zero_value_for_split_t_uint256
in let~ ' var_X_60 := pure zero_t_uint256_1
  in let~ ' expr_66 := pure 170141183460469231731687303715884105728
    in let~ ' var mask 63
```

Command “l”

# COQ PROOF

```
(1/1)
{{?codes, environment,
Some
  (make_state environment state
    [mem0; mem1; 0; mem3; mem4; mem5; mem6; mem7; mem8; mem9; 480; mem11;
     mem12; mem13; mem14; Q.(PA.X); Q.(PA.Y); Q'.(PA.X);
     Q'.(PA.Y); p; a; G.(PA.X); G.(PA.Y); G'.(PA.X);
     G'.(PA.Y); 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0];
    []])
  | M.call Contract_91.Contract_91_deployed.zero_value_for_split_t_uint256
  || ?output_inter0 | ?state_inter0?}}}
```

Command “c”

# COQ PROOF

```
(1/1)
{{?codes, environment,
Some
  (make_state environment state
    [mem0; mem1; 0; mem3; mem4; mem5; mem6; mem7; mem8; mem9; 480; mem11;
     mem12; mem13; mem14; Q.(PA.X); Q.(PA.Y); Q'.(PA.X);
     Q'.(PA.Y); p; a; G.(PA.X); G.(PA.Y); G'.(PA.X);
     G'.(PA.Y); 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0;
     0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0; 0])
  | Contract_91.Contract_91_deployed.zero_value_for_split_t_uint256
  || ?output_inter1 | ?state_inter1?}}
```

Call to previous proof



## WE GET

- A proof of equivalence with a functional version of the contract
- We proceed by refinements up to the original elliptic curve formula
- Still ongoing

# THANKS

To get your smart contract

verified:

[contact@formal.land](mailto:contact@formal.land)