Puzzle

Friday, June 9, 2017 5:40 PM

Suppose you're editing a text file from a blank text editor. You have a keyboard with 4 keys: select all, copy, paste, and type 1 character.

Given n allowed keystrokes, find the sequence of keystrokes which maximizes the total number of characters in the end. First solve the simpler problem of finding how MANY characters you can create with n keystrokes. Backtrack the solution later to figure out the sequence of keystrokes.

Define c[n] to be the optimal number of CHARACTERS given n allowed keystrokes.

Action	Letter
Select all	S
Copy selection	С
Paste clipboard	Р
Type 1 letter	Т

Base cases:

c[0] = 0

c[1] = 1, T

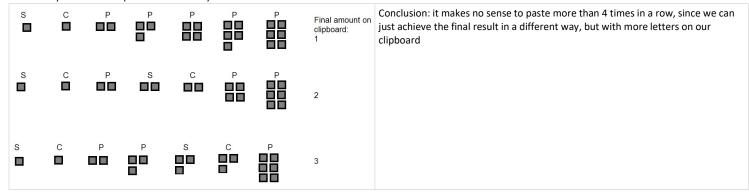
c[2] = 2, TT

c[3] = 3, TTT

c[4] = 4, TTTT

At some step n, there are 2 things I can do. I could type 1 character, or I could select all, copy, and paste a certain number of times. However, there must be a limit on the number of consecutive pastes we can do before it becomes more efficient to do another select all and copy to increase the number of letters in our clipboard. However, we know that there must be at least 1 paste. If we selected all and copied, it would be inefficient to type 1 character, since the clipboard has more than 1 character (assuming non base case).

How many times can we paste consecutively before it becomes inefficient?



Therefore, at a particular step, I have 5 possible move sequences:

Type 1 character	c[n] = c[n -	- 1] + 1				
Select all, copy, paste 1 time	Step $n-2$	Step $n-1$	Step n			
	Select	Сору	Paste			
	X	Х	XX			
	(assuming at $c[n] = c[n -$		•	-	-3] = X let	ters available)
Select all, copy, paste 2 times	Step $n-3$	Step $n-2$	Step $n-1$	Step n		
	Select	Сору	Paste	Paste		
	X	X	XX	XXX		
	c[n] = c[n -	-4] + c[n -	[4] + c[n -	4] = 3c[n -	- 4]	
Select all, copy, paste 3 times	Step n - 4	Step $n-3$	Step $n-2$	Step $n-1$	Step n	
	Select	Сору	Paste	Paste	Paste	
	X	Х	XX	XXX	XXXX	
	c[n] = c[n -	-5] + c[n -	[5] + c[n -	5] + c[n -	5] = 4c[n -	- 5]
Select all, copy, paste 4 times	Step $n-5$	Step $n-4$	Step $n-3$	Step $n-2$	Step $n-1$	Step n

	Select	Сору	Paste	Paste	Paste	Paste	
	Х	Х	XX	XXX	XXXX	XXXXX	
c[n] = c[n-6] + c[n-6] + c[n-6] + c[n-6] + c[n-6] = 5c[n-6]							

$$c[n] = \max\left(\max_{2 \le k \le 5} \{k*c[n-k-1]\}, c[n-1]+1\right)$$

Recursive solution

```
\begin{array}{ll} \text{def } f(n): & \text{Value in } c[n] \text{ depends on the immediate 6 values behind it} \\ & \text{if } n{<}{=}4: \\ & \text{return } n \\ & \text{x } = f(n{-}1){+}1 \\ & \text{for i in range}(2, 5): \\ & \text{x } = \max(x, \ i{+}f(n{-}i{-}1)) \\ & \text{return } x \end{array}
```

Dynamic programming solution

```
def f(n): c = ([0, 1, 2, 3, 4] + [0]*(n+1-5)) for k in range(5, n+1): x = c[k-1]+1 for i in range(2, 6): x = max(x, i*c[max(k-i-1, 0)]) Loop if from [2, 5] Apply the recurrence c[k] = x return c[n]
```

Constructing the solution

```
def f(n):
c = ([0, 1, 2, 3, 4] + [0]*(n+1-5))
d = [0]*(n+1) #tracks which case we choose
 for k in range(1, n+1):
    x = c[k-1]+1
    case = -1
    for i in range (2, 6):
        if i*c[max(k-i-1, 0)] >= x:
            x = i*c[max(k-i-1, 0)]
            case = i
    c[k] = x
    d[k] = case
 #return c[n]
print("n = " + str(n) + ", max chars: " + str(c[n]))
k = n
while k > 0:
    if d[k] == -1:
        print(str(k) +". Type 1 character")
         k-=1
    else:
         case = d[k]
         for in xrange(case-1):
            print(str(k) +". Paste selection")
            k = 1
         print(str(k) +". Copy selection")
         print(str(k) +". Select all")
         k-=1
```