Feuille d'exercice n° 03 : Systèmes linéaires - fiche d'entraînement - corrigé

Exercice 1

$$\mathbf{1)} \ \left\{ \begin{pmatrix} 1 \\ 1 \end{pmatrix} \right\}$$

$$\mathbf{2)} \ \left\{ \frac{1}{4} \begin{pmatrix} 1 \\ -5 \end{pmatrix} \right\}$$

$$3) \left\{ \begin{pmatrix} 0 \\ 1 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ -(1+\sqrt{2}) \end{pmatrix} \mid \lambda \in \mathbb{R} \right\}$$

Exercice 2

$$1) \left\{ \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ -3 \\ -5 \end{pmatrix} \middle| \lambda \in \mathbb{R} \right\}$$

$$\mathbf{2)} \left\{ \left. \frac{1}{11} \begin{pmatrix} 0\\9\\19 \end{pmatrix} + \lambda \begin{pmatrix} 11\\-16\\-13 \end{pmatrix} \right| \lambda \in \mathbb{R} \right\}$$

3)
$$\left\{ \left. \frac{1}{11} \begin{pmatrix} 0 \\ 10 \\ 7 \end{pmatrix} + \lambda \begin{pmatrix} 11 \\ -2 \\ -19 \end{pmatrix} \right| \lambda \in \mathbb{R} \right\}$$

4)
$$\left\{ \begin{pmatrix} 0 \\ 0 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ 0 \\ -2 \end{pmatrix} + \mu \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} \middle| \lambda, \mu \in \mathbb{R} \right\}$$

Exercice 3

$$1) \left\{ \frac{1}{3} \begin{pmatrix} 1 \\ 1 \\ 5 \end{pmatrix} \right\}$$

$$2) \left\{ \frac{1}{2} \begin{pmatrix} 25 \\ -9 \\ -20 \end{pmatrix} \right\}$$

$$\mathbf{3)} \left\{ \left. \frac{1}{3} \begin{pmatrix} 0 \\ -1 \\ 8 \end{pmatrix} + \lambda \begin{pmatrix} 3 \\ -1 \\ -7 \end{pmatrix} \right| \lambda \in \mathbb{R} \right\}$$

$$4) \left\{ \frac{1}{9} \begin{pmatrix} 2\\ -17\\ -10 \end{pmatrix} \right\}$$