Feuille d'exercice n° 01 : Fonctions usuelles - fiche d'entraînement - Corrigé

Exercice 1

1)
$$f'(x) = \frac{-2}{(x-1)^2}$$

2)
$$f'(x) = 20x^3 + 15x^2 + 34x - 3$$

3)
$$f'(x) = -\frac{25}{x^6}$$

4)
$$f'(x) = -\frac{25}{x^6} - \frac{6}{x^3}$$

5)
$$f'(x) = -\frac{1}{2x\sqrt{x}}$$

6)
$$f'(x) = -\frac{3}{2\sqrt{x^5}}$$

7)
$$f'(x) = \frac{2}{3\sqrt[3]{x}} + \frac{1}{2\sqrt{x}}$$

8)
$$f'(x) = 4(x^2 + 3x - 2)^3(2x + 3)$$

9)
$$f'(x) = \frac{x-1}{\sqrt{x^2-2x+3}}$$

10)
$$f'(x) = \frac{5x^4 - 3x^2}{4\sqrt[4]{(x^5 - x^3 - 2)^3}}$$

11)
$$f'(x) = -\frac{4x}{3\sqrt[3]{(x^4 - 1)^2(x^2 - 1)^2}}$$

12)
$$f'(x) = \frac{1}{2\sqrt{x}}.10^{\sqrt{x}}.\ln 10$$

13)
$$f'(x) = -2xe^{3-x^2}$$

14)
$$f'(x) = \frac{2e^{2x}(x-1)}{x^3}$$

15)
$$f'(x) = 3^{2x^2} \left(4x\sqrt{x} \cdot \ln 3 + \frac{1}{2\sqrt{x}} \right)$$

16)
$$f'(x) = \frac{8x^3 - 3x^2 + 6x - 3}{2x^4 - x^3 + 3x^2 - 3x}$$

17)
$$f'(x) = -\frac{2e^x}{e^{2x}-1}$$

18)
$$f'(x) = \frac{1}{1 - x^2}$$

19)
$$f'(x) = \frac{1-2x}{2x(1-x)}$$

20)
$$f'(x) = \frac{2}{3x(x+2)}$$

21)
$$f'(x) = \frac{5x-1}{(x-2)(2x-1)}$$

Exercice 2

1)
$$f'(x) = 6x^2 \cos(2x^3)$$

2)
$$f'(x) = 5x^4(1 + \tan^2(x^5))$$

3)
$$f'(x) = 2x(-2x^5\sin x^2 - 3\sin x^2 + 5x^3\cos x^2)$$

4)
$$f'(x) = \frac{2x(-2\cos(2x^3) - 6x^3\sin(2x^3) - 15x\sin(2x^3))}{\cos^2(2x^3)}$$

5)
$$f'(x) = 15x^4 \sin^2(x^5) \cos(x^5)$$

6)
$$f'(x) = 12x(-3x^2 + 2)\sin(-3x^2 + 2)^2$$

Exercice 3 Calculer les dérivées des fonctions suivantes :

1)
$$f'(x) = \frac{15x^{1/4}}{4}$$

2)
$$f'(x) = \frac{5}{6x^{1/3}}$$

3)
$$f'(x) = \frac{20}{x^6}$$

4)
$$f'(x) = -\frac{9}{x^4}$$

5)
$$f'(x) = -\frac{1}{2x^{3/4}}$$

6)
$$f'(x) = \frac{1}{3x^{2/3}} + \frac{1}{5x^{4/5}}$$

Exercice 4

1)
$$f'(x) = \frac{-8x^7 + 9x^6 - 12x^2 + 6x}{4x^{10} - 8x^5 + 4}$$

2)
$$f'(x) = \frac{9x^6 - 24x^3 - 18x^2}{9x^6 - 12x^3 + 4}$$

3)
$$f'(x) = \frac{12x^8 - 12x^5 + 100x^4 + 20x}{9x^8 + 30x^4 + 25}$$

4)
$$f'(x) = \frac{56x^{14/3} + 144x^3 - 8x^{8/3} - 72x - 50x^{2/3}}{12x^{10/3} + 36x^{5/3} + 27}$$

Exercice 5

1)
$$f'(x) = \frac{15x^2}{\sqrt{1 - 25x^6}}$$

2)
$$f'(x) = -\frac{4x}{\sqrt{1-4x^4}}$$

3)
$$f'(x) = \frac{8x^3}{4x^8 + 1}$$

4)
$$f'(x) = \frac{30x(Arcsin(5x^2))^2}{\sqrt{1-25x^4}}$$

5)
$$f'(x) = \frac{45x^4(3x^5+1)^2}{\sqrt{1-(3x^5+1)^6}}$$

6)
$$f'(x) = -\frac{16x \operatorname{Arccos}(4x^2)}{\sqrt{1 - 16x^4}}$$

7)
$$f'(x) = \frac{18x^2(-2x^3-3)^2}{\sqrt{1-(-2x^3-3)^6}}$$

Exercice 6

1)
$$f'(x) = \frac{4}{x \ln 2x^4}$$

2)
$$f'(x) = \frac{3}{x \ln 3x^3}$$

3)
$$f'(x) = -\frac{3\sin\ln 4x^3}{x}$$

4)
$$f'(x) = 6xe^{e^{3x^2} + 3x^2}$$

5) $f'(x) = 24x^2(4x^3 + 5)e^{(4x^3+5)^2}$

6)
$$f'(x) = \frac{-3x^3\ln(4x^2) - 2x^3 - 8}{x}$$

7)
$$f'(x) = \frac{5(x^3 - 12)}{x(x^3 - 3)}$$

8)
$$f'(x) = 4xe^{5x^4 - 4x^2 - 3}(5x^2 - 2)$$

Exercice 7 Déterminer les limites des expressions suivantes.

- 1) $+\infty$
- **2**) $\frac{1}{2}$
- **3)** 0
- 4) $\frac{\pi}{16}$
- **5)** 0

- **6**) $\frac{1}{4}$
- 7) $\frac{\pi}{2}$
- **8**) −∞
- **9**) 1
- **10)** 0

Exercice 8 Tableaux à venir.

1)
$$f': x \mapsto \frac{x-1}{e^x - x}$$

2)
$$g': x \mapsto (e^x - 1)(e^x - 2)$$

3)
$$\varphi': x \mapsto -\frac{(x-1)(x-3)}{e^x}$$

4)
$$\psi': x \mapsto \frac{e^{2x}(2x+\sqrt{6}+4)(2x-\sqrt{6}+4)}{2(x+2)^4}$$
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