Stdlib Sparse matrix API

Goals

To be compact instead of being exhaustive. It aims at supplying Fortran users with a minimum (yet useful) number of routines and data structures related to sparse matrices storage and operations. This library is particularly targeted at a non-expert in numerical computation public. Thus we aim at having a simple and easy to use API.

1 Sparse matrix representations supported

This section is based on Saad (1994). In that work, a much more complete and extensive list of formats is described. Here we take only the ones that we think are most useful at the moment.

SOME QUESTIONS:

SUPPORT ONE-BASED INDEXING?

SUPPORT ZERO-BASED INDEXING?

1.1 Coordinate format (COO)

Given an m by n real or complex matrix A containing nnz nonzero elements with each element denoted by a_{ij} this format represents A using a set of three arrays: *values, rows,* and *columns,* as described below.

values A real/complex array of size nnz containing the matrix elements a_{ij} in any order.

rows An integer array of size nnz containing the row indices of the elements a_{ij} .

columns An integer array of size nnz containing the column indices of the elements a_{ij} .

1.2 Compressed Sparse Row (CSR)

Given an m by n real or complex matrix A containing nnz nonzero elements with each element denoted by a_{ij} this format represents A using a set of three arrays: *values*, *ja*, and *ia*, as described below.

valuesA real/complex array of size nnz containing the matrix elements a_{ij} stored row by
row from row 1 to row n.jaAn integer array of size nnz containing the column indices of the elements a_{ij} as
stored in the array values.iaAn integer array of size n + 1 containing the index in the arrays values and ja
where each row starts. The value at ia(n + 1) always has the value ia(1) + nnz.

1.3 Compressed Sparse Column (CSC)

This format is similar to the CSR format described previously. The difference is that instead of storing row values we store column values in the array *values*. The exact description of this format is given below.

Given an m by n real or complex matrix A containing nnz nonzero elements with each element denoted by a_{ij} this format represents A using a set of three arrays: *values*, *ja*, and *ia*, as described below.

values	A real/complex array of size nnz containing the matrix elements a_{ij} stored column by column from column 1 to column m .
ia	An integer array of size nnz containing the <i>row</i> indices of the elements a_{ij} as stored in the array <i>values</i> .
ja	An integer array of size $m + 1$ containing the index in the arrays values and ia where each column starts. The value at $ja(m + 1)$ always has the value $ja(1) + nnz$.

2 Creational subroutines

3 Conversion subroutines

- 4 Algebraic operations
- 4 Utilities
- 4 Input/Output

References

Saad, Y., SPARSKIT: A basic tool kit for sparse matrix computation, *1994*.<u>https://www-users.cs.umn.edu/~saad/software/SPARSKIT/</u>