10주차(3/3)

XOR 신경망 구현

파이썬으로배우는기계학습

한동대학교 김영섭교수

XOR 신경망

- 학습 목표
 - 다층 신경망을 경사하강법과 역전파 알고리즘으로 구현한다.
 - XOR로 신경망을 학습하고 테스트한다.
- 학습 내용
 - 객체지향 다층 신경망 구현하기
 - fit() 메소드
 - net_input() 메소드
 - predict() 메소드
 - XOR 신경망 학습

기본 메소드: 생성자, 활성화 함수, 활성화 함수 미분

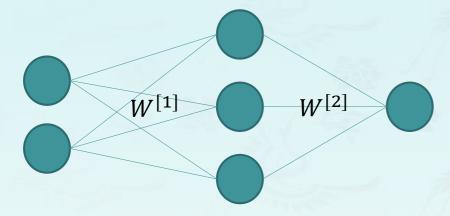
- 클래스
 - 이름: NeuralNetwork
 - 생성자: __init__()
 - 활성화 함수: g()
 - 활성화 함수 미분 : g_prime()

```
class NeuralNetwork():
           This class implements a multi-perceptron
           with backpropagation. This handles a simple logics
           such as OR, AND, NAND, and NOR gates, including XOR.
       def init (self, net arch, eta=0.1, epochs=10000,
                    random seed=1):
           self.layers = len(net arch)
           self.net arch = net arch
           self.eta = eta
           self.epochs = epochs
12
           self.random seed = random seed
13
14
       def g(self, x):
           return 1/(1 + np.exp((-x)))
16
       def g prime(self, x):
18
           return self.g(x) * (1 - self.g(x))
19
20
       def fit(self, X, Y):
```

- 클래스
 - 이름: NeuralNetwork
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 - 활성화 함수 미분 : g_prime()
 - 학습 메소드: fit()

```
def fit(self, X, Y):
      inp.random.seed(self.random seed)
      W1 shape = (self.net arch[1], self.net arch[0])
      W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
      self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for in range(self.epochs):
           A0 = X
12
           Z1 = np.dot(self.W1, A0)
13
           A1 = self.q(Z1)
14
           Z2 = np.dot(self.W2, A1)
15
           A2 = self.q(Z2)
16
           E2 = Y - A2
17
           E1 = np.dot(self.W2.T, E2)
18
19
20
           dZ2 = E2 * self.g prime(Z2)
           dZ1 = E1 * self.g prime(Z1)
21
22
23
           self.W2 += np.dot(dZ2, A1.T)
24
           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost .append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

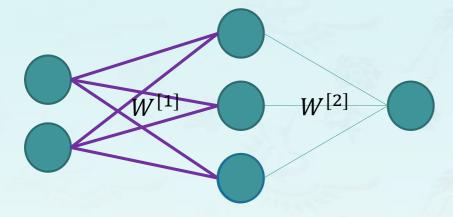
- 클래스
 - 학습 메소드: fit()



```
self.net_arch = [2, 3, 1]
```

```
def fit(self, X, Y):
      inp.random.seed(self.random seed)
      W1 shape = (self.net arch[1], self.net arch[0])
      W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
 5
      self.W2 = 2*np.random.random(W2 shape) - 1
 6
       self.cost = []
       for in range(self.epochs):
           A0 = X
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           Z1 = np.dot(self.W1, A0)
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           A1 = self.q(Z1)
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           dZ2 = E2 * self.g prime(Z2)
           dZ1 = E1 * self.g prime(Z1)
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           self.W2 += np.dot(dZ2, A1.T)
24
           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

- 클래스
 - 학습 메소드: fit()

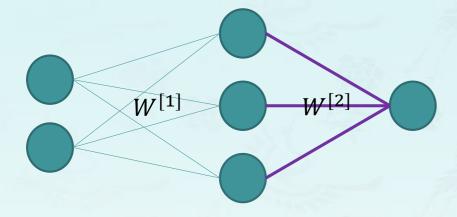


 $self.net_arch = [2, 3, 1]$

```
W1_shape = (self.net_arch[1], self.net_arch[0])
W2_shape = (self.net_arch[2], self.net_arch[1])
self.W1 = 2*np.random.random(W1_shape) - 1
self.W2 = 2*np.random.random(W2_shape) - 1
```

```
def fit(self, X, Y):
      inp.random.seed(self.random seed)
      W1 shape = (self.net arch[1], self.net arch[0])
      W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
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           dZ2 = E2 * self.g prime(Z2)
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- 클래스
 - 학습 메소드: fit()

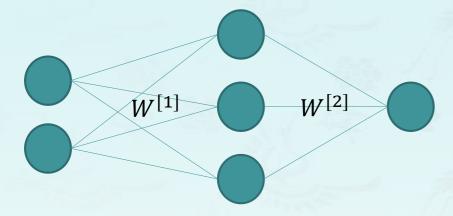


```
self.net_arch = [2, 3, 1]
```

```
W1_shape = (self.net_arch[1], self.net_arch[0])
W2_shape = (self.net_arch[2], self.net_arch[1])
self.W1 = 2*np.random.random(W1_shape) - 1
self.W2 = 2*np.random.random(W2_shape) - 1
```

```
def fit(self, X, Y):
      inp.random.seed(self.random seed)
      W1 shape = (self.net arch[1], self.net arch[0])
      W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
      self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for in range(self.epochs):
           A0 = X
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```

- 클래스
 - 학습 메소드: fit()



```
self.net_arch = [2, 3, 1]
```

```
W1_shape = (self.net_arch[1], self.net_arch[0])
W2_shape = (self.net_arch[2], self.net_arch[1])
self.W1 = 2*np.random.random(W1_shape) - 1
self.W2 = 2*np.random.random(W2_shape) - 1
```

```
def fit(self, X, Y):
      inp.random.seed(self.random seed)
      W1 shape = (self.net arch[1], self.net arch[0])
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       self.W1 = 2*np.random.random(W1 shape) - 1
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           A0 = X
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           dZ2 = E2 * self.g prime(Z2)
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           self.W2 += np.dot(dZ2, A1.T)
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           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost .append(np.sqrt(np.sum(E2 * E2)))
       return self
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```

fit() 메소드: 오차

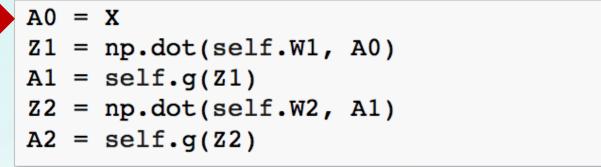
- 클래스
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 - 학습 메소드: fit()

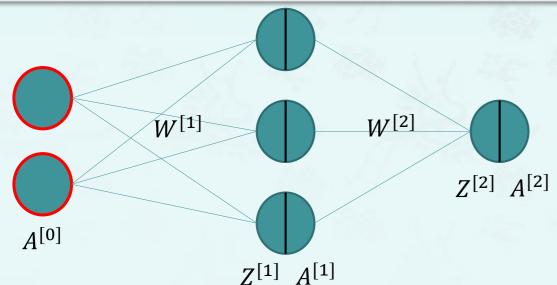
```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
 8
       self.cost = []
 9
       for _ in range(self.epochs):
           A0 = X
12
           Z1 = np.dot(self.W1, A0)
13
           A1 = self.q(Z1)
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           Z2 = np.dot(self.W2, A1)
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           A2 = self.q(Z2)
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           E2 = Y - A2
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           E1 = np.dot(self.W2.T, E2)
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           dZ2 = E2 * self.g prime(Z2)
           dZ1 = E1 * self.g prime(Z1)
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           self.W2 += np.dot(dZ2, A1.T)
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           self.W1 += np.dot(dZ1, A0.T)
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           self.cost .append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

- 클래스
 - 학습 메소드: fit()
 - 순전파

```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
10
       for in range(self.epochs):
11
          A0 = X
12
          Z1 = np.dot(self.W1, A0)
          A1 = self.g(Z1)
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           Z2 = np.dot(self.W2, A1)
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           self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
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```

- 클래스
 - 학습 메소드: fit()
 - 순전파 : 입력층 → 은닉층





```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net_arch[2], self.net_arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
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       for in range(self.epochs):
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- 클래스
 - 학습 메소드: fit()
 - 순전파 : 입력층 → 은닉층

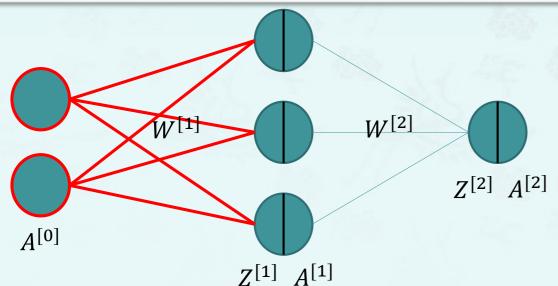
```
A0 = X

Z1 = np.dot(self.W1, A0)

A1 = self.g(Z1)

Z2 = np.dot(self.W2, A1)

A2 = self.g(Z2)
```



```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
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- 클래스
 - 학습 메소드: fit()
 - 순전파 : 입력층 → 은닉층

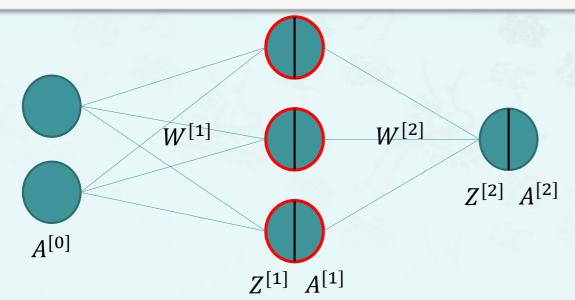
```
A0 = X

Z1 = np.dot(self.W1, A0)

A1 = self.g(Z1)

Z2 = np.dot(self.W2, A1)

A2 = self.g(Z2)
```



```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
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       self.W1 = 2*np.random.random(W1 shape) - 1
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           dZ2 = E2 * self.g prime(Z2)
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           dZ1 = E1 * self.g prime(Z1)
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           self.W2 += np.dot(dZ2, A1.T)
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24
           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost .append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

- 클래스
 - 학습 메소드: fit()
 - 순전파 : 은닉층 → 출력층

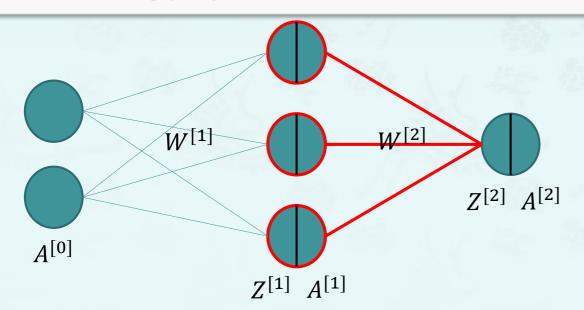
```
A0 = X

Z1 = np.dot(self.W1, A0)

A1 = self.g(Z1)

Z2 = np.dot(self.W2, A1)

A2 = self.g(Z2)
```



```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net_arch[2], self.net_arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
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- 클래스
 - 학습 메소드: fit()
 - 순전파 : 은닉층 → 출력층

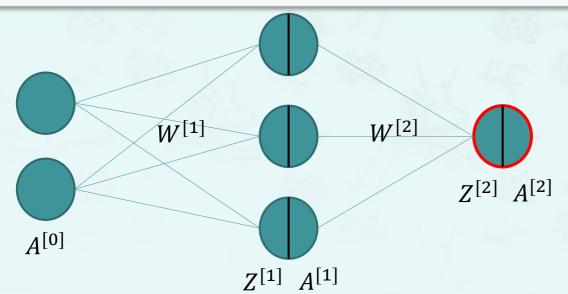
```
A0 = X

Z1 = np.dot(self.W1, A0)

A1 = self.g(Z1)

Z2 = np.dot(self.W2, A1)

A2 = self.g(Z2)
```



```
def fit(self, X, Y):
       np.random.seed(self.random seed)
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           self.cost .append(np.sqrt(np.sum(E2 * E2)))
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```

fit() 메소드: 오차

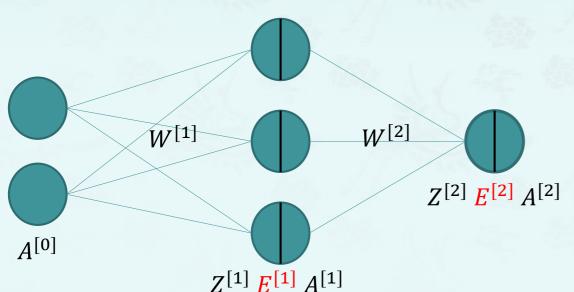
```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2_shape = (self.net_arch[2], self.net_arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
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       for in range(self.epochs):
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           self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
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```

fit() 메소드: 오차

■ 역전파: 오차 계산

$$E^{[2]} = Y - A^{[2]}$$

 $E^{[1]} = W^{[2] \cdot T} \cdot E^{[2]}$



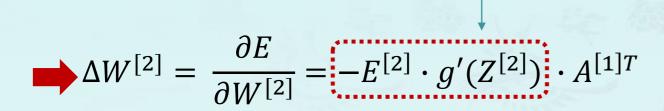
```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1_shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for in range(self.epochs):
10
11
           A0 = X
12
           Z1 = np.dot(self.W1, A0)
13
           A1 = self.q(Z1)
14
           Z2 = np.dot(self.W2, A1)
15
           A2 = self.q(Z2)
16
17
           E2 = Y - A2
18
           E1 = np.dot(self.W2.T, E2)
19
20
           dZ2 = E2 * self.g prime(Z2)
21
           dZ1 = E1 * self.g prime(Z1)
22
23
           self.W2 += np.dot(dZ2, A1.T)
24
           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

$$\Delta W^{[2]} = \frac{\partial E}{\partial W^{[2]}} = -E^{[2]} \cdot g'(Z^{[2]}) \cdot A^{[1]T}$$

$$\Delta W^{[1]} = \frac{\partial E}{\partial W^{[1]}} = -E^{[1]} \cdot g'(Z^{[1]}) \cdot A^{[0]T}$$

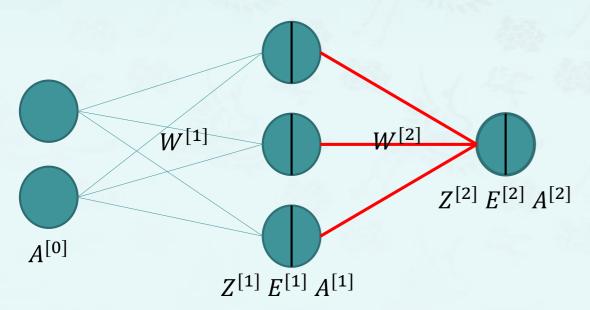
dZ1

```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net_arch[1], self.net_arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for _ in range(self.epochs):
          A0 = X
          Z1 = np.dot(self.W1, A0)
          A1 = self.g(Z1)
          Z2 = np.dot(self.W2, A1)
          A2 = self.g(Z2)
15
16
          E2 = Y - A2
18
          E1 = np.dot(self.W2.T, E2)
19
         dZ2 = E2 * self.g_prime(Z2)
          dZ1 = E1 * self.g_prime(Z1)
22
23
           self.W2 += np.dot(dZ2, A1.T)
24
           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost .append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```



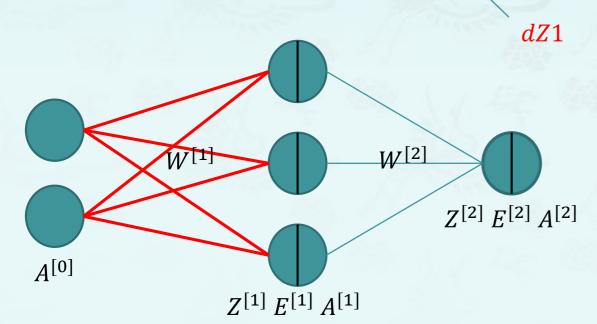
dZ2

$$\Delta W^{[1]} = \frac{\partial E}{\partial W^{[1]}} = -E^{[1]} \cdot g'(Z^{[1]}) \cdot A^{[0]T}$$



```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1_shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for _ in range(self.epochs):
           A0 = X
           Z1 = np.dot(self.W1, A0)
13
          A1 = self.q(Z1)
          Z2 = np.dot(self.W2, A1)
15
          A2 = self.q(Z2)
16
          E2 = Y - A2
18
          E1 = np.dot(self.W2.T, E2)
19
20
           dZ2 = E2 * self.g prime(Z2)
21
           dZ1 = E1 * self.g prime(Z1)
22
23
          self.W2 += np.dot(dZ2, A1.T)
          self.W1 += np.dot(dZ1, A0.T)
25
           self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

$$\Delta W^{[2]} = \frac{\partial E}{\partial W^{[2]}} = -E^{[2]} \cdot g'(Z^{[2]}) \cdot A^{[1]T}$$



```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for in range(self.epochs):
           A0 = X
           Z1 = np.dot(self.W1, A0)
13
          A1 = self.q(Z1)
          Z2 = np.dot(self.W2, A1)
14
15
          A2 = self.q(Z2)
16
          E2 = Y - A2
18
           E1 = np.dot(self.W2.T, E2)
19
20
           dZ2 = E2 * self.g prime(Z2)
21
           dZ1 = E1 * self.g prime(Z1)
22
23
          self.W2 += np.dot(dZ2, A1.T)
24
          self.W1 += np.dot(dZ1, A0.T)
25
           self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net_arch[1], self.net_arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for in range(self.epochs):
11
           A0 = X
12
           Z1 = np.dot(self.W1, A0)
13
          A1 = self.q(Z1)
14
           Z2 = np.dot(self.W2, A1)
15
          A2 = self.q(Z2)
16
17
           E2 = Y - A2
18
           E1 = np.dot(self.W2.T, E2)
19
20
           dZ2 = E2 * self.g prime(Z2)
           dZ1 = E1 * self.g prime(Z1)
21
22
23
           self.W2 += np.dot(dZ2, A1.T)
24
          self.W1 += np.dot(dZ1, A0.T)
25
          self.cost_.append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

fit() 메소드: 오차

- 클래스
 - 이름: NeuralNetwork
 - 생성자: __init__()
 - 활성화 함수: g()
 - 활성화 함수 미분 : g_prime()
 - 학습 메소드: fit()

```
def fit(self, X, Y):
       np.random.seed(self.random seed)
       W1 shape = (self.net arch[1], self.net arch[0])
       W2 shape = (self.net arch[2], self.net arch[1])
       self.W1 = 2*np.random.random(W1 shape) - 1
       self.W2 = 2*np.random.random(W2 shape) - 1
       self.cost = []
       for in range(self.epochs):
           A0 = X
12
           Z1 = np.dot(self.W1, A0)
13
           A1 = self.g(Z1)
14
           Z2 = np.dot(self.W2, A1)
15
           A2 = self.q(Z2)
16
           E2 = Y - A2
17
           E1 = np.dot(self.W2.T, E2)
18
19
20
           dZ2 = E2 * self.g prime(Z2)
           dZ1 = E1 * self.g prime(Z1)
21
22
23
           self.W2 += np.dot(dZ2, A1.T)
24
           self.W1 += np.dot(dZ1, A0.T)
25
           self.cost .append(np.sqrt(np.sum(E2 * E2)))
       return self
26
```

기본 메소드: 순입력

- 클래스
 - 이름: NeuralNetwork
 - 생성자: __init__()
 - 활성화 함수: g()
 - 활성화 함수 미분 : g_prime()
 - 학습 메소드: fit()
 - 순입력: net_input()

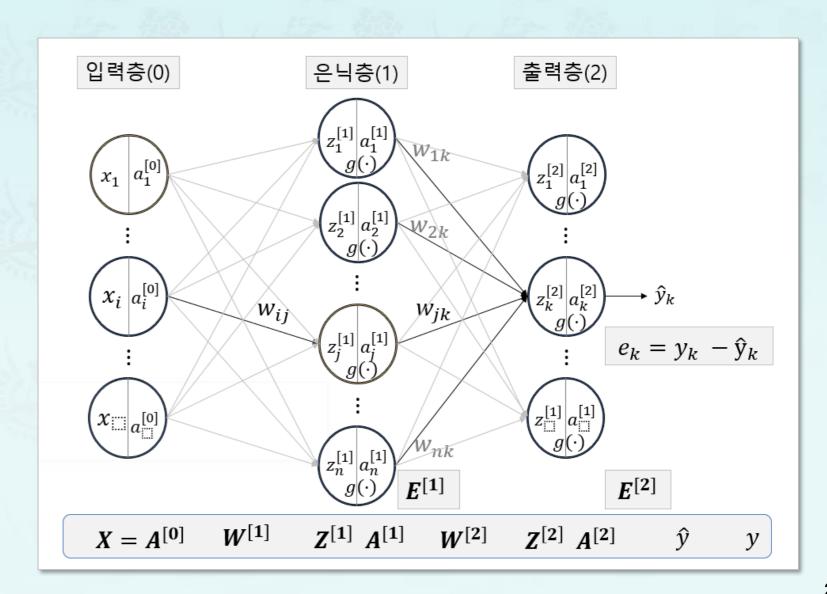
```
44
               self.W1 += np.dot(dZ1, A0.T)
45
               self.cost .append(np.sqrt(
46
                   np.sum(E2 * E2)))
47
           return self
48
      def net input(self, X):
49
           if X.shape[0] == self.w.shape[0]:
50
51
               return np.dot(X, self.w)
52
           else:
53
               return np.dot(X, self.w[1:]) + self.w[0]
54
55
       def predict(self, X):
56
           Z1 = np.dot(self.W1, X)
           A1 = self.q(Z1)
57
58
           Z2 = np.dot(self.W2, A1)
59
           A2 = self.q(Z2)
60
           return A2
```

기본 메소드: 예측

- 클래스
 - 이름: NeuralNetwork
 - 생성자: __init__()
 - 활성화 함수: g()
 - 활성화 함수 미분 : g_prime()
 - 학습 메소드: fit()
 - 순입력: net_input()
 - 예측: predict()

```
44
               self.W1 += np.dot(dZ1, A0.T)
               self.cost .append(np.sqrt(
45
46
                    np.sum(E2 * E2)))
           return self
47
48
49
       def net input(self, X):
           if X.shape[0] == self.w.shape[0]:
50
51
               return np.dot(X, self.w)
52
           else:
53
               return np.dot(X, self.w[1:]) + self.w[0]
54
55
       def predict(self, X):
56
           Z1 = np.dot(self.W1, X)
           A1 = self.q(Z1)
57
58
           Z2 = np.dot(self.W2, A1)
59
           A2 = self.q(Z2)
60
           return A2
```

XOR 신경망 학습



```
1 print("Final prediction of all")
2 A2 = nn.predict(X)
3 for x, yhat in zip(X.T, A2.T):
4  print(x, np.round(yhat, 3))
```



```
1 print("Final prediction of all")
2 A2 = nn.predict(X)
3 for x, yhat in zip(X.T, A2.T):
4  print(x, np.round(yhat, 3))
```



```
Final prediction of all
[0 0] [ 0.048]
[0 1] [ 0.955]
[1 0] [ 0.499]
[1 1] [ 0.501]
```

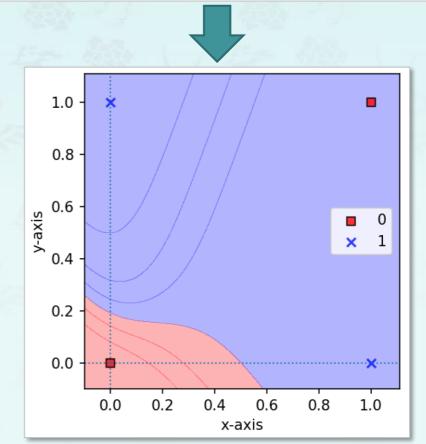
[0, 0, 1, 1],

[0, 1, 0, 1]

 $7 \mid Y = np.array([0, 1, 1, 0])$

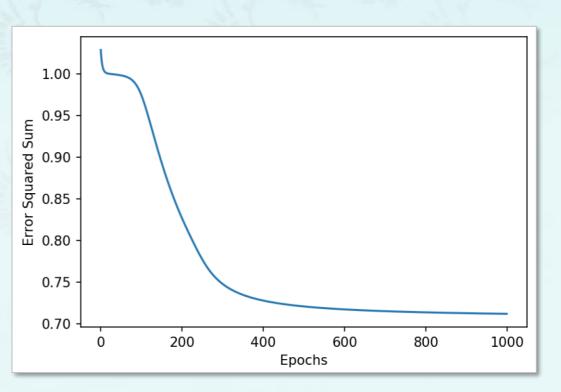
8 nn.fit(X, Y)

joy.plot_decision_regions(X.T, Y,









```
print("Final prediction of all")
A2 = nn.predict(X)
for x, yhat in zip(X.T, A2.T):
    print(x, np.round(yhat, 3))
```



```
1 print("Final prediction of all")
2 A2 = nn.predict(X)
3 for x, yhat in zip(X.T, A2.T):
4  print(x, np.round(yhat, 3))
```



```
Final prediction of all
[0 0] [ 0.077]
[0 1] [ 0.935]
[1 0] [ 0.94]
[1 1] [ 0.043]
```

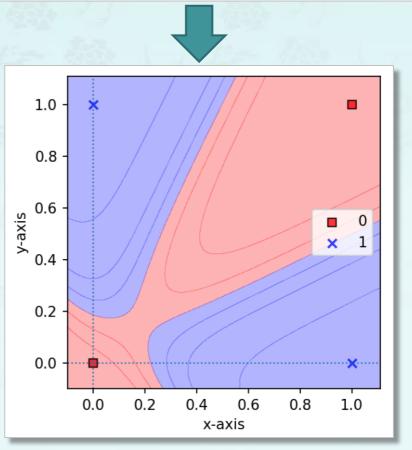
[0, 0, 1, 1],

[0, 1, 0, 1]

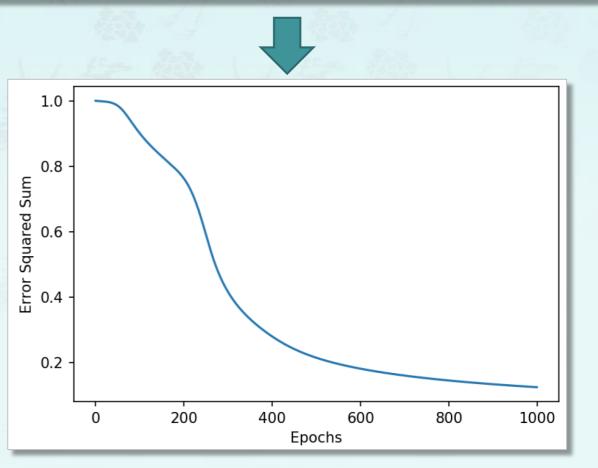
 $7 \mid Y = np.array([0, 1, 1, 0])$

8 nn.fit(X, Y)

joy.plot_decision_regions(X.T, Y,







XOR 신경망

- 학습 정리
 - XOR 신경망을 코드를 이해한다.
 - XOR 신경망의 은닉층의 갯수에 따른 결과를 확인한다.

■ 10-1 다층 신경망의 행렬 모델링

10주차(3/3)

XOR 신경망 구현

파이썬으로배우는기계학습

한동대학교 김영섭교수