### Foundations of Software

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Course material by Martin Odersky,  $\ensuremath{\mathsf{EPFL}}$ 

Slides in part adapted from: University of Pennsylvania CIS 500: Software Foundations - Fall 2006 by Benjamin Pierce

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# Course Overview

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 ${\sf Pronunciation} \qquad \qquad {\sf Dutch/French/Japanese/English}$ 

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# What is "software foundations"?

Software foundations (or "theory of programming languages") is the mathematical study of the  $\frac{1}{2}$  meaning of programs.

The goal is finding ways to describe program behaviors that are both precise and abstract.

- ▶ precise so that we can use mathematical tools to formalize and check interesting properties
- abstract so that properties of interest can be discussed clearly, without getting bogged down in low-level details

### Why study software foundations?

- ➤ To prove specific properties of particular programs (i.e., program verification)
  - ▶ Important in some domains (safety-critical systems, hardware design, security protocols, inner loops of key algorithms, ...), but still quite difficult and expensive
- lacktriangle To develop intuitions for informal reasoning about programs
- ➤ To prove general facts about all the programs in a given programming language (e.g., safety or isolation properties)
- ➤ To understand language features (and their interactions) deeply and develop principles for better language design (PL is the "materials science" of computer science...)

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### What you can expect to get out of the course

- ► A more sophisticated perspective on programs, programming languages, and the activity of programming
  - See programs and whole languages as formal, mathematical objects
  - ▶ Make and prove rigorous claims about them
  - Detailed knowledge of a variety of core language features
- ▶ Deep intuitions about key language properties such as type safety
- ▶ Powerful tools for language design, description, and analysis

Most software designers are language designers!

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#### Greenspun's Tenth Rule Of Programming

Any sufficiently complicated C or Fortran program contains an ad-hoc, informally-specified, bug-ridden, slow implementation of half of Common Lisp.

Philip Greenspun

#### What this course is not

- ► An introduction to programming
- A course on functional programming (though we'll be doing some functional programming along the way)
- A course on compilers (you should already have basic concepts such as lexical analysis, parsing, abstract syntax, and scope under your belt)
- A comparative survey of many different programming languages and styles

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### Approaches to Program Meaning

- Denotational semantics and domain theory view programs as simple mathematical objects, abstracting away their flow of control and concentrating on their input-output behavior.
- Program logics such as Hoare logic and dependent type theories focus on logical rules for reasoning about programs.
- Operational semantics describes program behaviors by means of abstract machines. This approach is somewhat lower-level than the others, but is extremely flexible.
- Process calculi focus on the communication and synchronization behaviors of complex concurrent systems.
- Type systems describe approximations of program behaviors, concentrating on the shapes of the values passed between different parts of the program.

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#### Overview

This course will concentrate on operational techniques and type systems.

- ► Part I: Modeling programming languages
  - ▶ Syntax and parsing
  - ▶ Operational semantics
  - ▶ Inductive proof techniques
  - ▶ The lambda-calculus
  - ▶ Syntactic sugar; fully abstract translations
- ▶ Part II: Type systems
  - ▶ Simple types
  - ▶ Type safety
  - ▶ References
  - Subtyping

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#### Overview

- ▶ Part III: Object-oriented features (case study)
  - ▶ A simple imperative object model
  - ▶ An analysis of core Java
  - ▶ An analysis of core Scala.js IR

Organization of the Course

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# Information

Textbook: Types and Programming Languages,

Benjamin C. Pierce, MIT Press, 2002

Webpage: https://fos-2022.github.io Q&A Ed Discussions via Moodle

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### Elements of the Course

- ▶ The Foundations of Software course consists of
  - ▶ lectures (Tue 14:15-16:00, INF 1)
  - ▶ exercises and project work (Wed 11:15-13:00, INJ 218)
- ▶ The lecture will follow in large parts the textbook.
- ► For lack of time, we cannot treat all essential parts of the book in the lectures, that's why the textbook is required reading for participants of the course.

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### Homework and Projects

You will be asked to

- > solve and hand in some written exercise sheets,
- ▶ do a number of programming assignments, including
  - parsers,
  - $\,\,\vartriangleright\,\,$  interpreters and reduction engines,
  - ▶ type checkers

for a variety of small languages.

▶ The implementation language for these assignments is Scala.

Scala

- Scala is a functional and object-oriented language that is closely interoperable with Java.
- ▶ It is very well suited as an implementation language for type-checkers, in particular because it supports:
  - ▶ pattern matching,
  - higher-order functions,
  - ▶ inheritance and mixins.

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### Learning Scala

If you don't know Scala yet, there's help:

► The Scala web site:

www.scala-lang.org

- ➤ On this site, the documents:
  - $\begin{tabular}{ll} $ \land$ $A$ Brief Scala Tutorial an introduction to Scala for Java programmers. (short and basic). \end{tabular}$

  - $\,\,\vartriangleright\,\, An\,\, Overview\,\, of\,\, the\,\, Scala\,\, Programming\,\, Language$  (high-level).
- ► The assistants.

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### Grading and Exams

Final course grades will be computed as follows:

- ► Homework and project: 40%
- ➤ Final exam: 60%

#### Exams:

 $1. \ \, \mathsf{Final} \,\, \mathsf{exam} \mathsf{:} \,\, \mathsf{to} \,\, \mathsf{be} \,\, \mathsf{announced}$ 

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#### Collaboration

- ► Collaboration on homework is strongly encouraged.
- $\,\blacktriangleright\,$  Studying with other people is the best way to internalize the material
- ➤ Form pair programming and study groups!

  2-3 people is a good size. 4 is too many for all to have equal input.

 $^{\prime\prime}$  You never really misunderstand something until you try to teach it...

" – Anon.

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### Plagiarism

- ▶ A single group will of course share code.
- ▶ But plagiarizing code by other groups as part of a project is unethical and will not be tolerated, whatever the source.

### Part I

# Modeling programming languages

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### Syntax and Parsing

- ► The first level of modeling a programming language concerns its context-free syntax.
- ► Context-free syntax determines a set of legal phrases and determines the (tree-)structure of each of them.
- ▶ It is often given on two levels:
  - ▷ concrete: determines the exact (character-by-character) set of legal phrases
  - □ abstract: concentrates on the tree-structure of legal phrases.
- ▶ We will be mostly concerned with abstract syntax in this course.
- ▶ But to be able to write complete programming tools, we need a convenient way to map character sequences to trees.

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### Approaches to Parsing

There are two ways to construct a parser:

- ▶ By hand Derive a parser program from a grammar.
- ► Automatic Submit a grammar to a tool which generates the parser

In the second approach, one uses a special grammar description language to describe the input grammar.

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### Domain-Specific Languages

- ► The grammar description language is an example of a domain-specific language (DSL).
- ➤ The parser generator acts as a processor ("compiler") for this language — that's why it's sometimes called grandly a "compiler-compiler".
- ▶ Example of a "program" in the grammar description DSL:

```
 \begin{array}{lll} \mathsf{Expr} & ::= \mathsf{Term} \ \{'+' \ \mathsf{Term} \ | \ '-' \ \mathsf{Term} \}. \\ \mathsf{Term} & ::= \mathsf{Factor} \ \{'*' \ \mathsf{Factor} \ | \ '/' \ \mathsf{Factor} \}. \\ \mathsf{Factor} & ::= \mathsf{Number} \ | \ '(' \ \mathsf{Expr} \ ')'. \end{array}
```

### Embedded Domain-Specific Languages

- ▶ An alternative to a stand-alone DSL is an Embedded DSL.
- Here, the DSL does not exist as a separate language but as an API in a host language.
- ► The host language is usually a general purpose programming language.

We will now develop this approach for grammar description languages.

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### An EDSL for Parsing in Scala

```
\begin{array}{lll} \mathsf{def}\;\mathsf{expr}\; : \mathsf{Parser}[\mathsf{Any}] = \mathsf{term}\; \mathsf{"rep}("+"\; \mathsf{`term}\; |\; "-"\; \mathsf{`term}) \\ \mathsf{def}\;\mathsf{term}\; : \mathsf{Parser}[\mathsf{Any}] = \mathsf{factor}\; \mathsf{``rep}("*"\; \mathsf{``factor}\; |\; "/"\; \mathsf{``factor}) \\ \mathsf{def}\;\mathsf{factor}: \mathsf{Parser}[\mathsf{Any}] = "("\; \mathsf{``expr}\; \mathsf{``"})"\; |\; \mathsf{numericLit} \end{array}
```

A small Perl hack could derive the above code from the informal grammar definition above:

- ▶ Insert a def at the beginning of each production.
- $\blacktriangleright \ \, \text{The "::=" becomes ": Parser[Any] ="}.$
- ➤ Sequential composition is now expressed by a ~.
- ▶ Repetition {...} is now expressed by rep(...).
- $\blacktriangleright$  Option [...] is now expressed by  $\mathsf{opt}(...).$

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#### Parser Combinators

► The differences between Grammar A and Grammar B are fairly minor.

(Note in particular that existing DSLs for grammar descriptions also tend to add syntactic complications to the idealized Grammar A we have seen).

- ➤ The important difference is that Grammar B is a valid Scala program, when combined with an API that defines the necessary primitives.
- ▶ These primitives are called parser combinators.

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#### The Basic Idea

For each language (identified by grammar symbol S), define a function  $f_S$  that, given an input stream i,

- ▶ if a prefix of i is in S, return Success(Pair(x, i')) where x is a result for S and i' is the rest of the input.
- otherwise, return Failure(msg, i) where msg is an error message string.

The first behavior is called  ${\it success}$ , the second  ${\it failure}$ .

### The Basic Idea in Code

#### Assume:

```
class StandardTokenParsers {
    type Parser = Input ⇒ ParseResult

where

type Input = Reader[Token] // a stream of Tokens with positions.

and we assume a class Token with subclasses

▷ case class Keyword(chars: String) for keywords,

▷ case class NumericLit(chars: String) for numbers,

▷ case class StringLit(chars: String) for strings,

▷ case class Identifier(chars: String) for identifiers.
```

Also assume a class  $\mathsf{ParseResult}[\mathsf{T}]$  with subclasses

```
\label{eq:case_class_success} $$\operatorname{Case}_{T}(\operatorname{result}: T, \operatorname{in}: \operatorname{Input})$ extends $\operatorname{ParseResult}[T]$ $$\operatorname{case}_{t}: \operatorname{Case}_{t}: \operatorname
```

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# Object-Oriented Parser Combinators

- ▶ In fact, we will also need to express | and ~ as methods of parsers.
- ▶ That's why we extend the function type of parsers as follows:

```
abstract class Parser[T] extends (Input \Rightarrow ParseResult[T]) { // An unspecified method that defines the parser function. def apply(in: Input): ParseResult[T] // A parser combinator for sequential composition def ^{\circ} ... // A parser combinator for alternative composition def | ... }
```

It remains to define concrete combinators that implement this class (see below).  $% \begin{center} \end{center} \$ 

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### A Generic Single-Token Parser

- ► The following parser succeeds if the first token in the input satisfies a given predicate p.
- ▶ If it succeeds, it reads the token string and returns it as a result.

```
\begin{array}{l} \mathsf{def}\;\mathsf{token}(\mathsf{kind}:\mathsf{String})(\mathsf{p}\colon\mathsf{Token}\Rightarrow\mathsf{boolean}) = \mathsf{new}\;\mathsf{Parser}[\mathsf{String}]\; \{ \\ \mathsf{def}\;\mathsf{apply}(\mathsf{in}:\mathsf{Input})\colon\mathsf{ParseResult}[T] = \\ \mathsf{if}\;(\mathsf{p}(\mathsf{in}.\mathsf{head}))\;\mathsf{Success}(\mathsf{in}.\mathsf{head}.\mathsf{chars},\;\mathsf{in}.\mathsf{tail}) \\ \mathsf{else}\;\mathsf{Failure}(\mathsf{kind}+"\;\mathsf{expected}",\;\mathsf{in}) \\ \} \end{array}
```

### Specific Single-Token Parsers

- ➤ The following parser succeeds if the first token in the input is the given keyword chars:
- ▶ If it succeeds, it returns a keyword token as a result.

```
\label{eq:continuity} \begin{split} & \text{implicit def keyword(chars: String): Parser[String] = token("""+chars+""") } \left\{ & \text{case Keyword(chars1)} \Rightarrow \text{chars} == \text{chars1} \\ & \text{case } \bot \Rightarrow \text{false} \\ \right\} \end{split}
```

 Note that keyword is marked implicit, so that you can usually write "if" instead of keyword("if").

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The following parsers succeed if, respectively, the first token in the input is a numeric or string literal, or an identifier.

```
\label{eq:defnumericLit} \begin{split} & \mathsf{def} \ \mathsf{numericLit} = \mathsf{token}("\mathsf{number"})(\_\mathsf{isInstanceOf}[\mathsf{NumericLit}]) \\ & \mathsf{def} \ \mathsf{stringLit} = \mathsf{token}("\mathsf{string} \ \mathsf{literal"})(\_\mathsf{isInstanceOf}[\mathsf{StringLit}]) \\ & \mathsf{def} \ \mathsf{ident} = \mathsf{token}("\mathsf{identifier"})(\_\mathsf{isInstanceOf}[\mathsf{Identifier}]) \end{split}
```

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# The Sequence Combinator

- $\blacktriangleright$  The sequence combinator P ~ Q succeeds if P and Q succeed sequentially, and returns the concatenation of their results.
- ▶ " is implemented as a method of class Parser.

```
abstract class Parser[T] {  \begin{tabular}{ll} def & $ [U](q: Parser[U])$: $Parser[T & U] = new Parser[T & U]$ { \\ def apply(in: Input)$: $ParseResult[T & U] = Parser.this(in)$ match { \\ case Success(x, in1) \Rightarrow & q(in1)$ match { \\ case Success(y, in2) \Rightarrow Success(new & (x, y), in2)$ case failure <math>\Rightarrow failure \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ &
```

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#### Concatenating Results

The  $\tilde{\ }$  combinator returns the results of the two parsers that are run sequentially wrapped in a  $\tilde{\ }$  -object.

The case class  $\tilde{\ }$  is similar to Pair (but  $\tilde{\ }$  turns out to be nicer – see below).

```
case class ~[T, U](_1: T, _2: U) { override def toString = "("+ _1+" ~ "+ _2 +")" }
```

There are also two variants of  $\tilde{\ }$  which return only the left or only the right operand:

```
P < ^{\sim} Q // returns only P's result P \sim Q // returns only Q's result
```

#### The Alternative Combinator

- $\blacktriangleright$  The alternative combinator  $P \mid Q$  succeeds if either P or Q succeeds
- ▶ It returns the result of P if P succeeds, or the result of Q, if Q succeeds.
- The alternative combinator is implemented as a method of class Parser.

```
 \begin{array}{l} \mathsf{def} \ | \ (q \colon \Rightarrow \mathsf{Parser}[T]) \colon \mathsf{Parser}[T] = \mathsf{new} \ \mathsf{Parser}[T] \ \{ \\ \mathsf{def} \ \mathsf{apply}(\mathsf{in} \colon \mathsf{Input}) \colon \mathsf{ParseResult}[T] = \mathsf{Parser.this}(\mathsf{in}) \ \mathsf{match} \ \{ \\ \mathsf{case} \ \mathsf{s1} \ @ \ \mathsf{Success}(\neg, \neg) \Rightarrow \mathsf{s1} \\ \mathsf{case} \ \mathsf{failure} \Rightarrow \mathsf{q}(\mathsf{in}) \\ \} \\ \} \end{array}
```

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#### Failure And Success Parsers

The parser failure(msg) always fails with the given error message. It is implemented as follows:

```
\begin{array}{l} \mathsf{def} \ \mathsf{failure}(\mathsf{msg} : \mathsf{String}) \colon \mathsf{Parser}[\mathsf{Nothing}] = \mathsf{new} \ \mathsf{Parser}[\mathsf{Nothing}] \ \{ \\ \mathsf{def} \ \mathsf{apply}(\mathsf{in} : \mathsf{Input}) \colon \mathsf{ParseResult}[\mathsf{Nothing}] = \mathsf{Failure}(\mathsf{msg}, \ \mathsf{in}) \\ \} \end{array}
```

► The parser success(result) always succeeds with the given result. It does not consume any input. It is implemented as follows:

```
 \begin{array}{ll} \mathsf{def} \ \mathsf{success}[T](\mathsf{result} \colon T) \colon \mathsf{Parser}[T] = \mathsf{new} \ \mathsf{Parser}[T] \ \{ \\ \mathsf{def} \ \mathsf{apply}(\mathsf{in} \colon \mathsf{Input}) \colon \mathsf{ParseResult}[T] = \mathsf{Success}(\mathsf{result}, \, \mathsf{in}) \\ \} \end{array}
```

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# Result Conversion

The parser  $P \ \hat{} f$  succeeds iff P succeeds. In that case it returns the result of applying f to the result of P.

```
 \begin{array}{l} \mathsf{def} \, {}^{\smallfrown} \, [U](f\colon T \Rightarrow U) \colon \mathsf{Parser}[U] = \mathsf{new} \, \mathsf{Parser}[U] \; \{ \\ \mathsf{def} \, \mathsf{apply}(\mathsf{in} \colon \mathsf{Input}) \colon \mathsf{ParseResult}[U] = \mathsf{Parser.this}(\mathsf{in}) \, \, \mathsf{match} \; \{ \\ \mathsf{case} \, \mathsf{Success}(x, \, \mathsf{in1}) \Rightarrow \mathsf{Success}(f(x), \, \mathsf{in1}) \\ \mathsf{case} \, f \Rightarrow f \\ \} \end{array}
```

A variant  $\hat{\ \ }\hat{\ \ }$  takes a value V as right hand side argument.

It returns  $\boldsymbol{V}$  if the left hand parser succeeds:

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#### Option and Repetition Combinators

 $\blacktriangleright$  The  $\mathsf{opt}(P)$  combinator always succeeds and returns an Option result.

It returns  $\mathsf{Some}(R)$  iff P succeeds with R. In case of failure, the result is None.

 $\begin{tabular}{ll} \hline \begin{tabular}{ll} \hline \end{tabular} & \end{tabula$ 

The two combinators are implemented as follows:

```
 \begin{array}{ll} \mathsf{def}\;\mathsf{opt}[T](p\colon\mathsf{Parser}[T])\colon\mathsf{Parser}[\mathsf{Option}[T]] &= \\ p \; \widehat{}^{\wedge}\;\mathsf{Some} \; |\; \mathsf{success}(\mathsf{None}) \\ \mathsf{def}\;\mathsf{rep}[T](p\colon\mathsf{Parser}[T])\colon\mathsf{Parser}[\mathsf{List}[T]] &= \\ p \; \widehat{}^{\;}\;\mathsf{rep}(p) \; \widehat{}^{\wedge}\; \{\; \mathsf{case}\; \mathsf{x} \; \widehat{}^{\;}\; \mathsf{xs} \; \Rightarrow \mathsf{x} \; \colon \colon \mathsf{xs} \; \} \; |\; \mathsf{success}(\mathsf{List}()) \\ \end{array}
```

Note that neither of these combinators can fail!

### The Interleaved Repetition Combinator

The  $\operatorname{repsep}(P,\,Q)$  parser parses a (possibly empty) sequence

```
P\ Q\ P\ ...\ Q\ P
```

It returns a list of all results returned by P.

 $\begin{tabular}{ll} \textbf{Example: repsep(ident, ",") parses a list of identifiers separated by commas.} \end{tabular}$ 

The repsep combinator is implemented as follows:

```
\begin{array}{ll} \mathsf{def}\;\mathsf{repsep}[\mathsf{T},\;\mathsf{U}](\mathsf{p}\colon\mathsf{Parser}[\mathsf{T}],\;\mathsf{q}\colon\mathsf{Parser}[\mathsf{U}])\colon\mathsf{Parser}[\mathsf{List}[\mathsf{T}]] \;=\; \\ \mathsf{p}\;\;\tilde{}\;\mathsf{rep}(\mathsf{q}\;\tilde{}\;\;\mathsf{>}\;\mathsf{p})\;\;\hat{}\;\;\{\;\mathsf{case}\;\mathsf{r}\;\;\tilde{}\;\;\mathsf{rs}\;\;\mathsf{>}\;\mathsf{r}\;\colon\mathsf{rs}\;\;\}\;\;|\;\;\mathsf{success}(\mathsf{List}()) \end{array}
```

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#### Other Combinators

More combinators can be defined if necessary.

**Exercise:** Implement the rep1(P) parser combinator, which applies P one or more times.

Exercise: Define opt and rep directly, without making use of  $\tilde{\ }$ ,  $\ |\$ , and empty.

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# An Example: JSON

 $\ensuremath{\mathsf{JSON}},$  or  $\ensuremath{\mathsf{JavaScript}}$  Object Notation, is a popular data interchange format.

JSON data essentially consists of objects  $\{...\},$  arrays [...], numbers, and strings.

Here is an example of a JSON value:

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#### A JSON parser

```
package examples.parsing
// import the standard parser class
import scala.util.parsing.combinator.syntactical.StandardTokenParsers
object JSON extends StandardTokenParsers {

// fix some delimiter symbols ...
lexical.delimiters += (" {", " }", " [", "]", ":")

// ... and some reserved words
lexical.reserved += ("null", "true", "false")

// here are the four productions making up the JSON grammar
def obj : Parser[Any] = " {" " repsep(member.",") " " "}
def arr : Parser[Any] = " [" " repsep(value, ",") " " "]
def member: Parser[Any] = stringLit " " " value
def value : Parser[Any] = stringLit " numericLit | obj | arr |

"null" | "true" | "false"
```

# Testing the JSON Parser

Add a method main that can be used to test the parser.

```
\label{eq:def-main} \begin{split} & \text{def main(args: Array[String]): Unit} = \{ \\ & \text{val tokens} = \text{new lexical.Scanner(args(0))} \\ & \text{println(args(0))} \\ & \text{println(phrase(value)(tokens))} \\ \} \\ & \text{Here are two test runs:} \\ & > \text{java examples.parsing.JSON "} \{ \text{"x": true, "y": [1, 2, 3] } \} \\ & \{ \text{x: true, y: [1, 2, 3] } \} \\ & [1.26] \text{ parsed: (({\{ \text{``} \text{List(((x \text{``:}) \text{``} \text{true}), ((y \text{``:}) \text{``} (([[ \text{``} \text{List(1, 2, 3)) \text{``}})))) \text{``} } ))} \end{split}
```

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# Getting Better Output

- ➤ The result of the previous JSON parser was a tree containing all input tokens (slightly chaotically).
- ▶ We transform the productions using the ^^ combinator to get more structured output:

```
\label{eq:def-obj} \begin{array}{ll} \text{def obj} & : \mathsf{Parser}[\mathsf{Any}] = // \mathsf{return \ a \ Map} \\ \text{``'['' \ ^\sim \mathsf{rep}(\mathsf{member}) \ <^-'']'' \ ^^ (\mathsf{ms} \Rightarrow \mathsf{Map}() \ ++ \ \mathsf{ms}) \\ \text{def arr} & : \mathsf{Parser}[\mathsf{Any}] = // \mathsf{return \ a \ List} \\ \text{``['' \ ^\sim \mathsf{rep}(\mathsf{value}) <^-'']''} \\ \text{def member} : \mathsf{Parser}[\mathsf{Any}] = // \mathsf{return \ a \ name/value \ pair} \\ \text{stringLit `` ''' \ '' value } ^^ \\ \text{{case name } `` '' :'' \ ^\sim \mathsf{value} \Rightarrow (\mathsf{name, value}) \ } \end{array}
```

Question: What are more precise types for obj, arr, and member?

### Table of Parser Combinators

```
ident
                      identifier
\mathsf{keyword}(...)
                      keyword or special symbol (implicit)
numericLit
                      integer number
stringLit
                      string literal
P ~ Q
                      sequential composition
P < ~ Q, P ~> Q
                      sequential composition; keep left/right only
P | Q
                      alternative
\mathsf{opt}(\mathsf{P})
                      option
rep(P)
                      repetition
repsep(P, Q)
P ^^ f
P ^^^ v
                      interleaved repetition
                      result conversion
                      constant result
```

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### Arithmetic Expressions Again

Here is the full parser for arithmetic expressions:

```
\begin{split} & \text{object Arithmetic extends StandardTokenParsers } \\ & \text{lexical.delimiters } ++= \text{List}("(",")","+","-","*","/") \\ & \text{def expr: Parser[Any]} = \text{term } \texttt{"} \text{ rep}("+" \texttt{"} \text{ term } | "-" \texttt{"} \text{ term}) \\ & \text{def term: Parser[Any]} = \text{factor } \texttt{"} \text{ rep}("*" \texttt{"} \text{ factor } | "/" \texttt{"} \text{ factor}) \\ & \text{def factor: Parser[Any]} = "(" \texttt{"} \text{ expr} \texttt{"} ")" \mid \text{numericLit} \end{split}
```

Question: How can we make it evaluate the parsed expression?

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# A Problem with Top-Down Parsing

As parser combinators work top-down, they don't allow left-recursion. A production like

```
\mathsf{def}\;\mathsf{expr}=\mathsf{expr}\;\tilde{\ }"-"\;\tilde{\ }\mathsf{term}
```

would go into an infinite recursion when executed.

The alternative:

```
\label{eq:defexp} \begin{split} \text{def expr} &= \text{term "rep("-" " term)} \\ \text{produces a "right-leaning" tree: } X - Y - Z \text{ parses} \\ X ^ \text{``List("-" "Y, "-" "Z)} \end{split}
```

But the correct reduction/evaluation of +,-,\*,/ is left-leaning!

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#### Evaluate by FoldLeft

We can solve this problem by delaying reduction until all elements of a repetition have been parsed and then performing a fold left on the list:

```
\begin{split} & \mathsf{def} \; \mathsf{expr} \; : \mathsf{Parser[Int]} = \\ & \mathsf{term} \; " \; \mathsf{rep} \; ("+" \; " \; \mathsf{term} \; | "-" \; " \; \mathsf{term}) \; {}^{\smallfrown} \; \mathsf{reduceList} \\ & \mathsf{def} \; \mathsf{term} \; : \; \mathsf{Parser[Int]} = \\ & \mathsf{factor} \; " \; \mathsf{rep} \; ("*" \; " \; \mathsf{factor} \; | "/" \; " \; \mathsf{factor}) \; {}^{\smallfrown} \; \mathsf{reduceList} \\ & \mathsf{def} \; \mathsf{factor} : \; \mathsf{Parser[Int]} = \\ & " \; (" \; "> \; \mathsf{expr} < " \; ")" \; | \; \mathsf{numericLit} \; {}^{\smallfrown} \; ( \ldots \mathsf{tolnt}) \end{split}
```

Here, reduceList is defined using foldLeft

```
\label{eq:value_problem} \begin{array}{l} \mathsf{val} \ \mathsf{reduceList} \colon \mathsf{Expr} \ \tilde{\ } \ \mathsf{List}[\mathsf{String} \ \tilde{\ } \ \mathsf{Expr}] \Rightarrow \mathsf{Expr} = \{ \\ \mathsf{case} \ \mathsf{i} \ \tilde{\ } \ \mathsf{ps} \Rightarrow \mathsf{ps.foldLeft}(\mathsf{i})(\mathsf{reduce}) \\ \} \end{array}
```

... and reduce is defined as follows:

```
\label{eq:case problem} \begin{array}{l} \text{def reduce}(x\colon Int, \, r\colon String\ ^{\circ}\ Int)\colon Int = r\ \mathsf{match}\ \{\\ & \text{case}\ ^{\circ}+^{\circ}\ ^{\circ}\ y \Rightarrow x + y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x - y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ ^{\circ}\ y \Rightarrow x / y\\ & \text{case}\ ^{\circ}-^{\circ}\ y \Rightarrow x / y
```

java examples.parsing.ArithmeticParsers1 " 2\*(3+7) " 2\*(3+7) [1.12] parsed : 20

(Note: the chainl combinator in the parsing library does this for you.)

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### Conclusion

- Parser combinators provide a concise, flexible, and high-level way to construct parsers.
- ► The token classes of a context-free grammar are modeled as primitive parsers.
- ▶ The combination forms are modeled as higher-order parsers.
- ▶ Parser combinators are an example of an embedded DSL.
- ▶ By contrast, classical parser generators are stand-alone DSLs.
- Advantage of an embedded DSL over a parser generator: it is easier to connect the results of parser combinators with the environment.
- ▶ Disadvantage: lower efficiency but this can be overcome (using packrat parsing)