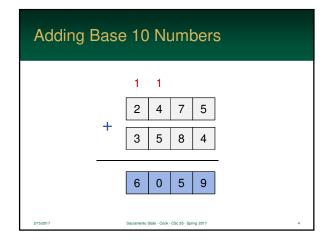
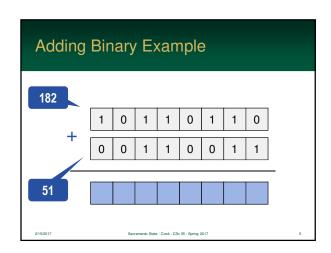
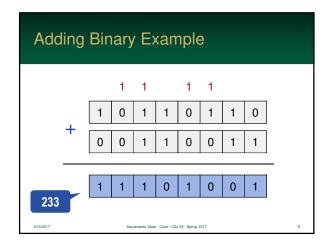
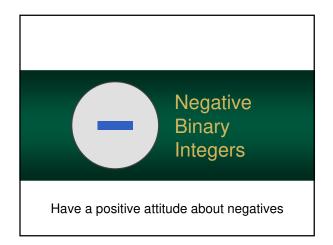


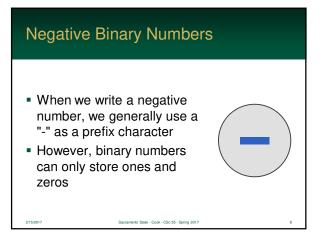
Computer's add binary numbers the same way that we do with decimal Columns are aligned, added, and "1's" are carried to the next column In computer processors, this component is called an adder



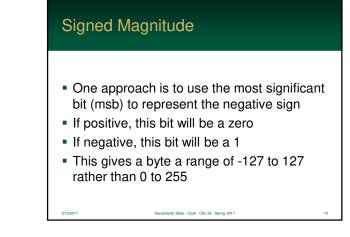


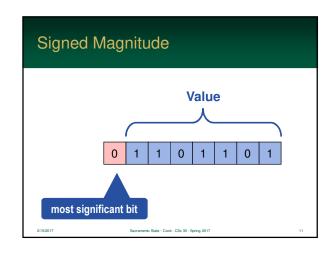


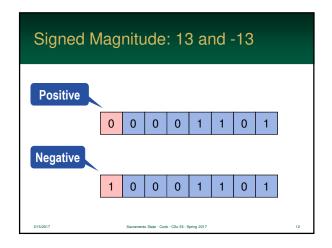




Negative Binary Numbers So, how we store a negative a number? When a number can represent both positive and negative numbers, it is called a signed integer Otherwise, it is unsigned



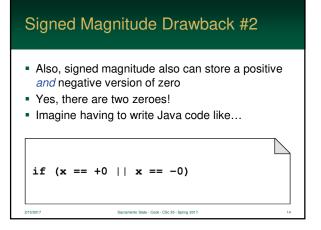


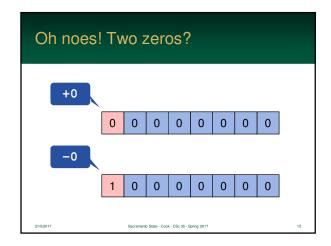


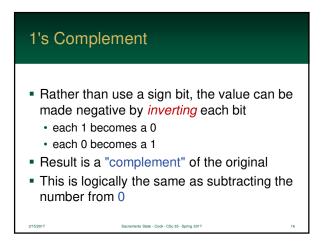
Signed Magnitude Drawback #1

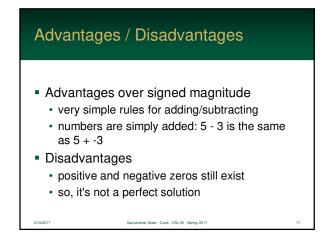
- When two numbers are added, the system needs to check and sign bits and act accordingly
- For example:
 - if both numbers are positive, add values
 - if one is negative subtract it from the other
 - etc
- There are also rules for subtracting

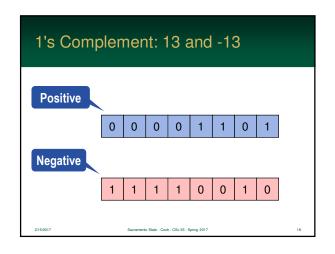
2/15/2017

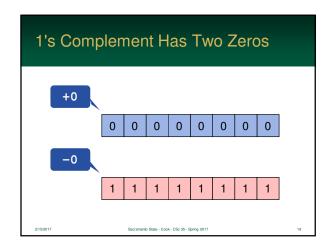


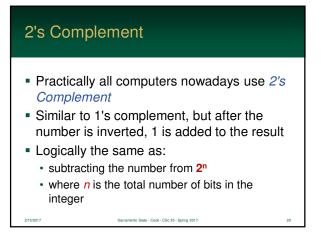




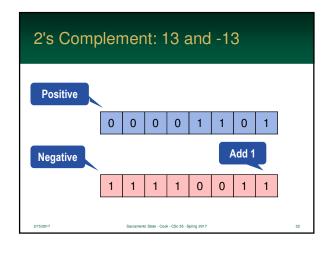


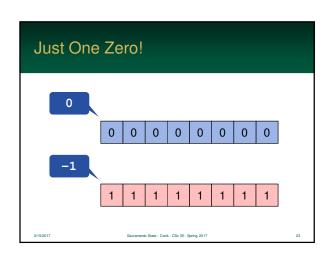


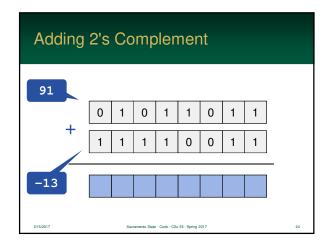


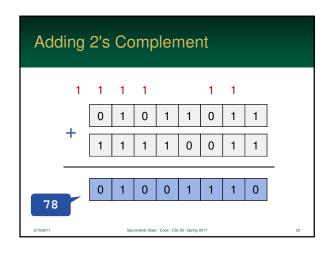


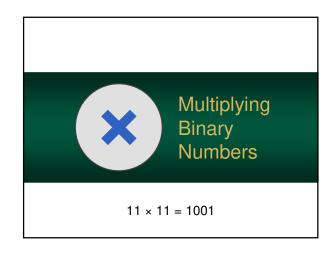












Multiplying Binary Numbers

- Many processors today provide complex mathematical instructions
- However, the processor only needs to know how to add
- Historically, multiplication was performed with successive additions



Sacramento State - Cook - CSc 35 - Spring 2017

Multiplying Scenario

- Let's say we have two variables: A and B
- Both contain integers that we need to multiply
- Our processor can only add (and subtract using 2's complement)
- How do we multiply the values?

2/15/20

Sacramento State - Cook - CSc 35 - Spring 2017

Multiplying: The Bad Way



- One way of multiplying the values is to create a For Loop using one of the variables – A or B
- Then, inside the loop, continuously add the other variable to a running total

Sacramento State - Cook - CSc 35 - Spring 2017

Multiplying: The Bad Way

```
total = 0;
for (i = 0; i < B; i++)
{
   total += A;
}</pre>
```

Multiplying: The Bad Way

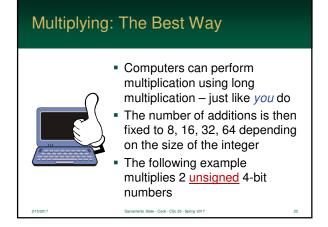
- If one of the operands A or B

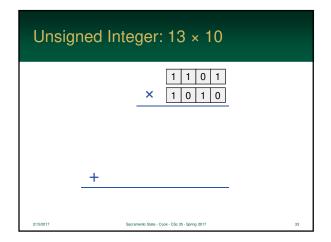
 is large, then the computation could take a long time
- This is incredibly inefficient
- Also, given that A and B could contain drastically different values – the number of iterations would vary
- Required time is not constant

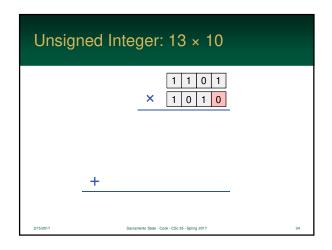
2/15/2017

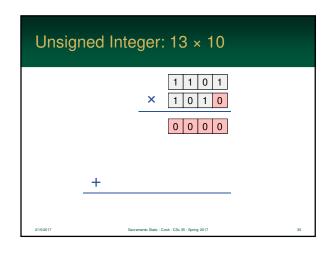
Sacramento State - Cook - CSc 26 - Soving 201

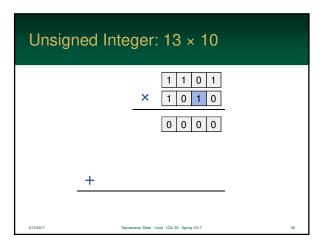


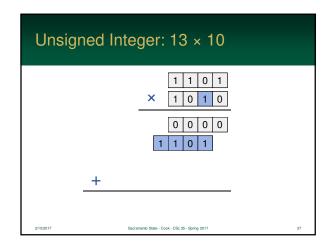


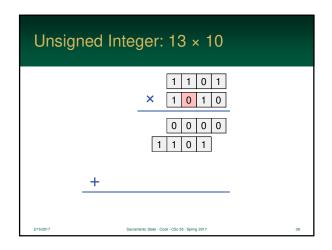


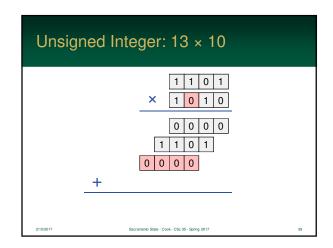


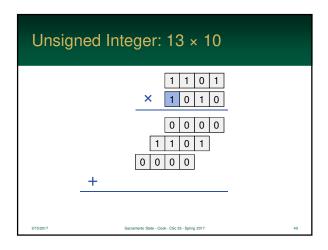


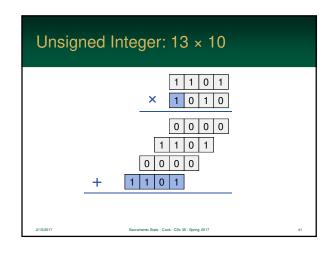


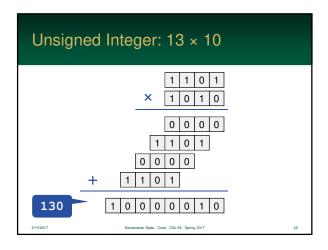










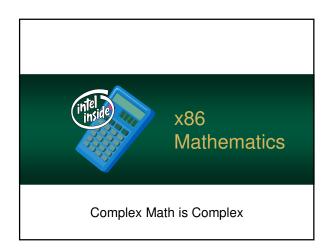


Multiplication Doubles the Bit-Count

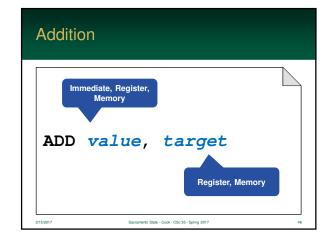
- When two numbers are multiplied, the product will have twice the number of digits
- Examples:
 - 8-bit × 8-bit → 16-bit
 - 16-bit × 16-bit → 32-bit
- Often processors...
 - · will store the result in the original bit-size
 - and flag an overflow if it does not fit

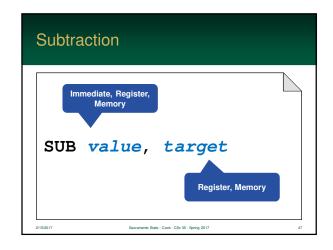
15/2017

Sacramento State - Cook - CSc 35 - Spring 2017

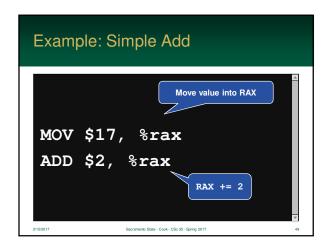


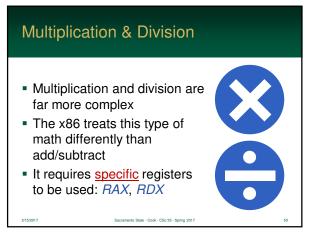
The Add and Subtract instructions take two operands and store the result in the second operand This is the same as the += and -= operators used in Visual Basic .NET, C, C++, Java, etc...

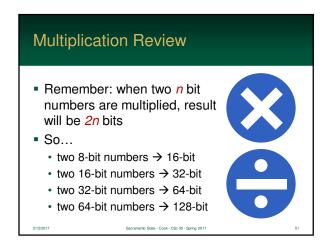


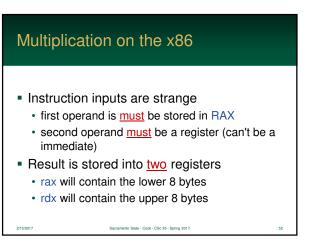


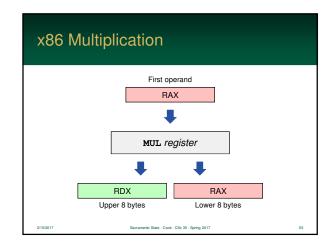


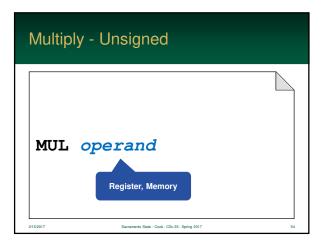


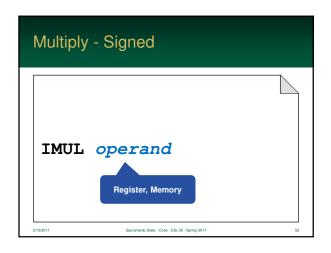


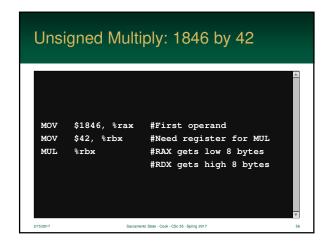












Multiplication Tips

- Even though you are just using RAX as input, both RAX and RDX will change
- Be aware that you might lose important data, and backup to memory if needed



2/15/2017

acramento State - Cook - CSc 35 - Spring 2017

Additional x86 Multiply Instructions

- x86 also contains versions of the IMUL instruction that take multiple operands
- Allows "short" multiplication just stored in 1 register
- Please note: these do <u>not</u> exist for MUL



2017 Sacramento State - Cook - CSc 3

IMUL (few more combos)

IMUL immediate, reg

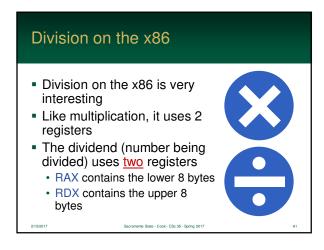
IMUL memory, reg

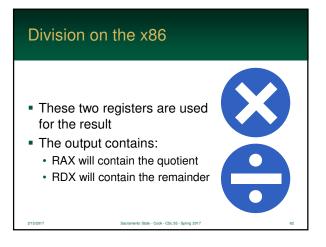
IMUL reg, reg

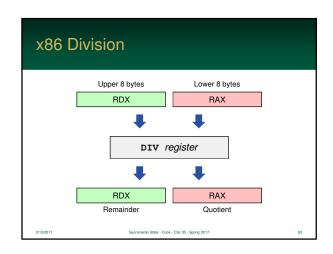
2/15/2017 Sacramento State - Cook - CSc 35 - Spring 2017

Signed Multiply: 1846 by 42



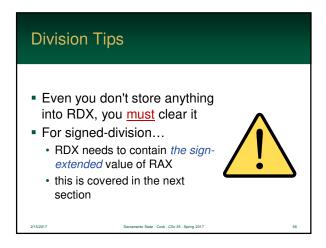














Multiplying Rules

- Sign Magnitude
 - create a new sign that is a XOR of the old ones
 - · clear the old sign bits and expand with zeros
- 2's complement
 - both values must be expanded to the destination size (twice the original)
 - this must be done beforehand
 - · otherwise the result will be incorrect

2017

Extending Unsigned Integers

- Often in programs, data needs to moved to a integer with a larger number of bits
- For example, an 8-bit number is moved to a 16-bit representation



2/15/2017

Sacramento State - Cook - CSc 35 - Spring 2017

Extending Unsigned Integers

- For unsigned numbers is fairly easy – just add zeros to the left of the number
- This, naturally, is how our number system works anyway: 000456 = 456



2/15/2017

Sacramento State - Cook - CSc 35 - Spring 2017

Unsigned 13 Extended 0 0 0 0 1 1 0 1 0 0 0 0 0 0 1 1 0 1 2150017 Secremento State - Cook - Clic 35 - Spring 2017 75

Extending Signed Integers

- When the data is stored in a signed integer, the conversion is a little more complex
- Simply adding zeroes to the left, will convert a negative value to a positive one
- Each type of signed representation has its own set of rules

2/15/201

Sacramento State - Cook - CSc 35 - Spring 2017

