

## Software Solutions for the Critical Section Problem with $N$ Processes

- Eisenberg and McGuire's Algorithm for  $N$  processes, where  $N \geq 2$ .
- Bakery Algorithm for  $N$  Processes, where  $N \geq 2$ .
- Note: Peterson's solution (given in our text book) can be used only for two cooperating processes, like a producer process and a consumer process.

## Eisenberg and McGuire's Algorithm for $N$ processes

- Shared variables:  
`enum pstate {idle, want_in, in_cs};`  
`pstate flag[n];` // initialized to idle  
`int turn;` // initialized to any value in  $[0, n-1]$
- The first contending process in the cyclic order ( $P_{\text{turn}}, P_{\text{turn}+1}, \dots, P_{n-1}, P_0, \dots, P_{\text{turn}-1}$ ) will enter the critical section.

## Eisenberg and McGuire's Algorithm (cont'd)

- **Structure of Process  $P_i$**

```
do {
    while (true) {
        flag[ i ] = want_in;
        int j = turn;

        while (j != i) {
            if (flag[ j ] != idle)
                j = turn; /* to repeat scan from P_turn to P_i */
            else j = (j + 1) % n;
        }

        flag[i] = in_cs; /* flag[ i ] == in_cs doesn't imply
                           turn == i or only P_i is in in_cs */

        j = 0;
        while ( (j < n) && (j == i || flag[ j ] != in_cs)) j++;
        if ( (j >= n) && (turn == i || flag[turn] == idle))
            break;
    }

    turn = i;
```

```
// critical section
j = (turn + 1) % n;
while (flag[ j ] == idle)
    j = (j + 1) % n;
turn = j;
flag[ i ] = idle;
// remainder section
} while(true);
```

## Eisenberg and McGuire's Algorithm (cont'd)

- It is possible that more than one process has *in\_cs* state.
  - Suppose there are 5 processes ( $P_0, P_1, P_2, P_3, P_4$ ) and *turn* is 1. Initially all the processes are in *idle* state.
  - $P_4$  executes the 2nd while statement and its state becomes *in\_cs*.
  - Shortly after that,  $P_3$  executes the 2nd while statement and its state also becomes *in\_cs*.
  - Both  $P_4$  and  $P_3$  execute their 3rd while statement and find each other in *in\_cs* state. So, they will escape their 3rd while statement (with  $j < n$ ) and start their entry sections all over again.
  - In this 2nd iteration of the entry section,  $P_4$  will find that  $P_3$  is not idle, so  $P_4$  cannot change its state from *want\_in* to *in\_cs*. On the other hand,  $P_3$  will change its state from *want\_in* to *in\_cs*, then breaks out of the 1st while statement and set *turn*=3.
    - Before  $P_3$  breaks out of the 1st while statement, it checks whether it has the *turn* or  $P_{turn}$  is still idle.
- After a process, say  $P_i$ , finishes its critical section, it will scan the states of other processes, starting from process  $P_{i+1}$  (in cyclic order), and the *turn* will be given to the first non-idle process.
  - If all other processes are idle when  $P_i$  finishes its critical section, the *turn* will remain as  $i$ .

## Bakery Algorithm for $N$ Processes

- Before entering its critical section, each process picks up a ticket number, that is  $(1 + \text{the largest ticket number assigned to some other process})$ . A process that holds the smallest positive number will enter the critical section.
- The numbers picked up by the processes that want to enter their critical sections are monotonically increasing; e.g., 1, 2, 3, 3, 3, 3, 4, 5, ... . That means, two or more processes may pick up the same number.
- Suppose that processes  $P_i$  and  $P_j$  have picked up the same number. In that case, their process ids are used as a tie-breaker:
  - If  $i < j$ , then  $P_i$  enters its critical section first; otherwise  $P_j$  enters its critical section first.

## Bakery Algorithm (cont'd)

- Notation  $<$  is used for lexicographical ordering of different pairs of (ticket #, process id).
  - $(a, b) < (c, d)$  if  $a < c$ , or if  $a = c$  and  $b < d$
- $\max(a_0, \dots, a_{n-1})$  is a number  $k$ , such that  $k \geq a_i$  for  $i = 0, \dots, n-1$ .
- Shared variables:
  - boolean choosing[n];** // initialized to false
  - int number[n];** // initialized to 0
  - choosing[i] is true when process  $P_i$  wants to enter its critical section but has not picked up a number yet.

## Bakery Algorithm (cont'd)

- Structure of Process  $P_i$

```
do {
    choosing[i] = true;
    number[i] = max(number[0], number[1], ... ,
                    number [n-1]) + 1;
    choosing[i] = false;
    for (j = 0; j < n; j++) {
        while (choosing[ j]) ; /* busy waiting until Pj
                               picks up a ticket number */
        while ((number[ j] != 0) && ((number[ j], j) <
                                     number[ i], i))) ; /* busy waiting until
                                                         Pi has higher priority than Pj */
    }
    // critical section
    number[ i] = 0;
    // remainder section
} while (true);
```