

# Apprentissage machine: projet applications en recherche clinique

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# Plan

Survival Super Learner (SL)

SL for analyzing RCT

SL for predicting time-to-cure

SL for time-dependent propensity scores



## The problematic of the method choice for survival prediction

- ▶ The prediction of the probability that a subject experienced an event is often of interest.
- ▶ Several regressions can be used for right-censored data. :
  - ▶ Most of the studies use proportional hazard (PH)-based assumption.
  - ▶ Other models such as accelerated failure time (AFT) approaches are not frequent.
- ▶ Machine learning is increasingly used and avoids such modeling assumptions :
  - ▶ Random survival forests.
  - ▶ Survival neural networks.
  - ▶ Support-vector machines.
  - ▶ Etc.



# A super learner (SL) allows us to combine regressions and algorithms

- ▶ In 2011, Polley and van der Laan proposed a survival SL (right censoring).<sup>1</sup>
- ▶ Two R packages are available :
  - ▶ The first one was proposed by Golmakani et al. (2020). It allows us to obtain the linear predictor of a PH regression.
  - ▶ The second one was developed by Westling et al. (2021) with additional learners : several parametric PH models, a generalized additive Cox regression, and a random survival forest.
- ▶ **We aimed to extend these packages to additional learners and loss functions.**

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1. Super Learning for Right-Censored Data. In MJ van der Laan, S Rose (eds.), Targeted Learning, Springer Series in Statistics.



# The survival SL is estimated by minimizing the cross-validated loss function

- ▶  $S_m(\cdot)$  is the survival function obtained by the  $m^{\text{th}}$  learner ( $m = 1, \dots, M$ ).
- ▶  $w_m$  is the corresponding weight with respect to  $\sum_1^M w_m = 1$  and  $0 \leq w_m \leq 1$ .
- ▶ The sample is randomly divided into  $V$  cross-validated sub-samples.
- ▶ For each of the folds, one can estimate the  $M$  learners from the training subjects and predict  $\tilde{S}_m(\cdot)$  of the leaving subjects.
- ▶ The weights  $\hat{w}_m$  are then obtained by minimizing the loss function, i.e., distance between the observations and the predictions  $\tilde{S}_{sl}(t | Z) = \sum_{m=1}^M w_m \tilde{S}_m(t | Z)$ .
- ▶ The final survival SL is obtained by  $\hat{S}_{sl}(t | Z) = \sum_{m=1}^M \hat{w}_m \hat{S}_m(t | Z)$ , where  $\hat{S}_m(t | Z)$  are estimated on the entire sample.



## The implemented learners

- ▶ Parametric AFT models. (Weibull, Gamma and generalized Gamma distributions).
- ▶ Parametric PH models (Exponential or Gompertz distributions).
- ▶ Semiparametric PH models with a non-parametric baseline hazard function estimated by using the Breslow estimator (with an option for covariates selection by forward AIC-based selection).
- ▶ Penalized PH models (Lasso, Ridge, or Elastic-Net). The quantitative covariates are transformed with B-splines to relax the log-linear assumption.
- ▶ Random survival forests.
- ▶ Survival neural networks (NN). The linear predictor of the previous semi-parametric PH model is obtained by a single hidden layer network with non-linear activation functions.

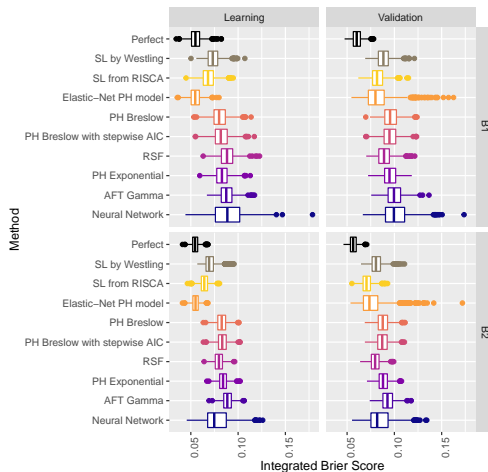


## The implemented loss functions

- ▶ The Brier Score (BS) for right-censored data and a prediction at time  $t$ .
- ▶ The negative binomial log-likelihood (BLL) for a prognostic at time  $t$ .
- ▶ The integrated BS and BLL up to the maximum follow-up time.
- ▶ The restricted integrated BS and BLL up to a time  $t$ .



# The performances of the survival SL





# Our recent implementation of neural network for survival data in R : the partial logistic regression approach (PLANN)

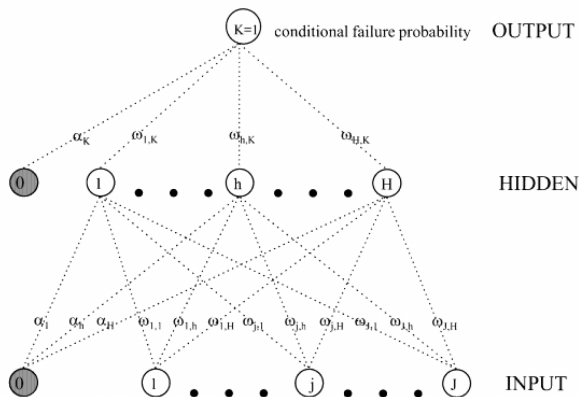


FIGURE – Biganzoli et al. Feed forward NN for t censored survival data. Stat Med. (1998)

## The current developments of R packages

- ▶ The survival neural network (PLANN) :

`https://github.com/chupverse/survivalPLANN`  
`https://cran.r-project.org/package=survivalPLANN`

- ▶ The survival super learner :

`https://github.com/chupverse/survivalSL`  
`https://cran.r-project.org/package=survivalSL`



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# Context

- ▶ In a randomized clinical trial with individual randomization (RCT), the random treatment allocation aims to balance the prognostic factors.
- ▶ But residual differences due to chance may persist, namely near-confounders.
- ▶ Three categories of methods for estimating marginal effects : propensity score, G-computation, and doubly robust estimators).
- ▶ Regarding our previous results in observational studies,<sup>2</sup> we hypothesized that G-computation associated with ML could be suitable for RCTs.

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2. Le Borgne et al. G-computation and machine learning for estimating the causal effects of binary exposure statuses on binary outcomes. Sci Rep (2021)

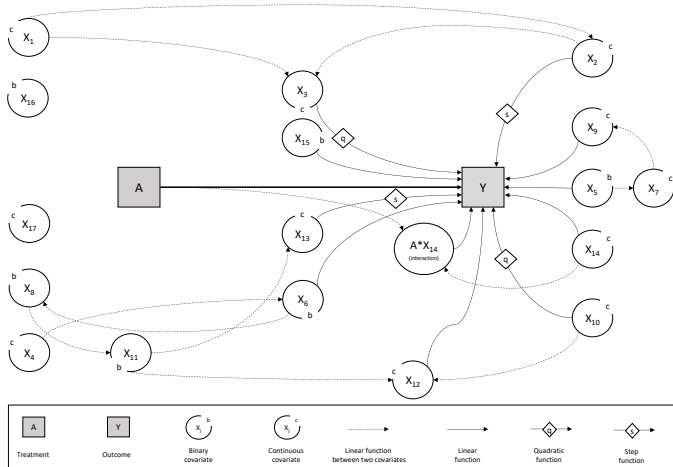


# The G-computation

- ▶ Let  $(Y, A, X)$  the binary outcome, the 1 :1 randomized treatment, and the set of baseline prognostic factors.
- ▶ Fit the outcome model.
- ▶ Predict the potential outcomes as if the subjects were included in the two arms.
- ▶ Compute the difference of the mean of the potential outcomes.
- ▶ We considered several models and algorithms as outcome models : Lasso and Elasticnet logistic regression, neural networks, support vector machine, and super learner of the previous methods.



## The simulations



# The simulations

Sample size	mOR*	Method	Absolute mean bias				log mÔR				
			$\hat{\pi}_0$	$\hat{\pi}_1$	log mÔR	$\Delta$	RMSE	VEB	Coverage	Error†	RSS
n = 200	1.9	Unadjusted	0.03%	-0.02%	0.0044	-0.05%	0.29	-0.43%	94.57%	42.58%	0.00%
		Elasticnet	-0.10%	0.03%	0.0108	0.13%	0.24	0.61%	94.54%	26.07%	31.07%
		Lasso	-0.11%	-0.07%	0.0071	0.04%	0.24	3.59%	95.24%	27.19%	27.53%
		Neural network	1.36%	-2.27%	-0.1439	-3.63%	0.27	-5.14%	93.07%	48.56%	-30.94%
		Support vector machine	0.80%	-1.78%	-0.1034	-2.59%	0.24	-9.94%	90.88%	31.22%	18.18%
		Super learner	1.71%	-0.58%	-0.0890	-2.29%	0.24	-7.09%	92.22%	29.16%	22.86%
	1.3	Unadjusted	0.00%	-0.06%	0.0000	-0.06%	0.29	-1.19%	91.96%	86.69%	0.00%
		Elasticnet	-0.11%	-0.08%	-0.0030	0.02%	0.24	-0.42%	95.04%	82.20%	32.90%
		Lasso	-0.13%	-0.12%	0.0025	0.01%	0.24	2.23%	94.65%	83.34%	30.28%
		Neural network	0.55%	-1.73%	-0.0899	-2.27%	0.23	3.16%	94.14%	92.03%	-79.15%
		Support vector machine	0.73%	-0.33%	-0.0415	-1.06%	0.21	-3.04%	94.80%	83.42%	25.90%
		Super learner	1.37%	0.20%	-0.0456	-1.17%	0.21	-3.01%	93.57%	83.94%	20.42%
	1.0	Unadjusted	-0.03%	0.02%	0.0020	0.05%	0.29	-1.38%	94.09%	5.93%	-
		Elasticnet	-0.13%	-0.08%	0.0020	0.05%	0.24	0.21%	94.39%	5.61%	-
		Lasso	-0.15%	-0.09%	0.0024	0.06%	0.24	2.72%	94.83%	5.17%	-
		Neural network	-0.05%	-1.25%	-0.0493	-1.20%	0.21	10.24%	95.76%	4.24%	-
		Support vector machine	0.58%	0.67%	0.0036	0.09%	0.20	-0.02%	94.20%	5.80%	-
		Super learner	1.10%	0.80%	-0.0131	-0.30%	0.20	-0.05%	94.01%	5.99%	-



## Conclusions

- ▶ G-computation with Elasticnet and splines when appropriate represents a relevant approach for increasing the power of RCTs.
- ▶ This approach is particularly effective when the outcome model has significant predictive capacities.
- ▶ It remains robust even with very small sample sizes ( $n = 60$ ).
- ▶ We should avoid complex outcome models when the sample size is small.





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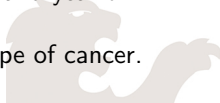


# Context

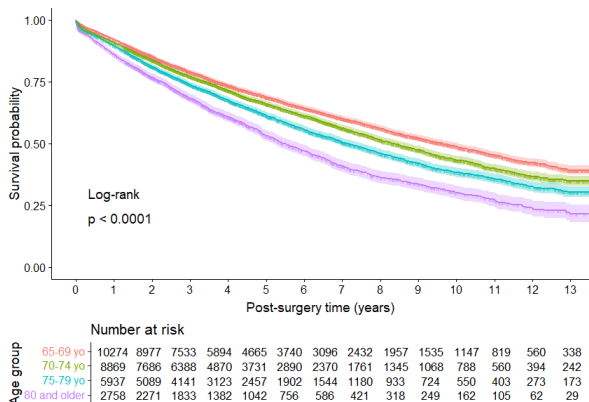
- ▶ There has been an increase in the incidence of cancers but a decrease in associated mortality.
- ▶ Interest in predicting probability of cure and time to cure for the right to be forgotten and the patient information
- ▶ Two competing deaths :  $Y = (E, P)$  due or not to the cancer.

$$\lambda_O(t \mid X_P, X_E) = \tilde{\lambda}_P(t \mid X_P) + \lambda_E(t \mid X_E)$$

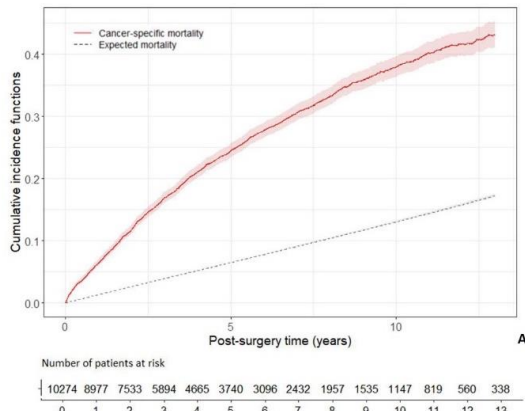
- ▶  $\lambda_O(t \mid \cdot)$  is the overall instantaneous hazard at time  $t$ .
- ▶  $\tilde{\lambda}_P(t \mid X_P)$  is the population hazard and  $X_P$  the predictors : age, sex, and year of diagnosis.
- ▶  $\lambda_E(t \mid X_E)$  the excess hazard and  $X_E$  the predictors : age, sex, and type of cancer.



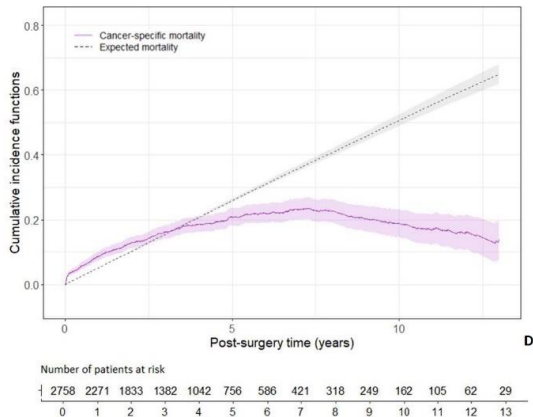
# Current application : post-surgery lung cancer (French EPITHOR registry)



# Cumulative incidence functions in patients in-between 60 and 69 years old



# Cumulative incidence functions in patients older than 80 years



# The current flexible strategy for time-to-cure estimation<sup>3</sup>

- ▶ Maximum likelihood estimation for each stratum  $s, c$  :

$$\lambda_E(t \mid \text{sex} = s, \text{cancer} = c, \text{age} = a) = \lambda_{b,s,c}(t) \exp \left( \sum_i \beta_{s,c,i}(t) \mathbb{1}\{a \in A_i\} \right)$$

- ▶  $\lambda_{s,c}(t)$ , strata-specific baseline hazard function by cubic splines (4 internal nodes).
  - ▶  $A_1 = [45; 55[$  ,  $A_2 = [55; 65[$  ,  $A_3 = [65; 75[$
  - ▶  $\beta_{s,c,i}(t)$ , strata-specific function by cubic splines (2 internal nodes).
- 
- ▶ Avoid assumptions of log-linearity and hazards proportionality.

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3. Boussari et al. A new approach to estimate time-to-cure from cancer registries data. Cancer Epidemiology 2018.



## Method limitations : small effective per stratum <sup>4</sup>

Cancer site	15-44 years		45-54 years		55-64 years		65-74 years	
	P (95% CI)	TTC (95% CI)	P (95% CI)	TTC (95% CI)	P (95% CI)	TTC (95% CI)	P (95% CI)	TTC (95% CI)
Breast	72 (71-74)	12.1 (11.5-12.7)	80 (80-81)	10.6 (10.0-11.1)	79 (78-79)	11.2 (10.6-11.8)	73 (71-74)	12.3 (11.7-12.9)
Central nervous system	38 (33-42)	10.4 (6.2-14.5)	19 (15-23)	10.8 (3.3-18.3)	NC	NC	NC	NC
Cervix uteri	77 (75-79)	6.5 (4.3-8.7)	63 (60-67)	8.5 (4.6-12.5)	49 (45-53)	11.0 (7.6-14.5)	46 (42-51)	10.7 (6.3-15.2)
Colon <sup>a</sup>	62 (58-66)	7.4 (3.8-11.1)	62 (59-64)	6.8 (4.5-9.2)	58 (56-60)	8.1 (6.1-10.1)	55 (53-57)	8.6 (6.9-10.2)
<u>Colon and Rectum</u>	62 (59-65)	7.6 (4.8-10.4)	59 (57-61)	8.1 (6.2-10.0)	8 (57-60)	8.5 (7.1-10.0)	53 (52-55)	9.2 (7.9-10.5)
Corpus uteri	81 (75-86)	6.8 (0.3-13.3)	77 (73-79)	8.4 (5.0-11.8)	75 (73-77)	8.8 (6.5-11.1)	63 (60-65)	10.9 (8.8-13.0)

FIGURE – Proportion of cured patients (P) and time-to-cure (TTC) in women.

4. Romain et al. Time-to-cure and cure proportion in solid cancers in France. A population based study. Cancer Epidemiology, 2019.



## Our proposal : estimate $\lambda_{O,i}(\cdot)$ by ML and deduce the other quantities

- ▶ Excess hazard function

$$\lambda_{E,i}(t | X_{Ei}) = \lambda_{O,i}(t | X_{Ei}, X_{Pi}) - \tilde{\lambda}_{P,i}(t | X_{Pi})$$

- ▶ Cumulative incidence functions ( $k = E, P$ ) :

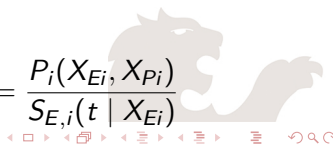
$$F_{k,i}(t | X_{Ei}, X_{Pi}) = Pr(T_i \leq t, Y_i = k) = \int_0^t S_{O,i}(u- | X_{Ei}, X_{Pi}) \tilde{\lambda}_{k,i}(u | X_{Pi}) du$$

- ▶ Probability of being cured, i.e. , dying from another cause :

$$P_i(X_{Ei}, X_{Pi}) = F_{P,i}(\infty | X_{Ei}, X_{Pi})$$

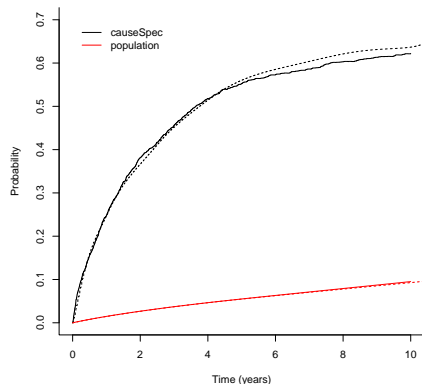
- ▶ Probability of being cured in patients alive at time  $t$  :

$$Pr(Y_i = P | T_i \geq t) = \frac{Pr(T_i \geq t | Y_i = P)Pr(Y_i = P)}{Pr(T_i \geq t)} = \frac{P_i(X_{Ei}, X_{Pi})}{S_{E,i}(t | X_{Ei})}$$





# Application in patients with colon cancer in the Slovene registry (R data)



**FIGURE** – Marginal cumulative incidence functions  $F_P(t)$  and  $F_E(t)$ . Solid line : the Pohar-Perm non-parametric estimation. Dotted line : the Survival Neural Network.



## The current developments of R packages

- The survival neural network with relative survival :

<https://github.com/chupverse/survivalPLANN>  
<https://cran.r-project.org/package=survivalPLANN>

- The flexible B-spline approach :

<https://github.com/chupverse/survivalNET>



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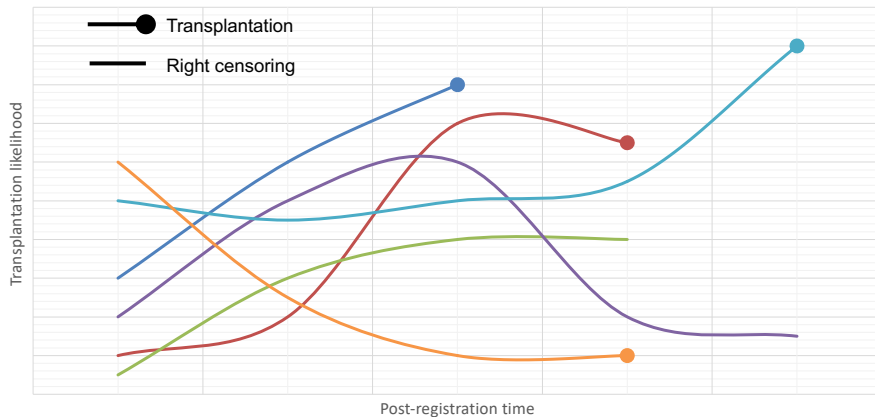


# Context

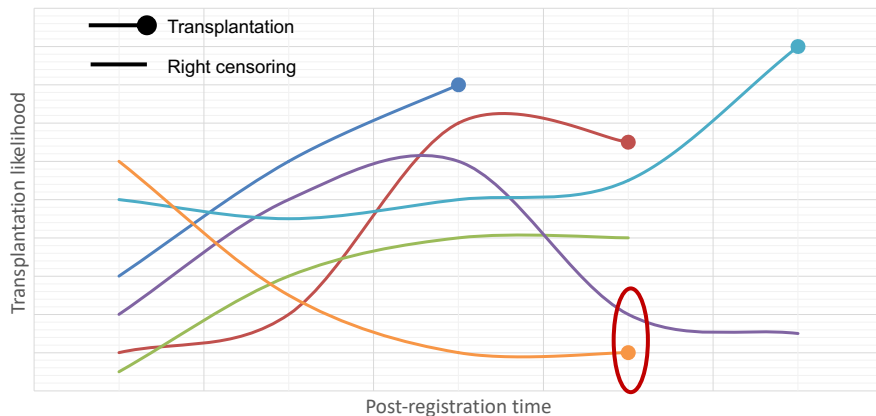
- ▶ The estimation of the impact of a treatment/exposure versus no intervention from real life data.
- ▶ Example : the impact of transplantation compared to waiting in dialysis.
- ▶ Two main issues :
  - ▶ The unbalanced time-dependent confounders at the time of the decision.
  - ▶ The absence of event to determine the baseline in the non-intervention group.



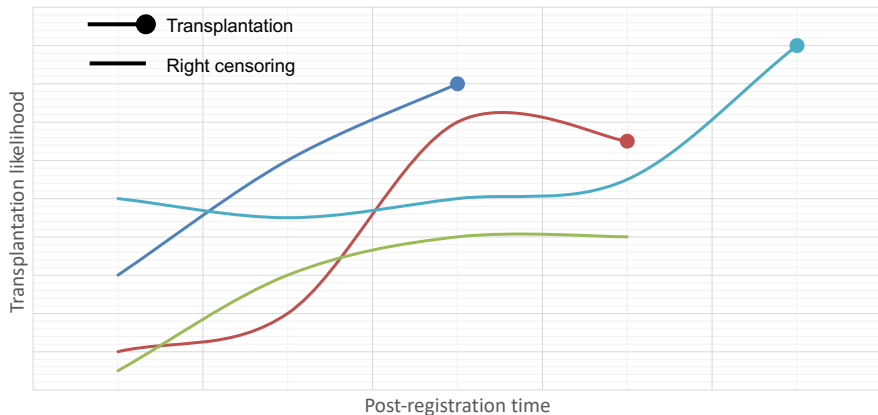
# Matching on time-dependent propensity scores



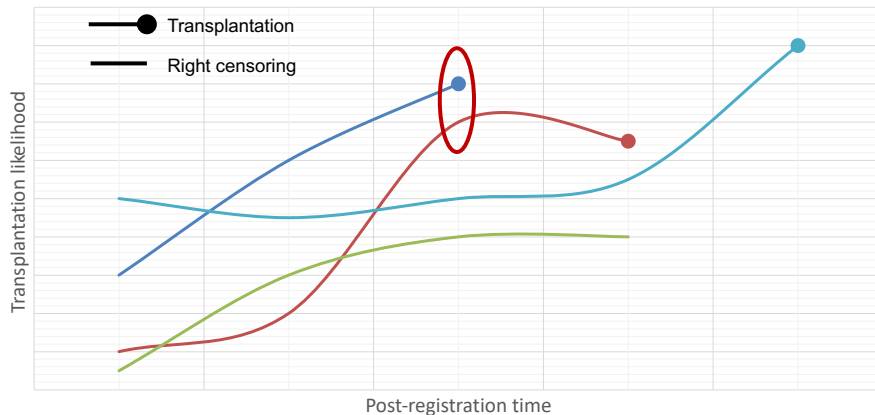
# Matching on time-dependent propensity scores



# Matching on time-dependent propensity scores

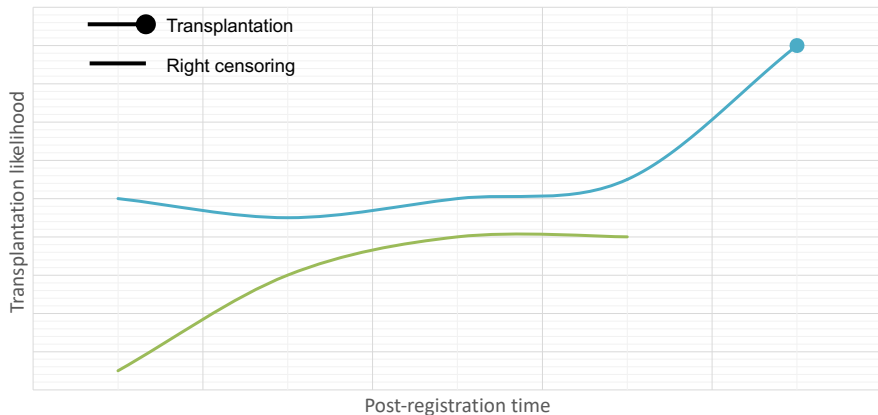


# Matching on time-dependent propensity scores

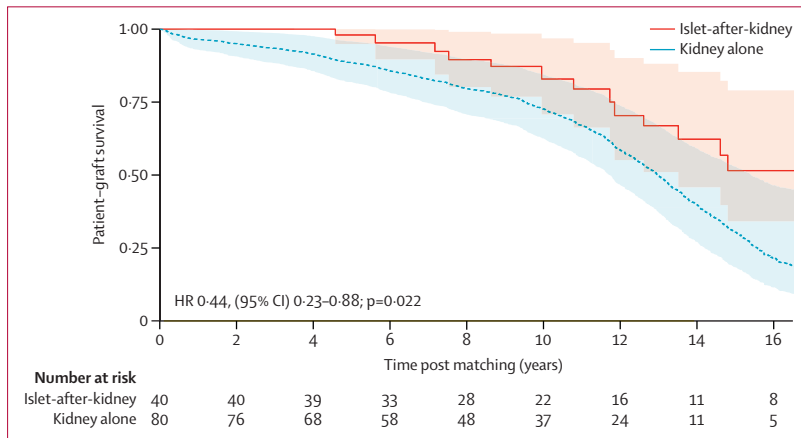




# Matching on time-dependent propensity scores



# Islet-after-kidney transplantation versus kidney alone (type 1 diabetes)<sup>5</sup>



5. Maanaoui, et al. The Lancet Diabetes and Endocrinology, 2024.

## The issue when modeling time-dependent propensity scores

- ▶ The time-dependent predictors :  $X(t)$ .
- ▶ The time-varying effects of the time-dependent predictors :  $\beta(t)$ .

$$\lambda(t | X(t)) = \lambda_0(t) \exp(\beta(t)X(t))$$

- ▶ The "manual" modeling of such an updated Cox model is complex.
- ▶ Its construction cannot be included in the estimation of confidence intervals by bootstrapping.

### Our objective

- ▶ To describe the interest of survival SL for estimating the time-dependent propensity scores.

# Acknowledgments

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