

# **LOG 8371E**

# **Software Quality Engineering**

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**Lecture 06:**

**Software Performance Models**

**Armstrong Foundjem Ph.D. — Winter 2024**

# **Review:**

## **Software Performance Engineering**

# (Ultra) Large-Scale Software Systems



4 million users

2600-3000 req/sec on most weekdays

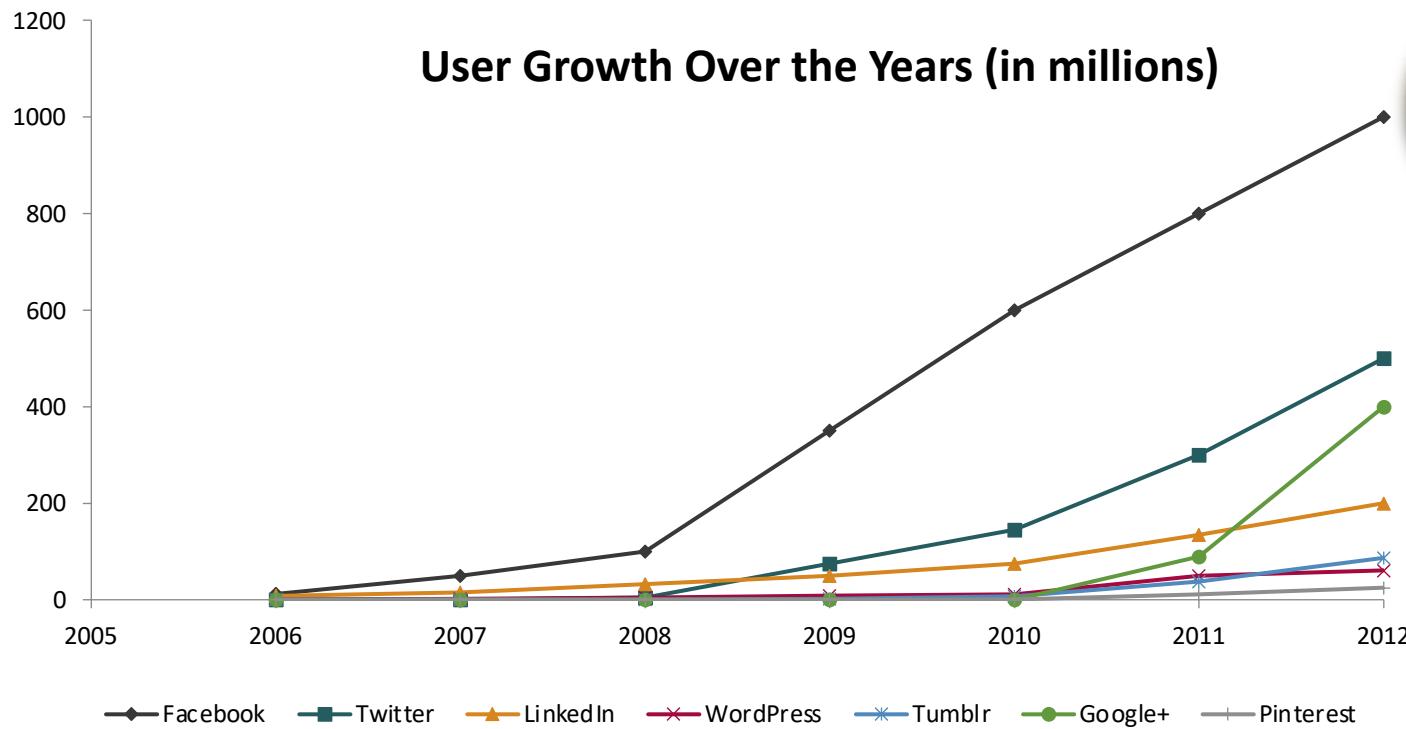


450 million active users

> 50 billion messages every day

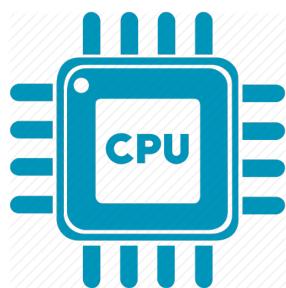


# Rapid Growth and Varying Usage Patterns



Failures of large-scale systems are often due to performance issues rather than functional bugs

# PERFORMANCE





A page load slowdown of only one second could cost \$1.6 billion

# Software Performance Engineering (SPE)

- The set of tasks or activities that need to be performed across the **Software Development Life Cycle (SDLC)** to meet the documented **Non-Functional Requirements** (Performance, Scalability, Availability, Reliability, etc.)

## Software Development Life Cycle

Functional Requirements Gathering

Architecture & Design

Implementation

System Test & User Acceptance Test

Deploy Into Production

## Performance Engineering Life Cycle

Non-functional Requirements Gathering

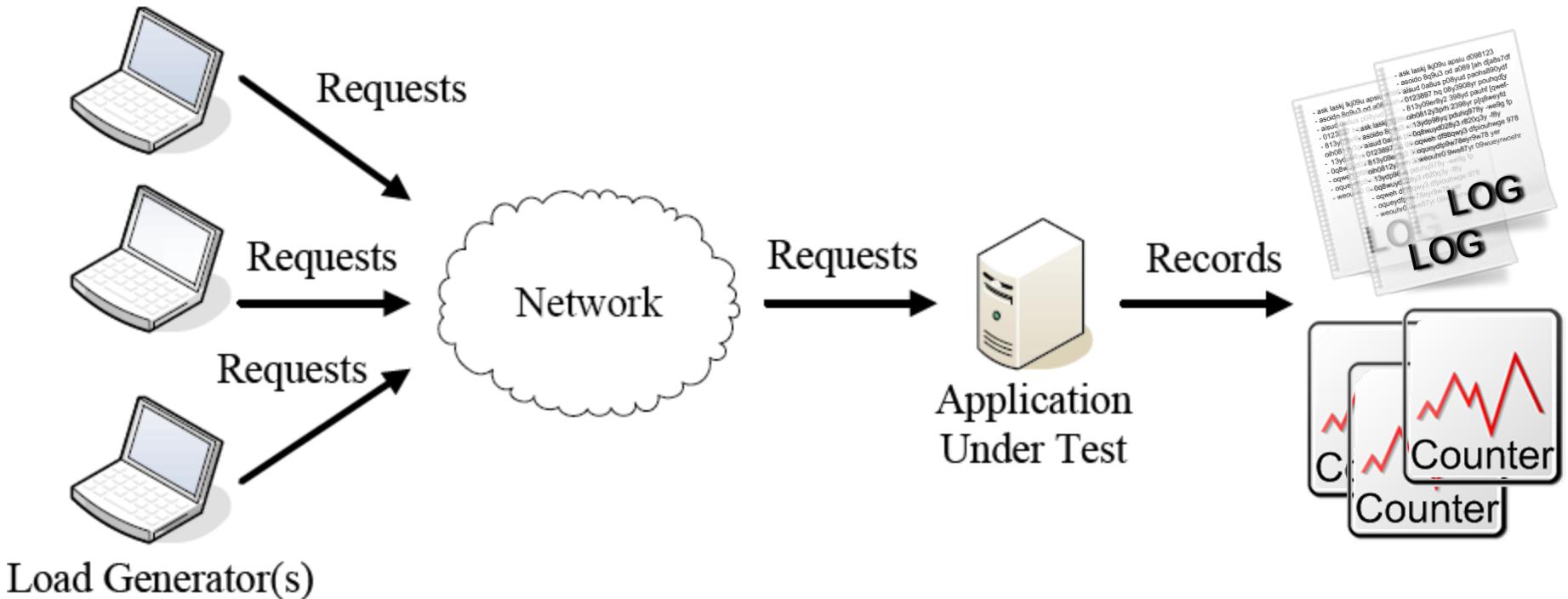
Design for High Performance

Unit Performance Test & Code Optimization

Performance Test

Monitoring & Capacity Management

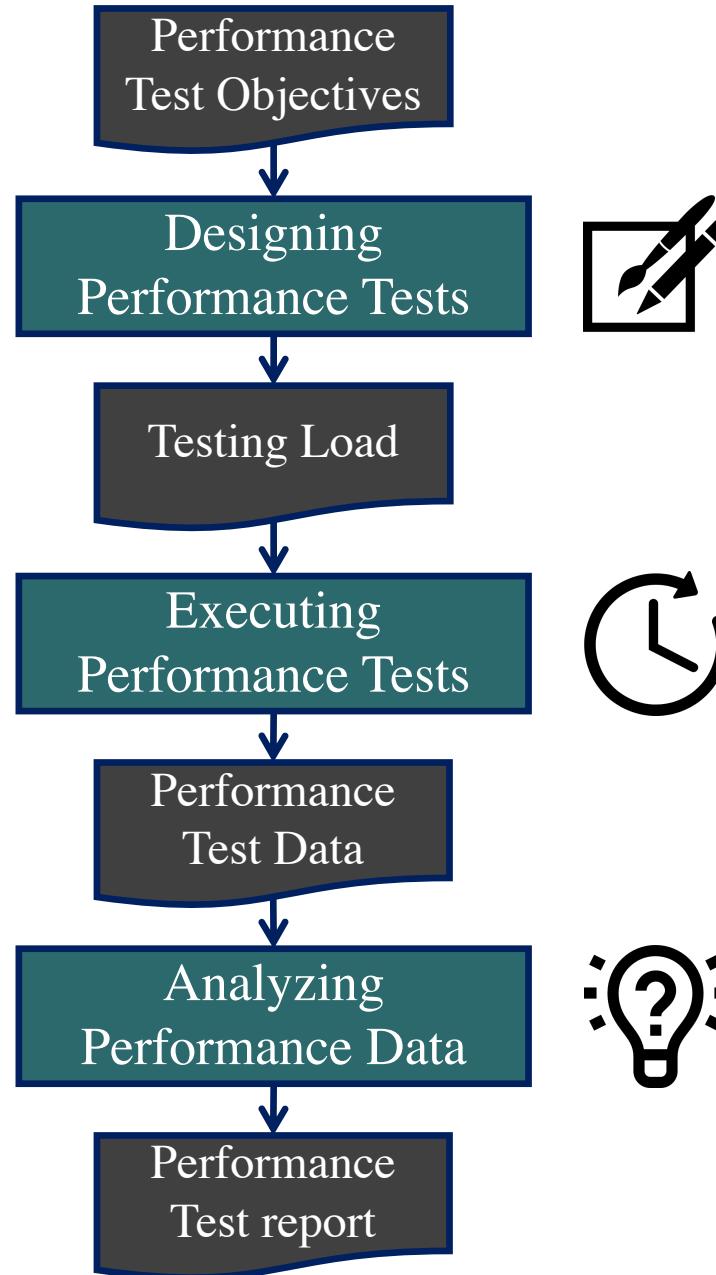
# Performance Testing



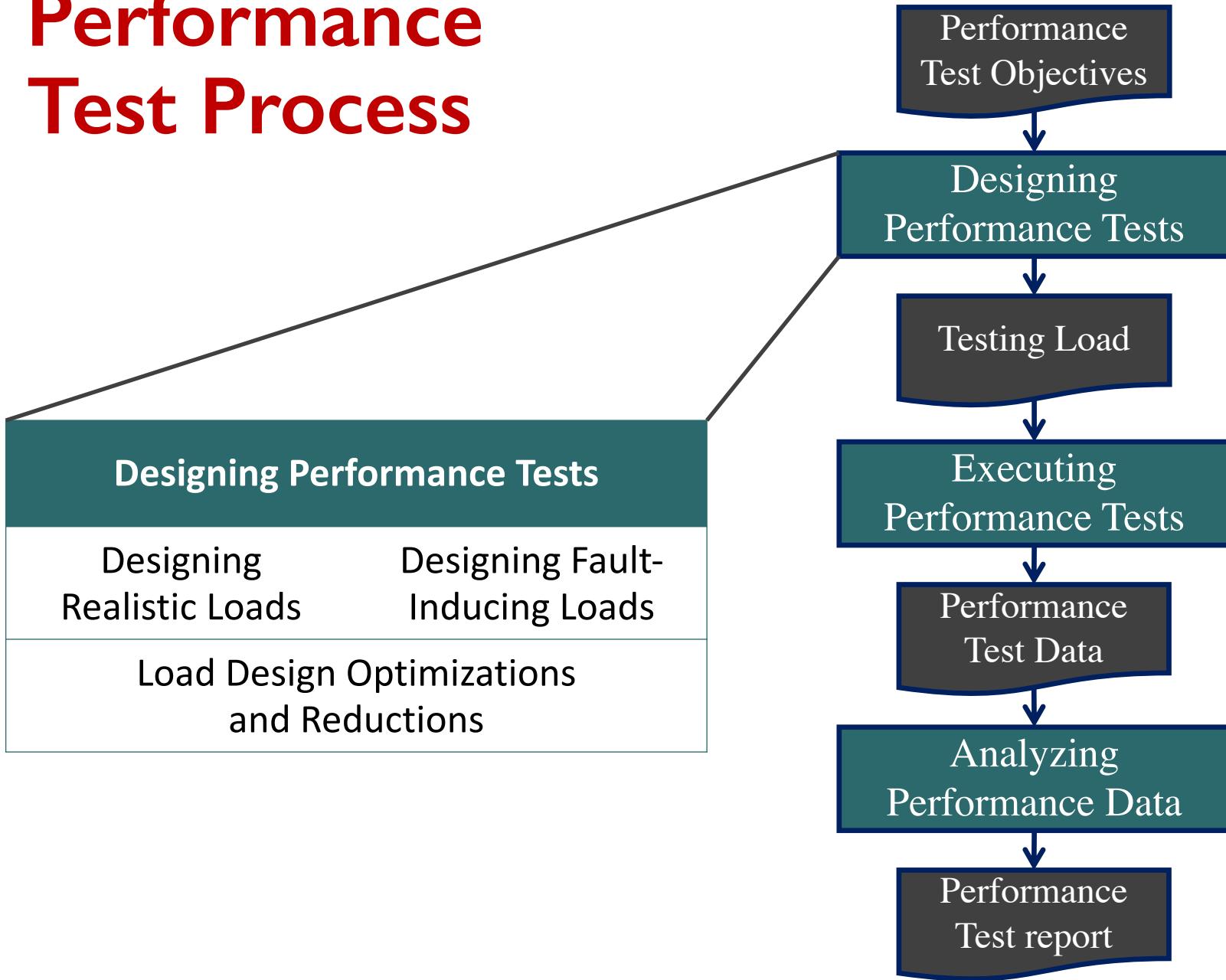
Mimics multiple users repeatedly performing the same tasks  
Take hours or even days

Produces GB/TB of data that must be analyzed

# Performance Test Process



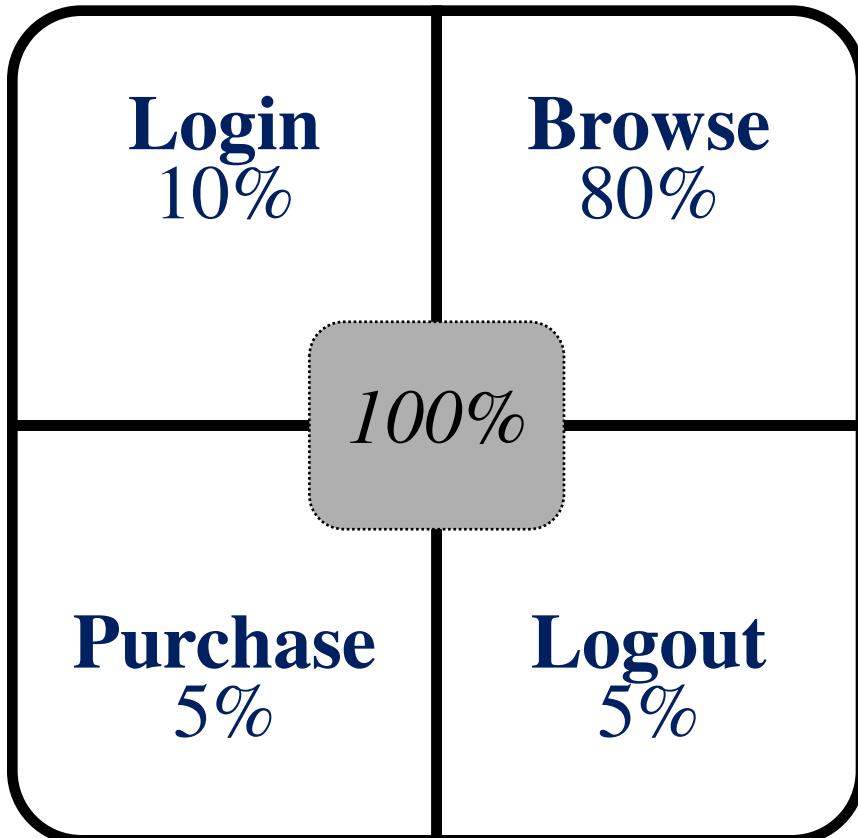
# Performance Test Process



# Designing Realistic Loads

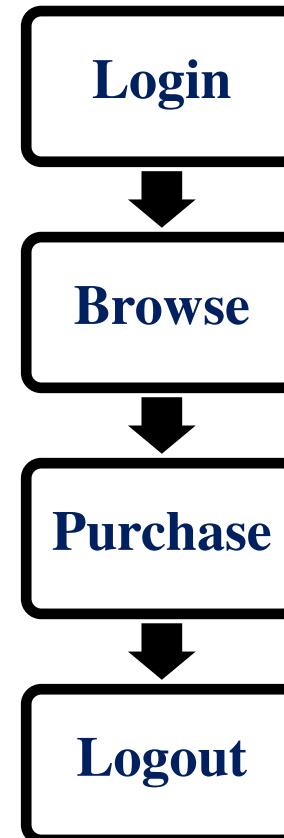
An E-Commerce System

## Aggregate Workload



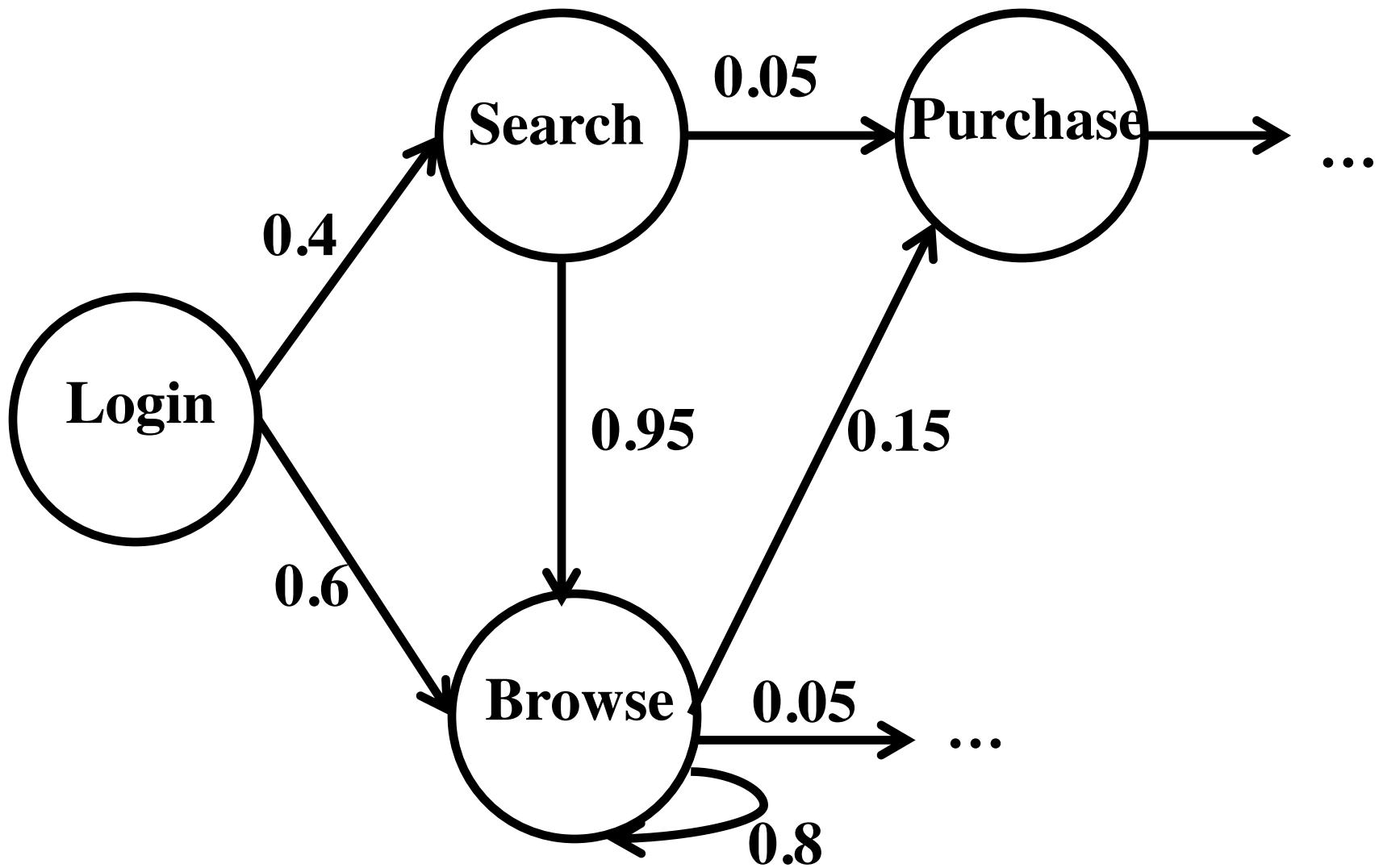
Steady Load, Step-wise load,  
Extrapolated load

## Use-Case

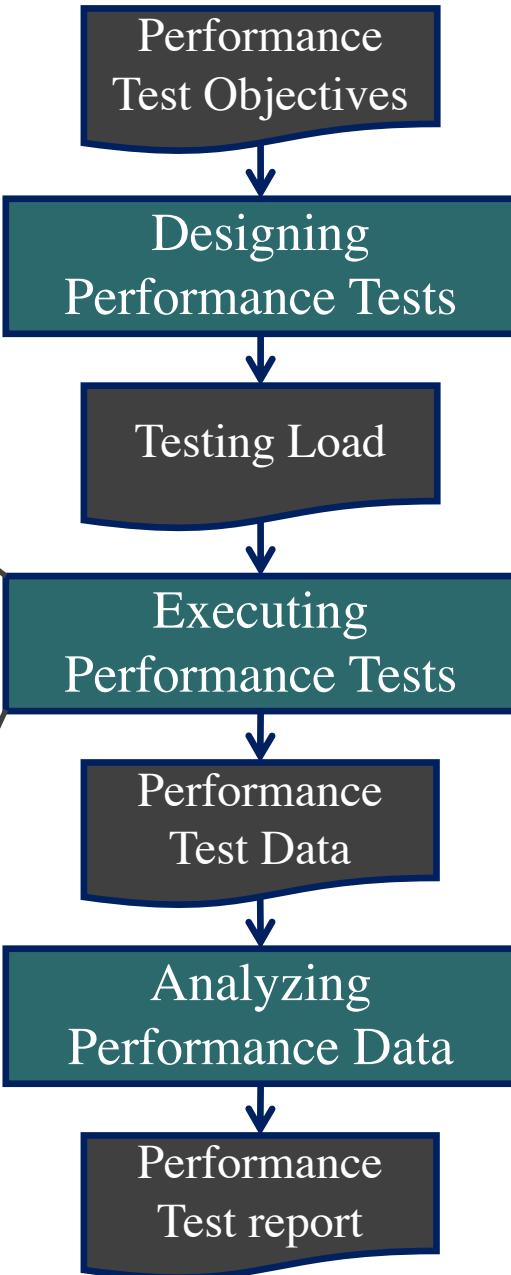
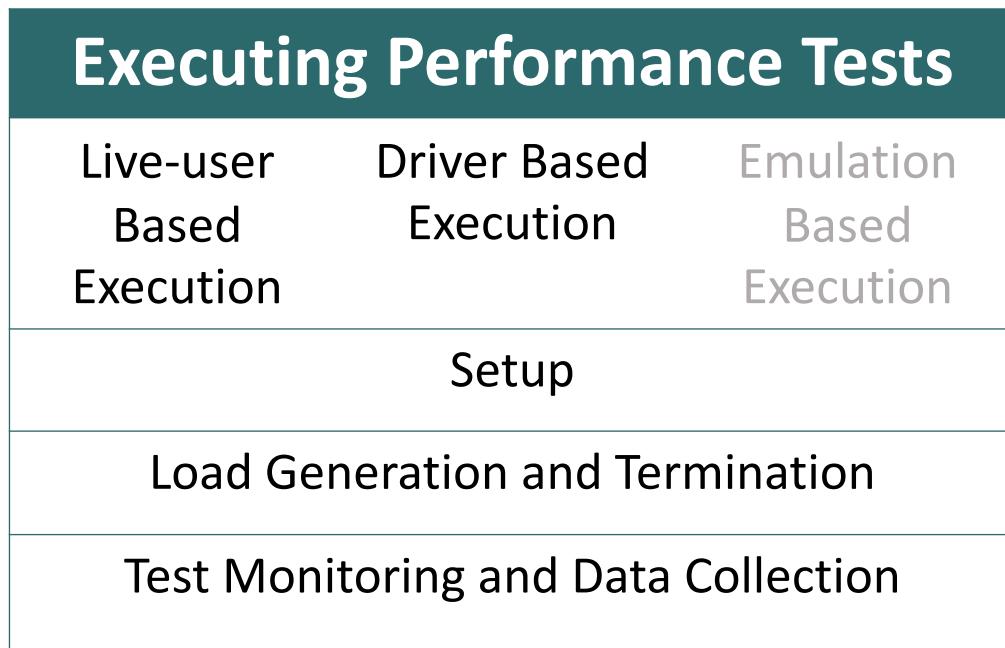


Load Derived from UML, Markov and  
Stochastic Form-oriented Models

# Use-Case (2) - Markov Chain



# Performance Test Process



# Live-user Based Test Execution



- Coordinated live-user testing
- Users are selected based on different testing criteria (e.g., locations, browser types, etc.)

- Reflects realistic user behavior
- Obtain real user feedbacks on acceptable performance and functional correctness
- ✗ Hard to scale (e.g., limited testing time)
- ✗ Limited test complexity due to manual coordination

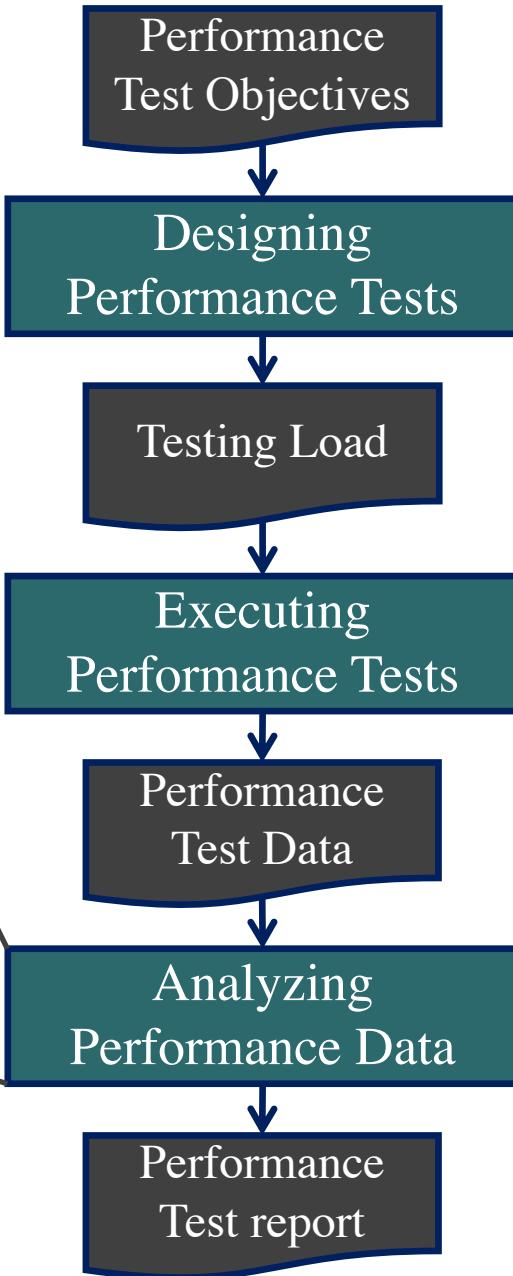
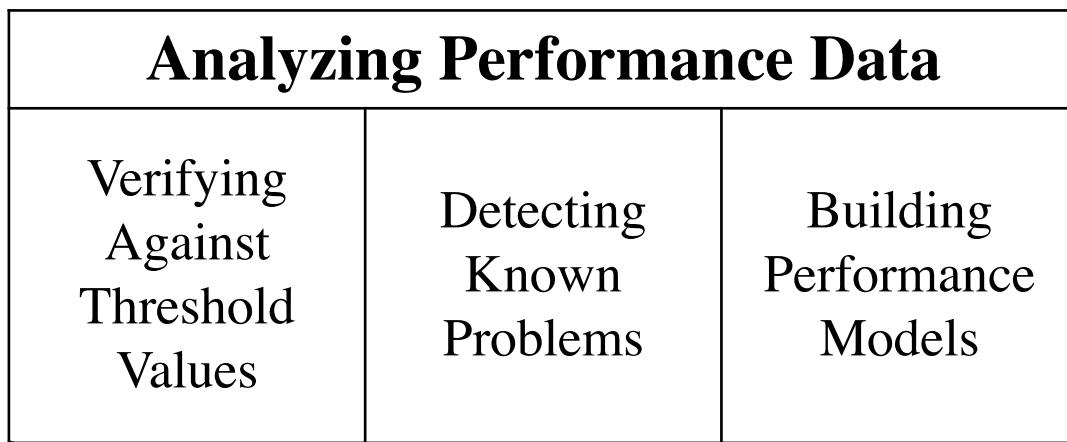
# Driver-based Test Execution



- Easy to automate
- Scale to large number of requests
  
- Load driver configurations
- Hard to track some system behavior  
(e.g., audio quality or image display)

- Specialized Benchmarking tools (e.g., LoadGen)
- Centralized Load Drivers (e.g., LoadRunner, WebLoad)
  - Easy to control load, but hard to scale (limited to a machine's memory)
- Peer-to-peer Load Drivers (e.g., JMeter, PeerUnit)
  - Easy to scale, but hard to control load

# Performance Test Process



# Sample Counters

|    | A             | B              | C               | D               | E       |
|----|---------------|----------------|-----------------|-----------------|---------|
| 1  | Time          | Disk Reads/sec | Disk Writes/sec | Page Faults/sec | Memory  |
| 2  | 2/29/08 16:58 | 0.049986394    | 0.000723659     | 0.003876542     | 3534848 |
| 3  | 2/29/08 17:01 | 0              | 0               | 0               | 3534848 |
| 4  | 2/29/08 17:04 | 0.060612225    | 0.027551011     | 0.016530607     | 3534848 |
| 5  | 2/29/08 17:07 | 0              | 0               | 0               | 3534848 |
| 6  | 2/29/08 17:10 | 0              | 0               | 0               | 3534848 |
| 7  | 2/29/08 17:13 | 0.060733302    | 0.027606046     | 0.016563628     | 3534848 |
| 8  | 2/29/08 17:16 | 0              | 0               | 0               | 3534848 |
| 9  | 2/29/08 17:19 | 0.060727442    | 0.027603383     | 0.01656203      | 3534848 |
| 10 | 2/29/08 17:22 | 0              | 0               | 0               | 3534848 |
| 11 | 2/29/08 17:25 | 0              | 0               | 0               | 3534848 |
| 12 | 2/29/08 17:28 | 0              | 0               | 0               | 3534848 |
| 13 | 2/29/08 17:31 | 0              | 0               | 0               | 3534848 |
| 14 | 2/29/08 17:34 | 0.121368621    | 0.055167555     | 0.038617289     | 3534848 |
| 15 | 2/29/08 17:37 | 0              | 0               | 0               | 3534848 |
| 16 | 2/29/08 17:40 | 0              | 0               | 0               | 3534848 |
| 17 | 2/29/08 17:43 | 0              | 0               | 0               | 3534848 |
| 18 | 2/29/08 17:46 | 0              | 0               | 0               | 3534848 |
| 19 | 2/29/08 17:49 | 0              | 0               | 0               | 3534848 |
| 20 | 2/29/08 17:52 | 0              | 0               | 0               | 3534848 |
| 21 | 2/29/08 17:55 | 0.121392912    | 0.055178596     | 0.033107158     | 3534848 |
| 22 | 2/29/08 17:58 | 0.060592703    | 0.027542138     | 0.02203371      | 3534848 |

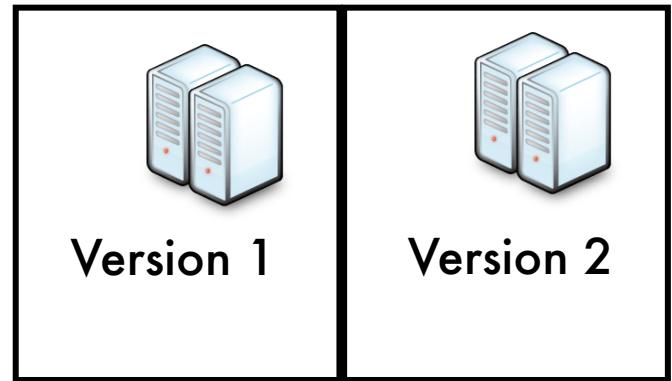
# Sample Execution Logs

| #  | Log Lines   |
|----|---|
| 1  | time=1, thread=1, session=1, receiving new user registration request                                  |
| 2  | time=1, thread=1, session=1, inserting user information to the database                               |
| 3  | time=1, thread=2, session=2, user=Jack, browse catalog=novels   |
| 4  | time=1, thread=2, session=2, user=Jack, sending search queries to the database                        |
| 5  | time=3, thread=1, session=1, user=Tom, registration completed, sending confirmation email to the user |
| 6  | time=3, thread=2, session=2, database connection error: session timeout                               |
| 7  | time=4, thread=1, session=1, fail to send the confirmation email, number of retry = 1                 |
| 8  | time=6, thread=2, session=2, user=Jack, successfully retrieved data from the database                 |
| 9  | time=7, thread=2, system health check   |
| 10 | time=8, thread=1, session=1, registration email sent successfully to user=Tom                         |
| 11 | time=9, thread=2, session=3, user=Tom, browse catalog=travel  |
| 12 | time=10, thread=2, session=3, user=Tom, sending search queries to the database                        |
| 13 | time=10, thread=3, session=4, user=Jim, updating user profile   |
| 14 | time=11, thread=3, session=4, user=Jim, database error: deadlock                                      |

# Verifying Against Threshold Values



Threshold from  
requirement



Threshold from a  
prior version

# Looking for known patterns: Deadlocks and memory leak



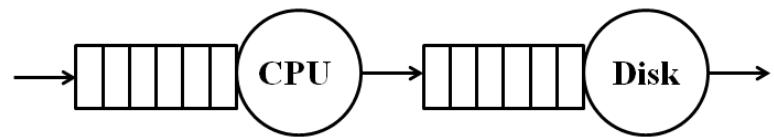
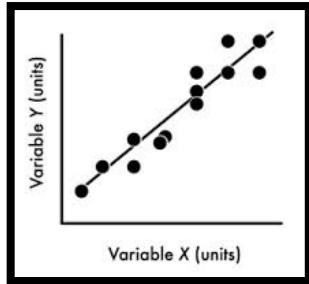
CPU

Memory

Performance data under steady load

[Avritzer et al., 2012]

# Building performance models



Machine learning  
(Black box) model

Queuing (white box)  
Model

WHAT IF...?



# Profiling

- A form of **dynamic program analysis** that measures the complexity of the program in terms of space (memory) or time, or the frequency and duration of function calls.
- Its objective is the **optimization of the program** and the management of resources.
- It is a process that helps to **understand the behavior** of a program.
- It also helps evaluate and **compare performance** of different architectures.
- Profiling has two important components: **instrumentation** and **sampling**.

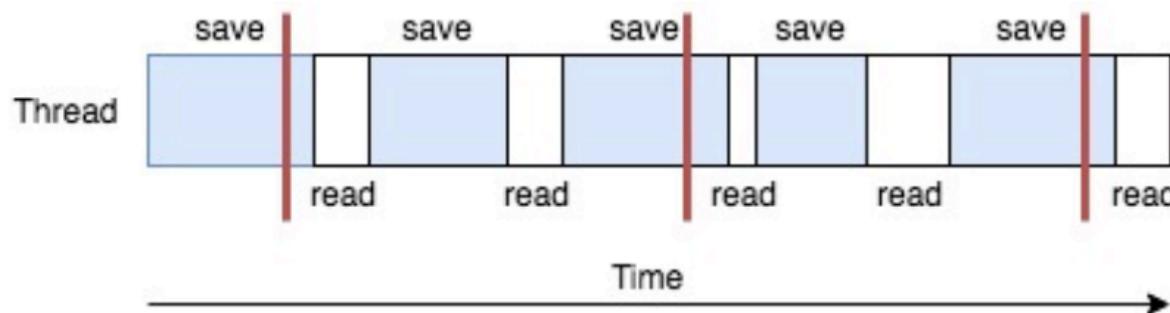
# Profiling: Instrumentation

- It is possible to collect data by external tools, but this data is not **detailed** enough and of a **sufficient level of granularity**.
- For this reason, instrumentation is used.
  - A technique that **adds code (probes)** in the monitored program to collect performance data.
- It is possible to add probes at several levels of the system.
  - Source code (manually or automatically)
  - Assisted by the compiler
  - Binary code
- Motivation for profiling:
  - Collect exactly the data needed and infer the locality of the data.
  - Control the granularity of data.
  - Control the measurement process by activating and deactivating probes.



# Profiling: Sampling

- Sampling does not affect the execution of the program.
  - No instruction is inserted in the source elbow nor in the compiled code.
- The operating system suspends the CPU at regular intervals and the profiler records the instruction that is currently executing.
- The profiler correlates the instruction with the corresponding point in the code.
- The profiler returns the frequency of execution of code points.
- Repeat profiling with sampling several times to obtain statistical significance.



# Profiling: Automated Profiling

- Automated profiling facilitates optimization and guarantees continuous integration and continuous quality assurance.
- It also reduces optimization costs.
- Profiling tools are able to calculate a large number of measurements and produce detailed reports.
- **Warning!** Some profiling methods are characterized as **intrusive**, which can affect the results of the process.



# Profiling vs Performance testing

## Profiling → Performance testing

- We can use profiling to understand the behavior of our program ...
- ... and identify the use of resources (CPU, memory etc.)
- After that, we can define the thresholds and objectives for the performance and test them.
- We can also train or provide inputs for our performance models.

## Performance testing → Profiling

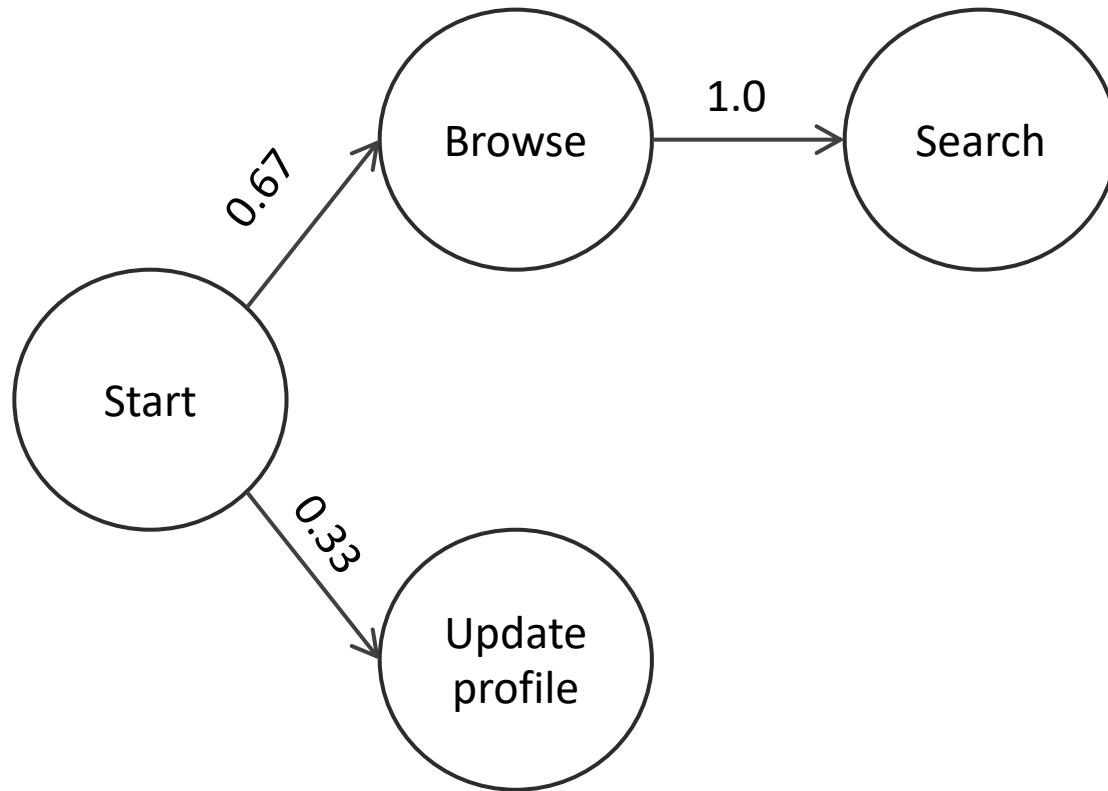
- Testing will indicate the presence of performance issues.
- According to this indication, profiling will reveal the exact point of the bottleneck.
- After, we optimize the code and rerun the tests.

# Exercise from last class: Design realistic loads for performance testing

- Based on the following sample logs, design a use-case model using the Markov chain

| #  | Log Lines   |
|----|---|
| 1  | time=1, thread=1, session=1, receiving new user registration request                                  |
| 2  | time=1, thread=1, session=1, inserting user information to the database                               |
| 3  | time=1, thread=2, session=2, user=Jack, browse catalog=novels   |
| 4  | time=1, thread=2, session=2, user=Jack, sending search queries to the database                        |
| 5  | time=3, thread=1, session=1, user=Tom, registration completed, sending confirmation email to the user |
| 6  | time=3, thread=2, session=2, database connection error: session timeout                               |
| 7  | time=4, thread=1, session=1, fail to send the confirmation email, number of retry = 1                 |
| 8  | time=6, thread=2, session=2, user=Jack, successfully retrieved data from the database                 |
| 9  | time=7, thread=2, system health check   |
| 10 | time=8, thread=1, session=1, registration email sent successfully to user=Tom                         |
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| 12 | time=10, thread=2, session=3, user=Tom, sending search queries to the database                        |
| 13 | time=10, thread=3, session=4, user=Jim, updating user profile   |
| 14 | time=11, thread=3, session=4, user=Jim, database error: deadlock                                      |

# Exercise from last class: Design realistic loads for performance testing



# Today: Software Performance Models

- Software Performance Modeling (SPM)
- Execution graphs
- Queuing Networks
- Machine learning based performance models
  
- References:
  - Jain, Raj. *The art of computer systems performance analysis - techniques for experimental design, measurement, simulation, and modeling.* Wiley professional computing, 1991.
  - Gao, Ruoyu, et al. *A framework to evaluate the effectiveness of different load testing analysis techniques.* ICST '16.
  - Connie U. Smith. *Performance Solutions: A Practical Guide to Creating Responsive, Scalable Software.* Addison-Wesley. 2001.
  - Kaushal Kumar's lecture slides for course *Software Performance Analysis* at Queen's University: <https://research.cs.queensu.ca/home/elgazzar/soft437/>

# Software Performance Models (SPM)

- Formal representations of the software to capture aspects and information of the performance.
- Built as early as design and architecture models to express and understand the non-functional requirements.



# Software Performance Models (SPM)

- They allow us to:
  - ✓ Estimate the performance of the software.
  - ✓ Estimate resource needs.
  - ✓ Identify performance issues as early as possible.
  - ✓ Simulate the execution of the software under certain conditions (number of users and size of the infrastructure).
  - ✓ Establish software performance for medium, best, and worst case scenarios.

# Software Performance Models (SPM)

- SPM sometimes provide a **graphical representation** of the system's execution that matches its structure.
  - It is possible to produce the performance models by transforming the design models.
- While the design models of the system capture the static aspects, the performance models capture the **dynamic aspects**.
- Types of performance models:
  - Software Execution Models
  - Queuing Networks (System Execution Models)
  - Machine learning based models
  - Others (e.g., Stochastic Petri Nets)

# **Software Execution Models**

# Software Execution Models

- Constructed early in the development process to ensure that the chosen software architecture can achieve the required performance objectives
- Captures essential performance characteristics of the software
- Provides a static analysis of the mean, best, and worst-case response time
- Characterizes the resource requirements of the proposed software alone, in the absence of other workloads, multiple users or delays due to contention for resources

# Software Execution Model (con't)

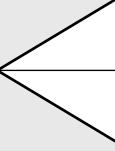
- Software execution models are generally sufficient for identifying serious performance problems at the architectural and early design phases
- We can refine software execution model in the critical areas

*The absence of problems in the software model does not mean that there are none*

# Execution graphs

- Execution graphs are one type of software execution model.
- The graphs represent the **execution (a sequence of operations)** of the system.
  - ✓ An execution graph is constructed for each performance scenario.
- Execution graphs are **not sufficient** for a complete analysis of software performance, but they work well for understanding the software and its non-functional requirements.
  - ✓ The special annotation can give us an **idea of the performance**.
  - ✓ We can **combine the graphs with other models** (like QN we will see) to complement the analysis.

# Graph notation

| Node types       | Graph notation  | Description  |
|------------------|---|--|
| Basic nodes      |    | Represent processing steps at the lowest level of detail that is appropriate for the current development stage |
| Expanded nodes   |    | Represent processing steps elaborated in another subgraph  |
| Repetition nodes |    | Subsequent nodes are repeated n times: the last node has an edge to the repeat node                            |
| Case node        |   | Represent conditional execution of processing steps; each attached node has a probability of execution         |
| Pardo node       |  | Attached nodes run in parallel: All nodes must complete (join) before proceeding.                              |
| Division node    |  | Attached nodes represent new processing threads; they need not all complete before proceeding.                 |

# Example: General ATM Scenario

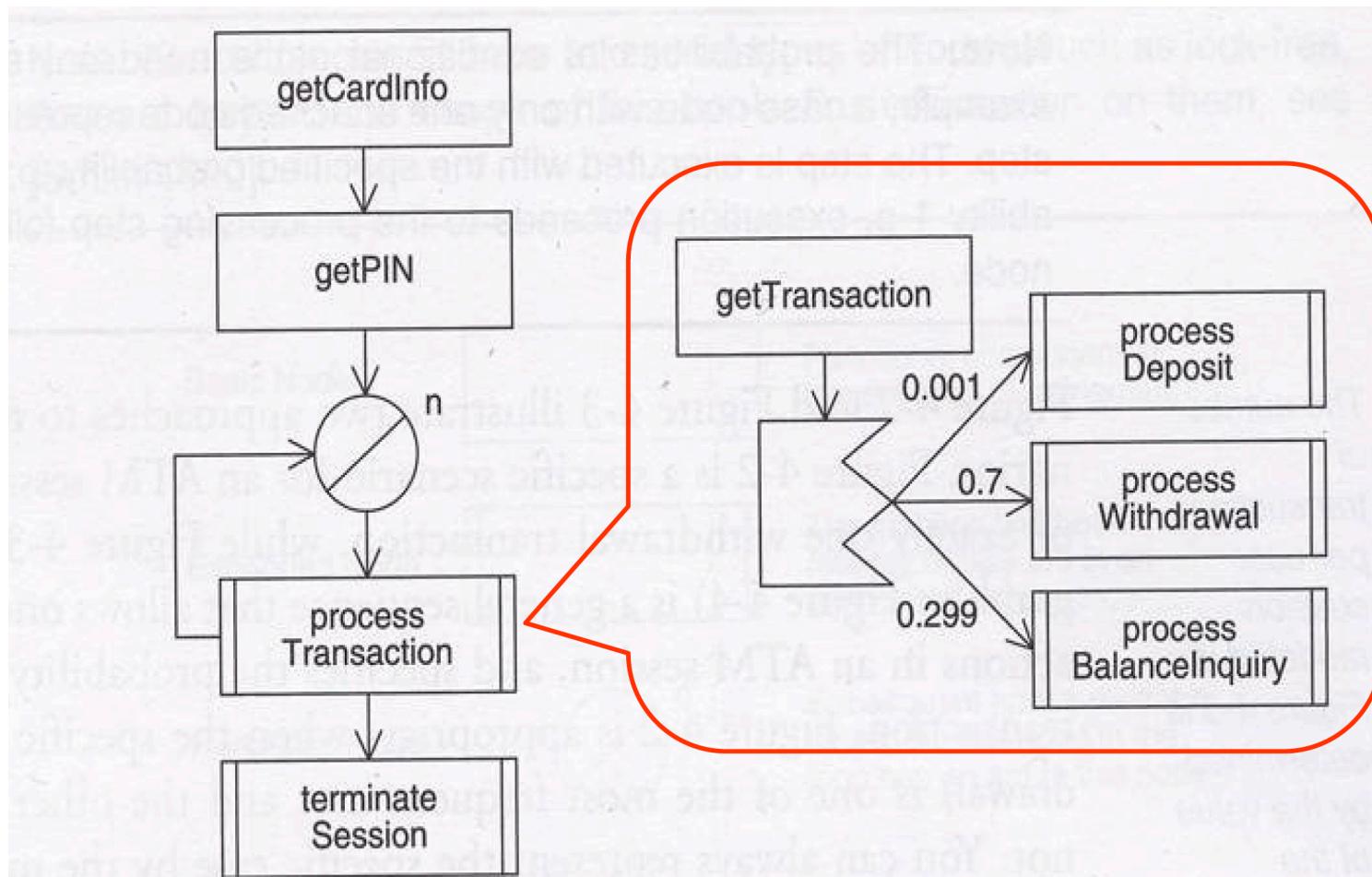


Figure 4-3: Execution Graph for General ATM Scenario

Figure 4-4: Subgraph for processTransaction Expanded Node

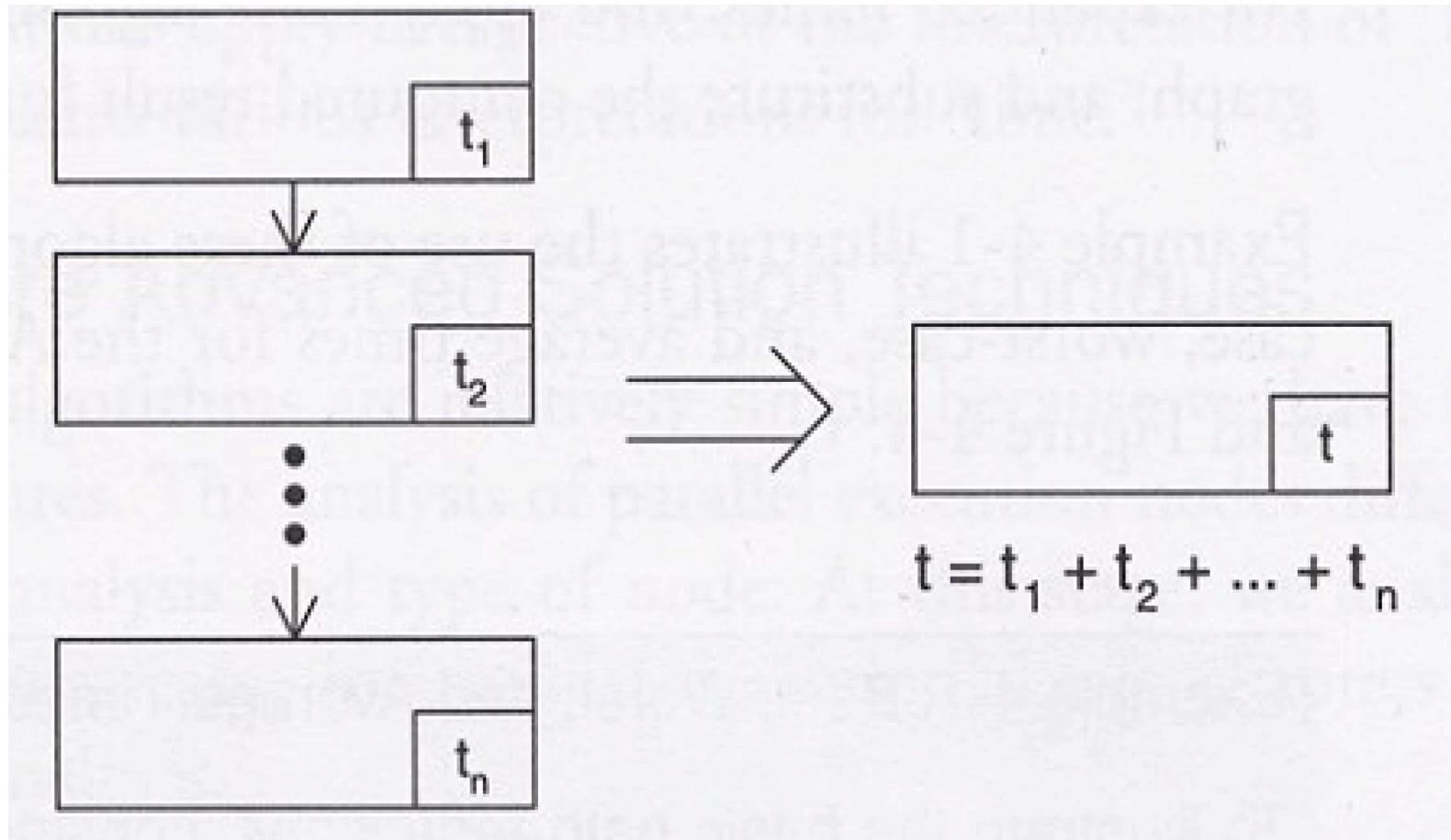
# Software Execution Model Analysis

- Primary purposes of software execution model analysis are
  - Make a quick check of the **best-case response time** in order to ensure the architecture and design will lead to satisfactory performance
  - Assess the performance impact of **alternatives**
  - Identify **critical parts** of the system for performance management
  - Derive **parameters** for the system execution model
- The algorithms are formulated for evaluating graphs

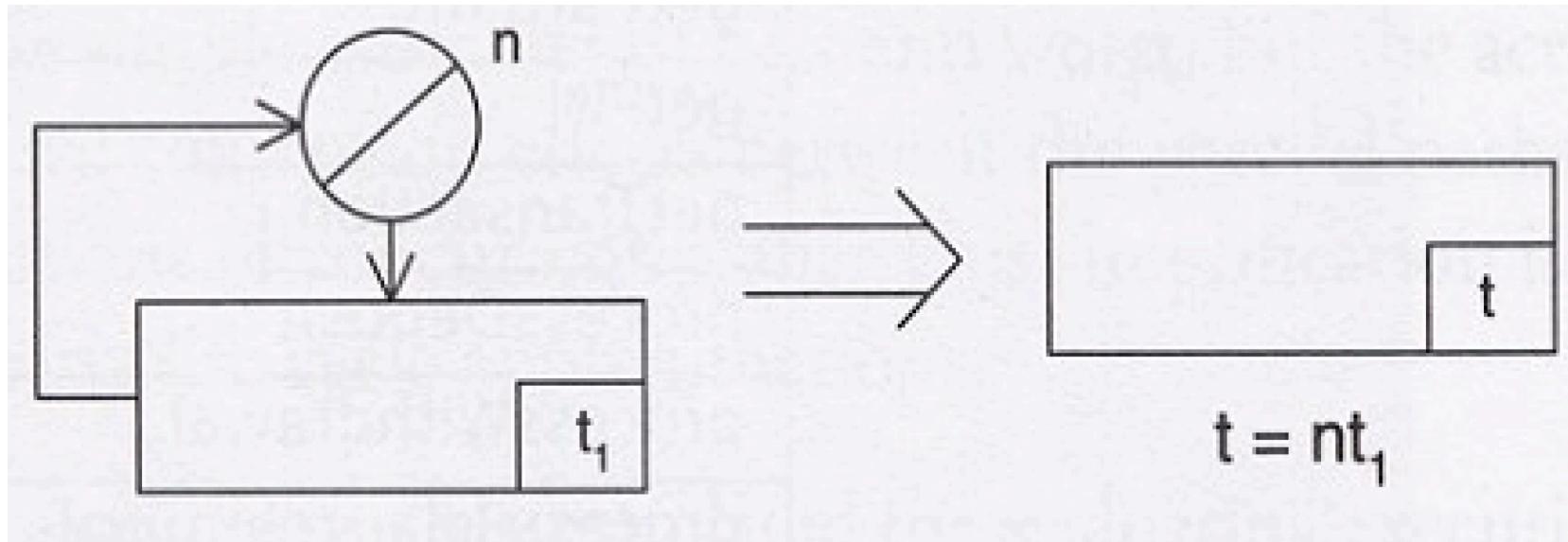
# Basic Solution Algorithms

- The algorithms are ‘easy’ to understand
  - Examine graphs and identify a basic structure
  - Compute the time of a basic structure and reduce the basic structure to a ‘computed node’
  - Continue until only one node left
- Basic structures are
  - Sequences
  - Loops
  - Cases

# Graph Reduction for Sequential Structures



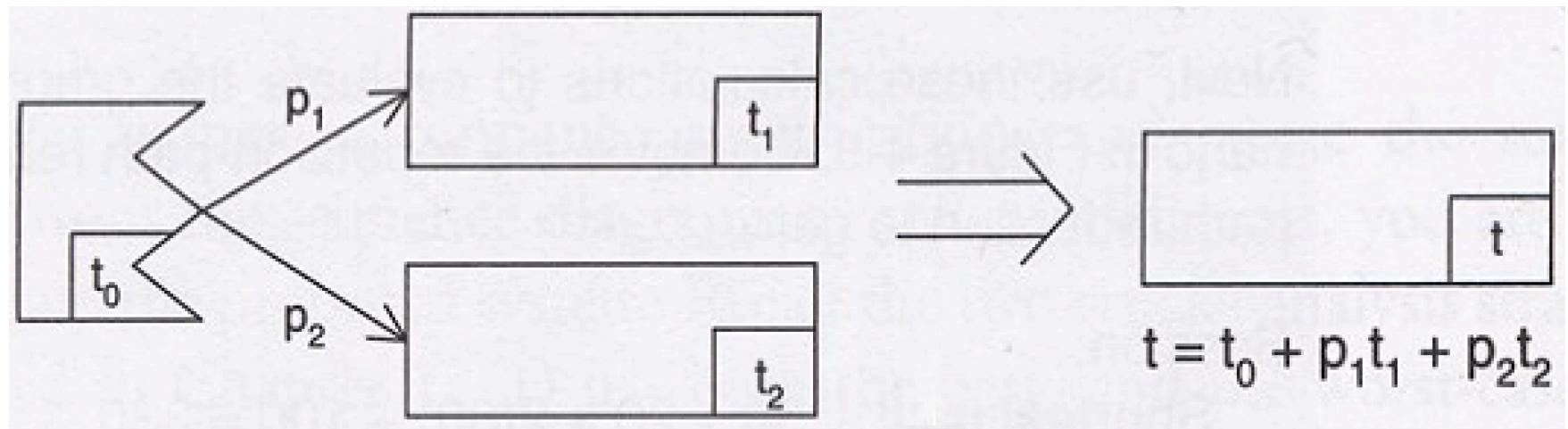
# Graph Reduction for Loop Structures



# Graph Reduction for Case Nodes

- The computation for case nodes differs for shortest path, longest path, and average analyses
  - Shortest path: the time for the case node is the minimum of the times for the conditionally executed nodes
  - Longest path: the time for the case node is the maximum of the times for the conditionally executed nodes
  - For the average analysis: the time is multiplying each node's time by its execution probability

# Graph Reduction for Case Nodes



# Exercise: ATM Scenario

## What's the best, worst, and average execution time?

To illustrate the basic path reductions, consider the ATM scenario in Figure 4-3 and the subgraph for processTransaction in Figure 4-4. Assume the node “times” in the following table.

| Node                  | Time |
|-----------------------|------|
| getCardInfo           | 50   |
| getPIN                | 20   |
| getTransaction        | 30   |
| processDeposit        | 500  |
| processWithdrawal     | 200  |
| processBalanceInquiry | 50   |
| terminateSession      | 100  |

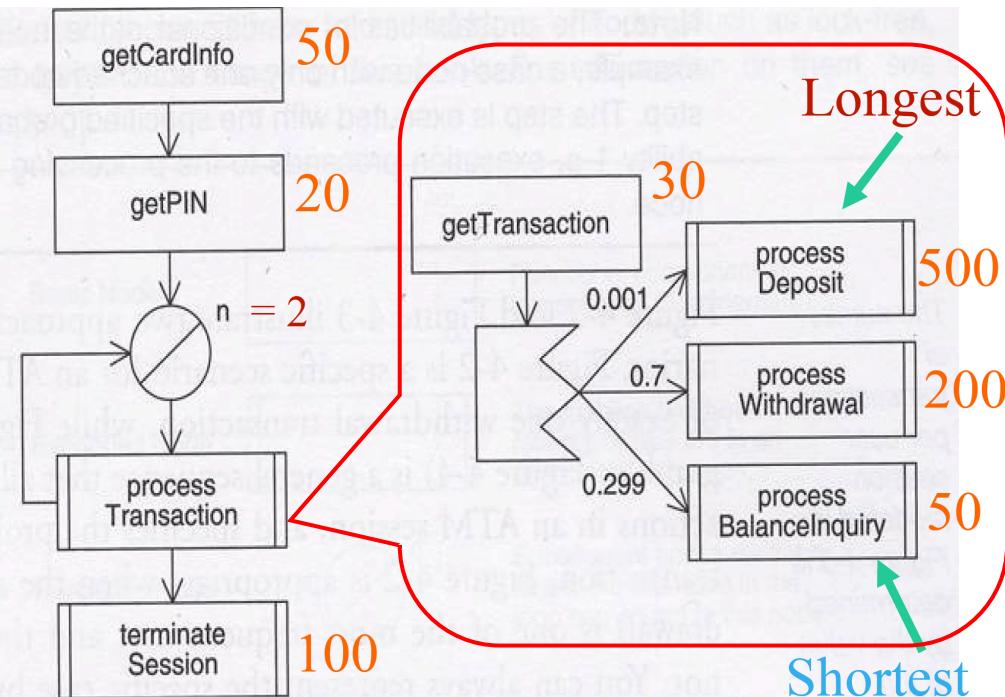


Figure 4-3: Execution Graph for General ATM Scenario

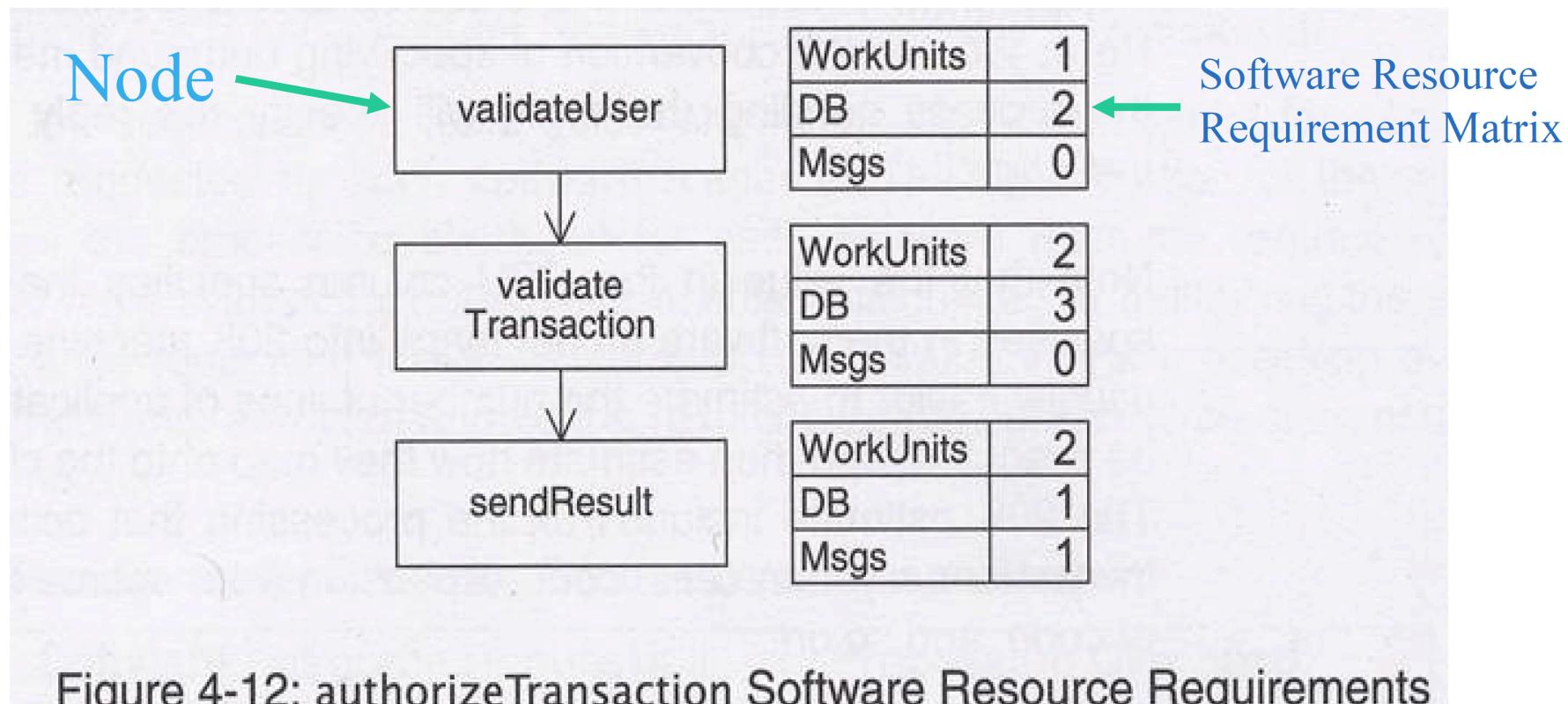
Figure 4-4: Subgraph for processTransaction Expanded Node

# Analysis Procedures

- Use both the best-and the worst-case estimates of resource requirements for each basic node
- Begin with a simplistic analysis of the best case and introduce more sophisticated analyses of realistic cases as more detailed information becomes available

# Software Resource Requirements

- Each basic **node** has specified SW resource requirements  $\mathbf{A}_j$  for each **service unit** j, e.g.



# Processing Overhead Matrix

- A chart of the computer resource requirements for each of the software resource requests

Table 4-1: Processing Overhead

| Device       | CPU     | Disk      |
|--------------|---------|-----------|
| Quantity     | 1       | 1         |
| Service Unit | Klnstr. | Phys. I/O |

| Network |
|---------|
| 1       |
| Msgs.   |

Hardware  
Resources

|   |
|---|
| 0 |
| 0 |
| 1 |

|          |     |   |
|----------|-----|---|
| WorkUnit | 20  | 0 |
| DB       | 500 | 2 |
| Msgs     | 10  | 2 |

Mapping between  
software resource  
requirements and  
computer device usage

|              |         |      |
|--------------|---------|------|
| Service time | 0.00001 | 0.02 |
|--------------|---------|------|

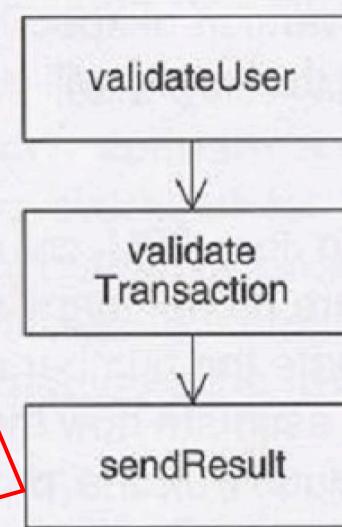
|      |
|------|
| 0.01 |
|------|

# Computing the total execution time

- **STEP 1:** uses the processing overhead matrix to calculate the total computer resources required per software resource for each node in the graph

Total Computer Resource Requirements for sendResult

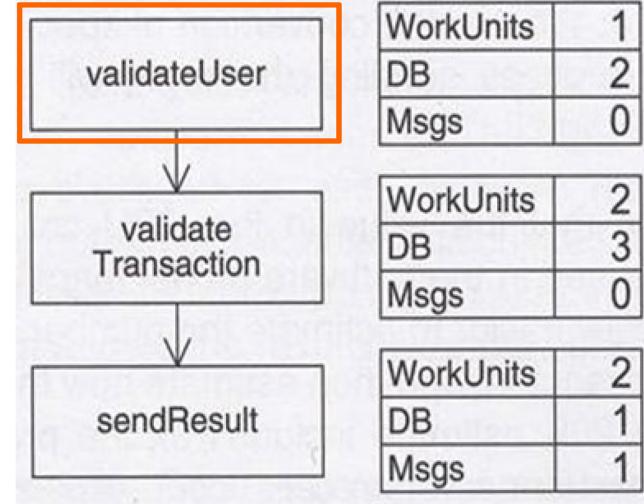
| Software Resource Requests |               | Processing Overhead |              |                  |
|----------------------------|---------------|---------------------|--------------|------------------|
| Name                       | Service Units | CPU Kinstr          | Physical I/O | Network Messages |
| WorkUnit                   | 2             | 20                  | 0            | 0                |
| DB                         | 1             | 500                 | 2            | 0                |
| Msgs                       | 1             | 10                  | 2            | 1                |
| <b>Total: sendResult</b>   |               | <b>550</b>          | <b>4</b>     | <b>1</b>         |



|           |   |
|-----------|---|
| WorkUnits | 1 |
| DB        | 2 |
| Msgs      | 0 |
| WorkUnits | 2 |
| DB        | 3 |
| Msgs      | 0 |
| WorkUnits | 2 |
| DB        | 1 |
| Msgs      | 1 |

Table 4-1: Processing Overhead

| Device       | CPU     | Disk      | Network |
|--------------|---------|-----------|---------|
| Quantity     | 1       | 1         | 1       |
| Service Unit | Klnstr. | Phys. I/O | Msgs.   |
| WorkUnit     | 20      | 0         | 0       |
| DB           | 500     | 2         | 0       |
| Msgs         | 10      | 2         | 1       |
| Service time | 0.00001 | 0.02      | 0.01    |



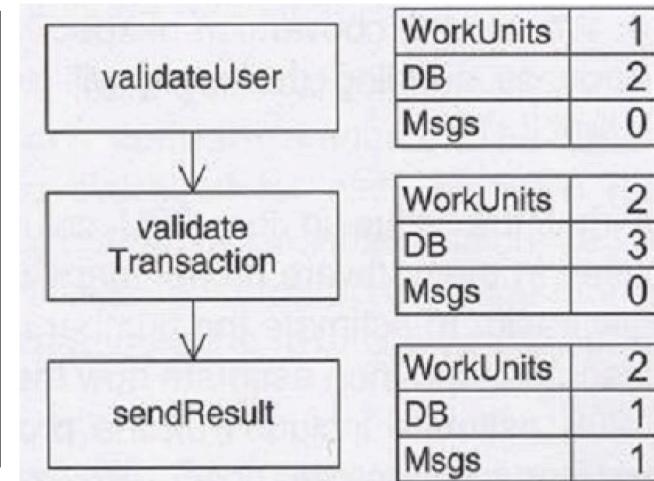
Software Resource Requirements

|              | Klnstr. | Phys. I/O | Msgs. |
|--------------|---------|-----------|-------|
| WorkUnits    | 1       | 20        | 0     |
| DB           | 2       | 500       | 2     |
| Msgs         | 0       | 10        | 2     |
| validateUser | 1020    | 4         | 0     |
|              | 0.00001 | 0.02      | 0.01  |

# Computing the total execution time

- **STEP 2:** computes the total computer resource requirements for the graph

| Processing Step                    | CPU<br>Kinstr | Physical<br>I/O | Network<br>Messages |
|------------------------------------|---------------|-----------------|---------------------|
| validateUser                       | 1,020         | 4               | 0                   |
| validateTransaction                | 1,540         | 6               | 0                   |
| sendResult                         | 550           | 4               | 1                   |
| <b>Total:</b> authorizeTransaction | 3,110         | 14              | 1                   |



# Computing the total execution time

- **STEP 3:** compute the best-case elapsed time

Table 4-1: Processing Overhead

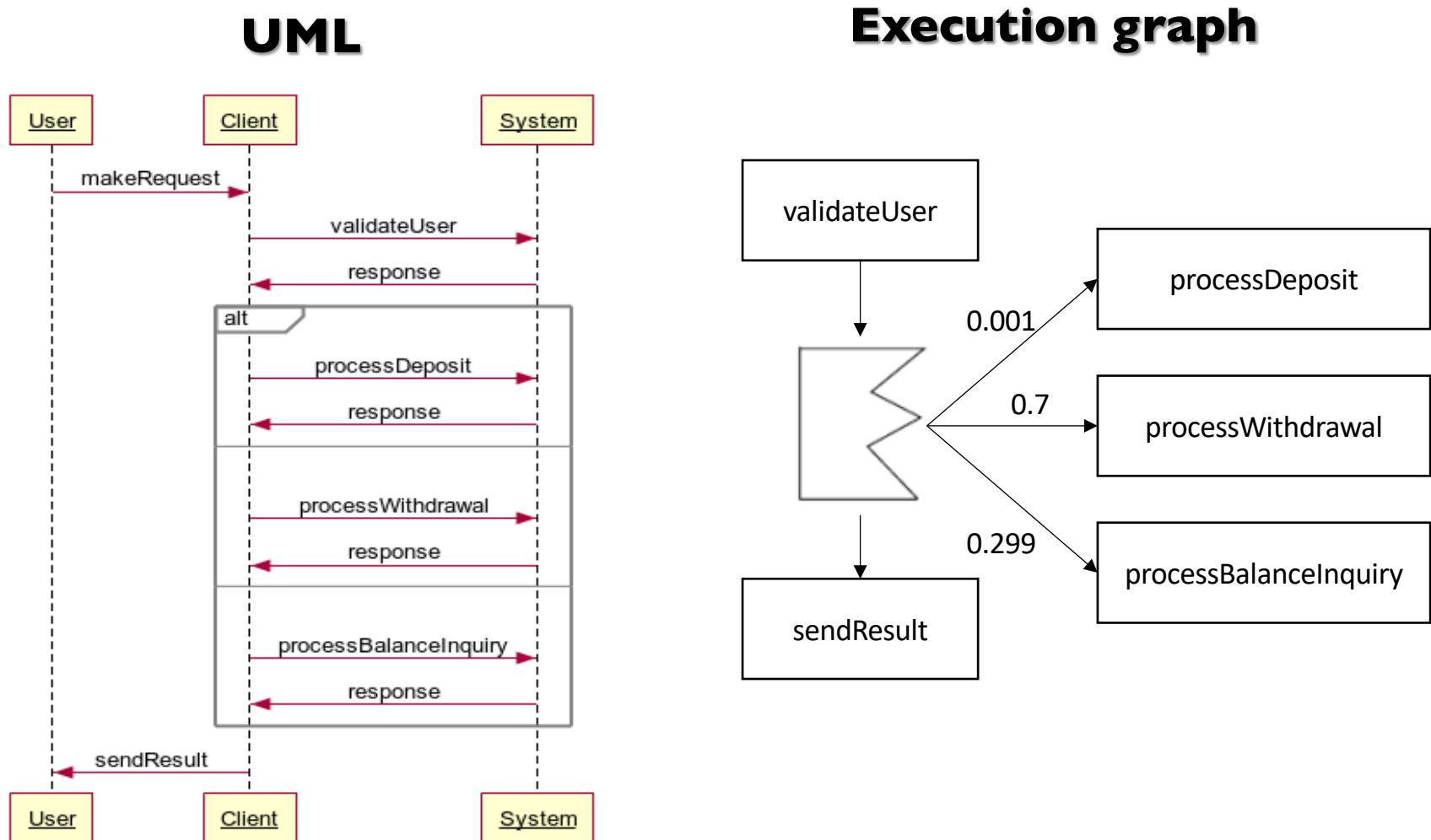
| Device              | CPU     | Disk      | Network |
|---------------------|---------|-----------|---------|
| Quantity            | 1       | 1         | 1       |
| Service Unit        | KInstr. | Phys. I/O | Msgs.   |
| WorkUnit            | 20      | 0         | 0       |
| DB                  | 500     | 2         | 0       |
| Msgs                | 10      | 2         | 1       |
| <b>Service time</b> | 0.00001 | 0.02      | 0.01    |

| Processing Step                    | CPU<br>Kinstr | Physical<br>I/O | Network<br>Messages |
|------------------------------------|---------------|-----------------|---------------------|
| validateUser                       | 1,020         | 4               | 0                   |
| validateTransaction                | 1,540         | 6               | 0                   |
| sendResult                         | 550           | 4               | 1                   |
| <b>Total: authorizeTransaction</b> | 3,110         | 14              | 1                   |

$$3,110 * 0.00001 + 14 * 0.02 + 1 * 0.01 = 0.32$$

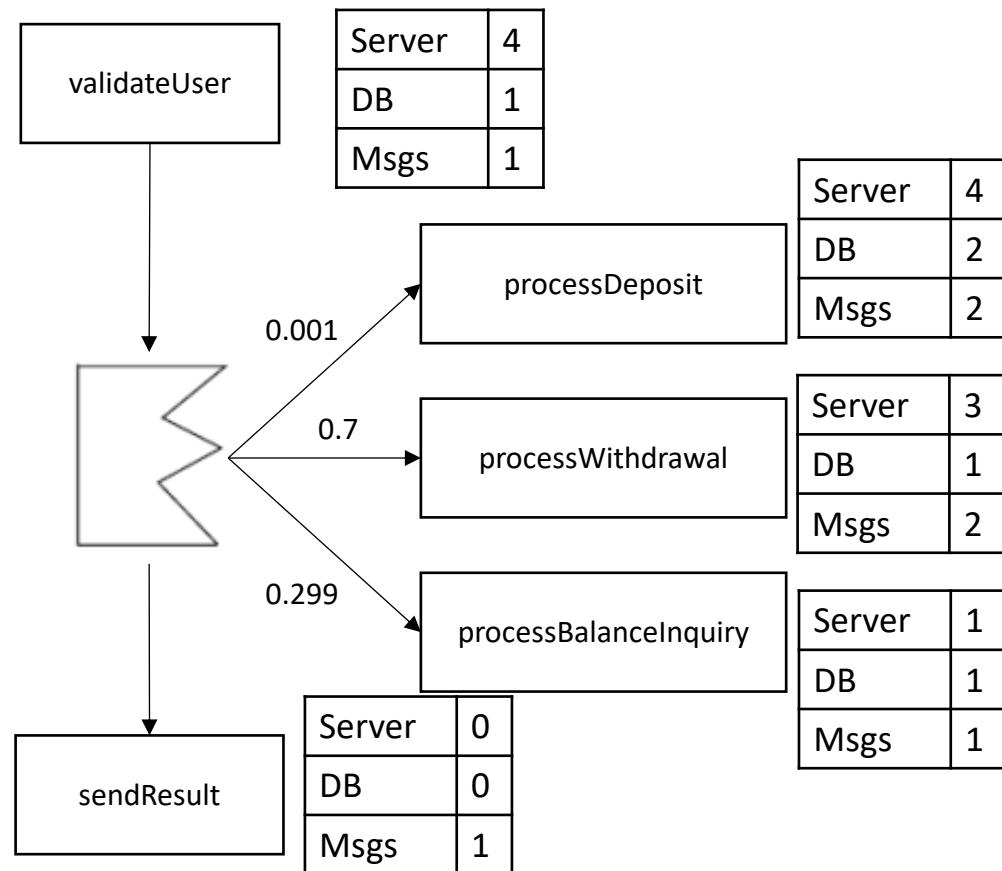
# Exercise: process Transaction scenario

## Estimate the best, worst, and average execution time



# Exercise: process Transaction scenario

## Estimate the best, worst, and average execution time



| Ressources   | CPU      | Disk  | Network |
|--------------|----------|-------|---------|
| Quantity     | 1        | 1     | 1       |
| Service unit | KInstr.  | I/O   | Msgs    |
|              |          |       |         |
| Server       | 800      | 0     | 0       |
| DB           | 200      | 2     | 1       |
| Msgs         | 10       | 2     | 1       |
|              |          |       |         |
| Service time | 0.000015 | 0.005 | 0.001   |

# **Queuing Network Models (System Execution Models)**

# Software Execution Models vs. Queuing Network Models

- **Software execution models**

- provide a static analysis of the **mean, best-and worst-case response times** for software
- characterize the resource requirements of the proposed software alone, in the **absence of other workloads or multiple users**

- **Queuing network models (QNM)**

- characterize the software's performance in the **presence of dynamic factors**, such as other work loads or multiple users
- aim to solve the **contention for resources**

If the software execution model indicates that there are no problems, then you are ready to construct and solve the queuing networks to account for contention efforts

# Benefits of QNM

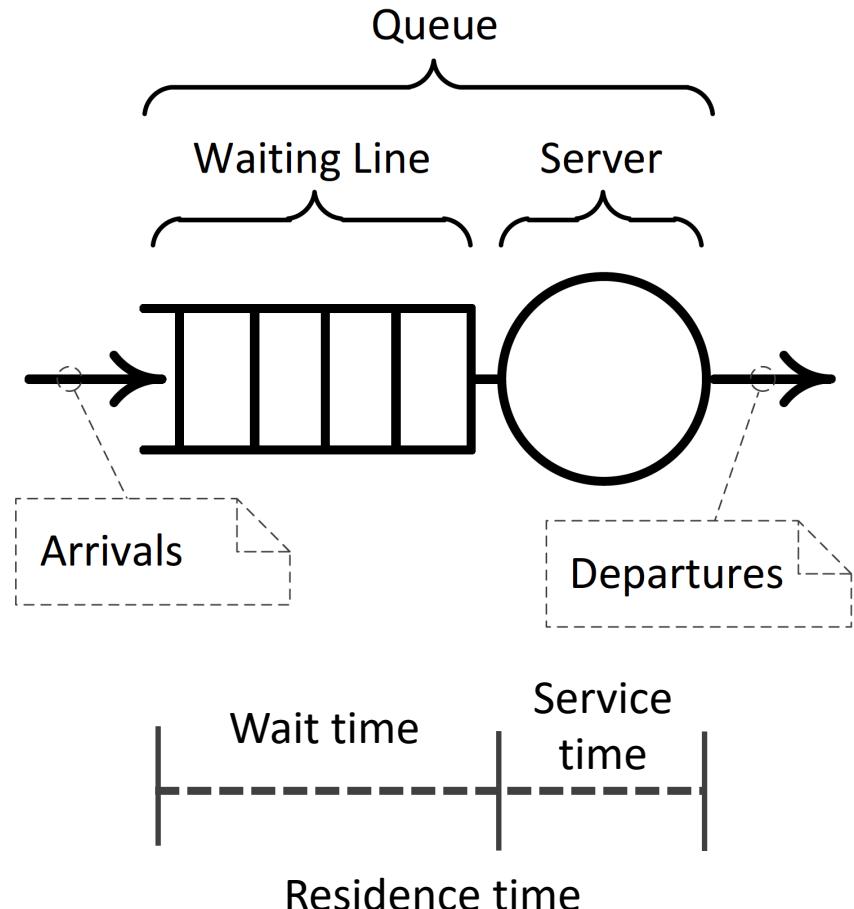
- More precise metrics that account for resource contention
- Sensitivity of performance metrics to variations in workload composition
- Scalability of the hardware and software to meet future demands
- Effect of new software on service level objectives of other systems
- Identification of bottleneck resources
- Comparative data on performance improvement options

# Sources of Contention for Resources

- **Multiple users** of an application or transaction executing at one time, e.g. several ATM customers do a withdrawal simultaneously
- **Multiple applications or systems** executing on the same hardware resources at one time
- The application under consideration can have separate **concurrent processes**
- The application may be **multi-threaded** to handle concurrent requests for different external processes

# QNM Basics: Queues

- The basic component of queuing networks is a **queue**, also referred to as a **service station** or **service center**.
- A queue consists of a **waiting line** and a **server** (e.g., CPU, disk, network), which serves incoming requests (a queue can have multiple servers)



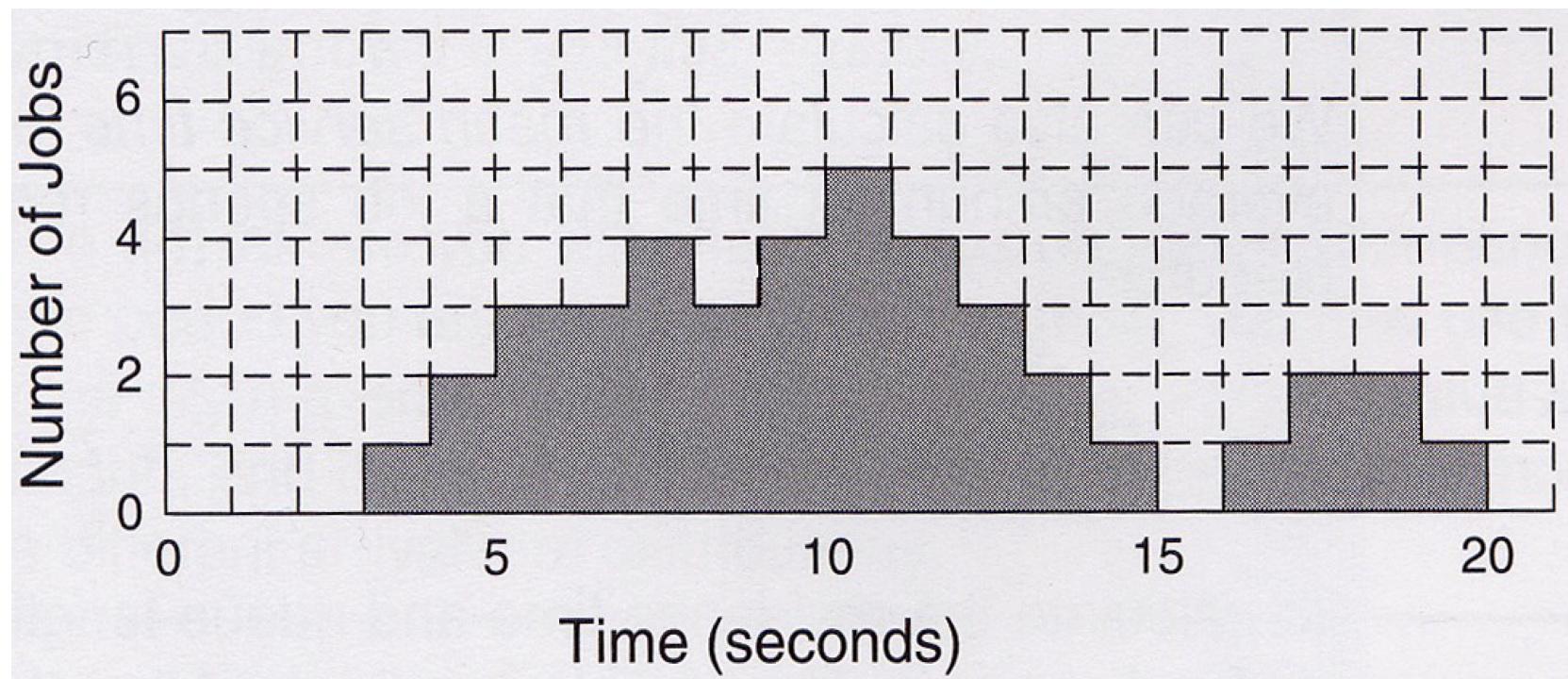
# Performance Metrics

- Performance metrics of interest for each server are
  - **Residence time, RT**: the average time jobs spend in the server, in service and waiting
  - **Utilization, U**: the average percentage of the time the server is busy
  - **Throughput, X**: the average rate at which jobs complete service
  - **Queue length, N**: the average numbers of jobs at the server (receiving service and waiting)

# Performance Metrics (con't)

- The value of these metrics depend on
  - The number of jobs
  - The amount of service they need
  - The time required for the server to process individual jobs
  - The policy used to select the next job from the queue (e.g., the first-come-first-served or priority scheduling)

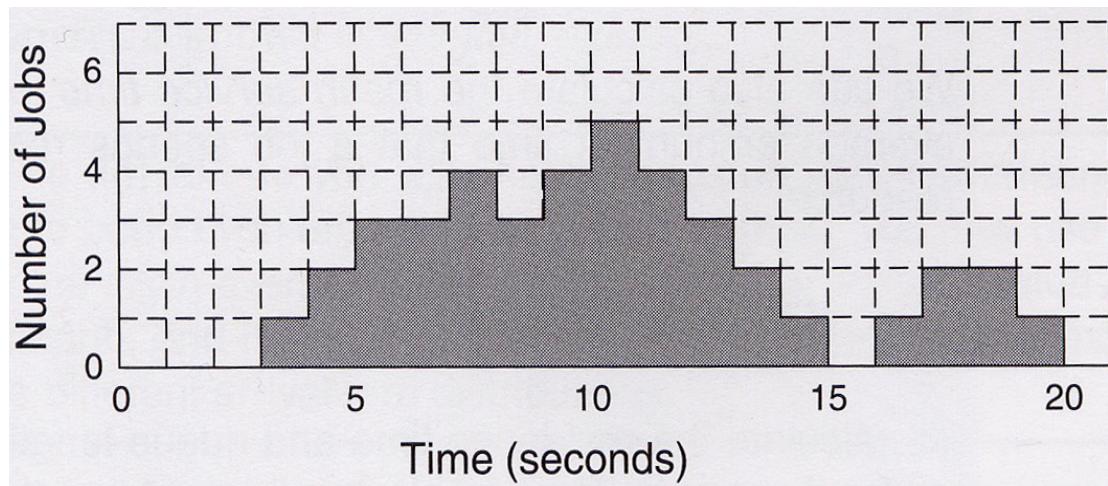
# Execution Profile



# Execution Profile (con't)

- From the execution profile, we obtain the following data:

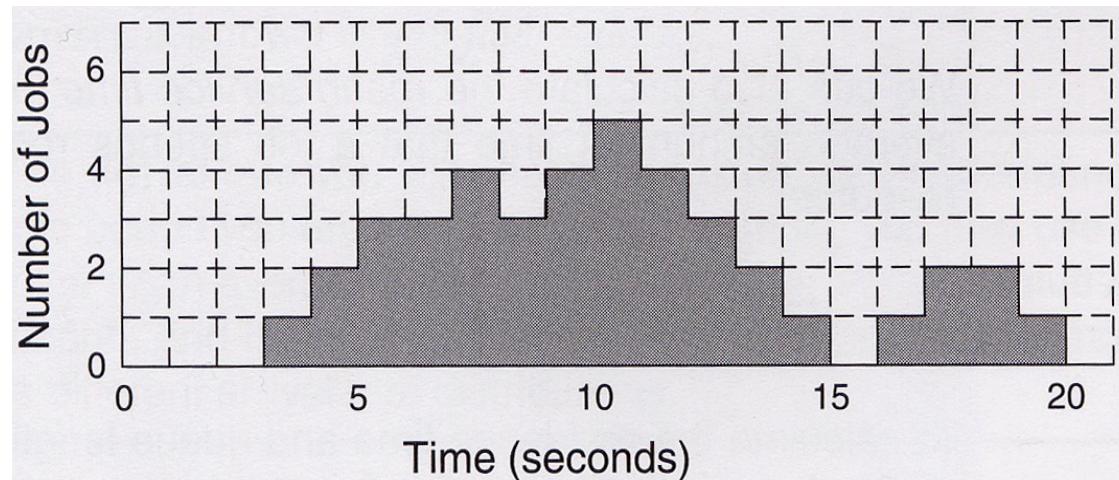
|                            |        |
|----------------------------|--------|
| ■ Measurement period, T    | 20 sec |
| ■ Number of arrivals, A    | 8 jobs |
| ■ Number of completions, C | 8 jobs |
| ■ Busy time, B             | 16 sec |



# Calculation of Performance Metrics

- Utilization,  $U = B/T$
- Throughput,  $X = C/T$
- Mean service time,  $S = B/C$
- Area under graph,  $W = \sum_{time}(\# \text{ of } jobs)$
- Residence time,  $RT = W/C$
- Queue length,  $N = W/T$

T: Total Period  
C: Completed  
B: Busy Time



# Calculation of Performance Metrics

- Utilization,

$$U = B/T = 0.8$$

T: Total Period = 20

C: Completed = 8

B: Busy Time = 16

- Throughput,

$$X = C/T = 0.4 \text{ jobs/sec}$$

- Mean service time,

$$S = B/C = 2 \text{ sec}$$

- Area under graph,

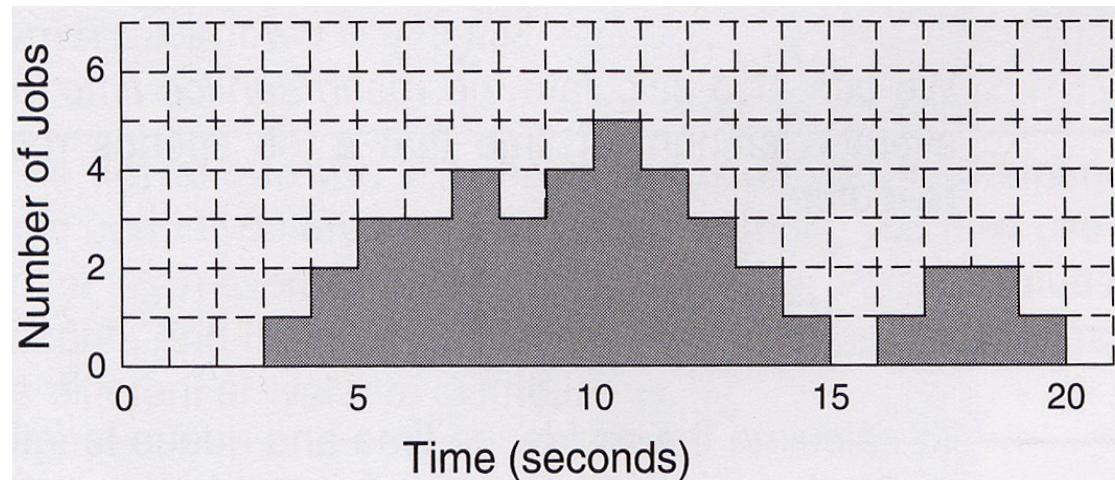
$$W = \sum_{time} (\# \text{ of jobs}) = 41 \text{ jobs}$$

- Residence time,

$$RT = W/C = 5.125 \text{ sec}$$

- Queue length,

$$N = W/T = 2.05 \text{ jobs}$$



# Solving the Queueing Model

- Use similar calculations, based on predicted **workload intensity** and **service requirements**
- **Workload intensity** is a measure of the number of requests made by a workload in a given time interval
- **Service requirements** are the amount of time that the workload requires from each of the devices in the processing facility

# Solving the Queueing Model (con't)

- Assume that the system is fast enough to handle the arrivals, and thus ***the completion rate or throughput equals the arrival rate***
- This property is called ***jobs-flow balance***

# Example

- Workload intensity
  - Arrival rate,  $\lambda = 0.4$  jobs per sec
- Service requirements
  - Mean service time,  $S = 2$  sec

We then calculate the following average values:

- Throughput,  $X = \lambda$
- Utilization,  $U = XS$  (Utilization Law)
- Residence time,  $RT = \frac{S}{1-U}$
- Queue length,  $N = X * RT$  (Little Law)

# Exercise: Use of Utilization Law

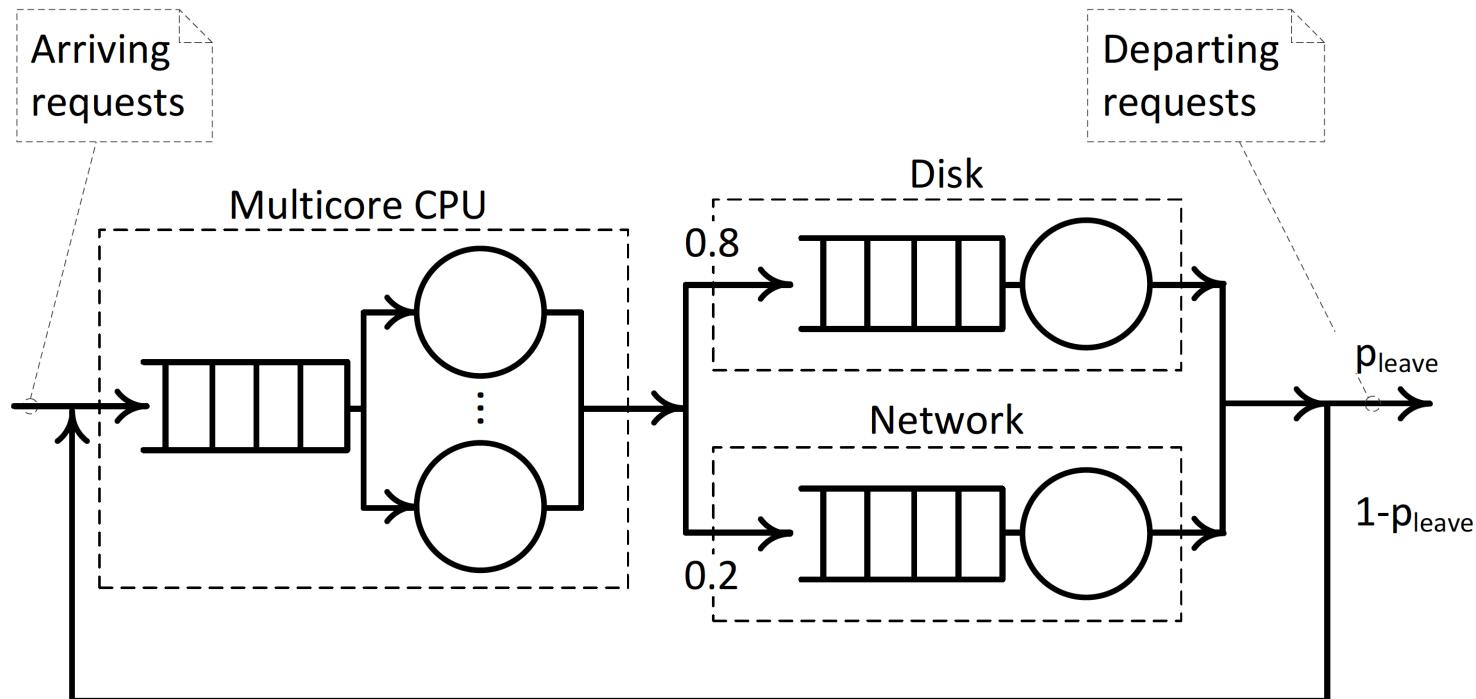
- A network segment transmits 1,000 packets/sec. Each packet has an average transmission time equal to 0.15 msec. What is the utilization of LAN segment?

# Exercise: Use of Little Law

- An NFS server was monitored during 30 minutes and the number of I/O operations performed during the period was found to be 10,800. The average number of active NFS requests was found to be three. What was the average response time per NFS request at the server?

# Queuing Network Models

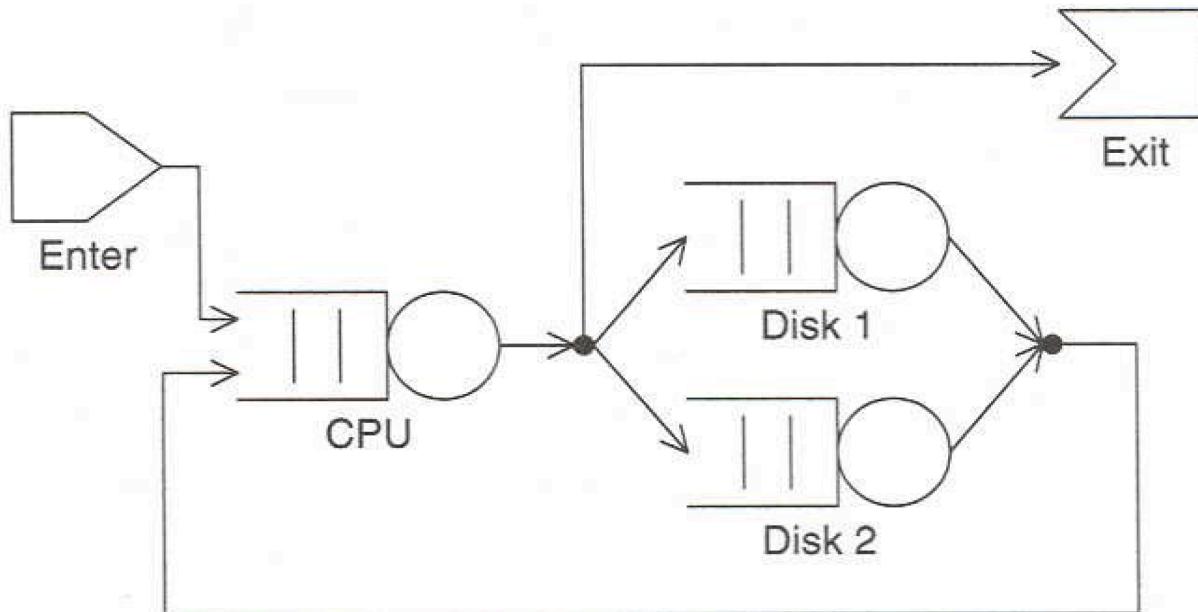
- A queueing network (QN) consists of **two or more queues** (service stations) that are connected together and serve requests sent by clients.
- The **routing of requests** in the queueing network is specified by a **probability matrix**.



# Types of QNM

- **Open models**
  - The requests come from a source that is external of the queueing network and leave the network after service completion
- **Closed models**
  - No external source of requests and no departing requests (the population of requests in the queueing network remains constant)
- **Mixed models**
  - Open for some workload classes and closed for others

# Open QNM



# Open QNM (con't)

- Open QNM is appropriate for systems with external arrivals and departures, such as ATM
- For an open QNM, specify the **workload intensity** and **service requirements**
- The workload is the **arrival rate** that rate at which jobs arrive for service
- The service requirements are **the number of visits** for each device, and **the average service time per visit**, or **the total demand** for that device

# Open QNM Computation

- We specify the following parameters:
  - $\lambda$  System arrival rate
  - $V_i$  Number of visits to device
  - $S_i$  Mean service time at device
- System throughput,  $X_0$   $X_0 = \lambda$
- Throughput of device  $i$ ,  $X_i$   $X_i = X_0 \times V_i$
- Utilization of device  $i$ ,  $U_i$ ,  $U_i = X_i \times S_i$
- Residence time per visit at device  $i$ ,  $RT_i$ 
$$RT_i = \frac{S_i}{1 - U_i}$$

# Open QNM Computation

- Queue length for device  $i$ ,  $N_i$

$$N_i = X_i \times RT_i$$

- System queue length,  $N$

$$N = \sum_i N_i$$

- System response time,  $RT$

$$RT = \frac{N}{X_0}$$

# Example: Open QNM Solution

- Sample parameters

System arrival rate,  $\lambda = 5$  jobs per second

| <b>Number of visits, V</b> |   | <b>Mean service time, S</b> |      |
|----------------------------|---|-----------------------------|------|
| CPU                        | 5 | CPU                         | 0.01 |
| Disk1                      | 3 | Disk1                       | 0.03 |
| Disk2                      | 1 | Disk2                       | 0.02 |

# Example: Open QNM Solution

| Metrics                         | CPU | Disk1 | Disk2 |
|---------------------------------|-----|-------|-------|
| 1. <b>X</b> , throughput        |     |       |       |
| 2. <b>S</b> , mean service time |     |       |       |
| 3. <b>U</b> , utilization       |     |       |       |
| 4. <b>RT</b> , residence time   |     |       |       |
| 5. <b>N</b> , queue length      |     |       |       |
| Total jobs in system =          |     |       |       |
| System response time =          |     |       |       |

# Example: Open QNM Solution

| Metrics   | CPU   | Disk1 | Disk2 |
|---|-------|-------|-------|
| 1. <b>X</b> , throughput                              | 25    | 15    | 5     |
| 2. <b>S</b> , mean service time                       | 0.01  | 0.03  | 0.02  |
| 3. <b>U</b> , utilization                             | 0.25  | 0.45  | 0.10  |
| 4. <b>RT</b> , residence time                         | 0.013 | 0.055 | 0.022 |
| 5. <b>N</b> , queue length                            | 0.325 | 0.825 | 0.111 |
| Total jobs in system = $0.325 + 0.825 + 0.111 = 1.26$ |       |       |       |
| System response time = $1.26/5 = 0.252$ sec           |       |       |       |

# Exercise: what if the arrival rate doubles?

- Sample parameters

System arrival rate,  $\lambda = 5$  jobs per second

10

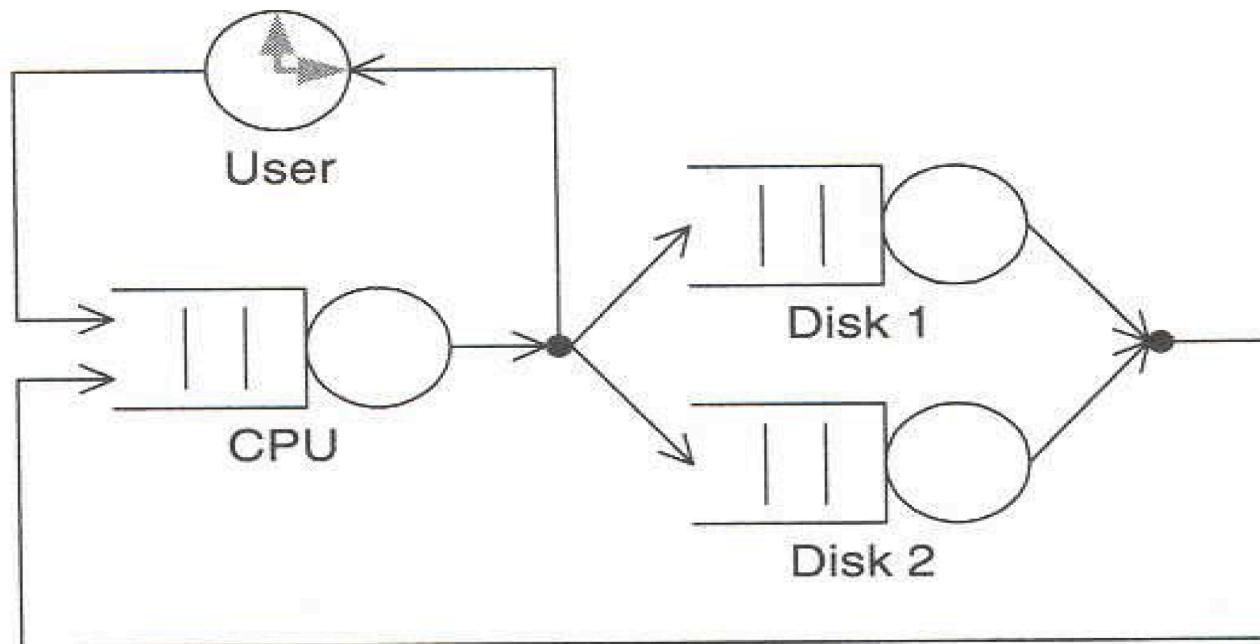
| Number of visits, V | Mean service time, S |
|---------------------|----------------------|
| CPU                 | 5                    |
| Disk1               | 3                    |
| Disk2               | 1                    |

# Exercise: what if the arrival rate doubles?

| Metrics                    | CPU | Disk1 | Disk2 |
|----------------------------|-----|-------|-------|
| 1. $X$ , throughput        |     |       |       |
| 2. $S$ , mean service time |     |       |       |
| 3. $U$ , utilization       |     |       |       |
| 4. $RT$ , residence time   |     |       |       |
| 5. $N$ , queue length      |     |       |       |
| Total jobs in system =     |     |       |       |
| System response time =     |     |       |       |

# Closed QNM

- Closed QNM has no external arrivals or departures
- A fixed number of jobs keep circulating among queues



# Solving Closed QNM

- This model needs
  - ***The number of users*** (or the number of simultaneous jobs)
  - ***The think time***, i.e., the average delay between the receipt of a response and the submission of the next
  - Number of visits
  - Service time
  - Total demand for each device

# Deriving System Model Parameters from Software Model Results

- **Step 1:** use queue-servers to represent the key computer resources or devices that you specified in the software execution model and add the connections between queues to **complete a model topology**
- **Step 2:** decide whether the system is best modeled as an **open or closed QNM**
- **Step 3:** determine the **workload intensities** for each scenario
- **Step 4:** specify the **service requirements**

# Example: ATM authorizeTransaction Scenario

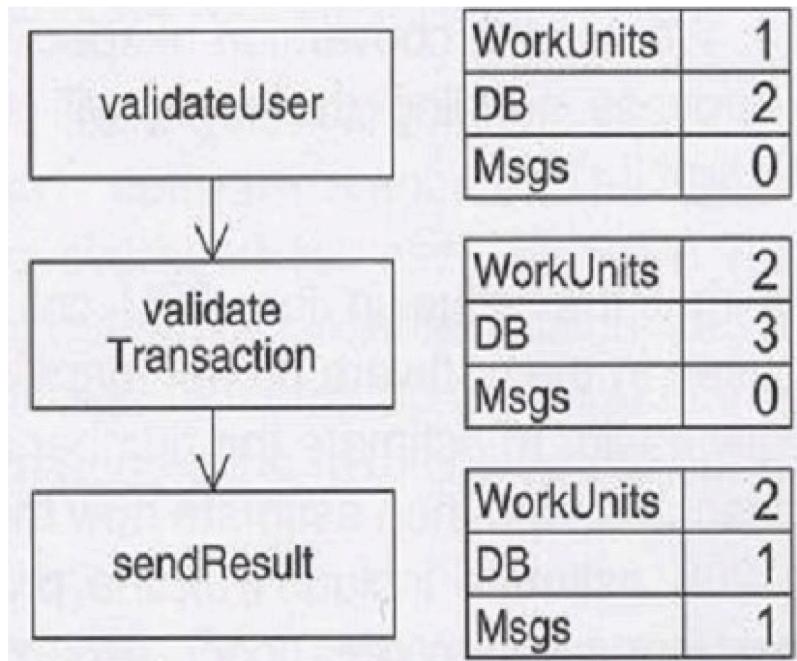
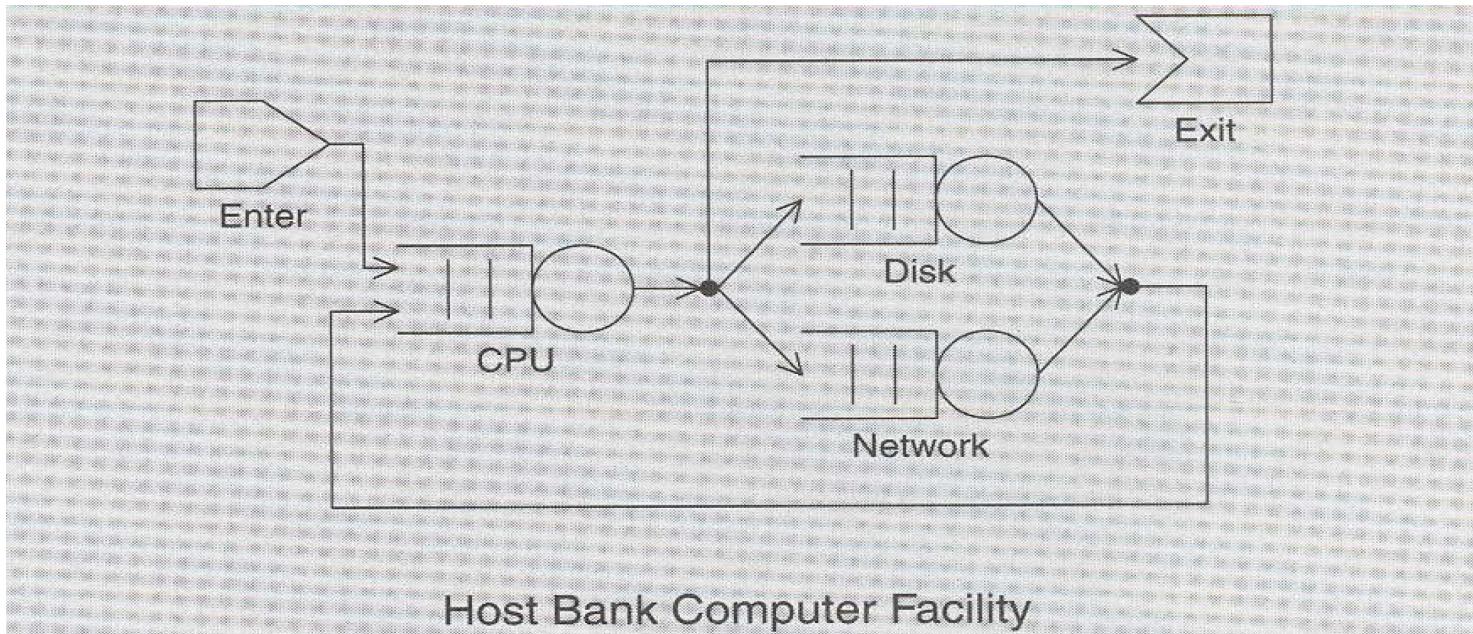


Table 4-1: Processing Overhead

| Device       | CPU     | Disk      | Network |
|--------------|---------|-----------|---------|
| Quantity     | 1       | 1         | 1       |
| Service Unit | Klnstr. | Phys. I/O | Msgs.   |
| WorkUnit     | 20      | 0         | 0       |
| DB           | 500     | 2         | 0       |
| Msgs         | 10      | 2         | 1       |
| Service time | 0.00001 | 0.02      | 0.01    |

Software Model for authorizeTransaction

# Example: ATM authorizeTransaction Scenario



| Processing step                    | CPU<br>Kinstr. | Disk      | Network<br>Messages |
|------------------------------------|----------------|-----------|---------------------|
| validateUser                       | 1,020          | 4         | 0                   |
| validateTransaction                | 1,540          | 6         | 0                   |
| sendResult                         | 550            | 4         | 1                   |
| <b>Total: authorizeTransaction</b> | <b>3,110</b>   | <b>14</b> | <b>1</b>            |

# Example: ATM authorizeTransaction Scenario

| Device  | Visits, V | Device Service Time, S |
|---------|-----------|------------------------|
| CPU     | all       | .0311                  |
| Disk    | 14        | .02                    |
| Network | 1         | .01                    |

# Modeling Hints

- **Multiple users and workload** (e.g., arrival rate, the number of users, and think time)
- **Average vs. Peak Performance**
  - Basis QNMs calculates average values
- **Sensitivity**: if a small change in one parameter causes a large change in the computed metrics, the model is sensitive to that quantity
- **Scalability**: improves response times for your anticipated future loads
- **Bottlenecks**: the bottleneck device is the one with the highest utilization

# Machine learning based performance models

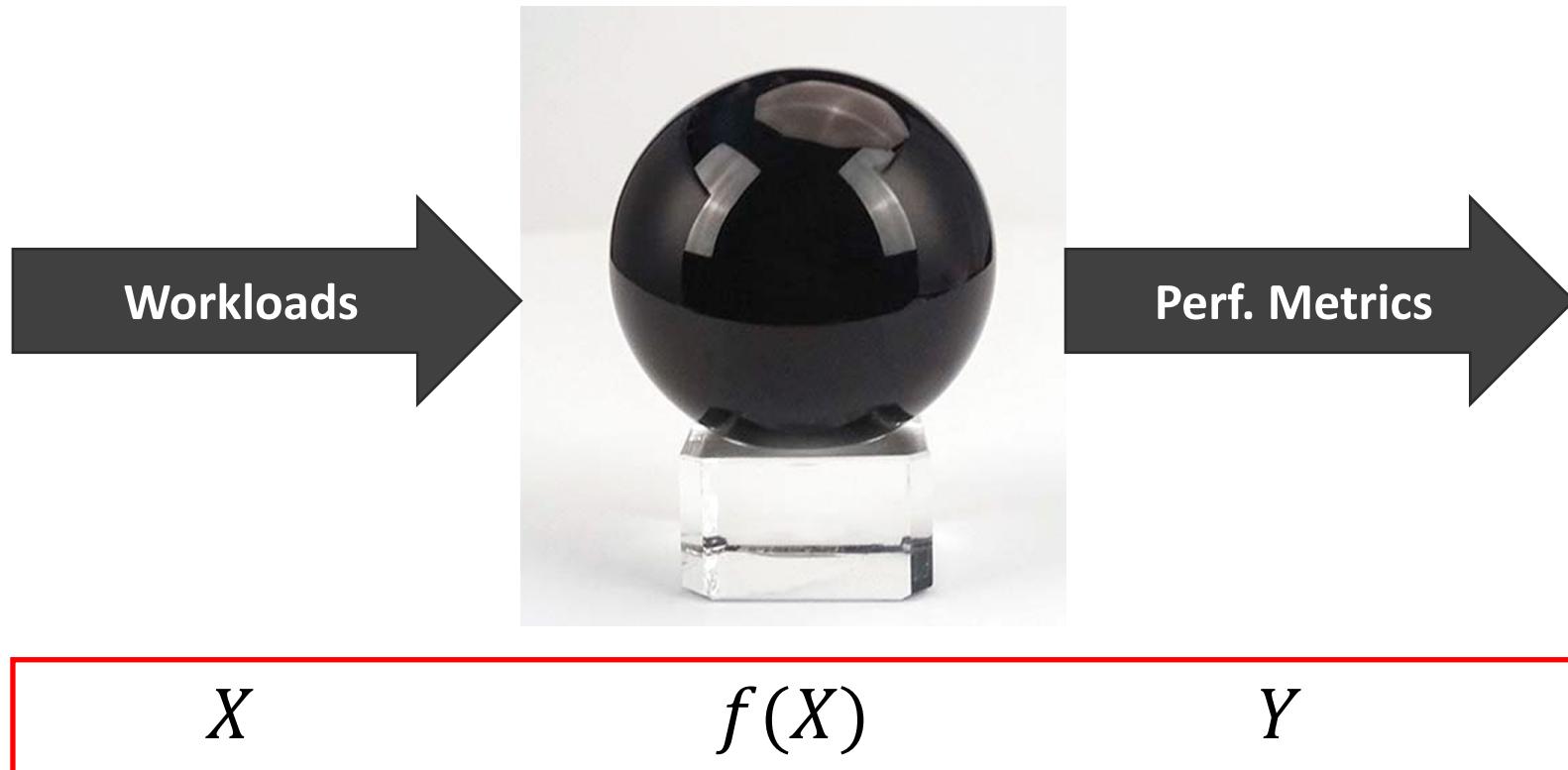
# Drawbacks of Queuing Network models

- Require extensive knowledge of the software and system
- Cannot handle **passive resources** (resource that are required for processing but do no work themselves, e.g., memory)
- Only estimates **average metrics**; cannot estimate minimum, maximum, variance, distributions, etc.
- **Difficult to scale** to large-scale software systems
- Can we treat of the software and system as a **black-box**?

# Black-box (machine learning based) performance models



# Black-box (machine learning based) performance models



# Black-box (machine learning based) performance models



$X$

$f(X)$

$Y$

Given workloads ( $X$ ) and measured performance metrics ( $Y$ ), we can train a machine learning model ( $Y = f(X)$ )

# Workloads (independent variables)

| Timestamp | Log line                                 |
|-----------|--|
| 00:00     | Load data by Alice with size 32768 bytes |
| 00:02     | Read data by Alice with size 2048 bytes  |
| 00:03     | Read data by Dan with size 1024 bytes    |
| 00:05     | Read data by Alice with size 16384 bytes |
| 00:06     | Write data by Alice with size 8192 bytes |

In the six seconds:

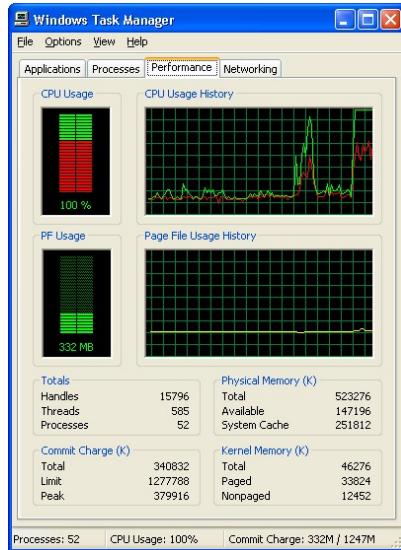
$$X(\text{Load}) = 1; X(\text{Read}) = 3; X(\text{Write}) = 1$$

# Performance metrics (dependent variables)

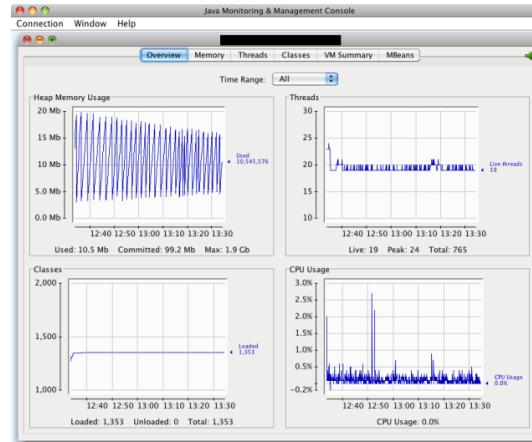
- Utilization (CPU, memory, disk, network)
- Response time
- Throughput
- Power consumption
- Battery
- ...

# How to collect performance metrics?

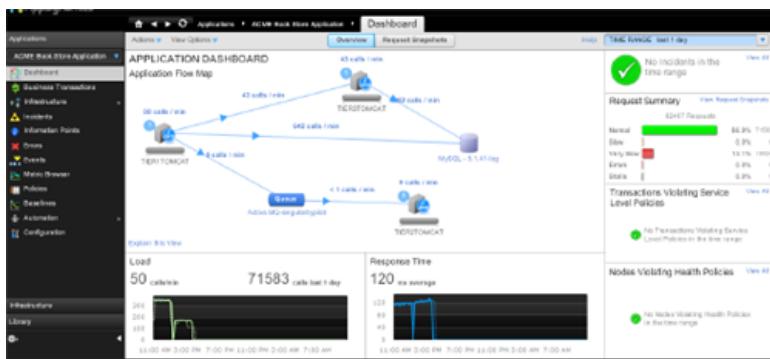
# Monitoring



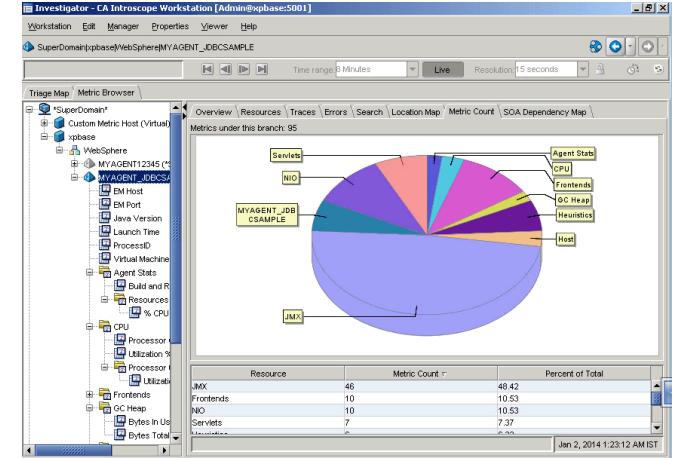
Task Manager



JConsole



App Dynamics



CA Willy

```
baban@hashprompt:~$ pidstat -u -r 1 1
Linux 3.2.0-36-generic (hashprompt)      Friday 15 February 2013   _x86_64_  (4 CPU)

03:24:49 IST    PID %usr %system %guest %CPU    CPU  Command
03:24:50 IST    1554 0.00 0.99 0.00 0.99 2 Xorg
03:24:50 IST    2708 2.97 0.00 0.00 2.97 0 cinnamon
03:24:50 IST    2731 0.00 0.99 0.00 0.99 0 gkrellm
03:24:50 IST    6231 0.99 0.00 0.00 0.99 3 chromium-browse
03:24:50 IST   17570 0.99 0.00 0.00 0.99 3 pidstat

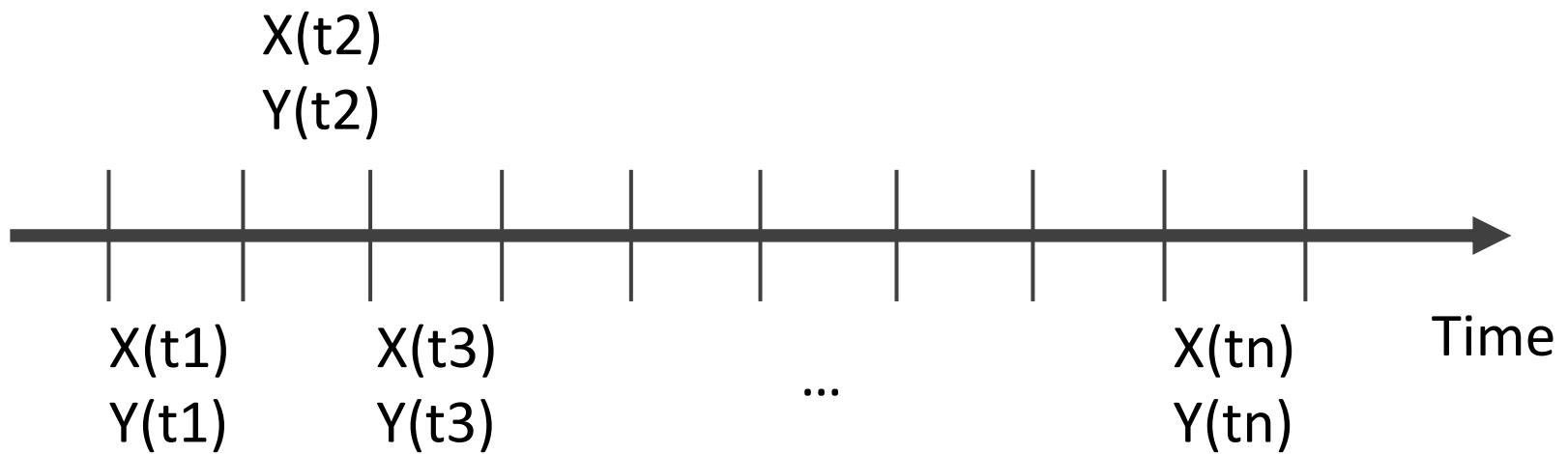
03:24:49 IST    PID minflt/s majflt/s VSZ  RSS %MEM  Command
03:24:50 IST   1939 114.85 0.00 107088 1260 0.03 cpufreqd
03:24:50 IST    2708 1.98 0.00 1673894 139240 3.63 cinnamon
03:24:50 IST    2731 11.88 0.00 578060 14500 0.38 gkrellm
03:24:50 IST   6231 100.99 0.00 1088184 165708 4.32 chromium-browse
03:24:50 IST   17570 369.31 0.00 95436 1072 0.03 pidstat

Average:    PID %usr %system %guest %CPU    CPU  Command
Average:   1554 0.00 0.99 0.00 0.99  Xorg
Average:   2708 2.97 0.00 0.00 2.97  - cinnamon
Average:   2731 0.00 0.99 0.00 0.99  - gkrellm
Average:   6231 0.99 0.00 0.00 0.99  - chromium-browse
Average:  17570 0.99 0.00 0.00 0.99  pidstat

Average:    PID minflt/s majflt/s VSZ  RSS %MEM  Command
Average:   1939 114.85 0.00 107088 1260 0.03 cpufreqd
Average:   2708  1.98 0.00 1673894 139240 3.63 cinnamon
Average:   2731 11.88 0.00 578060 14500 0.38 gkrellm
Average:   6231 100.99 0.00 1088184 165708 4.32 chromium-browse
Average:  17570 369.31 0.00 95436 1072 0.03 pidstat
baban@hashprompt:~$
```

pidstat

# Aligning workloads and performance metrics by fixed time intervals



How to aggregate workload variables and performance metrics into fixed time intervals (e.g., every minute)?

- Count (for workloads)
- Mean/Min/Max/Median/Sum (for performance metrics)

# Exercise: build a performance model for OpenMRS

- Given data:
  - Workload counts (extracted from logs) for every 30 seconds
  - Performance metrics (CPU utilization) averaged over every 30 seconds
- Build a machine-learning based performance model for OpenMRS
  - Given Python code in a Jupyter notebook
  - Using linear regression or random forest
- Download code and data:
  - [https://drive.google.com/drive/folders/168q\\_9hAYmf2x6fmLPqjqlC48UTVBLI2y?usp=sharing](https://drive.google.com/drive/folders/168q_9hAYmf2x6fmLPqjqlC48UTVBLI2y?usp=sharing)