



### Homework 4 B1141065 電機四乙 陳昱安

若  $D = \{[22,60], [40,25], [60,30], [64,66], [80,30], [82,55]\}$ , 請寫出使用 complete linkage 分群的計算過程, 建立 dendrogram, 最後分三群, 寫出最後哪些資料分在同一群

解: <key> 每次合併距離值最近的2個點(集合), 直到完成分群

1° 以全域計算距離

$$d([22,60], [40,25]) = 39.357 \quad d([22,60], [60,30]) = 48.414 \quad d([22,60], [64,66]) = 42.4264$$

$$d([22,60], [80,30]) = 65.299 \quad d([22,60], [82,55]) = 60.2079 \quad d([40,25], [60,30]) = 20.615$$

$$d([40,25], [64,66]) = 47.5078 \quad d([40,25], [80,30]) = 40.31 \quad d([40,25], [82,55]) = 51.6139$$

$$d([60,30], [64,66]) = 36.2215 \quad d([60,30], [80,30]) = 20 \quad d([60,30], [82,55]) = 33.3016$$

$$d([64,66], [80,30]) = 39.395 \quad d([64,66], [82,55]) = 21.095 \quad d([80,30], [82,55]) = 25.079$$

2° 第1輪分群

$\because d([60,30], [80,30]) = 20$  為目前最小  $\Rightarrow$  說明兩者距離值最近 5群羊

$\therefore$  將 [60,30] 與 [80,30] 合併  $\Rightarrow [22,60], [40,25], [60,30], [80,30], [64,66], [82,55]$

3° 第2輪分群

$$\textcircled{1} \quad d([22,60], [60,30], [80,30]) = \max \{d([22,60], [60,30]), d([22,60], [80,30])\} = 65.299$$

$$\textcircled{2} \quad d([40,25], [60,30], [80,30]) = \max \{d([40,25], [60,30]), d([40,25], [80,30])\} = 40.31$$

$$\textcircled{3} \quad d([64,66], [60,30], [80,30]) = \max \{d([64,66], [60,30]), d([64,66], [80,30])\} = 39.395$$

$$\textcircled{4} \quad d([82,55], [60,30], [80,30]) = \max \{d([82,55], [60,30]), d([82,55], [80,30])\} = 33.3016 \quad \dots$$

$\Rightarrow$  其中  $d([64,66], [82,55]) = 21.095$  為目前最小 4群羊

$\therefore$  將 [64,66] 與 [82,55] 合併  $\Rightarrow [22,60], [40,25], [60,30], [80,30], [64,66], [82,55]$

4° 第3輪分群

$$\textcircled{1} \quad d([22,60], [64,66], [82,55]) = \max \{d([22,60], [64,66]), d([22,60], [82,55])\} = 60.2079$$

$$\textcircled{2} \quad d([40,25], [64,66], [82,55]) = \max \{d([40,25], [64,66]), d([40,25], [82,55])\} = 51.6139$$

$$\textcircled{3} \quad d([60,30], [80,30], [64,66], [82,55]) = d([64,66], [80,30]) = 39.395 \text{ 此為目前最小}$$

$\Rightarrow$   $[60,30], [80,30]$  與  $[64,66], [82,55]$  合併

$\Rightarrow [22,60], [40,25], [60,30], [80,30], [64,66], [82,55]$  A: 共分成3群, 資料結果如下:

$$\begin{cases} c_1: [22,60] \\ c_2: [40,25] \\ c_3: [60,30], [80,30], [64,66], [82,55] \end{cases}$$

3群羊(完成)