



# 序列型樣探勘與軟體操作

---



國立宜蘭大學資訊工程系

吳政瑋 助理教授

[wucw@niu.edu.tw](mailto:wucw@niu.edu.tw)



# 本堂教學重點

---

- 傳統頻繁項目集探勘缺點
- 序列型樣探勘目的
- 序列型樣探勘應用
- 序列型樣探勘技術
- 序列型樣探勘軟體操作



## 傳統頻繁項目集探勘缺點 (Cont. 1/2)

- 頻繁項目集探勘(Frequent Itemset Mining；簡稱 FIM)常用於**購物籃分析(Market Basket Analysis)**的應用中。
- 在 FIM 的架構中
  - 僅能找出大部份顧客經常**同時一起購買**的商品組合
  - 無法找出大部份顧客**循序購買**商品的行為



## 傳統頻繁項目集探勘缺點 (Cont. 2/2)

- 隨著**條碼技術(Bar-code Technology)**的進步，零售組織能夠收集大量的銷售資料及交易資料。
- 此類資料中的記錄通常包含**交易日期(Transaction Date)**以及顧客所**購買的商品(Bought Items)**。
- 當顧客使用信用卡或會員卡購物時，或需填寫訂單時，此類資料通常還會包含**顧客的 ID (Customer ID)**。

# A Customer-Sequence Database & Sequential Patterns

Transaction Time	Customer Id	Items Bought
June 10 '93	2	10, 20
June 12 '93	5	90
June 15 '93	2	30
June 20 '93	2	40, 60, 70
June 25 '93	4	30
June 25 '93	3	30, 50, 70
June 25 '93	1	30
June 30 '93	1	90
June 30 '93	4	40, 70
July 25 '93	4	90



Customer Id	TransactionTime	Items Bought
1	June 25 '93	30
1	June 30 '93	90
2	June 10 '93	10, 20
2	June 15 '93	30
2	June 20 '93	40, 60, 70
3	June 25 '93	30, 50, 70
4	June 25 '93	30
4	June 30 '93	40, 70
4	July 25 '93	90
5	June 12 '93	90



Customer Id	Customer Sequence
1	$\langle (30) (90) \rangle$
2	$\langle (10\ 20) (30) (40\ 60\ 70) \rangle$
3	$\langle (30\ 50\ 70) \rangle$
4	$\langle (30) (40\ 70) (90) \rangle$
5	$\langle (90) \rangle$



Sequential Patterns with support $> 25\%$
$\langle (30) (90) \rangle$
$\langle (30) (40\ 70) \rangle$



# 序列型樣探勘的應用

---

## ■ 購物籃分析

- ex: <(營養補品), (無香味乳液), (無香味肥皂), (大包裝棉花球)>

## ■ 商品出租

- ex: <(星際大戰), (帝國大反擊), (絕地大反攻)>

## ■ 路徑分析

- ex: <(弘志路), (女中路), (神農路), (宜蘭大學)>

## ■ 3C用品銷售

- ex: <(電腦), (列表機, 列印紙), (墨水匣)>

# 序列型樣探勘相關定義 (Cont. 1/3)

## ■ Item

- ex: (40), (70)

## ■ Itemset

- ex: (40 70)

## ■ Sequence

- ex:  $\langle (30) (40\ 70) (90) \rangle$

## ■ Sub-sequence

- ex:  $\langle (30)(90) \rangle$  is a sub-sequence of  $\langle (30)(40\ 70)(90) \rangle$

## ■ Super-sequence

- ex:  $\langle (30) (40\ 70) (90) \rangle$  is a super-sequence of  $\langle (30)(90) \rangle$

## ■ Support count of a sequence

- ex:  $\langle (30)(90) \rangle : 2$

## ■ Support of a sequence

- ex:  $\langle (30)(90) \rangle : 2/5 = 40\%$

## ■ Sequence Database

Customer Id	Customer Sequence
1	$\langle (30) (90) \rangle$
2	$\langle (10\ 20) (30) (40\ 60\ 70) \rangle$
3	$\langle (30\ 50\ 70) \rangle$
4	$\langle (30) (40\ 70) (90) \rangle$
5	$\langle (90) \rangle$



# 序列型樣探勘相關定義 (Cont. 2/3)

---

- **Sequential Pattern (SP)**

- A sequence having a support no less than  $min\_sup$
- ex:  $min\_sup = 25\%$ ,  $\langle (30)(90) \rangle$ ,  $\langle (30)(40\ 70) \rangle$  are sequential patterns

- **Frequent Sequence**

- A sequential pattern is also called *frequent sequence*

- **Infrequent Sequence**

- A sequence is called *infrequent sequence* if its support is less than  $min\_sup$

- **Problem Statement**

- Given a  $min\_sup$ , a sequence database  $D$ , the problem to be solved is to find from  $D$  all the sequences having a support no less than  $min\_sup$ .





# 序列型樣探勘的主要挑戰

---

- 項目的爆炸性組合問題

- 例如：有三個項目 a, b, c，則可以組出的 itemset 有 {a}, {b}, {c}, {ab}, {ac}, {bc}, {abc}
- 可以組出的 sequence 有  $\langle a \rangle$ ,  $\langle b \rangle$ ,  $\langle c \rangle$ ,  $\langle aa \rangle$ ,  $\langle ab \rangle$ ,  $\langle ac \rangle$ ,  $\langle ba \rangle$ ,  $\langle bb \rangle$ ,  $\langle bc \rangle$ ,  $\langle ca \rangle$ ,  $\langle cb \rangle$ ,  $\langle cc \rangle$ ,  $\langle abc \rangle$ ,  $\langle abcc \rangle$ ,  $\langle abcca \rangle$ ...

- 計算成本更高
- 搜尋空間更大
- 空間用量更多



# 以暴力法探勘 Sequential Patterns

## ■ A Brute Force Approach for SP Mining

- 列舉出資料庫中所有 Sequence，並掃描資料庫計算每個 Sequence 的支持數。

## ■ 暴力法的主要缺點

- **空間問題**：若將所有 Sequence 儲存於 Memory 中，則需耗費大量空間。
- **時間問題**：搜尋 Sequence 的位置、比對 Sequence 耗費大量執行時間。



# 常見的序列型樣探勘演算法

---

- 常見的序列型樣探勘演算法包括：
  - AprioriAll
  - GSP
  - FreeSpan
  - SPADE
  - PrefixSpan



# GSP 演算法簡介

- GSP 演算法沿用 Apriori 架構，以廣度優先方式找出每個長度的 Sequential Patterns。
- **Step 1**：找出  $FS_1$ ，再利用  $FS_1$  組出長度為 2 的 Candidate Sequences ( $CS_2$ )
- **Step 2**：掃描原始資料庫一次，計算  $CS_k (k \geq 2)$  的支持數，找出  $FS_k$ 。
- **Step 3**：以  $FS_k$  組出  $CS_{k+1}$ 。
- **Step 4**： $k = k+1$ ，重複執行 Step 2 & 3 直到沒有任何 Candidate Sequences 可再被產生出來。

# 舉例說明：GSP 演算法

Sequence Database	
SID	Sequence
$S_1$	$\langle(a)(b)(a)(c)\rangle$
$S_2$	$\langle(a)(a)(c)(b)\rangle$
$S_3$	$\langle(b)(c)\rangle$
$S_4$	$\langle(c)(b)(e)(b)\rangle$

Seq	SC
$\langle(a)\rangle$	2
$\langle(b)\rangle$	4
$\langle(c)\rangle$	4
$\langle(d)\rangle$	1

Seq	SC
$\langle(a)(a)\rangle$	2
$\langle(a)(b)\rangle$	2
$\langle(a)(c)\rangle$	2
$\langle(b)(a)\rangle$	1
$\langle(b)(b)\rangle$	1
$\langle(b)(c)\rangle$	2
$\langle(c)(a)\rangle$	0
$\langle(c)(b)\rangle$	2
$\langle(c)(c)\rangle$	0

Seq	SC
$\langle(a)(a)(a)\rangle$	0
$\langle(a)(a)(b)\rangle$	1
$\langle(a)(a)(c)\rangle$	2
$\langle(a)(b)(c)\rangle$	1
$\langle(a)(c)(b)\rangle$	1
$\langle(b)(c)(b)\rangle$	0
$\langle(c)(b)(c)\rangle$	0

# Candidate Sequence 產生方式

- 產生規則：x 去頭、y 去尾、中間一樣，就可以組出 Candidate Sequence

Seq	SC
$\langle(a)(a)\rangle$	2
$\langle(a)(b)\rangle$	2
$\langle(a)(c)\rangle$	2
$\langle(b)(a)\rangle$	1
$\langle(b)(b)\rangle$	1
$\langle(b)(c)\rangle$	2
$\langle(c)(a)\rangle$	0
$\langle(c)(b)\rangle$	2
$\langle(c)(c)\rangle$	0

$\frac{aa}{aa}$	$\frac{aa}{ab}$	$\frac{aa}{ac}$	$\frac{ab}{ab}$	$\frac{ab}{bc}$	$\frac{ac}{ac}$
aaa	aab	aac	----	abc	----
$\frac{ac}{cb}$	$\frac{bc}{bc}$	$\frac{bc}{cb}$	$\frac{cb}{cb}$	$\frac{cb}{bc}$	
acb	----	bcb	----	cbc	

# Subsequence Checking

- 每當一個 Candidate  $(k+1)$ -Sequence  $Z$  被產生出來時，演算法將執行 Subsequence Checking，檢查  $Z$  長度減 1 的子序列是否皆為 Frequent Sequence。
- 若  $Z$  存在一個長度減 1 的子序列不為 Frequent Sequence，則  $Z$  不可能為 Frequent Sequence。

Seq	SC
$\langle(a)(a)\rangle$	2
$\langle(a)(b)\rangle$	2
$\langle(a)(c)\rangle$	2
$\langle(b)(c)\rangle$	2
$\langle(c)(b)\rangle$	2

$$\begin{array}{ccccc}
 \begin{array}{c} ac \\ cb \\ \hline acb \end{array} & 
 \begin{array}{c} bc \\ bc \\ \hline ---- \end{array} & 
 \begin{array}{c} bc \\ cb \\ \hline bcb \end{array} & 
 \begin{array}{c} cb \\ cb \\ \hline ---- \end{array} & 
 \begin{array}{c} cb \\ bc \\ \hline cbc \end{array}
 \end{array}$$

# Downward Closure Property in SPM

- 在傳統 SPM 的架構中，Sequence 遵循**向下封閉性(Downward Closure Property)**
  - 若  $S$  為 Frequent Sequence，則它所有的 Sub-sequence 皆為 Frequent Sequence
  - 若  $S$  為 Infrequent Sequence，則它所有的 Super-sequence 皆為 Infrequent Sequence

Sequence Database	
SID	Sequence
$S_1$	$\langle(a)(b)(a)(c)\rangle$
$S_2$	$\langle(a)(a)(c)(b)\rangle$
$S_3$	$\langle(b)(c)\rangle$
$S_4$	$\langle(c)(b)(e)(b)\rangle$

Seq	SC
$\langle(a)\rangle$	2
$\langle(b)\rangle$	4
$\langle(c)\rangle$	4
$\langle(d)\rangle$	1





# Applications

---

- **Basket Analysis**
  - i.e., Mining sequential patterns from sequence of transactions
- **Web Mining**
  - i.e., Mining sequential patterns from web logs
- **Mobile Mining**
  - i.e., Mining sequential patterns from moving logs (trajectories)
- **Bioinformatics**
  - i.e., Mining sequential patterns from DNA sequences
- **Multimedia**
  - i.e., Mining repeated patterns from music data



# Research Topics

---

- Constrained Sequential Pattern Mining
- Time-Interval Sequential Patterns
- Time-Gap Sequential Patterns
- Non-redundant Sequential Patterns
- Incremental Mining Sequential Patterns
- Mining Sequential Patterns over Data Streams
- High Utility Sequential Patterns
- Mining Sequential Patterns from Uncertain Data



# 結論

---

- 傳統頻繁項目集探勘缺點
- 序列型樣探勘目的
- 序列型樣探勘應用
- 序列型樣探勘技術
- 序列型樣探勘軟體操作



# Reference

---

- [1] Agrawal R., Srikant R., Mining sequential patterns, Proceedings 1995 Int. Conf. Very Large Data Bases (VLDB'94), pp. 487-499, 1995.
- [2] Srikant R., Agrawal R., Mining sequential pattern: Generalizations and performance improvements, Proceedings 5th Int. Conf. Extending Database Technology (EDBT'96), pp. 3-17, 1996.
- [3] Han J., Dong G., Mortazavi-Asl B., Chen Q., Dayal U., Hsu M.-C., Freespan: Frequent pattern-projected sequential pattern mining, Proceedings 2000 Int. Conf. Knowledge Discovery and Data Mining (KDD'00), pp. 355-359, 2000.
- [4] Pei J., Han J., Mortazavi-Asl J., Pinto H., Chen Q., Dayal U., Hsu M., PrefixSpan: Mining Sequential Patterns Efficiently by Prefix-Projected Pattern Growth , 17th International Conference on Data Engineering (ICDE), April 2001.
- [5] Zhao Q., Bhowmick S. S., Sequential Pattern Mining: A Survey. Technical Report Center for Advanced Information Systems, School of Computer Engineering, Nanyang Technological University, Singapore, 2003.

# 教師資訊



- ◎ 姓名：吳政瑋 (小吳老師)
- ◎ 現職：宜大資工助理教授
- ◎ 學歷：成功大學資工博士
- ◎ 研究興趣：資料探勘、人工智慧、AIoT應用
- ◎ 通訊方式
  - ◎ 電子信箱：wucw@niu.edu.tw
  - ◎ 校內電話：(03)9317331
  - ◎ Line: silvemoonfox
  - ◎ Office: 格致大樓E405室
  - ◎ 數位學習園區
- ◎ 實驗室：AI與資料科學實驗室
  - ◎ <https://sites.google.com/view/cwwuadslab/>



# 意見交流

歡迎提供意見與指導!!

您的寶貴意見將使本系更進步!!