

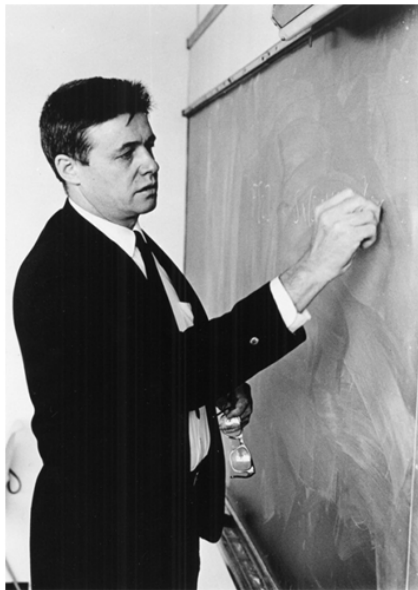
APL Programming Language: Introduction

Alexey Veretennikov
alexey@veroveli.com

Veroveli AB

January 11, 2017

APL Invented by Kenneth E. Iverson (1920-2004)



APL Programming Language

- Invented by [Ken Iverson](#) in 1960s, first working version: 1966, by [Larry Breed](#), IBM Research
- Stands for “A Programming Language” by the name of the book
- “Widely known” by its use of special characters, for example¹:

$\{(\phi \vee \backslash \phi \omega \neq ' ')/\omega\}$

- Ken Iverson received the Turing Award in 1979 for this language
- 51 years now!

¹Remove trailing blanks from the string

Examples

APL phrase	Description
$(\sim \wedge \backslash ' '=S)/S$	Remove leading blanks from string S
$(S \neq ' ')CS$	Split string S
$A, A+(\times B-A)\times \vee B-A$	List of integers from A to B
$(\sim R \in R \circ . \times R)/R \leftarrow 1 \downarrow \vee R$	Find all prime numbers from 1 to R
$(+/\div \neq)R$	Average value of the numeric array R
$+/(V \vee V)=\vee \rho V$	Count unique elements in vector V
$+/(CW) \circ . \equiv V$	Occurrences of word W in list V
$+\backslash (S='(')-0,^{-1} \downarrow S=')' '$	Depth of parenthesis in string S

Properties Of The Language

- Array-first programming language
- Discouraged use of explicit loops and control structures
- Interactive and workspace - oriented
- Modern dialects (Dyalog, J, IBM APL2) support OOP and FP
- Use special characters or combinations as a functions and operators
- Most APL characters have 1 or 2 meanings
- Extremely concise

Major Domain Fields

- Financial industry, bank sector
- Insurance industry
- Big data analysis
- Recreational programming and code contests

Array-Oriented Languages Family

- **A+** - Free, APL extension
- **J** - Free, dual license, ASCII characters
- **ELI** - Free, educational, APL extension
- **Q'Nial** - Free, English words
- **K** and **Q**(English-words wrapper around K) - Commercial, used with **KDB+**
- **MATLAB** influenced by APL - Commercial, mathematics

Current Implementations Of APL

- [Dyalog APL](#) - commercial, free personal version available; actively developed, lots of features
- [GNU APL](#) - free, actively developed
- [NARS2000](#) - free, Windows-only, actively developed
- [APL.js](#) - free, JavaScript-based
- [APL2000](#) - commercial
- [IBM APL2](#) still selling, no updates from 200x

Alphabet And Input Methods



- Windows:
 - Dyalog IME layout
 - Dyalog RIDE prefix keys
- MacOSX and Linux:
 - APL Keyboard Layout
 - [GNU Emacs mode](#) for GNU APL
 - Dyalog RIDE prefix keys
 - [APL Keyboard Translator](#)

Simple operations 1

Ordinary operations

$1 + 2$

3

$10 \times 1\ 2\ 3$

10 20 30

$10\ 20\ 30 \div 2\ 3\ 4$

5 6.666666667 7.5

Assignments

$a \leftarrow 10\ 20\ 30$

$a+1$

11 21 31

$a \leftarrow b \leftarrow c \leftarrow -1$

$a\ b\ c + 2\ 4\ 6$

1 3 5

Simple operations 2

Priority/Order of operations

$$2 \times 3 + 4$$

14

$$(2 \times 3) + 4$$

10

Unary operations

$$a \leftarrow 2$$

$$\div a$$

0.5

$$\lfloor 3.5 \ 0.5 \ 2.1$$

3 0 2

$$\sim 1 \ 0 \ 1 \ 1$$

0 1 0 0

N-adic functions

Definition

- Function without arguments called *niladic* function
- Function with one argument (to the right) is *monadic* function
- Function with two argument (left and right) is *dyadic* function

Example (Niladic function - current time)

□TS

2017 1 9 21 22 16 865

Example (Monadic and dyadic functions: \div)

$3 \div 2$

1.5

$\div 2$

0.5

$\text{lota}(\imath)$

Monadic $\text{lota}(\imath)$ - Index Generator

```
       $\imath 4$   
1 2 3 4  
       $\neg 1 + \imath 4$   
0 1 2 3
```

Dyadic $\text{lota}(\imath)$ - index of

```
      'aa' 'bb' 'cc'  $\imath$  'bb' 'cc'
```

2 3

```
      A  $\leftarrow$  'aa' 'bb' 'cc' 'aa'
```

A \imath A

```
1 2 3 1  
      (A  $\imath$  A)  $\neq \imath 4$   
0 0 0 1
```

Rho(ρ) - Shape of and Reshape

Monadic ρ - Shape Of

ρ 'aa' 'bb' 'cc'

3

ρ 5

5

Dyadic ρ - Reshape

2 2 ρ 1 2 3 4

1 2

3 4

2 2 ρ 4

1 2

3 4

3 ρ 0

0 0 0

Functions and operators: Replicate

“/” Replicate (could be used as a “mask”)

```
      1 0 1/1 2 3
1 3
      1 1 2/2 3
1 2 3 3
```

Let's find unique elements!

```
A ← 'aa' 'bb' 'cc' 'aa'
A % A
1 2 3 1
(A % A) = 2 4
1 1 1 0
((A % A) = 2 4) / A
aa bb cc
```

Functions and operators: Reduce

Definition

Operators take function and produce function

Boring code

$10+20+30$

60

$10\times 20\times 30$

6000

“/” as an operator: Reduce

$+ / 10 \ 20 \ 30$

60

$\times / 10 \ 20 \ 30$

6000

Reduce and Scan: the fun part

"\" scan operator: partial sums

$+/\backslash 4$

10

$+\backslash 4$

1 3 6 10

Let's count and remove leading spaces!

$S \leftarrow ' \text{hello world}'$

$S = ' '$

1 1 0 0 0 0 0 1 0 0 0 0 0

$\wedge \backslash S = ' '$

1 1 0 0 0 0 0 0 0 0 0 0 0

$+/\wedge \backslash S = ' '$

2

$(\sim \wedge \backslash S = ' ')/S$

hello world

Inner and outer product

"◦.fun" Outer product

$$(v_3) \circ . \times v_3$$

1 2 3

2 4 6

3 6 9

$$(v_3) \circ . \leq v_3$$

1 1 1

0 1 1

0 0 1

"fun1.fun2" Inner product

$$(v_3) + . \times 10 \ 20 \ 30$$

140

$$(1 \ 2 \ 3) \wedge . = v_3$$

1

" \in " - Membership

X " \in " Memerbers of Y

'hello' \in 'el'

0 1 1 1 0

(List \in Where) / λp List

('hello' \in 'el') / λp 'hello'

2 3 4

Some notable examples

Average

$V \leftarrow 12 \ 15 \ 21$

$(+/V) \div \rho V$

16

Definition (Drop “↓”)

$1 \downarrow 10 \ 20 \ 30$

20 30

$2 \downarrow 10 \ 20 \ 30$

30

Prime numbers

$(\sim R \in R \circ . \times R) / R \leftarrow 1 \downarrow \vee R$

References and bibliography

- TryAPL.org try APL online
- [APL Wiki](#)
- [Mastering Dyalog APL](#) free E-book
- [IBM APL2 Programming: Guide](#)
- [IBM APL2 Programming: Language Reference](#)
- APL2 at a Glance By James A. Brown, Sandra Pakin, and Raymond P. Polivka, 1988
- APL An Interactive Approach By Leonard Gilman and Allen J. Rose

The end

Questions?