

Initialization

$\|\nabla m\|_p$ = lp-norm on gradient

$\|m\|_q$ = lp-norm on model

λ = scaling factor [0 2]

m_1 = initial model

Iteration 1

minimize $\|Fm - d^{obs}\| + \beta_1(\|\mathbf{W}_\nabla \mathbf{m}_1\| + \|\mathbf{W}_m \mathbf{m}_1\|)$

Compute: φ_d^{start} , φ_m^{start}

β^{th} Iterations

Compute:

$$\mathbf{R}_\nabla = \text{diag}(|\nabla m_{i-1}|^{(p-2)} + \varepsilon)^{-0.5}$$

$$\mathbf{R}_m = \text{diag}(|m_{i-1}|^{(q-2)} + \varepsilon)^{-0.5}$$

$$\varphi_\nabla = \|\mathbf{W}_\nabla \mathbf{R}_\nabla \mathbf{m}_i\|$$

$$\varphi_m = \|\mathbf{W}_m \mathbf{R}_m \mathbf{m}_i\|$$

$$\mu = \frac{\|\varphi_\nabla\|}{\|\varphi_m\|}, \quad \alpha = \frac{\|\varphi_m^{start}\|}{(2 - \lambda)\|\varphi_\nabla\| + \mu \lambda \|\varphi_m\|}$$

minimize $\varphi_d + \beta_i \alpha ((2 - \lambda) \varphi_\nabla + \mu \lambda \varphi_m)$

$\varphi_d < \text{target}$

yes

End

no

$$\beta_{i+1} = \beta_i / 2$$