FEM 11087 - Applied Microeconometrics

Assignment 2: Panel Data Analysis Empirical Application

Group 33

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Question 1 [0.7 points]

A central question in labor economics is: **How much more do individuals earn with higher levels of education?** Economists often estimate the returns to education—that is, the increase in earnings associated with completing high school, college, or additional years of schooling.

Using the panel data provided, begin by constructing a bar chart showing mean income by education group. Group individuals based on their highest level of educational attainment (e.g., less than high school, high school graduate, some college, college degree or more), and plot the average income for each category.

We can begin by grouping the individuals according to their years of education, as follows:

The command graph (with the bar option) can then be used to create a bar chart:

graph bar (mean) income, over(edyears_cat)

40,000

30,000

20,000

10,000

Figure 1.1: Mean income by education level

1=Less than HS 2=HS Graduate 3=Some College 4=College degree or more

3

2

Recent debates around student debt and the value of higher education often assume that education "pays off" equally for everyone. **Does your analysis support that assumption?** To explore this, create **separate plots by gender** to highlight any differences in the relationship between education and earnings. Discuss your findings.

Separate plots by gender can be created using the by (male) option:

```
graph bar (mean) income, over(edyears_cat) by(male)
```

As seen in the resulting graphs (Figure 1.2, below), there is a stark contrast in average mean income across genders at every educational level.

Men consistently earn higher average incomes than women across every category. Male individuals with a college degree stand to earn around \$20,000 more on average than women with comparable education, while men belonging to the first three categories earn, on average, roughly three times as much as their female counterparts.

Even though the difference in amount of dollars earned appears to widen as educational level increases, the largest relative gap occurs at the first three levels; this

suggests a significant gender gap in average income across the board. These findings would challenge the assumption that education pays off for everyone. While both genders benefit from higher education, men benefit substantially more at every level.

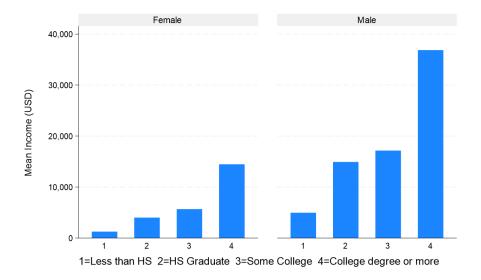


Figure 1.2: Mean income by education level, by gender

Question 2 [1 point]

Now, we turn to formally estimating the effect of years of education on income. Use **pooled OLS** to examine the impact of years of education (edyears) on **log(income)**, controlling for age, gender (male), marital status categories, ethnicity categories, and childbirth.

```
gen log_income = log(income)
reg log_income edyears age i.male ib0.mstatus ib4.ethnicity ///
i.child_birth
```

Table 2.1: Pooled OLS model

	Coefficient	Robust std. err.	P> t	Conf. int.
Explanatory variable				
Education years	0.1458	(0.0027)	0.000	[0.140,0.151]
Control variables				
Age	0.1263	(0.0014)	0.000	[0.123, 0.129]
Male	0.6000	(0.0126)	0.000	[0.575, 0.625]
Childbirth	-0.0795	(0.0184)	0.000	[-0.116, -0.043]
Married	0.6189	(0.0185)	0.000	[0.583,0.655]
Separated or divorced	0.0767	(0.0375)	0.041	[0.003, 0.150]
Widowed	0.0647	(0.2531)	0.798	[-0.431,0.561]
Black	-0.4286	(0.0139)	0.000	[-0.456,-0.401]
Hispanic	-0.0825	(0.0146)	0.000	[-0.111, -0.054]
Mixed Race (Non-Hispanic)	-0.3744	(0.0583)	0.000	[-0.489,-0.260]
Constant	3.0156	(0.0319)	0.000	[2.953,3.078]
Number of obs	55874			
F-statistic	3864.88			
Prob > F	0.0000			
R-squared	0.4089			
Adj. R-squared	0.4088			

a) What is the estimated return to <u>an additional year of education</u>? Interpret the coefficient on years of education in terms of its **sign**, **magnitude**, and **statistical significance**.

For each additional year of schooling, individuals receive a 15.69% higher average income, ceteris paribus. This difference is statistically significant at the 1% significance level.

b) Differences in returns to schooling by gender are sometimes interpreted as potential evidence of **labor market discrimination**. Test whether the effect of years of education using the categorical variable created in Question 1 on log(income) is the **same for men and women**. Based on your results, do you find any evidence consistent with discrimination?

reg log_income i.edyears_cat##i.male age ib0.mstatus ib4.ethnicity ///
i.child_birth

Table 2.2: Pooled OLS model with interaction effects

	Coefficient	Robust std. err.	P> t	Conf. int.
Explanatory variable				
HS graduate	0.3802	(0.0256)	0.000	[0.330,0.430]
Some college	0.6488	(0.0277)	0.000	[0.594,0.703]
College degree or more	1.0239	(0.0388)	0.000	[0.948,1.100]
Interaction terms				
HS graduate × Male	0.3836	(0.0302)	0.000	[0.324, 0.443]
Some college × Male	0.1664	(0.0326)	0.000	[0.102, 0.230]
College degree or more × Male	0.2206	(0.0432)	0.000	[0.136,0.305]
Control variables				
Age	0.1225	(0.0014)	0.000	[0.120, 0.125]
Male	0.4472	(0.0188)	0.000	[0.410, 0.484]
Childbirth	-0.0759	(0.0182)	0.000	[-0.112,-0.040]
Married	0.6013	(0.0183)	0.000	[0.565,0.637]
Separated or divorced	0.0631	(0.0372)	0.090	[-0.010,0.136]
Widowed	0.0932	(0.2509)	0.710	[-0.399,0.585]
Black	-0.4143	(0.0138)	0.000	[-0.441, -0.387]
Hispanic	-0.0732	(0.0145)	0.000	[-0.102, -0.045]
Mixed Race (Non-Hispanic)	-0.3752	(0.0578)	0.000	[-0.488,-0.262]
Constant	4.4713	(0.0289)	0.000	[4.415,4.528]
Number of obs	55874			
F-statistic	2690.54			
Prob > F	0.0000			
R-squared	0.4195			
Adj. R-squared	0.4193			

test 2.edyears_cat#1.male 3.edyears_cat#1.male 4.edyears_cat#1.male

Table 2.3: Joint significance test of interaction terms

F-statistic	54.85
Prob > F	0.0000

⁽¹⁾ HS graduate \times Male = 0

The interaction terms are highly statistically significant at the 1% significance

⁽²⁾ Some college \times Male = 0

⁽³⁾ College degree or more \times Male = 0

level, and we can therefore reject the null hypothesis that the interaction effects coefficients are equal to zero. In other words, men and women see significantly different income effects from additional education levels.

c) Under what conditions is the pooled OLS estimate of the effect of years of education **unbiased and efficient**? Do you believe these conditions are likely to hold in this context?

For a Pooled OLS model to be unbiased and efficient,

c) Under what conditions is the pooled OLS estimate of the effect of years of education **unbiased and efficient**? Do you believe these conditions are likely to hold in this context?

For a pooled OLS estimate to be unbiased, the explanatory variable must be uncorrelated with the error term. In our case, this would require that all relevant variables affecting income are either included in the model or are uncorrelated with education; otherwise, the model would suffer from endogeneity due to factors like individual ability, family background or motivation, which are not present in our model.

For the model to be efficient, serial correlation must not be present. Since individuals possess unobserved characteristics that remain constant across time and which impact their income across all time periods, this is highly unlikely. As a result, the error term for each individual is correlated across time periods. This does not create bias in the estimators, but it leads to unreliable significance tests and confidence intervals.

In the context of our model, these conditions are unlikely to hold. There are many personal factors that influence both educational levels and income, not all of which are accounted for in our model. Additionally, it is likely that unobserved individual characteristics which remain constant across time impact income across all time periods, which means that serial correlation is present and our estimate is inefficient.

Question 3 [0.5 points]

So far, the panel structure of the data has been largely unexploited. Random effects (RE) estimation can improve the efficiency of the estimates compared to pooled OLS.

a) Estimate the effect of years of education (edyears) on log(income) using the random

effects (RE) model, controlling for age, gender (male), marital status categories, ethnicity categories, and childbirth. Interpret the estimated coefficient for years of education in terms of its sign, magnitude, and statistical significance. Then, compare the RE estimate and standard error of the education coefficient with those obtained from the pooled OLS model.

```
xtset pid wave
xtreg log_income edyears age i.male ib0.mstatus ib4.ethnicity ///
i.child_birth, re
estimates store random
```

Table 3.1: Random effects (RE) model

	Coefficient	Std. err.	P> t	Conf. int.
Explanatory variable				
Education years	0.1509	(0.0031)	0.000	[0.145,0.157]
Control variables				
Age	0.1273	(0.0015)	0.000	[0.124, 0.130]
Male	0.5698	(0.0167)	0.000	[0.537, 0.603]
Childbirth	-0.0599	(0.0174)	0.001	[-0.094, -0.026]
Married	0.5107	(0.0197)	0.000	[0.472, 0.549]
Separated or divorced	0.0454	(0.0392)	0.246	[-0.031, 0.122]
Widowed	0.0855	(0.2619)	0.744	[-0.428, 0.599]
Black	-0.3833	(0.0192)	0.000	[-0.421, -0.346]
Hispanic	-0.0655	(0.0203)	0.001	[-0.105,-0.026]
Mixed Race (Non-Hispanic)	-0.3244	(0.0813)	0.000	[-0.484,-0.165]
Constant	2.9423	(0.0341)	0.000	[2.875,3.009]
Number of obs	55874			
Number of groups	7126			
R-squared within	0.3380			
R-squared between	0.5546			
R-squared overall	0.4084			
Wald χ^2	34633.21			
Prob $> \chi^2$	0.0000			
σ_u	0.4412			
σ_{-}^{e}	1.1766			
$ ho^-$	0.1233			

Dependent variable: log(income)

According to the RE model, for each additional year of schooling individuals re-

ceive a 16.28% higher average income, ceteris paribus. This difference is statistically significant at the 1% significance level.

Table 3.2: POLS, RE comparison

	POLS	RE
Explanatory variable		
Education years	0.1458***	0.1509***
,	(0.0027)	(0.0031)
Control variables		
Age	0.1263***	0.1273***
	(0.0014)	(0.0015)
Male	0.6000***	0.5698***
	(0.0126)	(0.0167)
Childbirth	-0.0795***	-0.0599***
	(0.0184)	(0.0174)
Black	-0.4286***	-0.3833***
	(0.0139)	(0.0192)
Hispanic	-0.0825***	-0.0655**
	(0.0146)	(0.0203)
Mixed Race (Non-Hispanic)	-0.3744***	-0.3244***
	(0.0583)	(0.0813)
Married	0.6189***	0.5107***
	(0.0185)	(0.0197)
Separated or divorced	0.0767*	0.0454
	(0.0375)	(0.0392)
Widowed	0.0647	0.0855
	(0.2531)	(0.2619)
Constant	3.0156***	2.9423***
Constant	(0.0319)	(0.0341)
Number of obs	55874	55874
Number of groups		7126
F-statistic	3864.88	
Wald χ^2	3004.00	34633.21
P-value	0.0000	0.0000
r-value	0.0000	0.0000
R-squared	0.4089	
Adj. R-squared	0.4088	
R-squared within		0.3380
R-squared between		0.5546
R-squared overall		0.4084
$\sigma_{\mathbf{u}}$		0.4412
σ_e		1.1766
ρ		0.1233

Standard errors in parentheses.
* p < 0.05, ** p < 0.01, *** p < 0.001

The RE estimate of 16.28% is 0.59% higher than the pooled OLS estimate of 15.69%, while yielding marginally higher standard error at 0.0031, compared to 0.0027 for the POLS model.

b) Under which conditions and why can the random effects estimator be **more efficient** than pooled OLS?

Random effects can be more efficient than pooled OLS when there is serial correlation in the POLS estimate, which RE models by taking into account the relation within individuals across different time periods with the use of GLS.

Question 4 [1.55 points]

Alternatively, the panel structure of the data can be used to perform fixed effects (FE) estimation.

a) Based on theoretical considerations, would you **prefer** fixed effects or random effects estimation? Justify your answer.

The choice between fixed effects or random effects hinges on whether or not individual effects are correlated with the explanatory variable. In our model, this is extremely likely, due to the fact that many individual factors, such as ability, motivation, background and socio-economic status are correlated with further education and also with higher income for factors other than higher education. Hence, we would prefer fixed effects since even though it cannot estimate the effect of time invariant characteristics on income, it can provide us with an unbiased estimator.

b) Use a **fixed effects estimator** to examine the impact of years of education (edyears) on **log(income)**, controlling for age, gender (male), marital status categories, ethnicity categories, and childbirth. Interpret the coefficient on years of education in terms of its **sign, magnitude**, and **statistical significance**. Compare your results with those from the **pooled OLS** and **random effects** models.

```
xtreg log_income edyears age i.male ib0.mstatus ib4. ethnicity ///
i.child_birth, fe
stimates store fixed
```

Table 4.1: Fixed effects (FE) model

	Coefficient	Std. err.	P> t	Conf. int.
Explanatory variable				
Education years	0.1610	(0.0038)	0.000	[0.153, 0.168]
Control variables				
Age	0.1259	(0.0017)	0.000	[0.123,0.129]
Childbirth	-0.0545	(0.017) (0.0180)	0.002	[-0.090,-0.019]
Married	0.4178	(0.0130) (0.0223)	0.002	[0.374,0.461]
Separated or divorced	-0.0112	(0.0223) (0.0432)	0.796	[-0.096,0.073]
Widowed	0.1575	(0.0432) (0.2861)	0.582	[-0.403,0.718]
Widowed	0.1373	(0.2001)	0.302	[-0.403,0.710]
Constant	3.1536	(0.0378)	0.000	[3.080,3.228]
Number of obs	55874			
Number of groups	7126			
R-squared within	0.3383			
R-squared between	0.4945			
R-squared overall	0.3713			
Wald χ^2				
Prob > χ^2	0.0000			
/\	0.0000			
$\sigma_{\mathbf{u}}$	0.8174			
_ σ_e	1.1766			
$ ho^-$	0.3255			

According to the FE model, for each additional year of schooling individuals receive a 17.46% higher average income, ceteris paribus. This difference is statistically significant at the 1% significance level.

Table 4.2: POLS, RE, FE comparison

14016 4.2. 1 01	POLS	RE	FE
P. 1 (1020		
Explanatory variable	0.1450***	0.1500***	0.1/10***
Education years	0.1458***	0.1509***	0.1610***
	(0.0027)	(0.0031)	(0.0038)
Control variables			
Age	0.1263***	0.1273***	0.1259***
C	(0.0014)	(0.0015)	(0.0017)
Male	0.6000***	0.5698***	0.0000
	(0.0126)	(0.0167)	(.)
Childbirth	-0.0795***	-0.0599***	-0.0545**
	(0.0184)	(0.0174)	(0.0180)
Black	-0.4286***	-0.3833***	0.0000
	(0.0139)	(0.0192)	(.)
Hispanic	-0.0825***	-0.0655**	0.0000
-	(0.0146)	(0.0203)	(.)
Mixed Race (Non-Hispanic)	-0.3744***	-0.3244***	0.0000
· · · · · · · · · · · · · · · · · · ·	(0.0583)	(0.0813)	(.)
Married	0.6189***	0.5107***	0.4178^{***}
	(0.0185)	(0.0197)	(0.0223)
Separated or divorced	0.0767*	0.0454	-0.0112
	(0.0375)	(0.0392)	(0.0432)
Widowed	0.0647	0.0855	0.1575
	(0.2531)	(0.2619)	(0.2861)
Constant	3.0156***	2.9423***	3.1536***
Constant	(0.0319)	(0.0341)	(0.0378)
Number of obs	55874	55874	55874
Number of groups		7126	7126
F-statistic	3864.88		4154.09
Wald χ^2		34633.21	
P-value	0.0000	0.0000	0.0000
R-squared	0.4089		0.3383
Adj. R-squared	0.4088		0.2415
R-squared within		0.3380	0.3383
R-squared between		0.5546	0.4945
R-squared overall		0.4084	0.3713
$\sigma_{ extsf{u}}$		0.4412	0.8174
_ σ_e		1.1766	1.1766
$ ho^-$		0.1233	0.3255
,			

Standard errors in parentheses.
* p < 0.05, ** p < 0.01, *** p < 0.001

Compared to the POLS and RE models, FE has both a higher coefficient (0.1610 compared to 0.1458 and 0.1509, respectively) as well as higher standard error (0.0038 compared to 0.0027 and 0.0031, respectively). This implies that individual-specific effects were negatively correlated with education, meaning the POLS and RE estimates had a downward bias.

The higher standard error can also be expected, since FE trades some amount of efficiency in exchange for an unbiased estimate.

c) Perform the **Hausman** test. What do the results indicate? Based on the test outcome, **which estimator** (RE or FE) is more appropriate in this context?

hausman fixed random

Table 4.3: Hausman test

χ^2	141.94
Prob > χ^2	0.0000

H0: Difference in β not systematic

The Hausman test checks the null hypothesis that the individual-specific effects are uncorrelated with the explanatory variable. These results indicate that we can reject the null hypothesis at the 1% significance level, meaning that the test indicates that individual-specific effects are correlated with education years.

Question 5 [0.9 points]

Next, estimate a **Correlated Random Effects** (CRE) model to examine the effect of years of education (edyears) on **log(income)**.

```
by pid: egen age_mean = mean(age)
by pid: egen mstatus_mean = mean(mstatus)

xtreg log_income edyears age i.male ib0.mstatus ib4.ethnicity ///
i.child_birth age_mean mstatus_mean, re
```

Table 5.1: Correlated Random Effects (CRE) model

Explanatory variable Education years 0.1505 (0.0031) 0.000 [0.144,0.156] Control variables Age 0.1282 (0.0016) 0.000 [0.125,0.131] Male 0.5600 (0.0178) 0.000 [0.525,0.595] Childbirth -0.0617 (0.0174) 0.000 [-0.096,-0.028] Married 0.4463 (0.0221) 0.000 [0.403,0.490] Separated or divorced -0.0669 (0.0430) 0.119 [-0.151,0.017] Widowed -0.0927 (0.2632) 0.725 [-0.609,0.423] Black -0.3703 (0.0194) 0.000 [-0.408,-0.332] Hispanic -0.0684 (0.0203) 0.001 [-0.108,-0.029] Mixed Race (Non-Hispanic) -0.3117 (0.0813) 0.000 [-0.471,-0.152] CRE variables age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [2.766,2.993] Number of obs 558		Coefficient	Std. err.	P> t	Conf. int.
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Male 0.5600 (0.0178) 0.000 [0.525,0.595] Childbirth -0.0617 (0.0174) 0.000 [-0.096,-0.028] Married 0.4463 (0.0221) 0.000 [0.403,0.490] Separated or divorced -0.0669 (0.0430) 0.119 [-0.151,0.017] Widowed -0.0927 (0.2632) 0.725 [-0.609,0.423] Black -0.3703 (0.0194) 0.000 [-0.408,-0.332] Hispanic -0.0684 (0.0203) 0.001 [-0.108,-0.029] Mixed Race (Non-Hispanic) -0.3117 (0.0813) 0.000 [-0.471,-0.152] CRE variables age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs Number of groups 7126 R-squared within 0.3382 R-squared overall 0.4					
Childbirth -0.0617 (0.0174) 0.000 [-0.096,-0.028] Married 0.4463 (0.0221) 0.000 [0.403,0.490] Separated or divorced -0.0669 (0.0430) 0.119 [-0.151,0.017] Widowed -0.0927 (0.2632) 0.725 [-0.609,0.423] Black -0.3703 (0.0194) 0.000 [-0.408,-0.332] Hispanic -0.0684 (0.0203) 0.001 [-0.108,-0.029] Mixed Race (Non-Hispanic) -0.3117 (0.0813) 0.000 [-0.471,-0.152] CRE variables age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs 55874 Number of groups 7126 R-squared within 0.3382			,		
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Black -0.3703 (0.0194) 0.000 $[-0.408, -0.332]$ Hispanic -0.0684 (0.0203) 0.001 $[-0.108, -0.029]$ Mixed Race (Non-Hispanic) -0.3117 (0.0813) 0.000 $[-0.471, -0.152]$ CRE variables age_mean 0.0013 (0.0032) 0.676 $[-0.005, 0.008]$ mstatus_mean 0.2142 (0.0340) 0.000 $[0.148, 0.281]$ Constant 2.8795 (0.0581) 0.000 $[2.766, 2.993]$ Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ e 0.4412 σ e 0.4412 σ e 0.1766	*		,		
Hispanic -0.0684 (0.0203) 0.001 [-0.108,-0.029] Mixed Race (Non-Hispanic) -0.3117 (0.0813) 0.000 [-0.471,-0.152] CRE variables age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ u 0.4412 σ e 1.1766			,		
Mixed Race (Non-Hispanic) -0.3117 (0.0813) 0.000 [-0.471,-0.152] CRE variables age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs Number of groups 7126 R-squared within R-squared between R-squared overall 0.3382 R-squared overall 0.4093 Wald χ^2 Prob > χ^2 34714.61 Prob > χ^2 0.0000 $\sigma_{-\mu}$ 0.4412 σ_{-e} 0.4412 σ_{-e} 1.1766			,		
CRE variables age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-u} 0.4412 σ_{-e} 1.1766	Hispanic	-0.0684	,		
age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 $\sigma_{_}$ u 0.4412 $\sigma_{_}$ e 1.1766	Mixed Race (Non-Hispanic)	-0.3117	(0.0813)	0.000	[-0.471, -0.152]
age_mean 0.0013 (0.0032) 0.676 [-0.005,0.008] mstatus_mean 0.2142 (0.0340) 0.000 [0.148,0.281] Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 $\sigma_{_u}$ 0.4412 $\sigma_{_e}$ 1.1766	CDE wariables				
mstatus_mean 0.2142 (0.0340) 0.000 $[0.148,0.281]$ Constant 2.8795 (0.0581) 0.000 $[2.766,2.993]$ Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-u} 0.4412 σ_{-e} 1.1766		0.0012	(0.0022)	0.676	[0 005 0 000]
Constant 2.8795 (0.0581) 0.000 [2.766,2.993] Number of obs Number of groups 55874 7126 R-squared within R-squared between R-squared overall 0.3382 0.5565 0.4093	9		,		
Number of obs 55874 Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	mstatus_mean	0.2142	(0.0340)	0.000	[0.148,0.281]
Number of groups 7126 R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	Constant	2.8795	(0.0581)	0.000	[2.766,2.993]
R-squared within 0.3382 R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	Number of obs	55874			
R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	Number of groups	7126			
R-squared between 0.5565 R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	D 1 111	0.0000			
R-squared overall 0.4093 Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766					
Wald χ^2 34714.61 Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766					
Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	R-squared overall	0.4093			
Prob > χ^2 0.0000 σ_{-} u 0.4412 σ_{-} e 1.1766	Wald χ^2	34714.61			
σ_{-} u 0.4412 σ_{-} e 1.1766					
σ_{-} e 1.1766	~				
	$\sigma_{ extsf{u}}$	0.4412			
0.4.000	σ_{-} e	1.1766			
ρ 0.1233	ρ	0.1233			

a) What is one advantage of the CRE estimator compared to the random effects (RE) estimator?

b) What is one advantage of the CRE estimator compared to the fixed effects (FE) estimator?

c) Compare the estimated coefficient for years of education from the **CRE model** with those from the **RE** and **FE** models. Are the coefficients similar or different? Explain why this is the case.

Table 5.2: POLS, RE, FE, CRE comparison

1able 5.2: F				
	POLS	RE	FE	CRE
Explanatory variable				
Education years	0.1458***	0.1509***	0.1610***	0.1505***
•	(0.0027)	(0.0031)	(0.0038)	(0.0031)
Control variables				
Age	0.1263***	0.1273***	0.1259***	0.1282***
26.1	(0.0014)	(0.0015)	(0.0017)	(0.0016)
Male	0.6000***	0.5698***	0.0000	0.5600***
Childbirth	(0.0126) -0.0795***	(0.0167) -0.0599***	(.) -0.0545**	(0.0178) -0.0617***
Ciliabirtii	(0.0184)	(0.0174)	(0.0180)	(0.0174)
Black	-0.4286***	-0.3833***	0.0000	-0.3703***
Bluck	(0.0139)	(0.0192)	(.)	(0.0194)
Hispanic	-0.0825***	-0.0655**	0.0000	-0.0684***
1	(0.0146)	(0.0203)	(.)	(0.0203)
Mixed Race (Non-Hispanic)	-0.3744***	-0.3244***	0.0000	-0.3117***
	(0.0583)	(0.0813)	(.)	(0.0813)
Married	0.6189***	0.5107***	0.4178^{***}	0.4463***
	(0.0185)	(0.0197)	(0.0223)	(0.0221)
Separated or divorced	0.0767*	0.0454	-0.0112	-0.0669
7471 1	(0.0375)	(0.0392)	(0.0432)	(0.0430)
Widowed	0.0647	0.0855	0.1575	-0.0927
	(0.2531)	(0.2619)	(0.2861)	(0.2632)
CRE variables				
age_mean				0.0013
				(0.0032)
mstatus_mean				0.2142***
				(0.0340)
Constant	3.0156***	2.9423***	3.1536***	2.8795***
	(0.0319)	(0.0341)	(0.0378)	(0.0581)
Number of obs	55874	55874	55874	55874
Number of groups		7126	7126	7126
F-statistic	3864.88		4154.09	
Wald χ^2		34633.21		34714.61
P-value	0.0000	0.0000	0.0000	0.0000
Daguarad	0.4000		0 2202	
R-squared Adj. R-squared	$0.4089 \\ 0.4088$		0.3383 0.2415	
R-squared within	0.4000	0.3380	0.2415	0.3382
R-squared between		0.5546	0.3383	0.5565
R-squared overall		0.3340 0.4084	0.3713	0.4093
required overtuin		0.1001	0.0710	0.10/0
$\sigma_{ extsf{u}}$		0.4412	0.8174	0.4412
σ_{e}		1.1766	1.1766	1.1766
$ ho^-$		0.1233	0.3255	0.1233
Standard arrors in parenthese				

Standard errors in parentheses. * p < 0.05, ** p < 0.01, *** p < 0.001

d) Based on your CRE estimates, does the assumption of **exogeneity** appear to hold? Which estimator would you consider most appropriate in this context?

Question 6 [0.9 points]

Recent research provides compelling evidence that after the birth of a first child, women's earnings decline sharply and remain persistently lower, while men's earnings remain largely unaffected.

a) Estimate the effect of childbirth on **log(income)** using the **most appropriate model**. Control for age, gender (male), marital status categories, ethnicity categories, and years of education (edyears). Interpret the estimated coefficient for childbirth in terms of its **sign, magnitude**, and **statistical significance**.

```
xtreg log_income i.child_birth age i.male ib0.mstatus ib4.ethnicity ///
edyears age_mean mstatus_mean, re
```

Table 6.1: Correlated Random Effects (CRE)

(0.0174) 0.000 [-0.096,-0.028] (0.0016) 0.000 [0.125,0.131] (0.0178) 0.000 [0.525,0.595] (0.0031) 0.000 [0.144,0.156] (0.0221) 0.000 [0.403,0.490]
(0.0016) 0.000 [0.125,0.131] (0.0178) 0.000 [0.525,0.595] (0.0031) 0.000 [0.144,0.156]
(0.0178) 0.000 [0.525,0.595] (0.0031) 0.000 [0.144,0.156]
(0.0178) 0.000 [0.525,0.595] (0.0031) 0.000 [0.144,0.156]
(0.0178) 0.000 [0.525,0.595] (0.0031) 0.000 [0.144,0.156]
(0.0031) 0.000 [0.144,0.156]
, ,
10.04411 0.000 10.403.0.4301
(0.0430) 0.119 $[-0.151, 0.017]$
(0.2632) 0.725 $[-0.609, 0.423]$
(0.0194) 0.000 $[-0.408, -0.332]$
(0.0203) 0.001 $[-0.108, -0.029]$
(0.0813) 0.000 [-0.471,-0.152]
(0.0032) 0.676 [-0.005,0.008]
, , ,
(0.0340) 0.000 [0.148,0.281]
(0.0581) 0.000 [2.766,2.993]
1

b) Test whether the effect of childbirth on log(income) differs between males and females. What conclusions can you draw from your results?

```
xtreg log_income i.child_birth##i.male age ib0.mstatus ib4.ethnicity ///
edyears age_mean mstatus_mean, re
```

Table 6.2: Correlated Random Effects (CRE) with interaction effects

	Coefficient	Std. err.	P> t	Conf. int.
Explanatory variable				
Childbirth	-0.3390	(0.0312)	0.000	[-0.400, -0.278]
Childbirth × Male	0.3959	(0.0370)	0.000	[0.323, 0.468]
Control variables		(0.001.1)		[0.454.0.450]
Age	0.1272	(0.0016)	0.000	[0.124,0.130]
Male	0.5165	(0.0183)	0.000	[0.481, 0.552]
Education years	0.1512	(0.0031)	0.000	[0.145,0.157]
Married	0.4458	(0.0221)	0.000	[0.403, 0.489]
Separated or divorced	-0.0692	(0.0429)	0.107	[-0.153,0.015]
Widowed	-0.0878	(0.2629)	0.739	[-0.603, 0.428]
Black	-0.3674	(0.0194)	0.000	[-0.405, -0.329]
Hispanic	-0.0680	(0.0203)	0.001	[-0.108, -0.028]
Mixed Race (Non-Hispanic)	-0.3043	(0.0813)	0.000	[-0.464, -0.145]
CRE variables				
age_mean	0.0021	(0.0032)	0.515	[-0.004,0.008]
mstatus_mean	0.2211	(0.0340)	0.000	[0.154,0.288]
	0.2211	(0.0010)	0.000	[0.10 1)0.200]
Constant	2.9032	(0.0582)	0.000	[2.789,3.017]
Number of obs	55874			
Number of groups	7126			
0 1				
R-squared within	0.3396			
R-squared between	0.5563			
R-squared overall	0.4106			
Wald χ^2	34887.51			
$\text{Prob} > \chi^2$	0.0000			
σ_u	0.4418			
σ_ e	1.1753			
	0.1238			
ρ	0.1230			

test 1.child_birth#1.male

Table 6.3: Single coeff. test

|--|

⁽¹⁾ Childbirth \times Male = 0

Question 7 [1.2 points]

Without conducting any empirical analysis:

- a) Compare the key assumptions underlying **pooled OLS**, **fixed effects (FE)**, and **random effects (RE)** estimators. Discuss theoretically in which scenarios you would prefer to use each method.
- b) Within the practical context of this assignment (effect of education on earnings), provide an example situation for each estimator in the form of a **Directed Acyclic Graph** (**DAG**). For each case (Pooled OLS, FE, and RE), explain why the assumptions required for the respective method hold in that example, and why that method would be preferred.

Question 8 [0.75 points]

Finally, revisit your data and evaluate whether **attrition** is present in your sample. Based on your preferred model, discuss the likelihood of **attrition bias**. What conclusions can you draw regarding its presence, and how might it affect the validity of your results?

```
bysort pid (wave): gen n_waves = _N
gen all_waves = n_waves == 17

xtreg log_income i.child_birth##i.male age ib0.mstatus ib4.ethnicity ///
edyears age_mean mstatus_mean all_waves, re
```

Table 8.1: Attrition bias: *all waves* indicator

	Coefficient	Std. err.	P> t	Conf. int.
Explanatory variable				
Childbirth	-0.3376	(0.0312)	0.000	[-0.399,-0.276]
Childbirth × Male	0.3971	(0.0370)	0.000	[0.325,0.470]
		,		
Control variables				
Age	0.1272	(0.0016)	0.000	[0.124, 0.130]
Male	0.5146	(0.0183)	0.000	[0.479, 0.550]
Education years	0.1511	(0.0031)	0.000	[0.145, 0.157]
Married	0.4451	(0.0221)	0.000	[0.402, 0.488]
Separated or divorced	-0.0687	(0.0429)	0.110	[-0.153, 0.015]
Widowed	-0.0913	(0.2629)	0.728	[-0.607, 0.424]
Black	-0.3660	(0.0194)	0.000	[-0.404, -0.328]
Hispanic	-0.0673	(0.0203)	0.001	[-0.107, -0.027]
Mixed Race (Non-Hispanic)	-0.3058	(0.0813)	0.000	[-0.465, -0.147]
CRE variables				
age_mean	-0.0001	(0.0033)	0.988	[-0.007,0.006]
mstatus_mean	0.2220	(0.0340)	0.000	[0.155, 0.289]
Bias indicator				
	0.0586	(0.0252)	0.020	[0 000 0 100]
all_waves	0.0360	(0.0252)	0.020	[0.009,0.108]
Constant	2.9418	(0.0605)	0.000	[2.823,3.060]
Number of obs	55874			
Number of groups	7126			
8-1-1				
R-squared within	0.3396			
R-squared between	0.5565			
R-squared overall	0.4108			
•				
Wald χ^2	34898.11			
$Prob > \chi^2$	0.0000			
$\sigma_{\mathbf{u}}$	0.4416			
$\sigma_{-}e$	1.1753			
ρ	0.1237			
Dependent variable: log(ince				

```
bysort pid (wave): gen next_wave = (wave[_n+1] == wave + 1)
```

xtreg log_income i.child_birth##i.male age ib0.mstatus ib4.ethnicity ///
edyears age_mean mstatus_mean next_wave, re

 Table 8.2: Attrition bias: next wave indicator

	Coefficient	Std. err.	P> t	Conf. int.
Explanatory variable				
Childbirth	-0.3361	(0.0312)	0.000	[-0.397,-0.275]
Childbirth × Male	0.3941	(0.0370)	0.000	[0.322,0.467]
		,		[,]
Control variables				
Age	0.1290	(0.0016)	0.000	[0.126, 0.132]
Male	0.5165	(0.0183)	0.000	[0.481, 0.552]
Education years	0.1509	(0.0031)	0.000	[0.145, 0.157]
Married	0.4435	(0.0221)	0.000	[0.400, 0.487]
Separated or divorced	-0.0704	(0.0429)	0.101	[-0.155, 0.014]
Widowed	-0.0932	(0.2629)	0.723	[-0.608, 0.422]
Black	-0.3668	(0.0194)	0.000	[-0.405, -0.329]
Hispanic	-0.0679	(0.0203)	0.001	[-0.108, -0.028]
Mixed Race (Non-Hispanic)	-0.3061	(0.0812)	0.000	[-0.465, -0.147]
CRE variables				
age_mean	-0.0014	(0.0033)	0.672	[-0.008, 0.005]
mstatus_mean	0.2226	(0.0340)	0.000	[0.156, 0.289]
Bias indicator				
next_wave	0.0641	(0.0139)	0.000	[0.037,0.091]
Constant	2.8931	(0.0582)	0.000	[2.779,3.007]
		(0.0302)	0.000	[2.777,3.007]
Number of obs	55874			
Number of groups	7126			
D 1 111	0.2200			
R-squared within	0.3398			
R-squared between	0.5567			
R-squared overall	0.4109			
Wald χ^2	34925.32			
Prob > χ^2	0.0000			
1100 / λ	0.0000			
σ_{-} u	0.4414			
σ_{e}	1.1752			
ρ	0.1236			
Donardant variable: log(inco				

xtreg log_income i.child_birth##i.male age ib0.mstatus ib4.ethnicity ///
edyears age_mean mstatus_mean n_waves, re

 Table 8.3: Attrition bias: number of waves indicator

	Coefficient	Std. err.	P> t	Conf. int.
Explanatory variable				
Childbirth	-0.3358	(0.0312)	0.000	[-0.397, -0.275]
Childbirth × Male	0.3979	(0.0370)	0.000	[0.325,0.470]
Control variables				
Age	0.1272	(0.0016)	0.000	[0.124, 0.130]
Male	0.5103	(0.0185)	0.000	[0.474, 0.546]
Education years	0.1510	(0.0031)	0.000	[0.145, 0.157]
Married	0.4451	(0.0221)	0.000	[0.402, 0.488]
Separated or divorced	-0.0699	(0.0429)	0.104	[-0.154, 0.014]
Widowed	-0.0865	(0.2629)	0.742	[-0.602, 0.429]
Black	-0.3666	(0.0194)	0.000	[-0.405,-0.329]
Hispanic	-0.0676	(0.0203)	0.001	[-0.107,-0.028]
Mixed Race (Non-Hispanic)	-0.3058	(0.0812)	0.000	[-0.465,-0.147]
CRE variables				
age_mean	-0.0058	(0.0045)	0.197	[-0.015, 0.003]
mstatus_mean	0.2210	(0.0340)	0.000	[0.154,0.288]
Bias indicator				
n_waves	0.0065	(0.0027)	0.014	[0.001,0.012]
Constant	3.0107	(0.0728)	0.000	[2.868,3.153]
Number of obs	55874			
Number of groups	7126			
R-squared within	0.3396			
R-squared between	0.5567			
R-squared overall	0.4108			
Wald χ^2	34902.86			
$\text{Prob} > \chi^2$	0.0000			
$\sigma_{\mathtt{u}}$	0.4412			
$\sigma_{-}e$	1.1753			
ρ	0.1235			
D 1				