

Class Discussion

Unit 5 Topic 1 Part 1 Basic Trigonometric Identities

Review Identities

1. Reciprocal identities

$\sin \theta = \frac{1}{\csc \theta}$	$\cos \theta = \frac{1}{\sec \theta}$	$\tan \theta = \frac{1}{\cot \theta}$
$\cot \theta = \frac{1}{\tan \theta}$	$\sec \theta = \frac{1}{\cos \theta}$	$\csc \theta = \frac{1}{\sin \theta}$

2. Quotient Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta}, \quad \cot \theta = \frac{\cos \theta}{\sin \theta}$$

3. Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

Ex1 Factor the following expressions completely

(a) $\sec^2 x - 2 \tan x$

(b) $4 \cos x - 3 \sin^2 x - 1$

(c) $2 \sec^3 x + 7 \sec^2 x + 2 \sec x - 3$

Ex 2 If $3 \sin x + 3 = 2 \cos^2 x$ and $\cos x < 0$, evaluate $\cos^2 x - \sin^2 x$