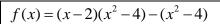
VD Unit 2 Topic 2

Sketch the following polynomials.

- 1. With analysis of the ending behavior and
- 2. details of the function around zeros



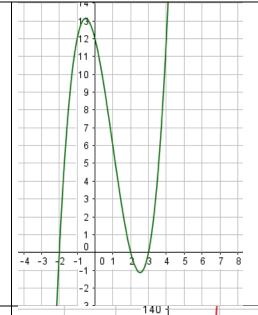
ending behaviors:

$$x \to \infty, f \to \infty$$

$$x \to -\infty, f \to -\infty$$

analysis around zeros:

@
$$x = -2$$
, $x = 2$, $x = 3$, $f(x)$ crosses x-axis



120

$$f(x) = x^3 + 6x^2 - 9x - 54$$

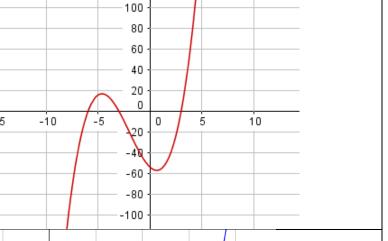
ending behaviors:

$$x \to \infty, f \to \infty$$

$$x \to -\infty, f \to -\infty$$

Analysis around zeros

@
$$x = -6$$
, $x = -3$, $x = 3$ $f(x)$ crosses x-axis



$$f(x) = (x^2 - 5x + 4)(x - 2) + 2(x - 2)$$

ending behaviors:

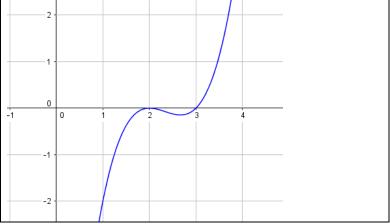
$$x \to \infty, f \to \infty$$

$$x \to -\infty, f \to -\infty$$

Analysis around zeros

@
$$x = 2$$
 $f(x)$ touches x-axis

$$@x = 3 f(x)$$
 crosses x-axis



VD Unit 2 Topic 2

 $f(x) = (x+2)(2x^2 - x - 6) - x^2(x^2 - 4)$

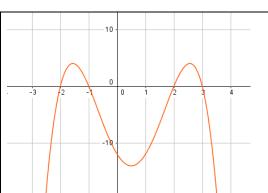
ending behaviors:

$$x \to \infty, f \to -\infty$$

$$x \to -\infty, f \to -\infty$$

Analysis around zeros

@
$$x = -2$$
, $x = -1$, $x = 2$, $x = 3$ $f(x)$ crosses x-axis



$$f(x) = (2x-1)^{2}(x-1) + (4x^{2}-1)$$

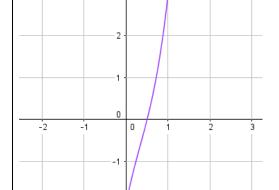
ending behaviors:

$$x \to \infty, f \to \infty$$

$$x \to -\infty, f \to -\infty$$

Analysis around zeros

$$@x = \frac{1}{2} f(x)$$
 crosses x-axis



$$f(x) = (x^2 - 3x + 2)(2x - 1) - (6x^2 + 7x - 5)(x - 2)$$

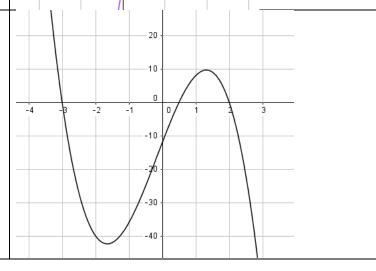
ending behaviors:

$$x \to \infty, f \to -\infty$$

$$x \to -\infty, f \to \infty$$

Analysis around zeros

@
$$x = -3, x = \frac{1}{2}, x = 2$$
 $f(x)$ crosses x-axis



VD Unit 2 Topic 2

 $f(x) = (x^2 - x - 2)(3x^2 - x) + (x + 1)(3x^2 - 7x + 2)$ ending behaviors:

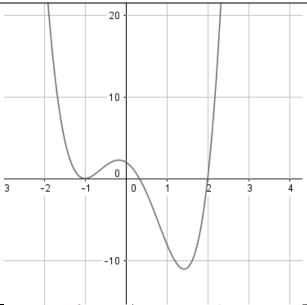
 $x \to \infty, f \to \infty$

$$x \to -\infty, f \to \infty$$

zero analysis:

@
$$x = -1$$
 $f(x)$ touches x-axis

@
$$x = \frac{1}{3}$$
, $x = 2$ $f(x)$ crosses x-axis



$$f(x) = x^4 - 3x^3 + 3x^2 - x$$

ending behaviors:

$$x \to \infty, f \to \infty$$

$$x \to -\infty, f \to \infty$$

zero analysis:

@
$$x = 0$$
, $x = 1$ $f(x)$ crosses x-axis

