

Class Discussion

Unit 9 Topic 5 Polar Coordinate System

$$\begin{cases} r = \sqrt{x^2 + y^2} \\ \theta = \arctan\left(\frac{y}{x}\right) \end{cases} \longleftrightarrow \begin{cases} x = r \cos \theta \\ y = r \sin \theta \end{cases}$$

If $(r; \theta)$ with $r < 0$ then $(r; \theta) = (r; \theta + \pi) = (r; \theta - \pi)$

Ex 1: Covert $(r; \theta)$ to (x, y)

(a) $(2; \frac{\pi}{4})$

(b) $(-3; \frac{\pi}{6})$

Ex 2: Convert (x, y) to $(r; \theta)$,for $0 \leq \theta < 2\pi$

(a) $(-3, 4)$

(b) $(\sqrt{3}, -1)$

Ex 3: Convert a rectangular equation to a polar equation $x^2 + y^2 - 6x = 0$