

VD 7.2

Solve the following system of equation algebraically

1. $\begin{cases} \frac{x+y}{2} - y = -\frac{1}{2} \\ x - y + \frac{3x-1}{2} = -\frac{3}{4} \end{cases}$	$\left(\frac{1}{2}, \frac{3}{2}\right)$
2. $\begin{cases} \frac{1}{x} + \frac{2}{y} = 4 \\ \frac{3}{y} + \frac{2}{x} = 3 \end{cases}$	$\left(-\frac{1}{6}, \frac{1}{5}\right)$
3. $\begin{cases} e^x + 2e^y = 2 \\ 2e^x - e^y = \frac{1}{2} \end{cases}$	$\left(\ln \frac{3}{5}, \ln \frac{7}{10}\right)$
4. $\begin{cases} xy = e^4 \\ \frac{x^3}{y^2} = e^5 \end{cases}$	$\left(e^{\frac{13}{5}}, e^{\frac{7}{5}}\right)$
5. $\begin{cases} \sqrt{x+1} + 2\sqrt{y+2} = 4 \\ 3\sqrt{x+1} - 7\sqrt{y+2} = -\frac{15}{2} \end{cases}$	$\left(0, \frac{1}{4}\right)$
6. $\begin{cases} \frac{2x+1}{x+1} + \frac{2y-1}{y-2} = \frac{3}{2} \\ \frac{3}{x+1} + \frac{y}{y-2} = 3 \end{cases}$	$(0, 0)$
7. $x + y \in [0, \frac{\pi}{2})$ and $x - y \in [0, \frac{\pi}{2})$ $\begin{cases} \sin(x+y) - \cos(x-y) = \frac{1}{3} \\ 2\sin(x+y) + 7\cos(x-y) = \frac{11}{3} \end{cases}$	$\left(\frac{1}{2}\left(\cos^{-1}\frac{1}{3} + \sin^{-1}\frac{2}{3}\right), \frac{1}{2}\left(\sin^{-1}\frac{2}{3} - \cos^{-1}\frac{1}{3}\right)\right)$