Class Discussion

Unit 5 Topic 5 Part 2 Sum to Product and Product to Sum Formulas

Objective: Students need to be able to apply these formula to solve trigonometric equations or manipulate trigonometric expressions.

Sum To Product:

$$\sin x + \sin y = 2\sin\left(\frac{x+y}{2}\right)\cos\left(\frac{x-y}{2}\right)$$

$$\sin x - \sin y = 2\cos\left(\frac{x+y}{2}\right)\sin\left(\frac{x-y}{2}\right)$$

$$\cos x + \cos y = 2\cos\left(\frac{x+y}{2}\right)\cos\left(\frac{x-y}{2}\right)$$

$$\cos x - \cos y = -2\sin\left(\frac{x+y}{2}\right)\sin\left(\frac{x-y}{2}\right)$$

Product To Sum:

$$\sin x \sin y = -\frac{1}{2} \left[\cos(x+y) - \cos(x-y) \right]$$

$$\cos x \cos y = \frac{1}{2} \left[\cos(x+y) + \cos(x-y) \right]$$

$$\sin x \cos y = \frac{1}{2} \left[\sin(x+y) + \sin(x-y) \right]$$

$$\cos x \sin y = \frac{1}{2} \left[\sin(x+y) - \sin(x-y) \right]$$

Ex 1: Solve $\sin 6x + \sin 2x = \sin 4x$ if $x \in [0, 2\pi)$

Ex 2: Solve
$$\frac{\sqrt{3}\sin x}{\cos 4x - \cos 2x} + 1 = 0$$
 if $x \in [0, 2\pi)$

Ex 3: Write the following expression of product into sum: $\cos x \cos 3x \cos 5x$

Ex 4: Solve
$$\frac{\sqrt{3}\sin 3x}{\cos 4x - \cos 2x} + 1 = 0$$