

VD 7.5.2

Let $A = [a_{ij}]$ be a matrix of dimension $m \times n$. A^T is the transpose of A . if $A^T = (b_{ij})$ then $b_{ij} = a_{ji}$.

(a) Given matrix x , write x^T

(b) Given matrix M , find xM

(c) Find products: xMx^T and $xM^T x^T$

| x | M | x^T | xM | xMx^T | $xM^T x^T$ |
|----------------|--|--|--------------------------|------------|------------|
| $(-1 \ 0 \ 1)$ | $\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 & \frac{\sqrt{2}}{2} \\ 0 & 1 & 0 \\ -\frac{\sqrt{2}}{2} & 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$ | $\begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}$ | $(-\sqrt{2} \ 0 \ 0)$ | $\sqrt{2}$ | $\sqrt{2}$ |
| $(2 \ 0 \ 3)$ | $\begin{pmatrix} 1 & \frac{1}{2} & 0 \\ 0 & -1 & 1 \\ 1 & 0 & 0 \end{pmatrix}$ | $\begin{pmatrix} 2 \\ 0 \\ 3 \end{pmatrix}$ | $(5 \ 1 \ 0)$ | 10 | 10 |
| $(-1 \ 2 \ 0)$ | $\begin{pmatrix} 0 & 0 & 0 \\ 1 & 2 & 1 \\ 3 & 4 & 0 \end{pmatrix}$ | $\begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix}$ | $(2 \ 4 \ 2)$ | 6 | 6 |
| $(4 \ 3 \ 2)$ | $\begin{pmatrix} 0 & \frac{1}{2} & -2 \\ 1 & 0 & \frac{2}{3} \\ -\frac{1}{4} & \frac{1}{2} & 0 \end{pmatrix}$ | $\begin{pmatrix} 4 \\ 3 \\ 2 \end{pmatrix}$ | $(\frac{5}{2} \ 3 \ 14)$ | 47 | 47 |
| $(1 \ 2 \ 1)$ | $\begin{pmatrix} 2 & 0 & 0 \\ 1 & 3 & 0 \\ 0 & 1 & -1 \end{pmatrix}$ | $\begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$ | $(4 \ 7 \ -1)$ | 17 | 17 |

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|-----------------|--|---|--|-----|-----|
| $(-1 \ 3 \ -5)$ | $\begin{pmatrix} 1 & \frac{1}{2} & 0 \\ 0 & -4 & 1 \\ 3 & \frac{1}{2} & 1 \end{pmatrix}$ | $\begin{pmatrix} -1 \\ 3 \\ -5 \end{pmatrix}$ | $(-16 \ -15 \ -2)$ | -19 | -19 |
| $(0 \ 1 \ -3)$ | $\begin{pmatrix} 1 & 2 & -1 \\ \frac{2}{3} & 0 & 3 \\ \frac{1}{3} & 1 & 4 \end{pmatrix}$ | $\begin{pmatrix} 0 \\ 1 \\ -3 \end{pmatrix}$ | $\begin{pmatrix} -\frac{1}{3} & -3 & -9 \end{pmatrix}$ | 24 | 24 |