Review Unit 3 (This worksheet bares no grades, but it is your resource to SA3)

Factor Completely

$$1.16xy + 4x + 4y + 1$$

2.
$$(x+3)^2 - 3x(x+3)$$

3.
$$(x^4-1)+(x-1)(x^3-1)$$

4.
$$4x^2 + 12xy + 9y^2 - 8x - 12y - 5$$

5.
$$x^3 + 4x^2 - 16x - 64$$

6.
$$(1-y)^2 + x + y - xy - y^2$$

7.
$$(2x+3)^2 - y(2x+3) - 2y^2$$

8.
$$3(x+1)^2 - 4(y+1)^2 + 4xy + 4x + 4y + 4$$

9.
$$a^3 - a - b + b^3$$

10.
$$a^4 - 2ab^3 + 2a^3b - b^4$$

Use long division to find quotients and remainders

11.
$$(x^3 - 2x + 1) \div (x - x^2)$$

12.
$$(x^4 + 3x^3 + 5x^2 - 7) \div (x^2 + 2x + 1)$$

13.
$$(x^6 - 2x + 2) \div (-x^2 + 2)$$

Use synthetic division to find remainders

14.
$$(3x^3 + \frac{1}{2}x^2 + 5x - 9) \div (2x - 1)$$

15.
$$(4x^4 - 15x^3 + 6x^2 - 7x + 1) \div (x - 2)$$

16.
$$((3x^3 - 2x^2 + 6x + 5) \div (3x - 5)$$

Evaluate the function:

$$f(x) = x^4 - 3x^2 + 2x^3 - 1$$

17.
$$f(-3)$$

18.
$$f(2)$$

19.
$$f(-\frac{1}{2})$$

20. Given
$$g(x) = 16x^4 + 4ax^3 - 12bx^2 - 5x - 1$$

(a) if remainder of $g(x) \div (x-1)$ is 14 and (x+1) is a factor of g(x). Find a and b

(b) verify that
$$(4x+1)$$
 is a factor of $g(x)$

(c) use what you learned from (a) and (b) find all zeros for g(x)

21. Solve the following equations: assume all unknowns are real numbers.

(a)
$$4 \cdot 8^{x+1} = 256$$

(b)
$$3^x \cdot 6^{y-2} = 2^{3+2x} \cdot 3^{2y+1}$$

(c)
$$\frac{18^x}{4^y} = 12^{2+4y}$$

22.
$$m(x) = 2x + 1$$
, $n(x) = x^2 + 2x$

if
$$\begin{cases} f(x) + 2g(x) = m(x) + n(x) \\ f(x) + 4g(x) = 3x^2 - 2x + 5 \end{cases}$$

and
$$h(x) = f(x) \cdot g(x)$$

Find

(a)
$$f(x)$$
 ?

(b)
$$g(x)$$
 ?

(c)
$$h(x)$$
?

(d)
$$h(1)$$
 ?

(e)
$$h(2)$$
 ?