

[System of Equations and Vectors]

1. (3 pts)

Given that m , n and k are real numbers.

Solve system of equations
$$\begin{cases} m + 2n - k = 3 \\ 3m + 7n - 5k = 14 \\ -2m - n - 3k = 8 \end{cases}$$

2. (3 pts) Define vectors $\vec{u} = m\vec{i} + n\vec{j}$ and $\vec{v} = k\vec{i} + \vec{j}$, where m , n and k are from question 1, find $\vec{u} \cdot \vec{v}$

3. (3 pts) Continues from question 2, what is the area of the triangle formed by the origin, end points of vector \vec{u} and vector \vec{v} ?

[Trigonometric equations]

4. (3 pts) if $x \in [0, 2\pi)$, solve $\sin 2x = 2 \sin x$

(exact value)

[Application]

5. **Height of a Tree(3 pts)**

A tree is on a hillside of slope 15° (from horizontal). 75 feet downhill from where the tree is, the angle of elevation at the top of the tree is 65° . Find the height of the tree. (round to the whole feet)