

lens
from the ground up

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motivations

the ground up

intuitions

```
data Lens a b = Lens {  
    get :: a -> b  
, set :: b -> a -> a  
}
```

intuitions

```
data Lens a b = Lens {  
    get :: a -> b  
, set :: b -> a -> a  
}
```

set-get ==>
 $\text{get } l (\text{set } l b a) == b$

Pierce's laws

get-set ==>
 $\text{set } l (\text{get } l a) a == a$

set-set ==>
 $\text{set } l c (\text{set } l b a) == \text{set } l c a$

but...

```
modify :: Lens a b -> (b -> b) -> a -> a
modify l f a = set l (f (get l a)) a

compose :: Lens a b -> Lens b c -> Lens a c
compose l j = Lens
  (\a -> get j (get l a))
  (\c a -> set l (set j c (get l a)) a)
```

but...

efficiency matters

```
modify :: Lens a b -> (b -> b) -> a -> a
modify l f a = set l (f (get l a)) a
```

```
compose :: Lens a b -> Lens b c -> Lens a c
compose l j = Lens
  (\a -> get j (get l a))
  (\c a -> set l (set j c (get l a)) a)
```

but...

```
data Wedge a =  
    Wedge { _name :: String, _val :: a }  
  
name :: Lens (Wedge a) String  
name = Lens _name (\n w -> w { _name = n })  
  
value :: Lens (Wedge a) a  
value = Lens _val (\v w -> w { _val = v })
```

but...

polymorphic update matters

```
data Wedge a =  
    Wedge { _name :: String, _val :: a }  
  
name :: Lens (Wedge a) String  
name = Lens _name (\n w -> w { _name = n })  
  
value :: Lens (Wedge a) a  
value = Lens _val (\v w -> w { _val = v })
```

but...

```
data Safety =  
  Safety { _readOnly :: String }  
  
readOnly :: Lens Safety String  
readOnly =  
  Lens _readOnly (error "don't do this")
```

but...

read only / write only matters

```
data Safety =  
  Safety { _readOnly :: String }  
  
readOnly :: Lens Safety String  
readOnly =  
  Lens _readOnly (error "don't do this")
```

but...

```
(&&&) :: Lens a b -> Lens a c -> Lens a (b, c)
(&&&) l j = Lens
  (\a -> (get l a, get j a))
  (\(b, c) a -> set j c (set l b a))
```

but...

```
(&&&) :: Lens a c -> Lens a (b, c)
(&&&) l j = Lens not a lens
  (\a -> (get l a, get j a))
  (\(b, c) a -> set j c (set l a))
```

but...

composition matters

```
(&&&) :: Lens a c -> Lens a (b, c)
(&&&) l j = Lens (\a -> (get l a, get j a))
              (\(b, c) a -> set j c (set l a))
```

not a lens

but...

```
data OneOf = First String | Second Int
```

```
first :: Lens OneOf (Maybe String)  
first = undefined
```

```
first :: Lens OneOf (Maybe String)  
first = undefined
```

but...

```
data OneOf = First String | Second Int
```

```
first :: Lens OneOf (String, String)
first = undefined
```

```
first :: Lens OneOf (Maybe String)
first = undefined
```

not a lens

but...

partiality matters

```
data OneOf = First String | Second Int
```

```
first :: Lens OneOf (String)
first = undefined
```

not a lens

```
first :: Lens OneOf (Maybe String)
first = undefined
```

failed experiments

```
data Store s a =  
  Store (s -> a) s  
  
data Lens a b =  
  Lens (a -> Store b a)
```

failed experiments

```
data Store s a =  
  Store (s -> a) s  
  
data Lens a b =  
  Lens (a -> Store b a)  
  
get :: Lens a b -> a -> b  
get (Lens l) a =  
  case l a of Store _ s -> s  
  
set :: Lens a b -> b -> a -> a  
set (Lens l) b a =  
  case l a of Store f _ -> f b
```

failed experiments

```
data Store s a =  
  Store (s -> a) s  
  
data Lens a b =  
  Lens (a -> Store b a)  
  
get :: Lens a b -> a -> b  
get (Lens l) a =  
  case l a of Store _ s -> s  
  
set :: Lens a b -> b -> a -> a  
set (Lens l) b a =  
  case l a of Store f _ -> f b
```

polymorphic update matters

read only / write only matters

composition matters

partiality matters

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
set :: Lens' a b -> b -> a -> a  
set = error "can we?"
```

```
get :: Lens' a b -> a -> b  
get = error "can we?"
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b a =  
  let x = const $ Identity b -- :: b -> Identity b  
  in undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b a =  
  let x = const $ Identity b -- :: b -> Identity b  
      y = l x -- :: a -> Identity a  
  in runIdentity z
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b a =  
  let x = const $ Identity b -- :: b -> Identity b  
      y = l x -- :: a -> Identity a  
      z = y a -- :: Identity a  
in undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b a =  
  let x = const $ Identity b -- :: b -> Identity b  
      y = l x -- :: a -> Identity a  
      z = y a -- :: Identity a  
  in runIdentity z
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b a =  
  runIdentity (l (const $ Identity b) a)
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b a =  
  runIdentity . l (const $ Identity b) $ a
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Identity a =  
  Identity { runIdentity :: a }
```

```
set :: Lens' a b -> b -> a -> a  
set l b =  
  runIdentity . l (const $ Identity b)
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype ??? a =  
  ???
```

```
get :: Lens' a b -> a -> b  
get l a =  
  undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  undefined
```

```
instance Functor (Const x) where  
  fmap _ = Const . runConst
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  let x = Const -- :: b -> Const b b  
  in undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  let x = Const    -- :: b -> Const b b  
      y = l x     -- :: a -> Const b a  
  in undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  let x = Const    -- :: b -> Const b b  
      y = l x     -- :: a -> Const b a  
      z = y a     -- :: Const b a  
  in undefined
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  let x = Const    -- :: b -> Const b b  
      y = l x     -- :: a -> Const b a  
      z = y a     -- :: Const b a  
  in runConst z
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  runConst (l Const a)
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l a =  
  runConst . l Const $ a
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
newtype Const x a =  
  Const x
```

```
get :: Lens' a b -> a -> b  
get l =  
  runConst . l Const
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
set :: Lens' a b -> b -> a -> a  
set l b = runIdentity . l (const $ Identity b)
```

```
get :: Lens' a b -> a -> b  
get l = runConst . l Const
```

back to the drawing board

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
set :: Lens' a b -> b -> a -> a  
set l b = runIdentity . l (const $ Identity b)
```

```
get :: Lens' a b -> a -> b  
get l = runConst . l Const
```

```
modify :: Lens' a b -> (b -> b) -> a  
modify l f = runIdentity . l (Identity . f)
```

functional elegance

composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b  
y :: Lens b c  
x . y :: Lens a c
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c  
x . y :: Lens a c
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)  
  
(.) :: (i -> j) -> (h -> i) -> h -> j
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)  
  
(.) :: (i -> j) -> (h -> i) -> h -> j  
  
x :: i -> j
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)  
  
(.) :: (i -> j) -> (h -> i) -> h -> j  
  
x :: i -> j, y :: h -> i
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

```
(.) :: (i -> j) -> (h -> i) -> h -> j
```

```
x :: i -> j, y :: h -> i  
i :: b -> f b
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

```
(.) :: (i -> j) -> (h -> i) -> h -> j
```

```
x :: i -> j, y :: h -> i  
i :: b -> f b, j :: a -> f a
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

```
(.) :: (i -> j) -> (h -> i) -> h -> j
```

```
x :: i -> j, y :: h -> i  
i :: b -> f b, j :: a -> f a, h :: c -> f c
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

```
(.) :: (i -> j) -> (h -> i) -> h -> j
```

```
x :: i -> j, y :: h -> i  
i :: b -> f b, j :: a -> f a, h :: c -> f c  
x . y :: h -> j
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

```
(.) :: (i -> j) -> (h -> i) -> h -> j
```

```
x :: i -> j, y :: h -> i  
i :: b -> f b, j :: a -> f a, h :: c -> f c  
x . y :: h -> j :: (c -> f c) -> (a -> f a)
```

function composition

```
type Lens' a b =  
  forall f. Functor f => (b -> f b) -> a -> f a
```

```
x :: Lens a b :: (b -> f b) -> (a -> f a)  
y :: Lens b c :: (c -> f c) -> (b -> f b)  
x . y :: Lens a c :: (c -> f c) -> (a -> f a)
```

```
(.) :: (i -> j) -> (h -> i) -> h -> j
```

```
x :: i -> j, y :: h -> i  
i :: b -> f b, j :: a -> f a, h :: c -> f c  
x . y :: h -> j :: (c -> f c) -> (a -> f a)
```

polymorphic update

```
type Lens a a' b b' =  
  forall f. Functor f => (b -> f b') -> a -> f a'  
  
type Lens' a b = Lens a a b b
```

polymorphic update

```
type Lens a a' b b' =  
  forall f. Functor f => (b -> f b') -> a -> f a'
```

```
type Simple f a b = f a a b b
```

```
type Lens' = Simple Lens
```

polymorphic update

```
type Lens a a' b b' =  
  forall f. Functor f => (b -> f b') -> a -> f a'
```

```
set :: Lens' a b -> b -> a -> a  
set l b = runIdentity . l (const $ Identity b)
```

```
get :: Lens' a b -> a -> b  
get l = runConst . l Const
```

```
modify :: Lens' a b -> (b -> b) -> a  
modify l f = runIdentity . l (Identity . f)
```

polymorphic update

```
type Lens a a' b b' =  
  forall f. Functor f => (b -> f b') -> a -> f a'
```

```
set :: Lens a a' b b' -> b' -> a -> a'  
set l b = runIdentity . l (const $ Identity b)
```

```
get :: Lens a a' b b' -> a -> b'  
get l = runConst . l Const
```

```
modify :: Lens a a' b b' -> (b -> b') -> a'  
modify l f = runIdentity . l (Identity . f)
```

polymorphic update

```
type Lens a a' b b' =  
  forall f. Functor f => (b -> f b') -> a -> f a'
```

```
set :: Lens a a' b b' -> b' -> a -> a'  
set l b = runIdentity . l (const $ Identity b)
```

```
get :: Lens a a' b b' -> a -> b'  
get l = runConst . l Const
```

```
modify :: Lens a a' b b' -> (b -> b') -> a'  
modify l f = runIdentity . l (Identity . f)
```

mirrored lenses

```
type Getter s a =  
  forall r. (a -> Const r a) -> s -> Const r s
```

```
type Setter s t a b =  
  (a -> Identity b) -> s -> Identity t
```

multiplate

```
type Traversal a a' b b' =  
  forall f. Applicative f =>  
  (b -> f b') -> a -> f a'
```

multiplate

```
type Traversal a a' b b' =  
  forall f. Applicative f =>  
    (b -> f b') -> a -> f a'
```

```
set :: Traversal a a' b b' -> b' -> a -> a'  
set l b = runIdentity . l (const $ Identity b)
```

```
get :: Traversal a a' b b' -> a -> b'  
get l = runConst . l Const
```

```
modify :: Traversal a a' b b' -> (b -> b') -> a'  
modify l f = runIdentity . l (Identity . f)
```

prisms / co-lens

```
type Prism s t a b =  
  forall p f. (Choice p, Applicative f) =>  
    p a (f b) -> p s (f t)
```

iso

```
type Iso s t a b =  
  forall p f. (Profunctor p, Functor f) =>  
    p a (f b) -> p s (f t)
```

code

gotchas

references

- Pierce's original work on lenses / bidirectional programming:
 - <http://www.cis.upenn.edu/~bcpierce/papers/index.shtml#Lenses>
- van Laarhoven's original write-up:
 - <http://www.twanvl.nl/blog/haskell/cps-functional-references>
- O'Connor's coining of the term “van Laarhoven lens” and the insight into polymorphic update:
 - <http://r6.ca/blog/20120623T104901Z.html>
- O'Connor's multiplate paper (a.k.a. traversals):
 - <http://arxiv.org/pdf/1103.2841v2.pdf>
- Kmett's expanding on mirrored lens insights (a.k.a. read-only / write only):
 - <http://comonad.com/reader/2012/mirrored-lenses/>
- lens website, lots of links and video:
 - <http://lens.github.io/>
- git repo:
 - <https://github.com/ekmett/lens>
- hackage:
 - <http://hackage.haskell.org/package/lens>

fin

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