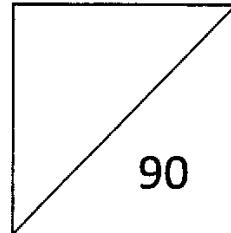


CANDIDATE NAME				
CLASS		INDEX NUMBER		

Anglo-Chinese School (Independent)



PRELIMINARY EXAMINATION 2024 YEAR FOUR EXPRESS MATHEMATICS PAPER 1

4052/01

Thursday**1 August 2024****2 hours 15 minutes**

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

Write your index number, name and class in the spaces on top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 90.

*Mathematical Formulae**Compound Interest*

$$\text{Total amount} = P \left(1 + \frac{r}{100}\right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4 \pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3} \pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3} \pi r^3$$

$$\text{Area of a triangle} = \frac{1}{2} ab \sin C$$

$$\text{Arc length} = r\theta, \text{ where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2} r^2 \theta, \text{ where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$\text{Mean} = \frac{\sum f x}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum f x^2}{\sum f} - \left(\frac{\sum f x}{\sum f}\right)^2}$$

3

Answer all the questions.

- 1 The point C lies on the line AB such $AC:AB = 2:7$.

- (a) Write AC as a fraction of BC .

Answer [1]

- (b) Given that AC is 24 cm, calculate the length of BC .

Answer cm [1]

- 2 (a) $\sin x^\circ = 0.66913$

Given that x is an obtuse angle, find x .

Answer $x = \dots$ [1]

- (b) $\cos y^\circ = -\cos 121^\circ$

Given that y is an acute angle, find the value of y .

Answer $y = \dots$ [1]

- 3 During a game, Lee rolled two fair six-sided die. To obtain the score, he subtracted the lower number from the higher number. If the numbers shown on the dice were the same, his score is zero.

(a) Construct a possibility diagram to show all possible outcomes. [1]

Answer

(b) Find the probability that Lee's score is 5.

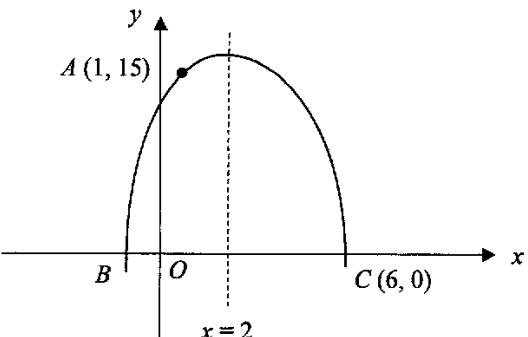
Answer [1]

- 4 A shopkeeper bought a pair of shorts for \$24. He made a percentage profit of 45% despite selling it at a discount of 20% off the listed price. Calculate the listed price for this pair of shorts.

Answer \$..... [2]

5

- 5 Part of the graph of a quadratic function is shown below.



The graph passes through the point $A(1, 15)$ and it cuts the x -axis at the points B and C .

Given that C is $(6, 0)$ and $x = 2$ is the line of symmetry of the graph,

- (a) write down the equation of the quadratic curve in the form $y = a(x - h)^2 + k$.

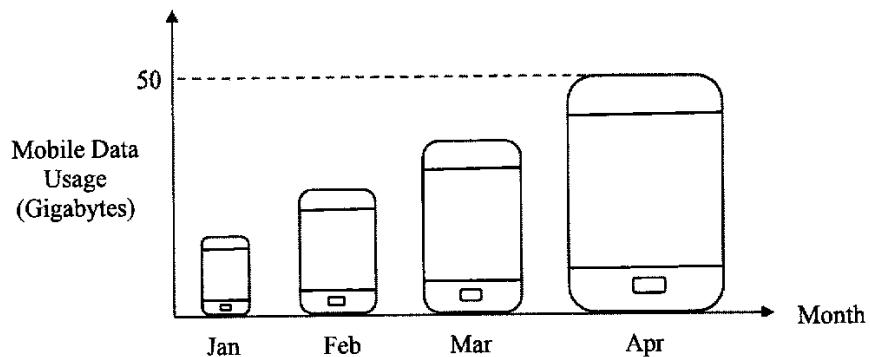
Answer [2]

- (b) find the positive value of x when $y = 4$, leaving your answer in exact form.

Answer $x = \dots$ [1]

6

- 6 Justin drew this graph to show his mobile data usage for each of the following four months.



State one aspect of the graph that may be misleading and explain how this may lead to a misinterpretation of the graph.

Answer

- 7 Simplify $\left(\frac{1}{2}x^2\right)^3 \div \left(4 \sqrt[3]{x^5}\right)$ giving your answer in the form of ax^n , where a and n are rational numbers.

Answer [2]

- 8 (a) Express 13 824 as a product of its prime factors.

Answer [1]

- (b) Explain why 13 824 is a perfect cube.

Answer

.....

.....

..... [1]

- (c) Given that a is a prime number, find the value of a such that $\frac{1}{8a} \times 13824$ is a perfect square.

Answer $a =$ [1]

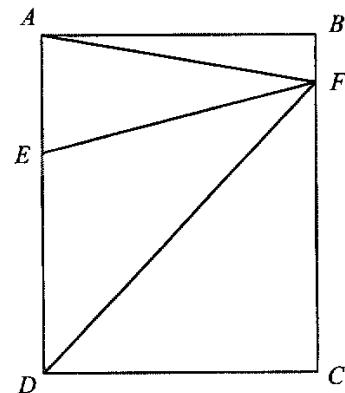
- 9 In the diagram, $ABCD$ is a rectangle and E and F are points on AD and BC respectively.

The ratio of the area of triangle ABF to the area of rectangle $ABCD$ is 1: 9.

The ratio of the area of triangle AFE to the area of rectangle $ABCD$ is $1:6$.

Explain with clear workings, if the following statements are true/ false.

- A: The ratio of the area of triangle ABF to that of triangle AFE is $2:3$.
 - B: The ratio of the area of triangle DFC to that of rectangle $ABCD$ is $2:5$.
 - C: The sum of the area of triangles ABF and triangle DFC is equal to the sum of the area of triangles AFE and EFD .



Answer

- 10 The ratio of the number of soccer balls and volleyballs in a sports shop was 11: 7. After 126 soccer balls were added and 233 volleyballs were sold, the ratio became 14: 3. How many volleyballs were there in the shop at first?

Answervolleyballs [3]

- 11 Explain why $(5n+2)^2 - (5n-2)^2$ is a multiple of 8 for all integer values of n .

Answer

.....

..... [2]

10**12** Factorise the following completely.

(a) $45b - 18ab - 2a^2 + 5a$,

Answer [2]

(b) $2p^2 - \frac{2}{3}p - \frac{1}{6}$.

Answer [2]

13 Simplify $\frac{x^2 - 9y^2}{3x^2 + 7xy - 6y^2}$.

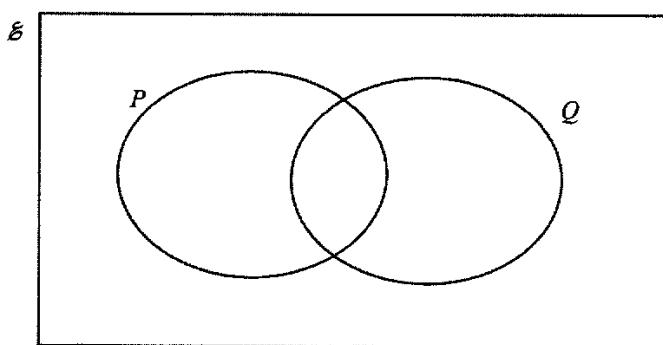
Answer [3]

- 14 The sets P and Q consists of the points whose coordinates (x, y) are given by $P = \{(x, y) : y = 2x + 3\}$ and $Q = \{(0, 0), (0, 3), (1, 5), (2, 5), (3, 9)\}$ respectively.

- (a) List the elements in $P \cap Q$.

Answer [2]

- (b) Shade the region which represents $(P \cup Q)^c$.



[1]

- 15 The distance between the points $M(k, 7)$ and $N(9, k)$ is $\sqrt{20}$ units.
Given that $k > 10$, find the value of k .

Answer $k = \dots$ [3]

12

- 16 Mr Tan took 4 hours to travel from Town A to Town B. Mr Lim took 8 hours to travel in the opposite direction from Town B to Town A using the same route. They both started at 11am. What time did they pass each other?

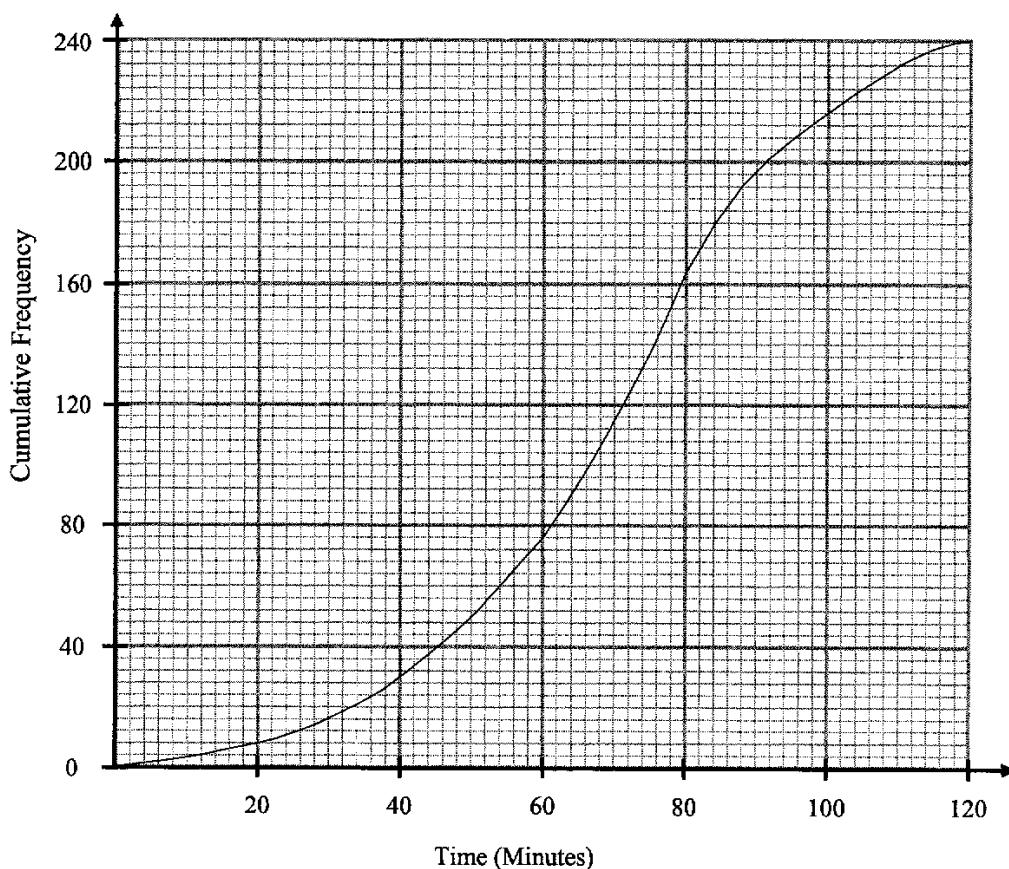
Answer pm [2]

- 17 Sam and Wilson can paint a house together in 6 days. They painted the house together for 5 days and then Sam completed the painting of the remaining house alone in 3 days. How many days would it take for Wilson to paint the entire house by himself?

Answer days [3]

13

- 18 The cumulative frequency curve below illustrates the wait time of 240 customers who visited a bank.



Use the graph to estimate

- (a) the 60th percentile,

Answer minutes [1]

- (b) the interquartile range of the wait time.

Answer minutes [2]

14

- (c) Only 10% of the customers complained about the long wait time they experienced. What was the minimum wait time for these customers?

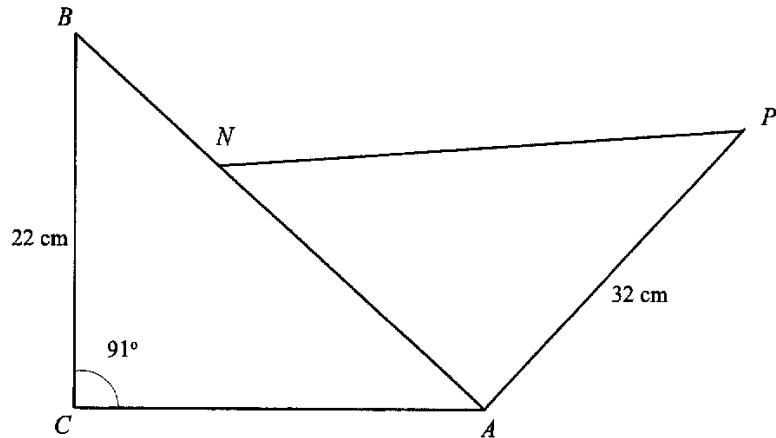
Answer minutes [2]

- (d) Two customers are chosen at random. Find the probability that one customer waited for less than or equal to 60 minutes and the other waited for more than 100 minutes.

Answer [2]

15

- 19 In the diagram below, triangle ABC is congruent to triangle PNA .



Given that $BC = 22 \text{ cm}$, $AP = 32 \text{ cm}$ and angle $ACB = 91^\circ$, calculate

- (a) the length of BN ,

Answer cm [3]

- (b) angle APN .

Answer Angle APN = [2]

16

20 The mean of ten different numbers is 11.8.

- (a) Write down a number which will generate a mean of 12, when added to these ten numbers.

Answer..... [1]

- (b) Each value within the ten numbers is adjusted as follows:

If the number is less than the mean, the number is decreased by 2,
if the number is greater than the mean, the number is increased by 2 and
if the number is equal to the mean, it remains unchanged.

Explain clearly how these adjustments would affect the standard deviation.

Answer

.....

.....

.....

.....

[2]

- 21** A tour agency sells cruise packages to Vietnam, Maldives and Taiwan at \$1299, \$1398 and \$2538 respectively. The table below shows the number of customers who have signed up for the respective cruise packages via the tour agency from January to June and from July to December.

	First Period	Second Period
	From January to June	From July to December
Vietnam	27	24
Maldives	23	29
Taiwan	19	22

The number of people who signed up for cruise packages to Vietnam, Maldives and Taiwan can be

represented by the matrix $P = \begin{pmatrix} 27 & 24 \\ 23 & 29 \\ 19 & 22 \end{pmatrix}$.

- (a)** The elements of matrix C , where $C = AP$, represents the total earnings for each period. Write down the matrix A .

Answer A = [1]

- (b)** Hence, by using matrix multiplication, determine the total earnings, C by the tour agency for each of the period respectively.

Answer C = [2]

18

- (c) Given $\mathbf{M} = \mathbf{CR}$, where $\mathbf{R} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$, find the matrix \mathbf{M} .

Answer $\mathbf{M} =$

[2]

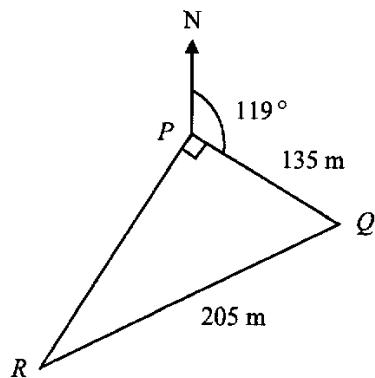
- (d) Describe what is represented by the element(s) of \mathbf{M} .

Answer

.....

..... [1]

- 22 P , Q and R are three points on level ground such that RPQ forms a right-angled triangle with PQ and RQ measuring 135 m and 205 m respectively. It is given that a building of height 50 m is situated at P and that the bearing of Q from P is 119° .



- (a) Calculate the bearing of R from Q .

Answer [2]

- (b) Calculate the largest possible angle of depression from the top of the building to any point on the path RQ .

Answer [3]

20

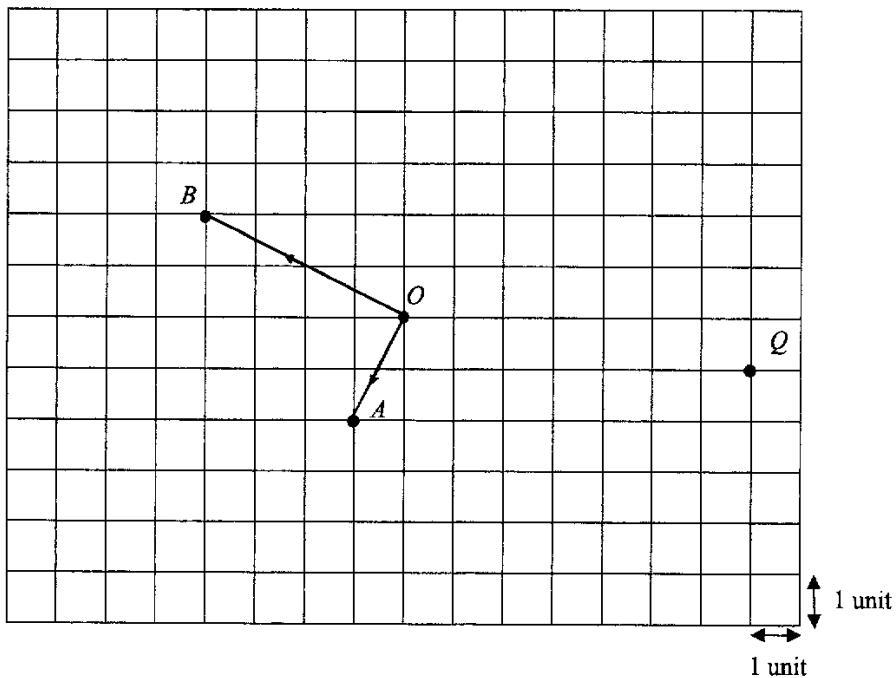
- 23 Jefferson and Victor were sent by their company to work in Washington D.C. and Beijing respectively. Jefferson rented a 696 sq ft apartment in Washington D.C. for 1800 USD while Victor rented a 60 m^2 apartment in Beijing for 8000 CNY. Given that the currency exchange rate for both cities is 1 USD = 7.25 CNY and that $1 \text{ m}^2 = 10.7639 \text{ sq ft}$, illustrate with clear working, which apartment has a higher rental cost.

Answer

..... [3]

21

- 24 In the grid, $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$. Q is a point on the grid.



- (a) Mark and label the point P such that $\overrightarrow{OP} = -\mathbf{b} - 2\mathbf{a}$. [1]
- (b) Express \overrightarrow{OQ} in the form $m\mathbf{a} + n\mathbf{b}$, where m, n are real numbers.

Answer $\overrightarrow{OQ} = \dots \dots \dots$ [1]

- (c) Given that $\overrightarrow{OC} = \begin{pmatrix} 6 \\ x \end{pmatrix}$ and \overrightarrow{OC} is parallel to \overrightarrow{AB} , find the value of x .

Answer $x = \dots \dots \dots$ [2]

22

- 25 Edwin deposited \$ P each into Bank A and Bank B . Bank A offered a simple interest of 4% per annum while Bank B offered an interest rate of 2% per half-year, compounded every six months. The difference in the amount Edwin received from both banks after a period of 7 years is \$513. Find P , correct your answer to the nearest hundred.

Answer [4]

- 26 X , Y , and Z are three points on a horizontal sea level map as shown below.
 X is due North of Y and Z is due east of Y .

Ship A is on a bearing of 070° from X and on a bearing of 350° from Z .

It is given that 1 cm represents 2 km on the sea level.

- (a) Label the position of Ship A and write down the actual distance AX .

Answer $AX = \dots$ km [2]

- (b) A boat, B stationed along path XZ is equidistant from Y and Z . Label the position of B . [2]

- (c) Showing your constructions clearly, draw a circle with centre O , on the map such that the lines XY , YZ and XZ are tangents to the circle. Hence write down the radius of the circle on the map.

Answer cm [2]

