

# Properties of Triangles

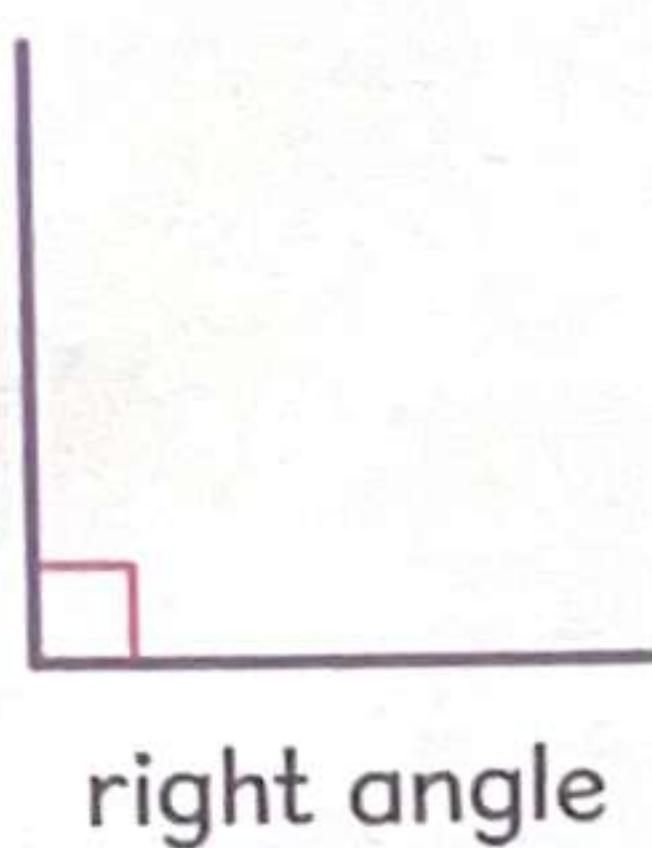


# Types of Triangles

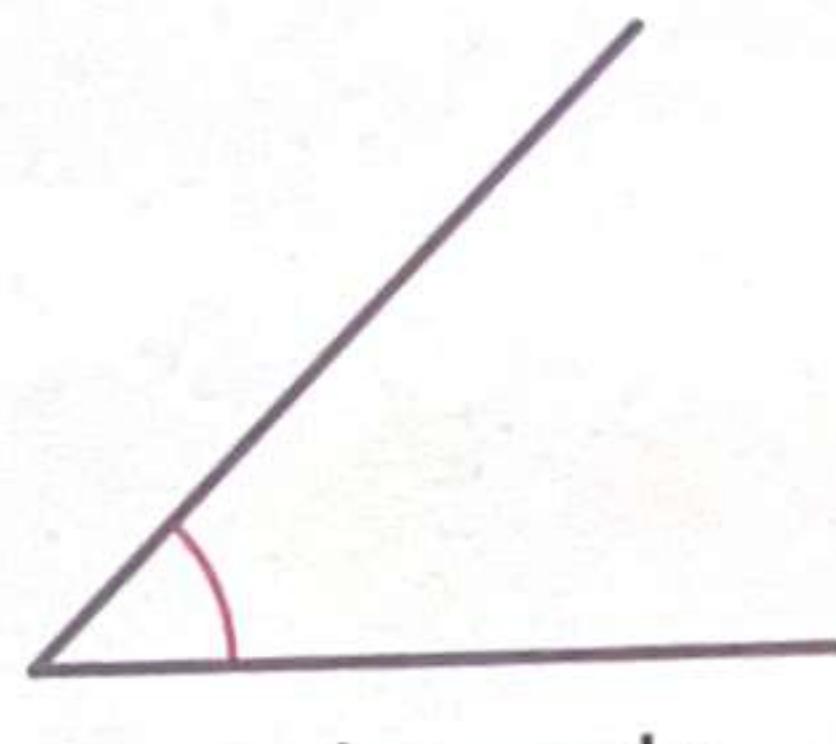


## Recall

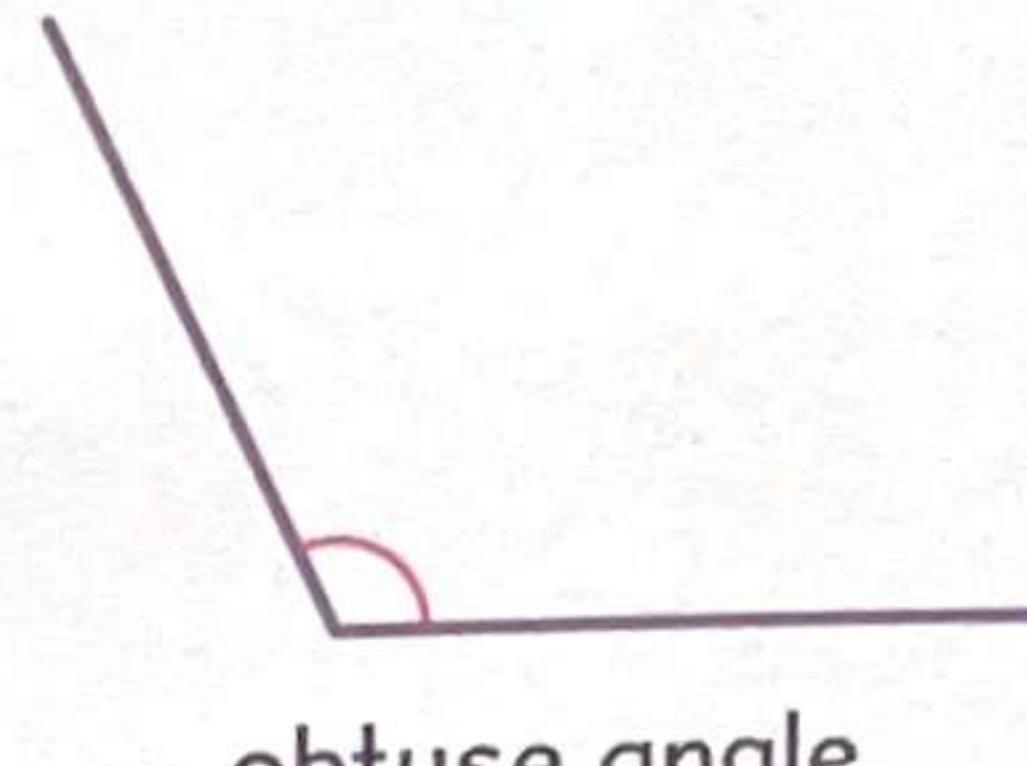
- 1 Angles are formed when 2 straight lines meet at a **vertex**.  
The size of an angle depends on the **amount of turning**.



right angle



acute angle

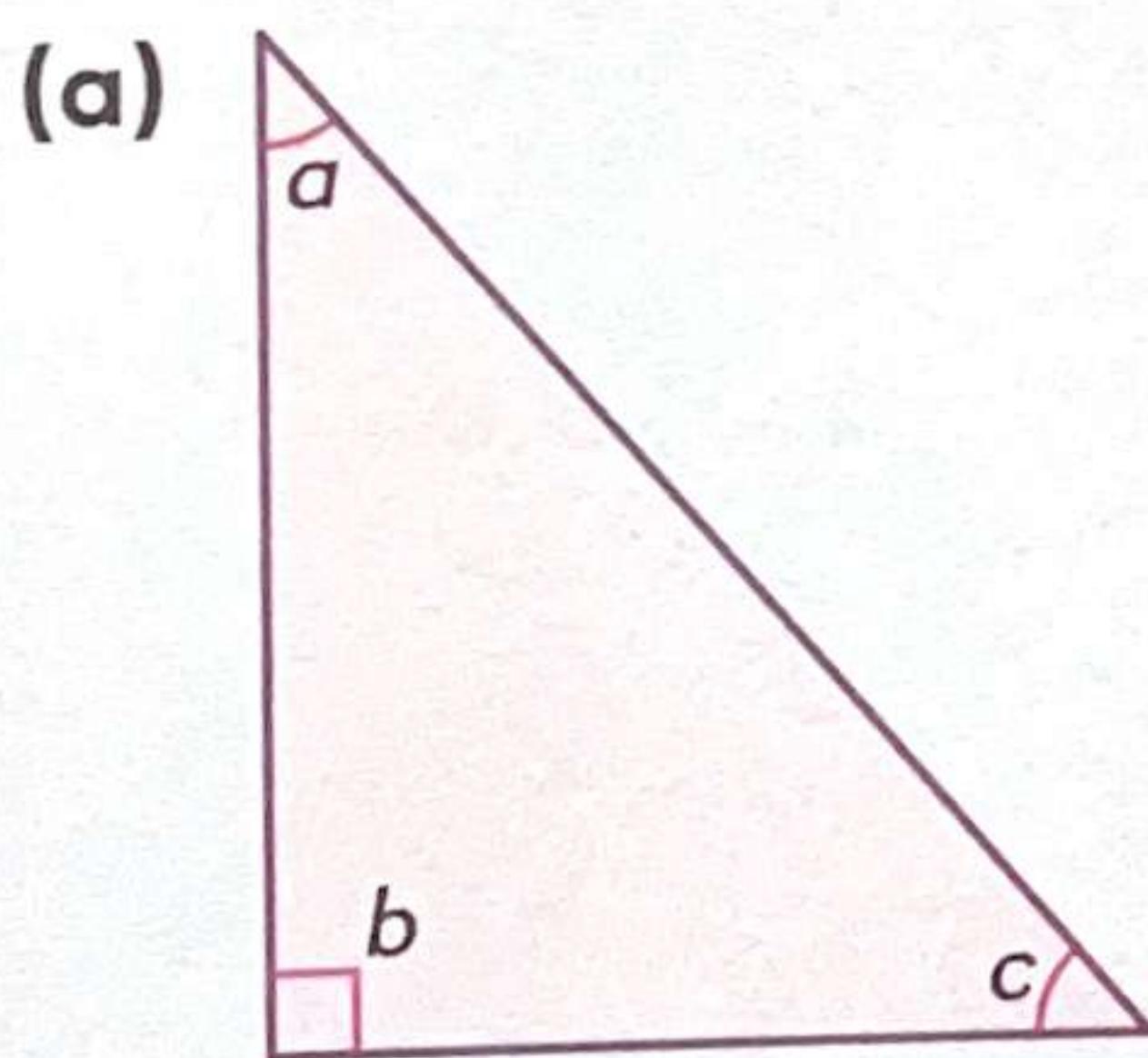


obtuse angle

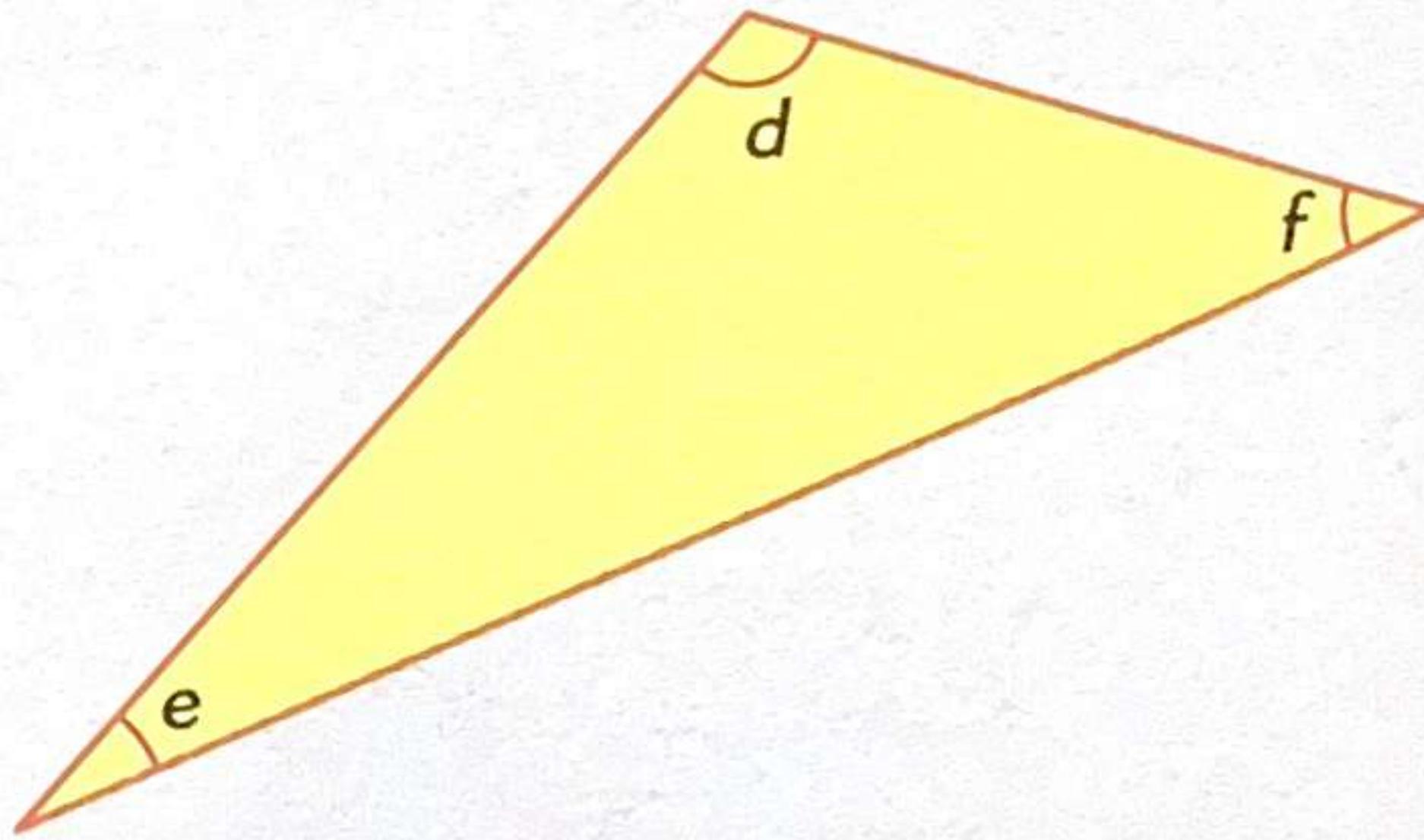
(a) An acute angle is  than a right angle.

(b) An obtuse angle is  than a right angle.

- 2 Identify the types of angles in each triangle.  
Are they acute, obtuse or right angles?



(a)



(b)

| Angle | Type of angles |
|-------|----------------|
| a     |                |
| b     |                |
| c     |                |

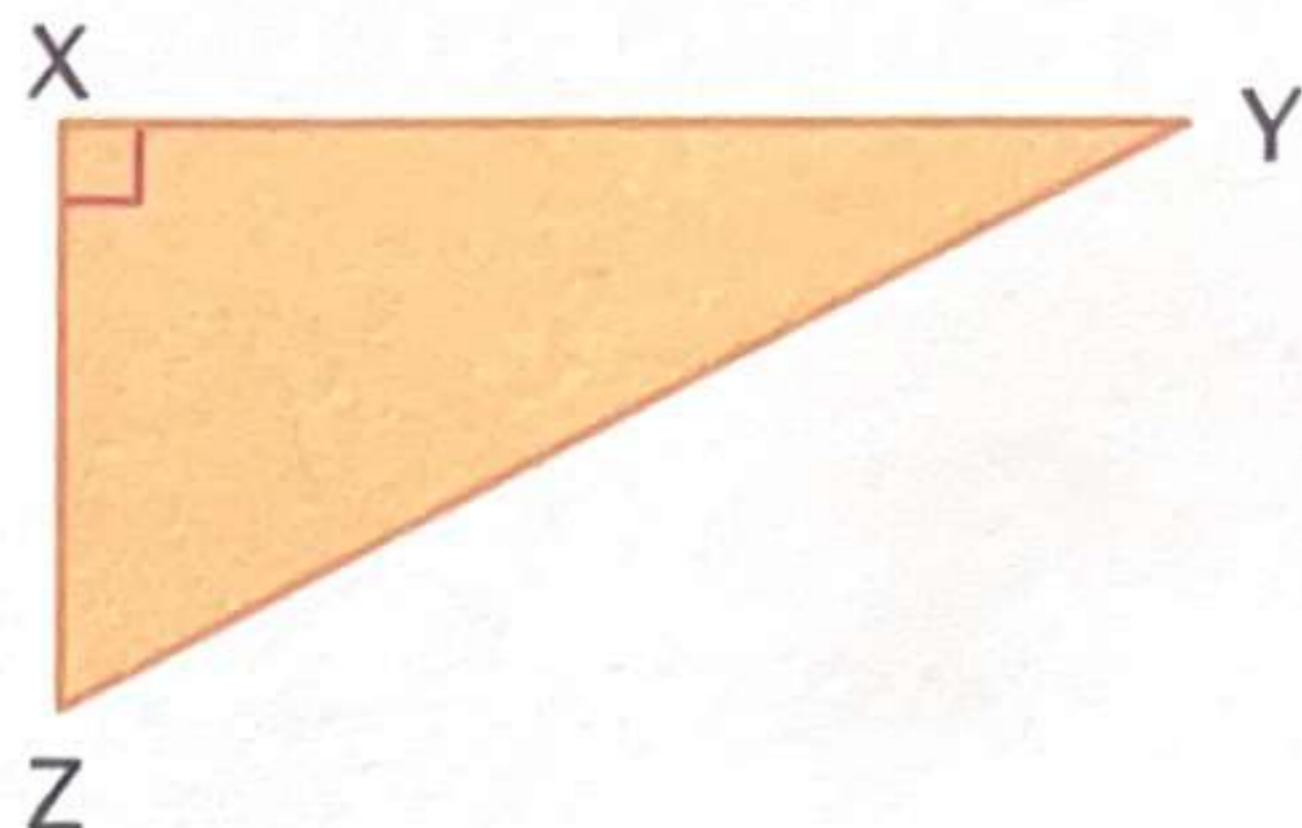
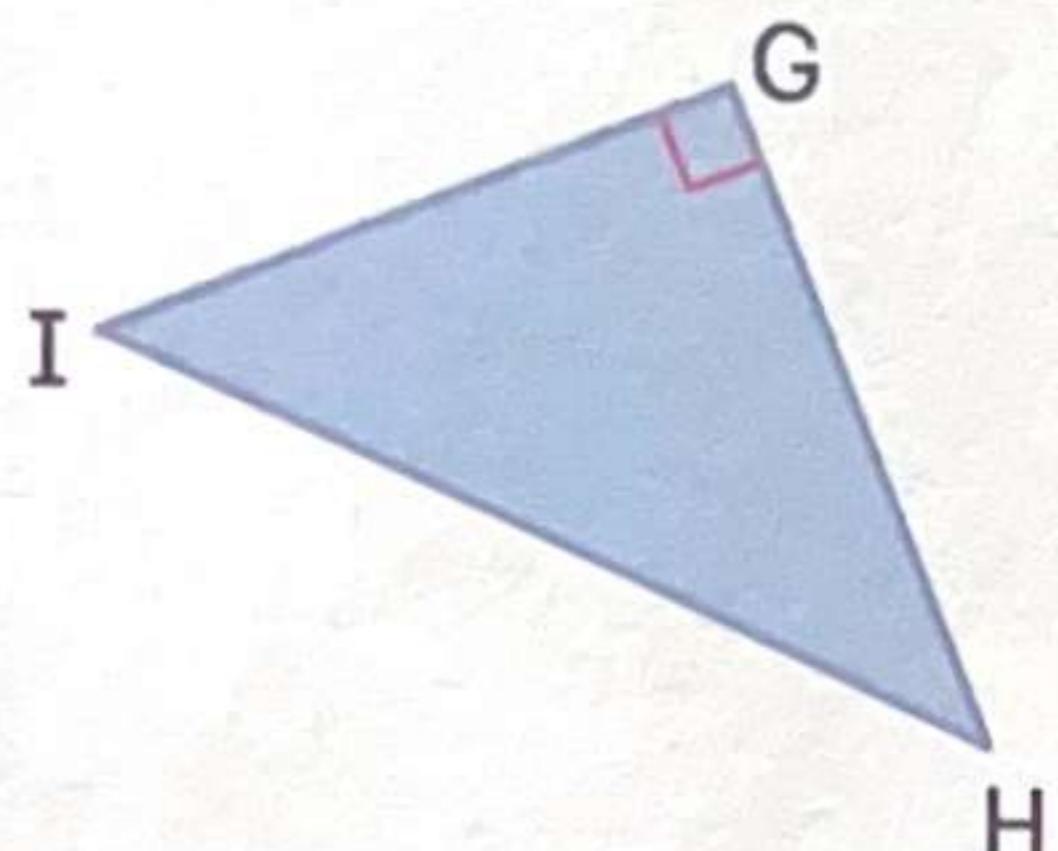
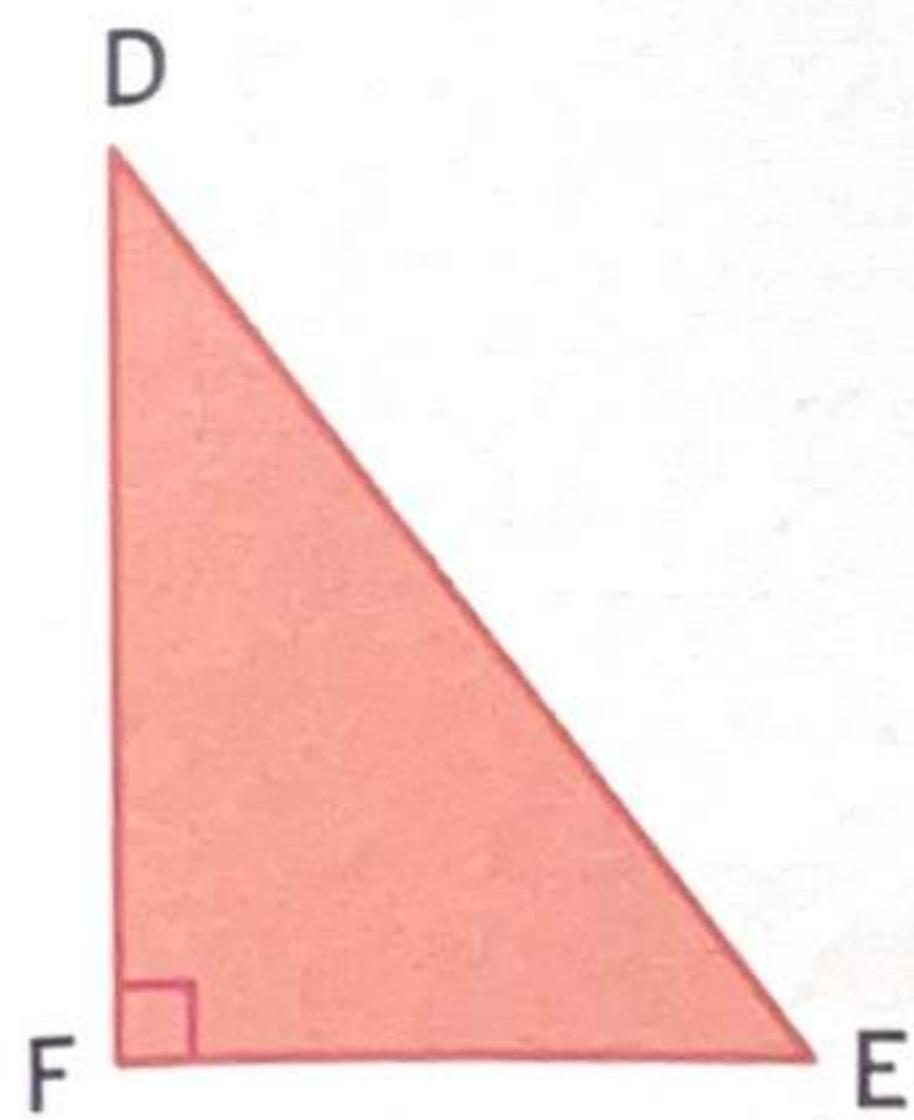
| Angle | Type of angles |
|-------|----------------|
| d     |                |
| e     |                |
| f     |                |





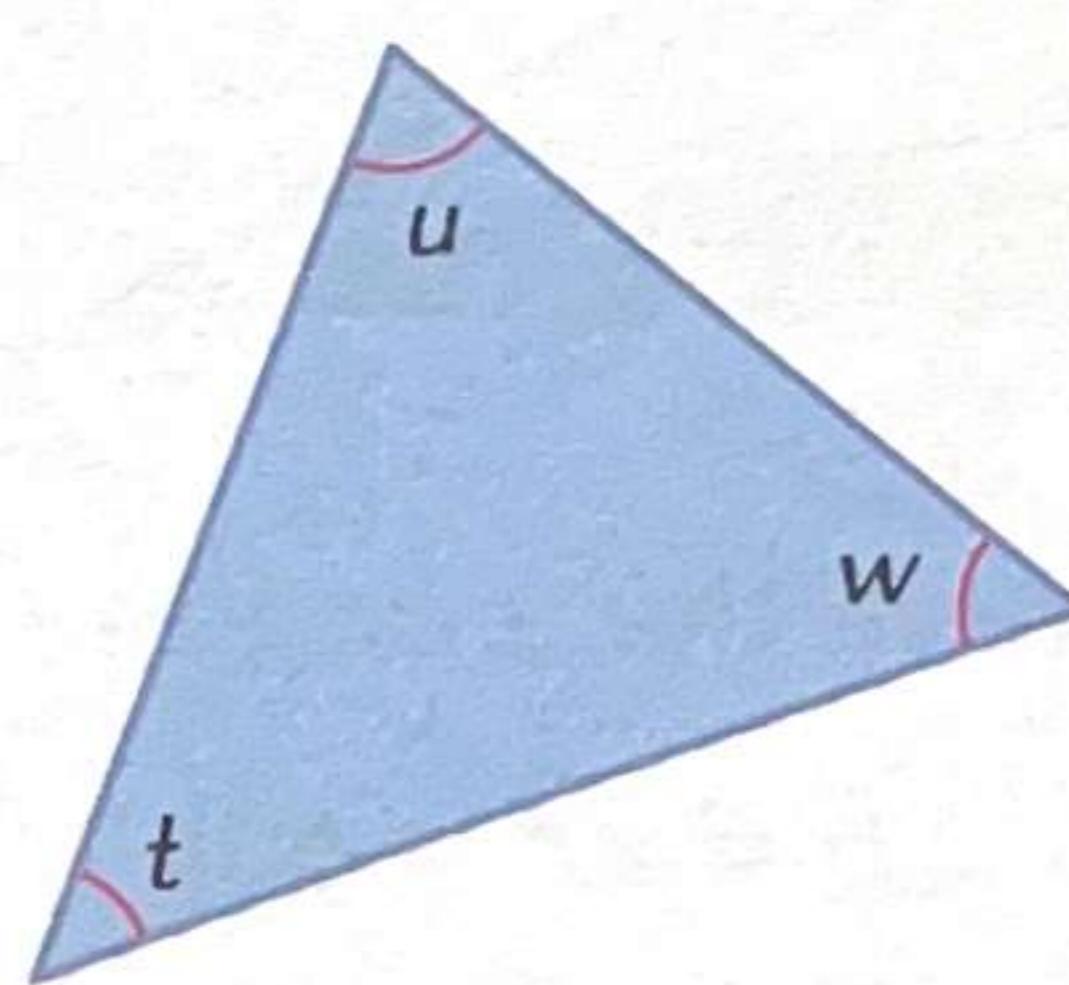
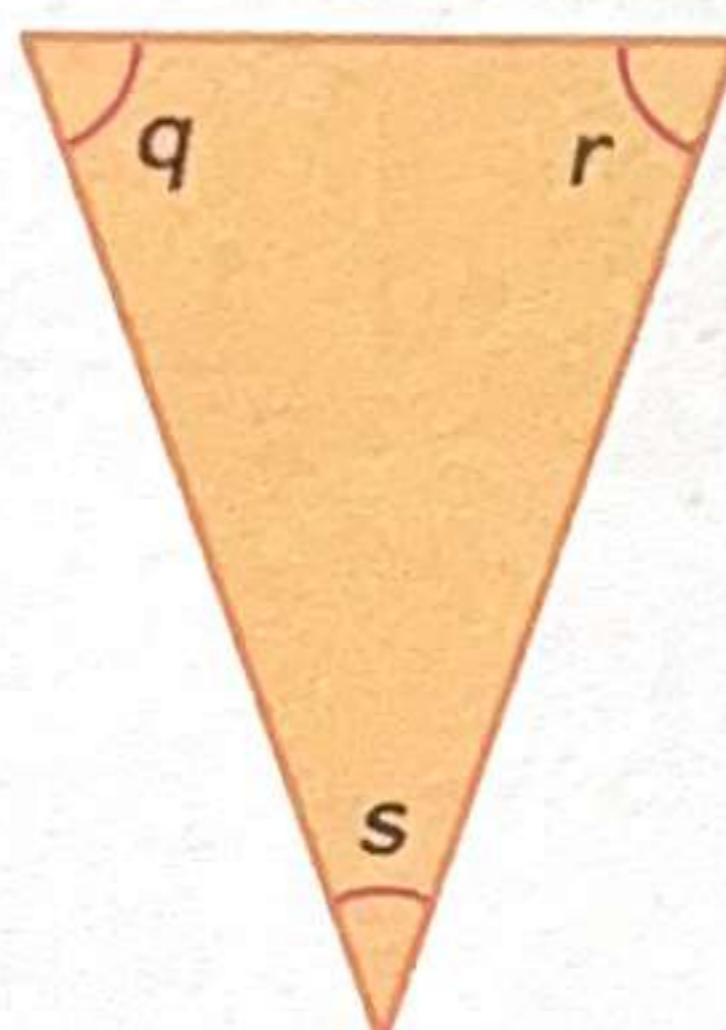
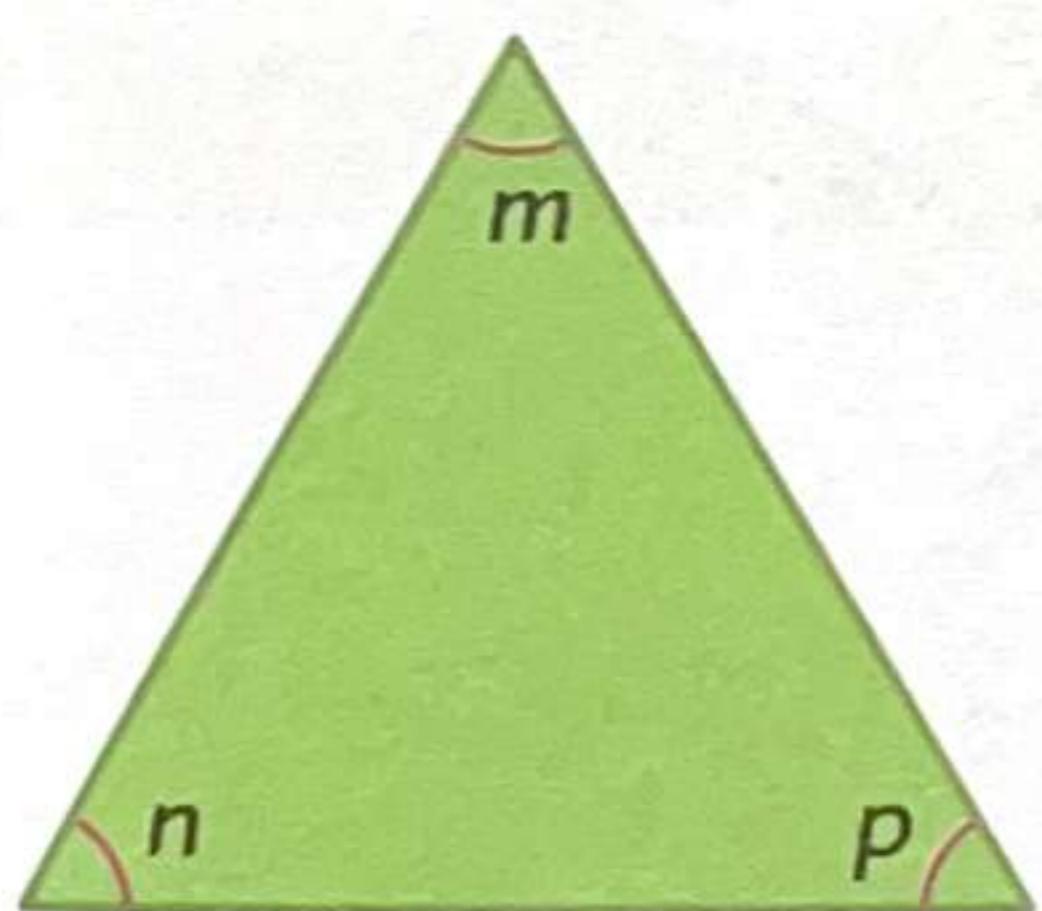
These are **right-angled triangles**.

A right-angled triangle has **two sides** that are **perpendicular** to each other.  
One of its angles is a **right angle**.



These are **acute-angled triangles**.

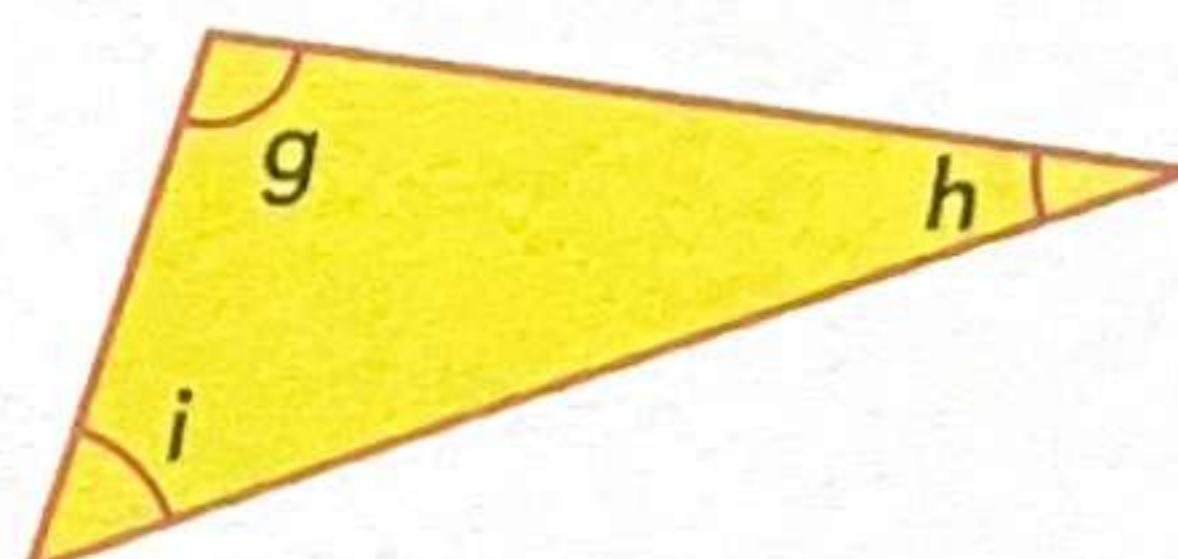
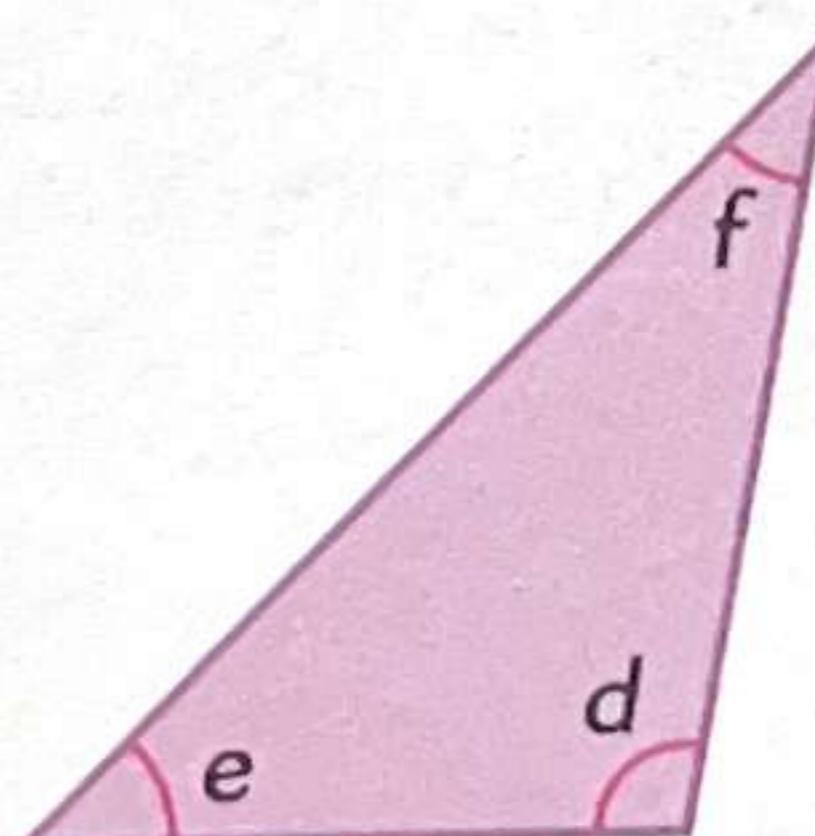
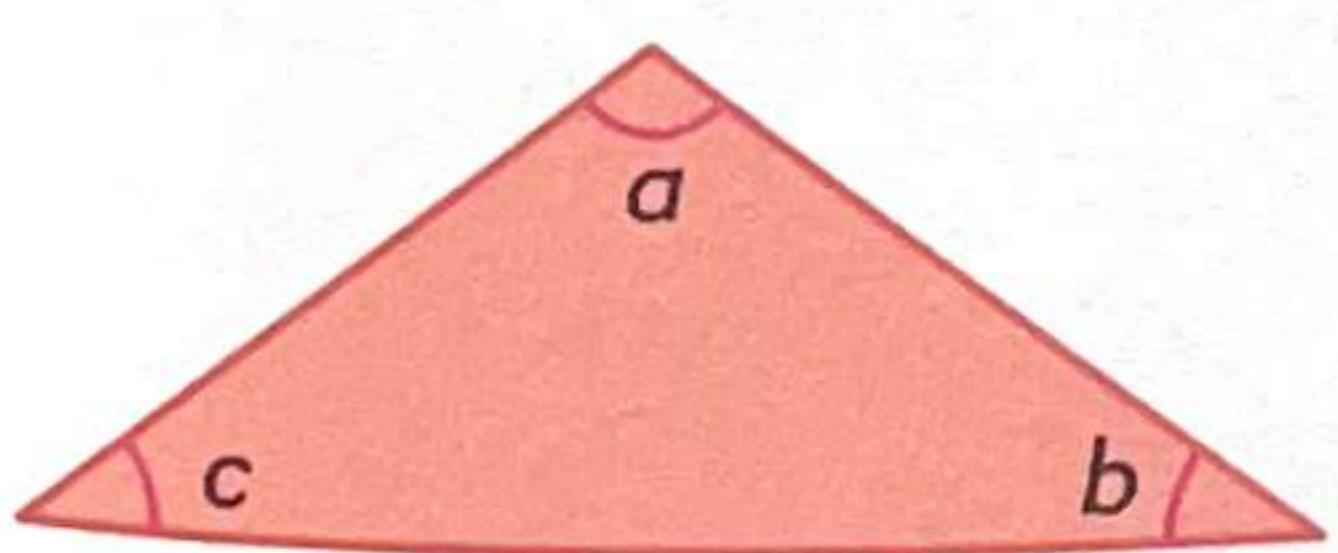
All the angles in the 3 triangles are **acute angles**.



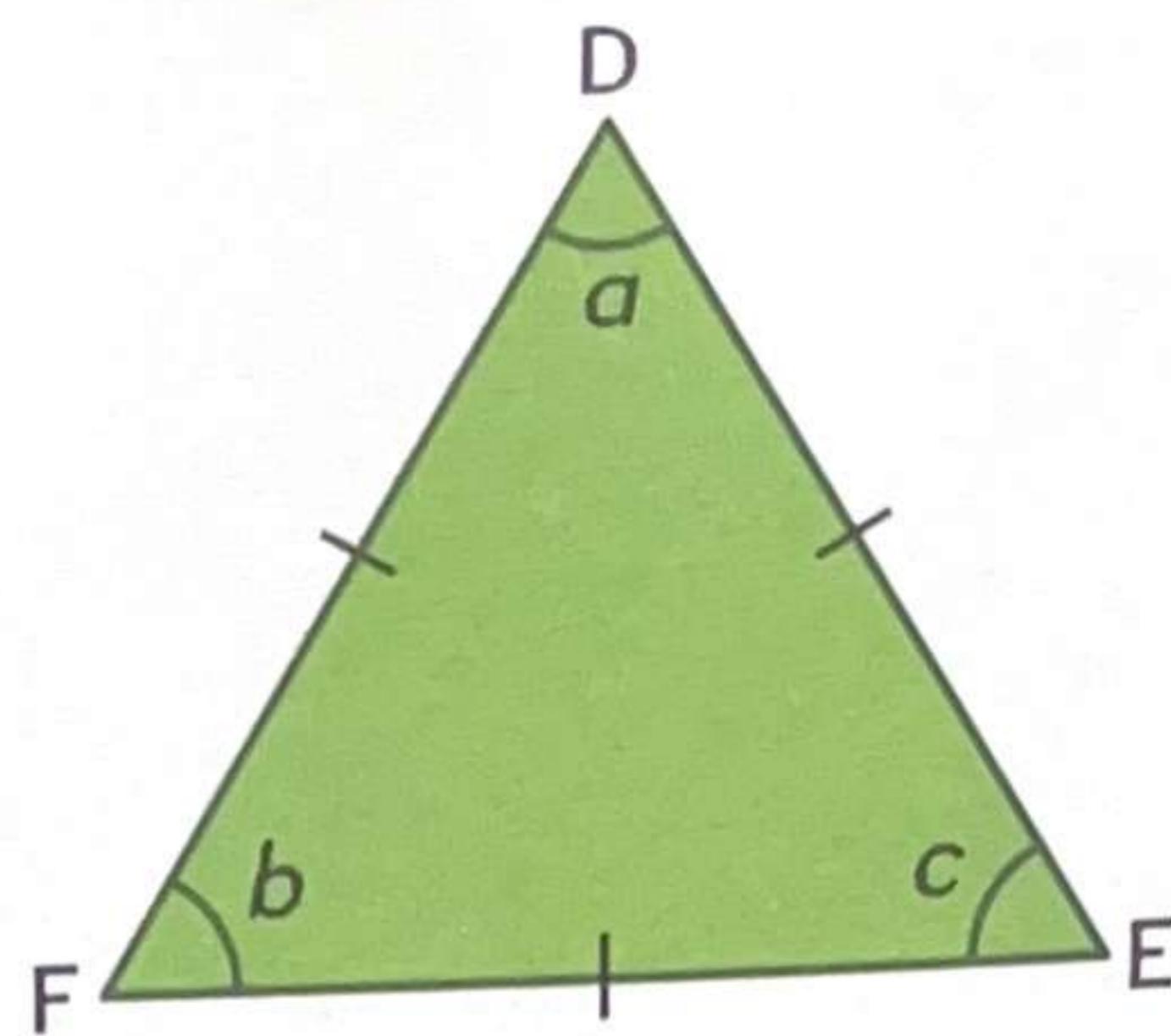
These are **obtuse-angled triangles**.

One of its angles is an **obtuse angle**.

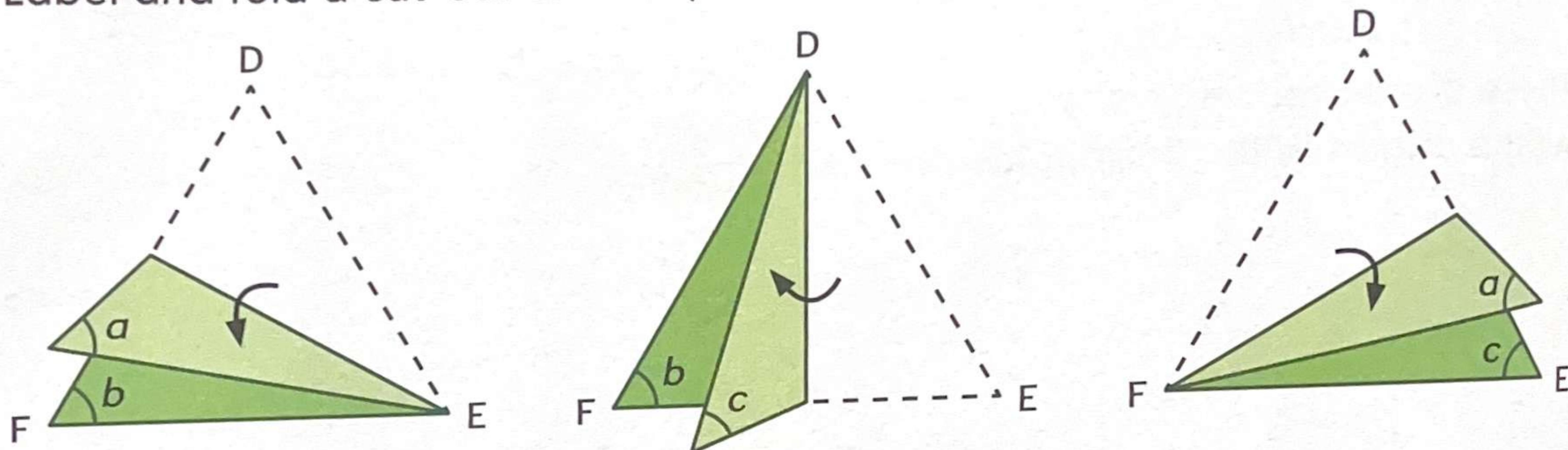
$\angle a$ ,  $\angle d$  and  $\angle g$  are obtuse angles.



This triangle is an **equilateral triangle**.  
An equilateral triangle has **3 equal sides** and **3 equal angles**.



Label and fold a cut-out of an equilateral triangle in the following 3 ways.



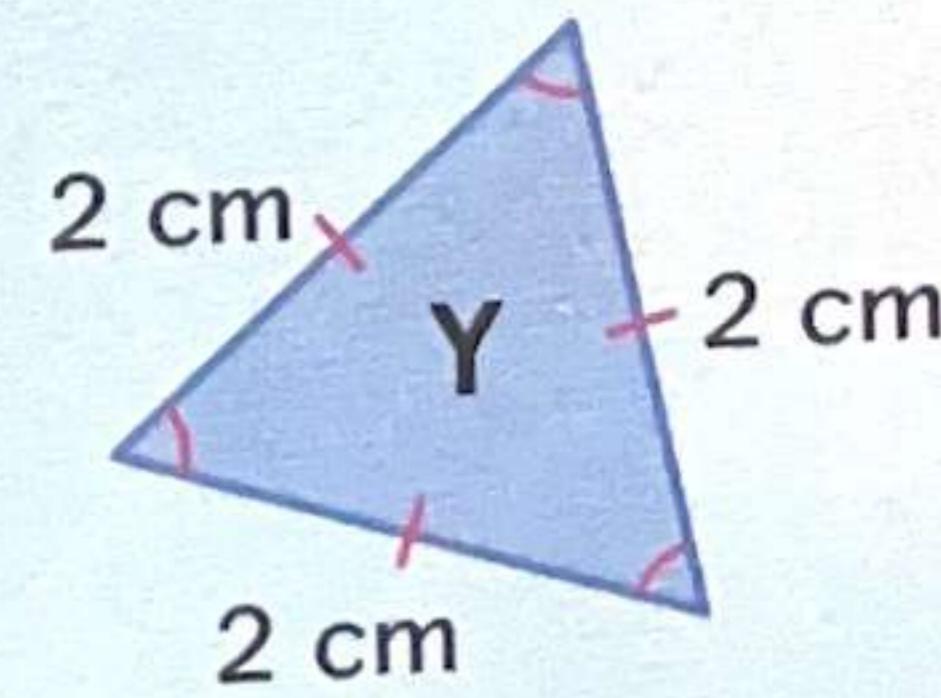
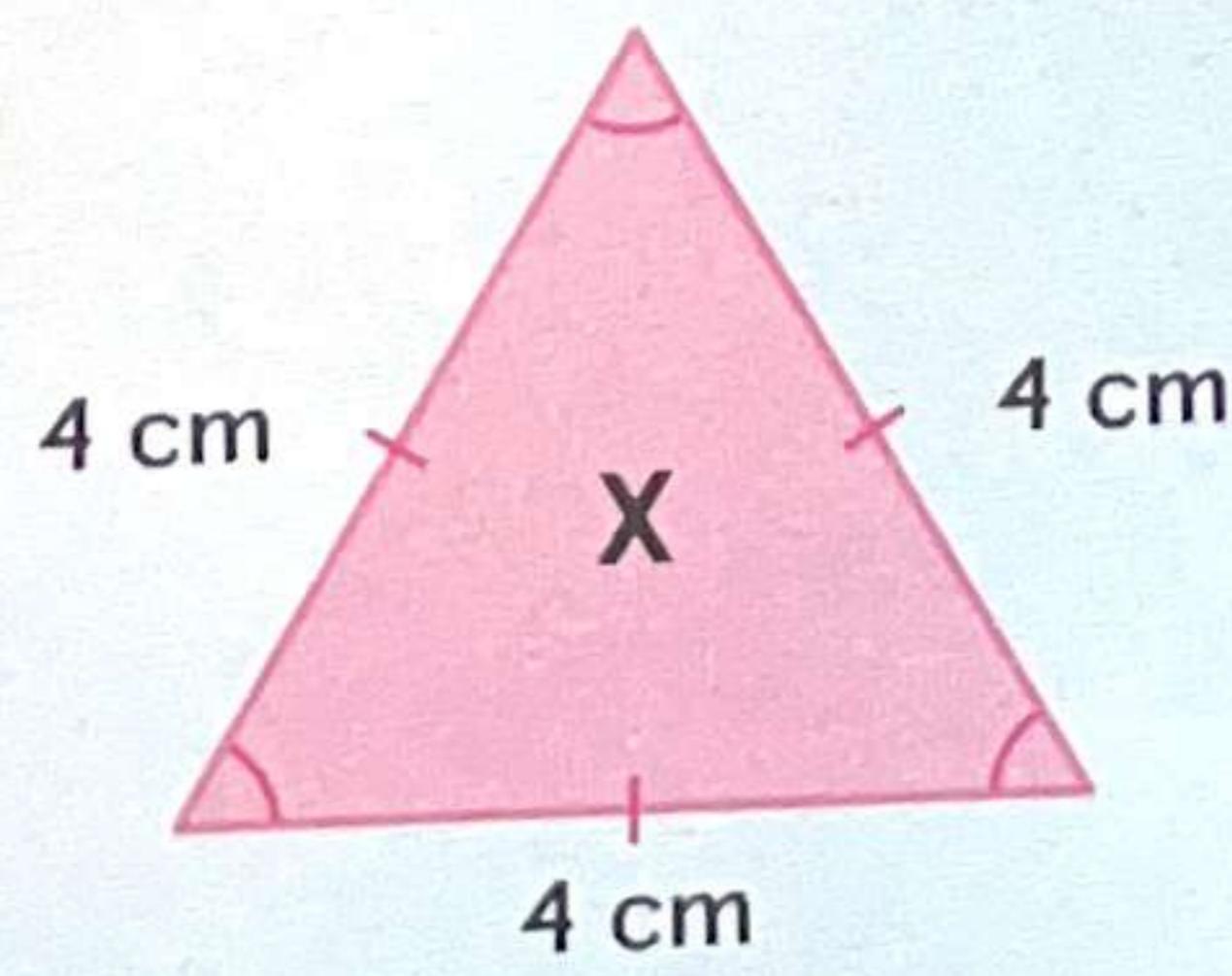
Observe the 3 angles.

$$\angle a = \angle b = \angle c = 60^\circ$$

Each angle in an equilateral triangle is **60°**.

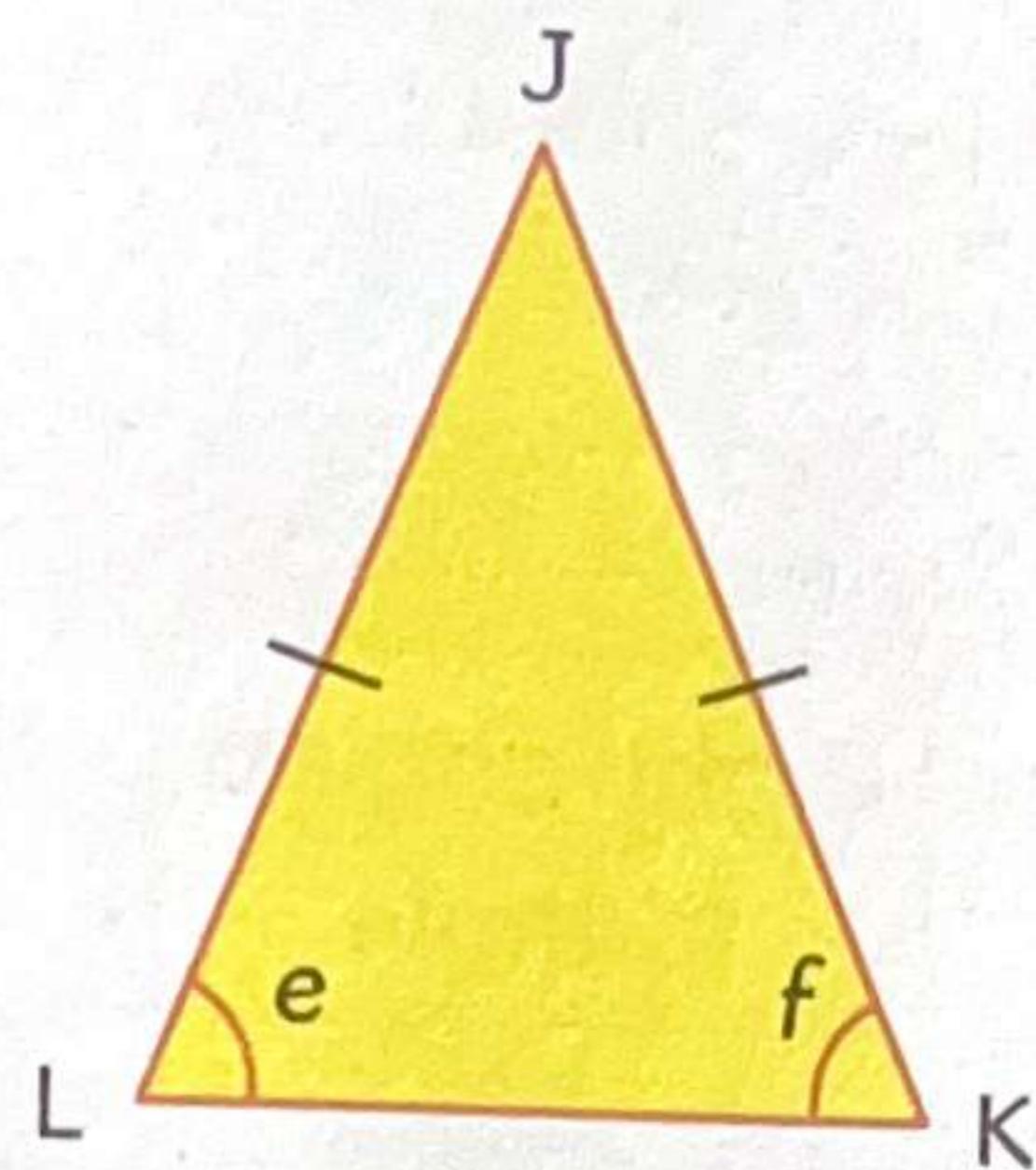
### Math Talk

Triangle Y is smaller than Triangle X.  
Are the angles in Triangle Y smaller than the angles in Triangle X?

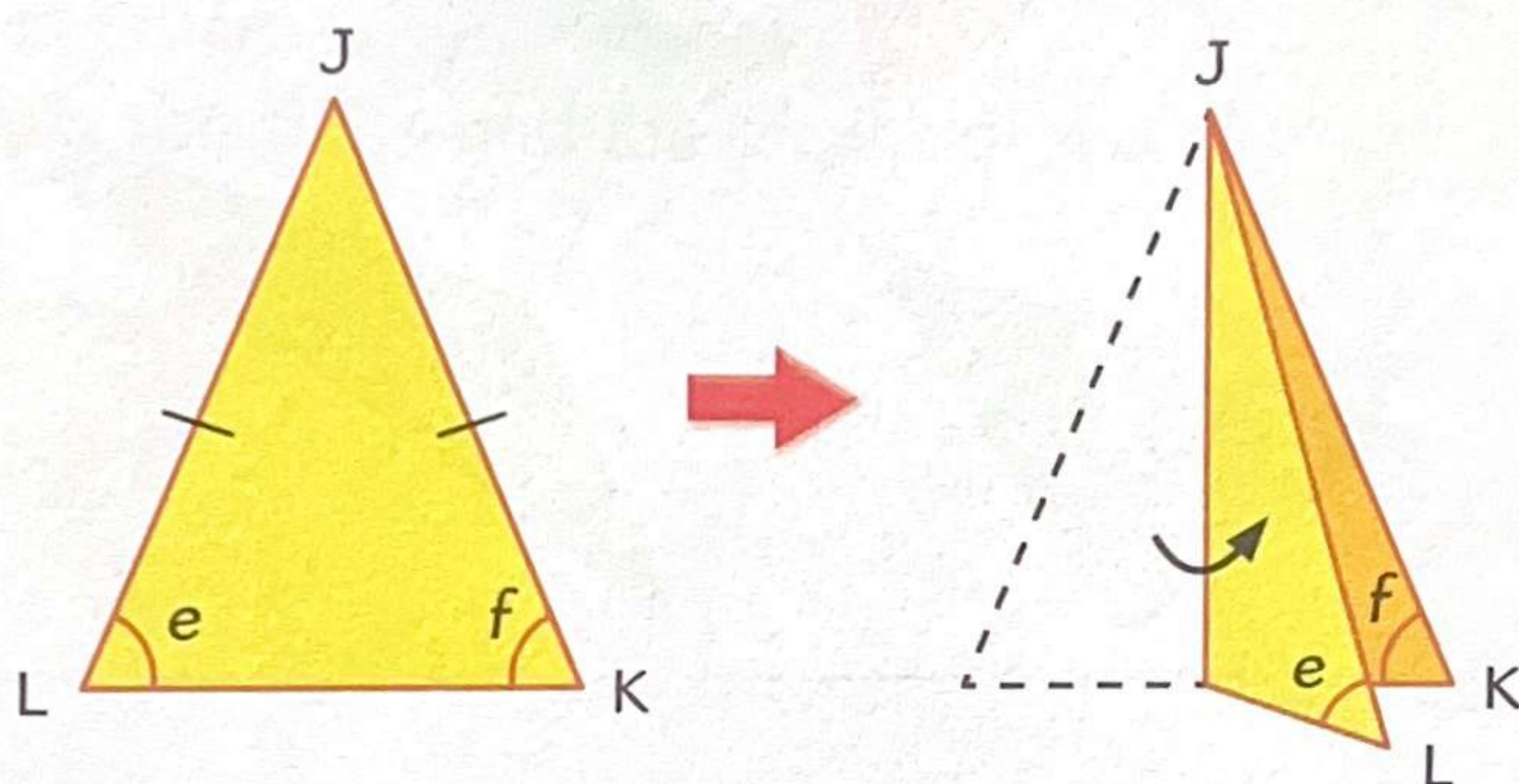


This triangle is an **isosceles triangle**.

An isosceles triangle has **two sides equal in length**.



Label and fold a cut-out of an isosceles triangle in half as shown.



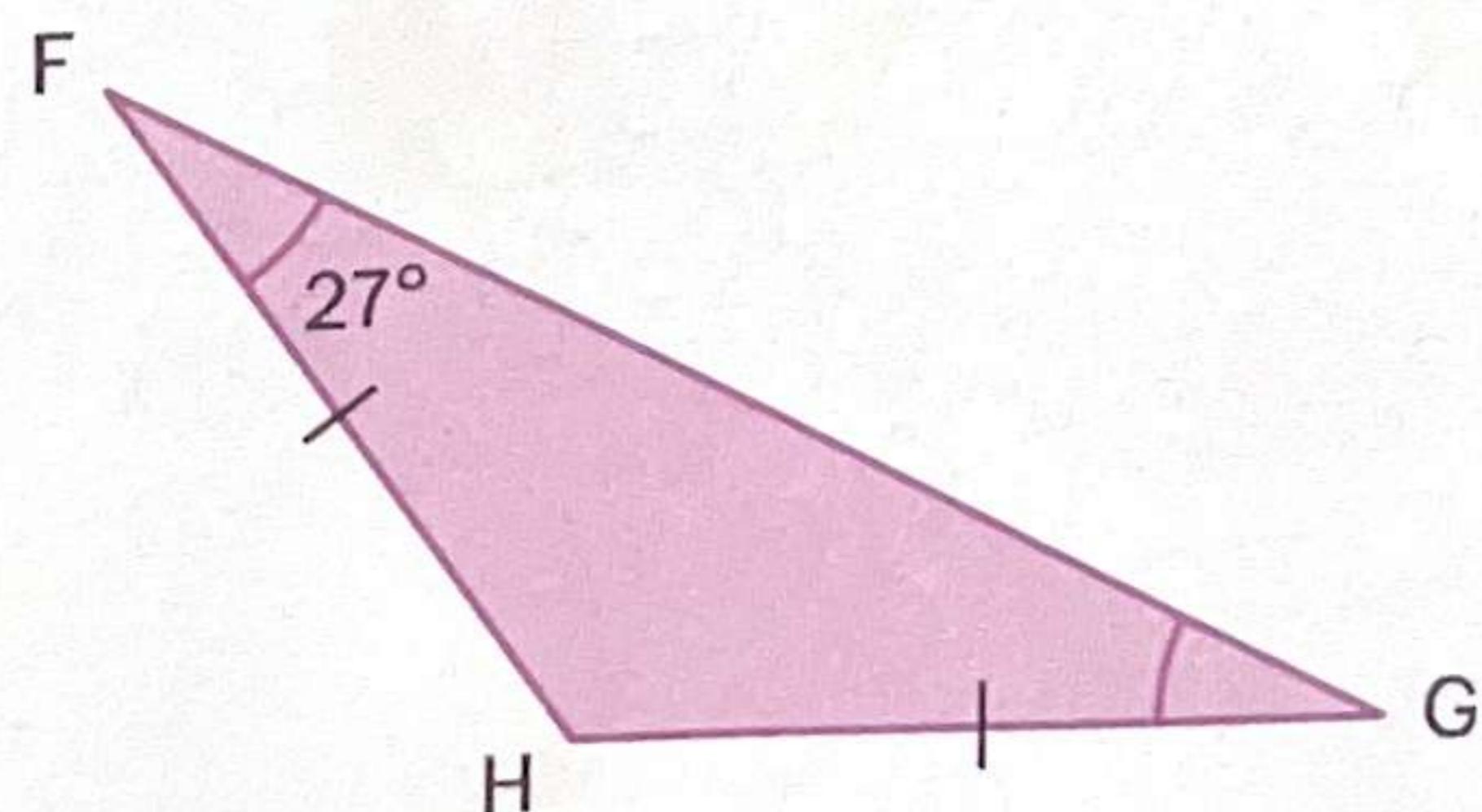
Observe the 2 angles.

$$\angle e = \angle f$$

The angles opposite the equal sides are equal.

**The base angles of an isosceles triangle are equal.**

FGH is an isosceles triangle. Find  $\angle FGH$ .

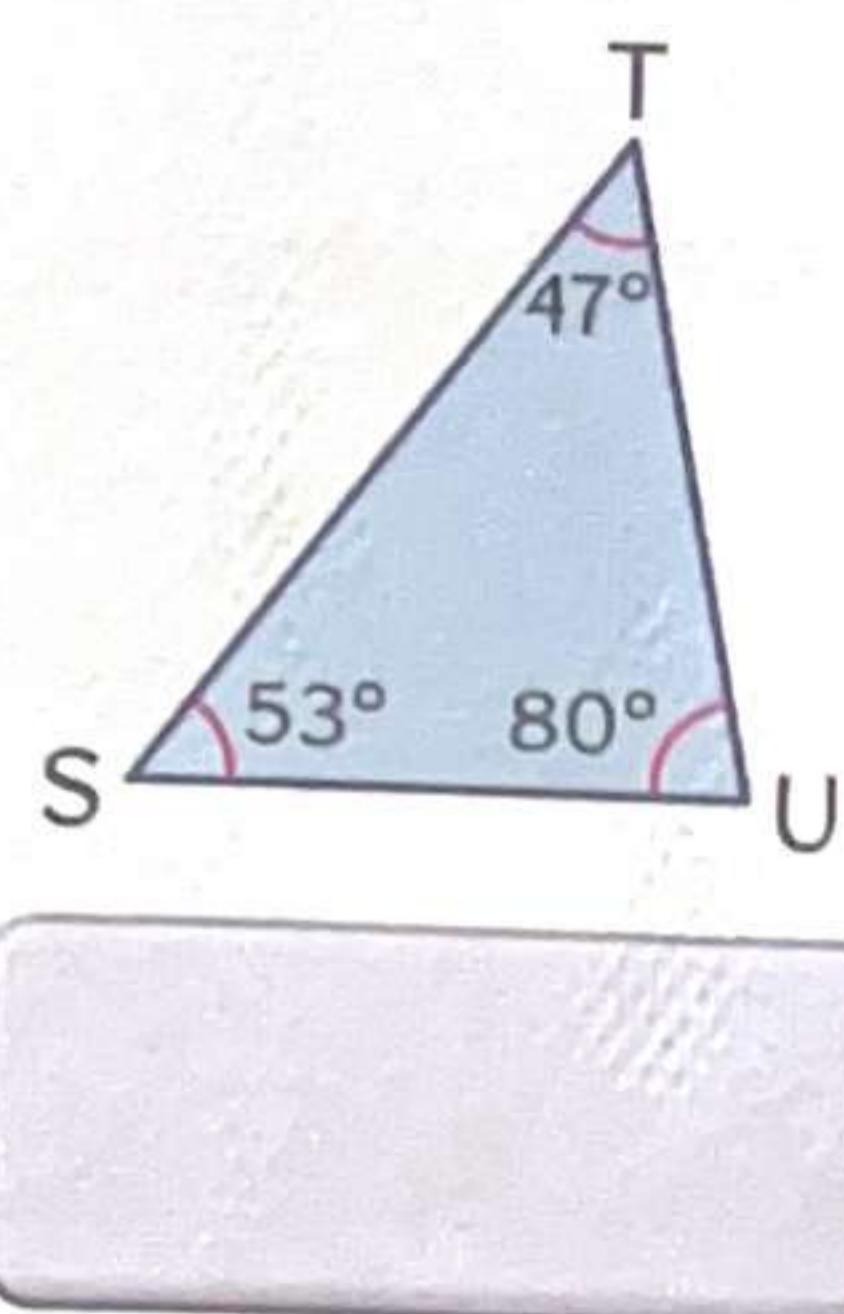


$$\begin{aligned}\angle FGH &= \angle HFG \\ &= 27^\circ\end{aligned}$$

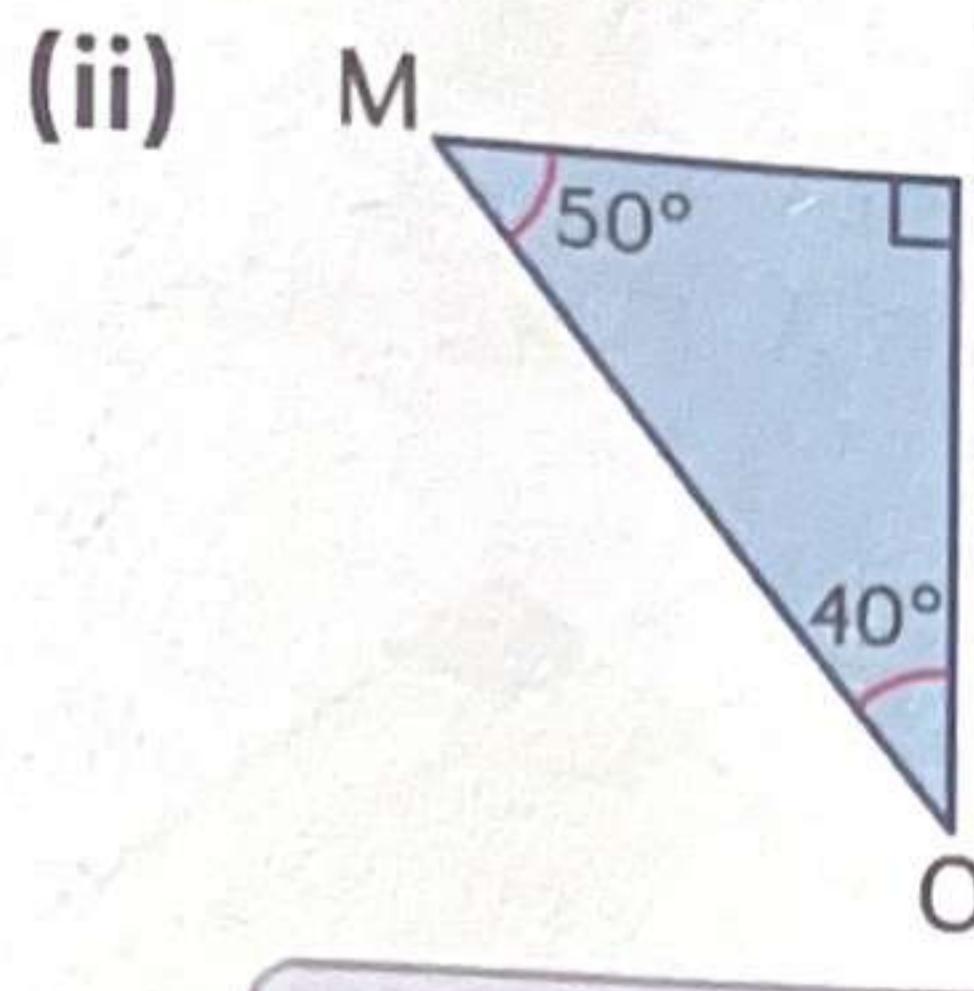
Let's Try  
1

(a) Name the types of triangles.

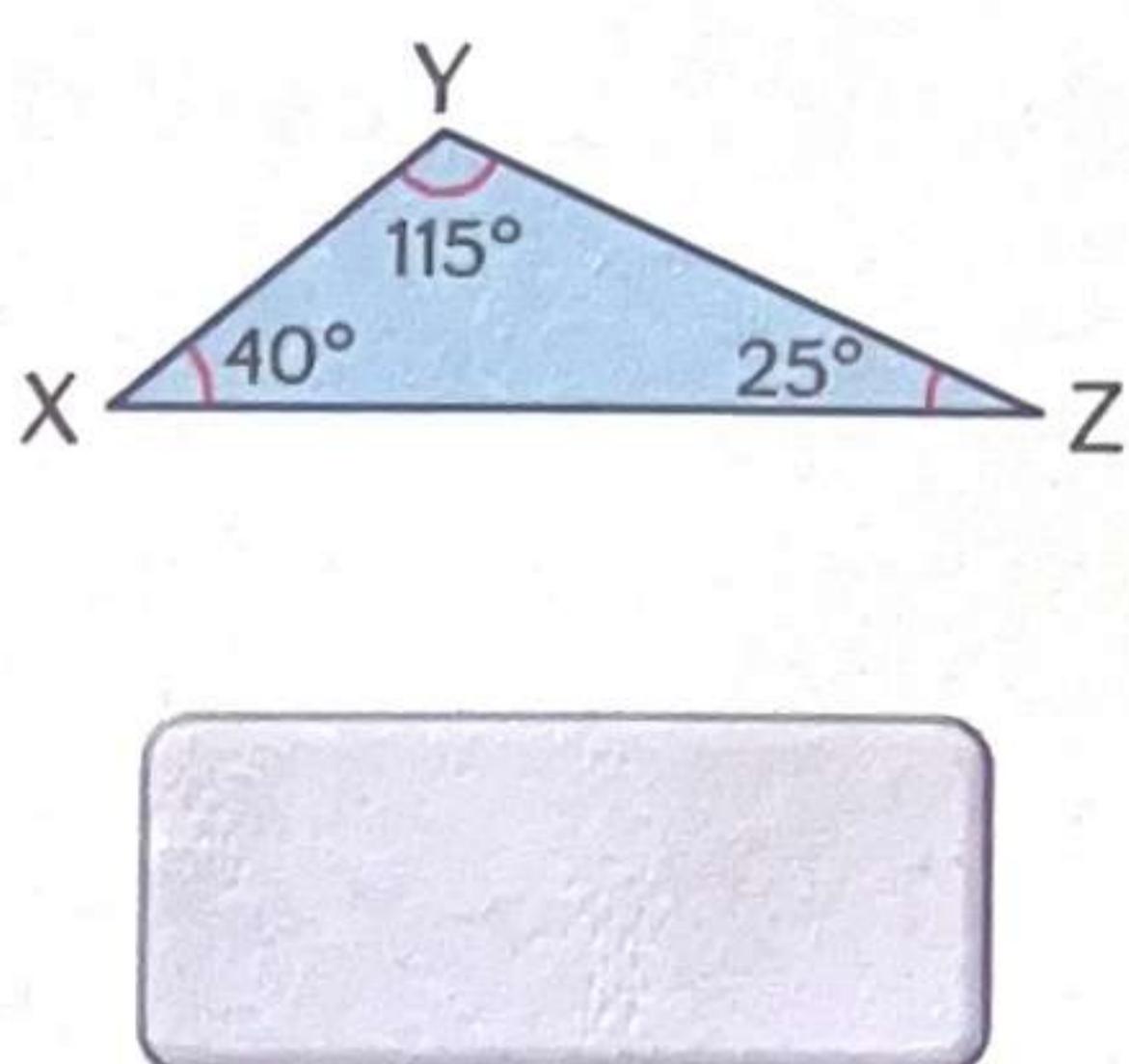
(i)



(ii)

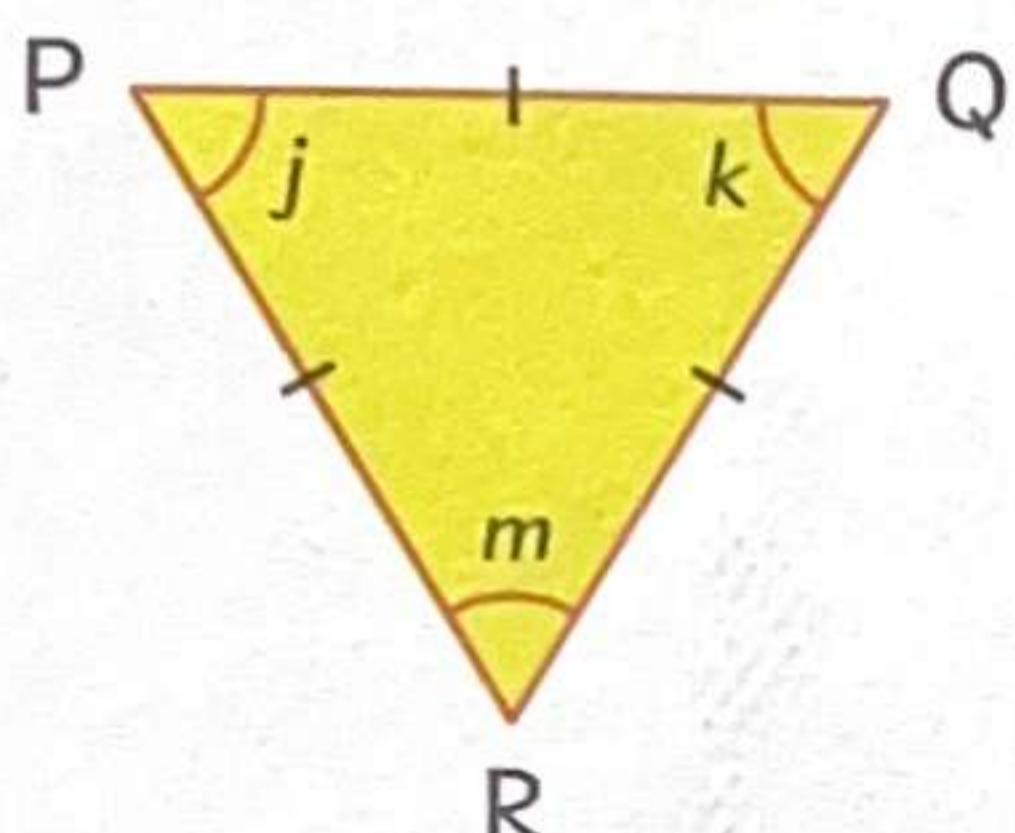


(iii)



(b) PQR is an equilateral triangle.

Identify the sides and the angles of the triangle.



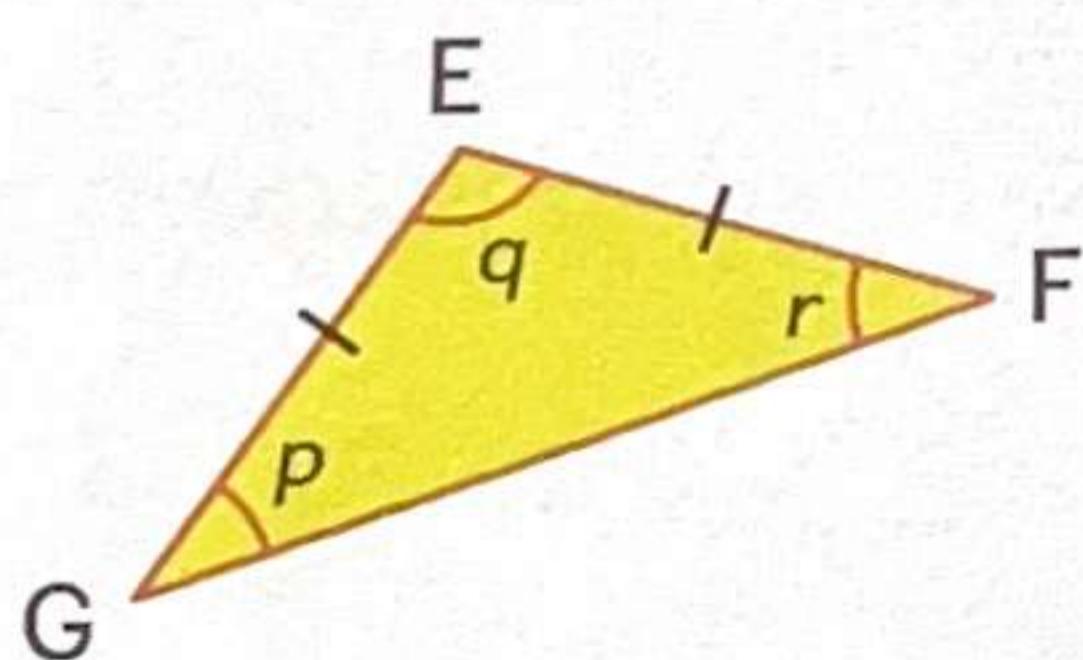
$$PQ = \boxed{\quad} = \boxed{\quad}$$

$$\angle j = \angle k = \angle \boxed{\quad}$$

$$= \boxed{\quad}^\circ$$

(c) EFG is an isosceles triangle.

Identify the sides and the angles of the triangle.

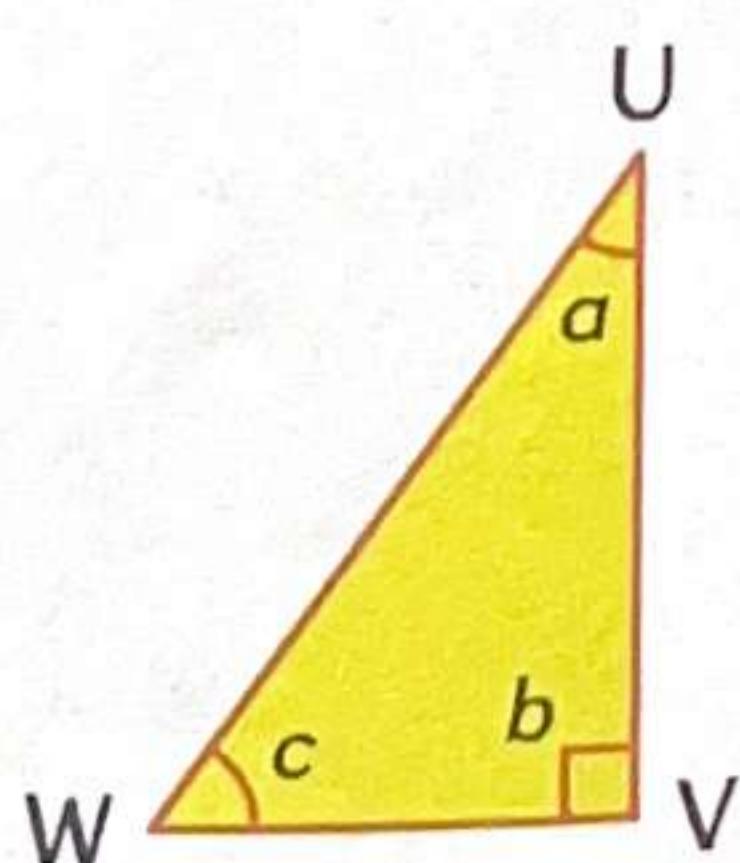


$$\angle p = \angle \boxed{\quad}$$

$$EG = \boxed{\quad}$$

(d) UVW is a right-angled triangle.

Which angle is equal to  $90^\circ$ ?



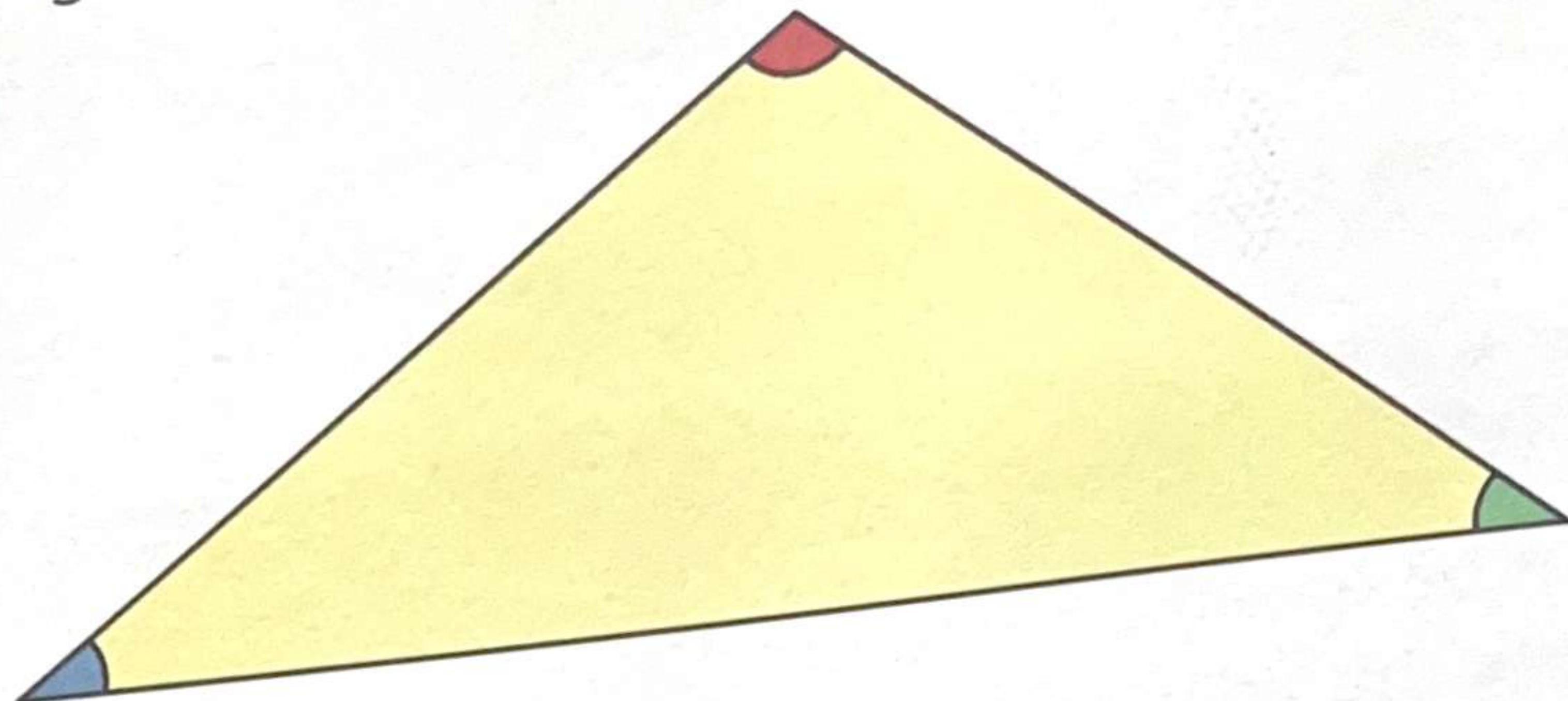
$$\angle \boxed{\quad} = 90^\circ$$



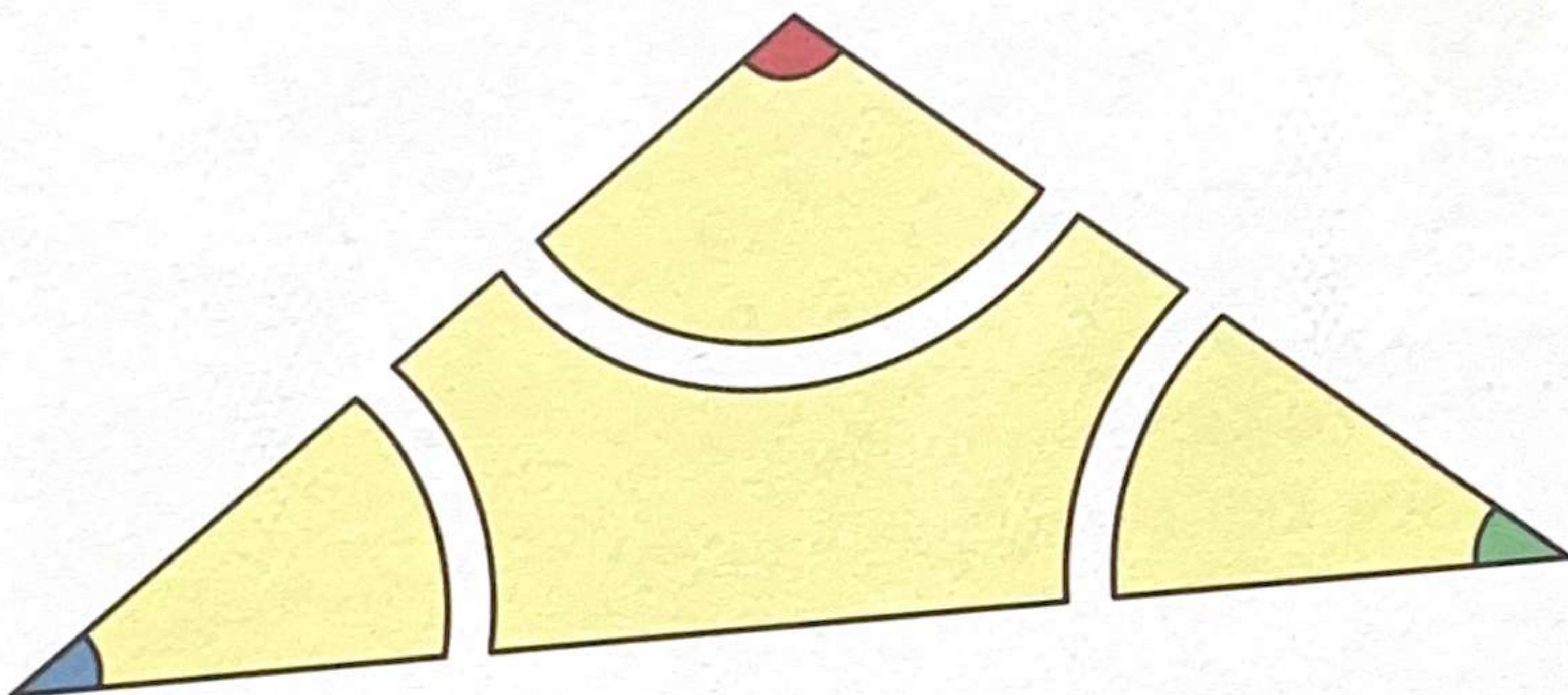
# Angle Sum of a Triangle

This is an obtuse-angled triangle.

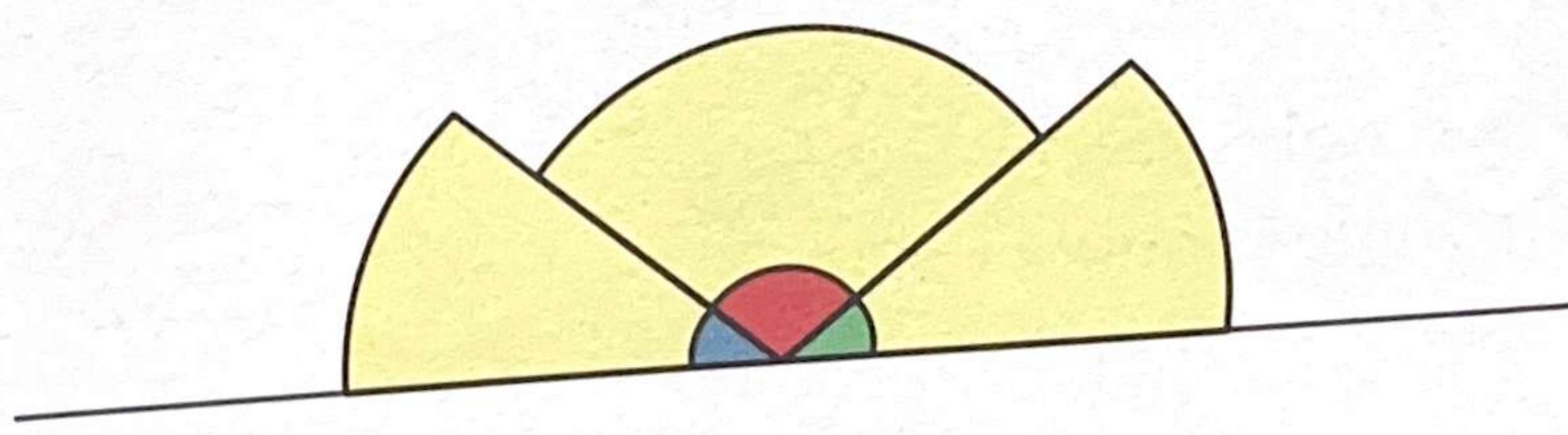
Colour the 3 angles of a triangle cut-out using different colours.



Cut out the 3 angles as shown.



Arrange the 3 angles as shown.



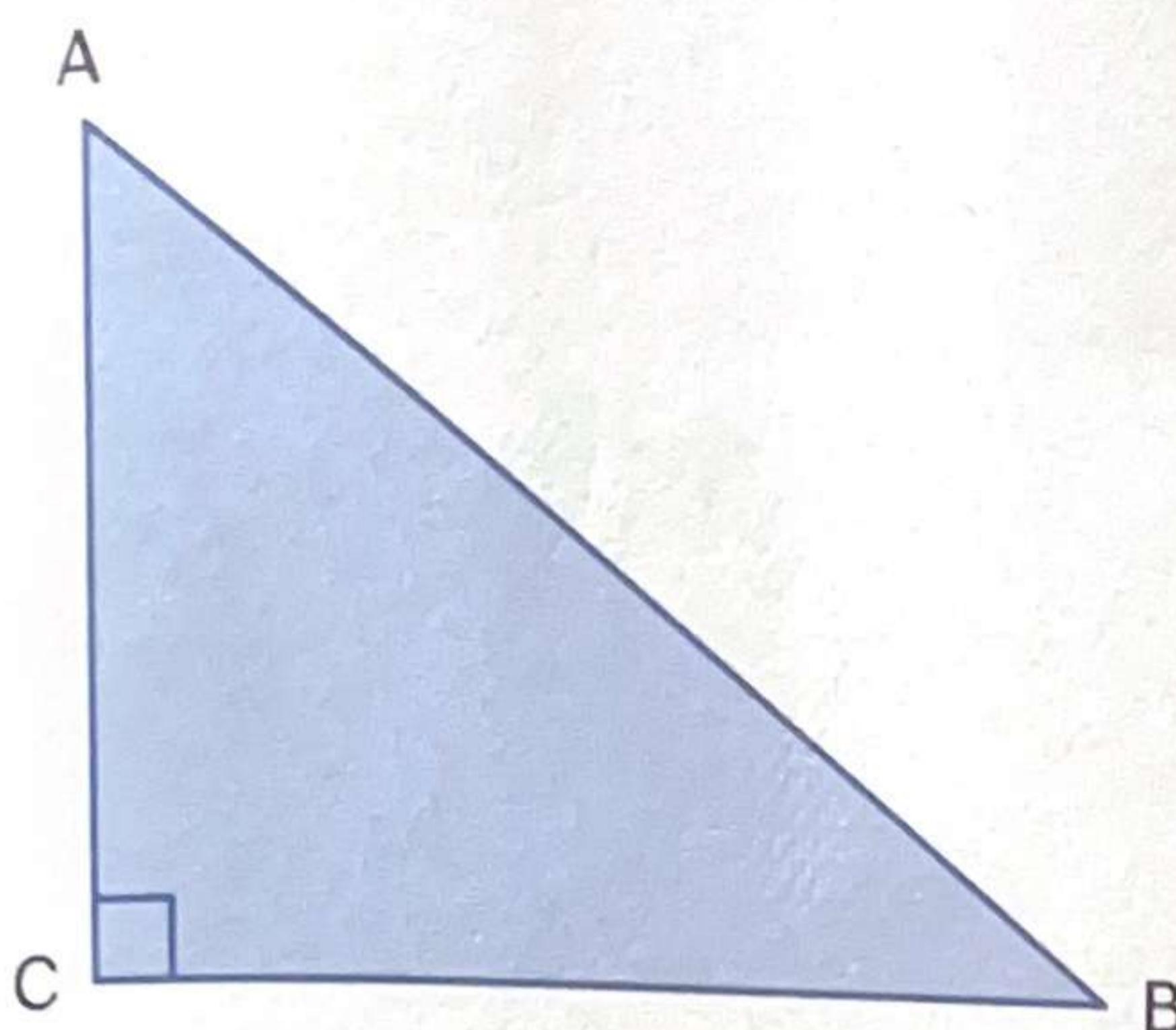
The 3 angles form angles on a straight line. The sum of angles on a straight line is  $180^\circ$ .



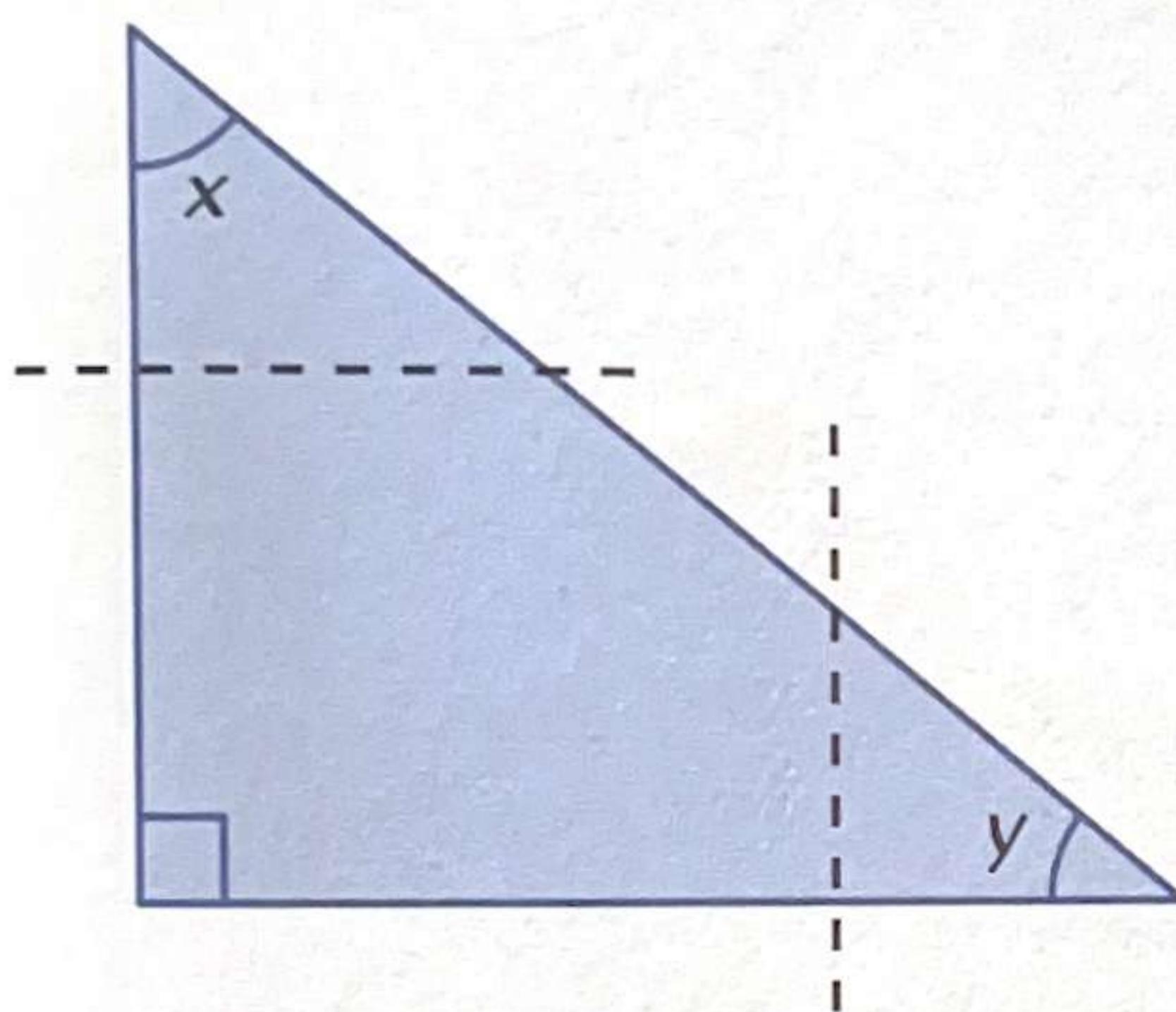
The **sum of angles in a triangle is  $180^\circ$** .



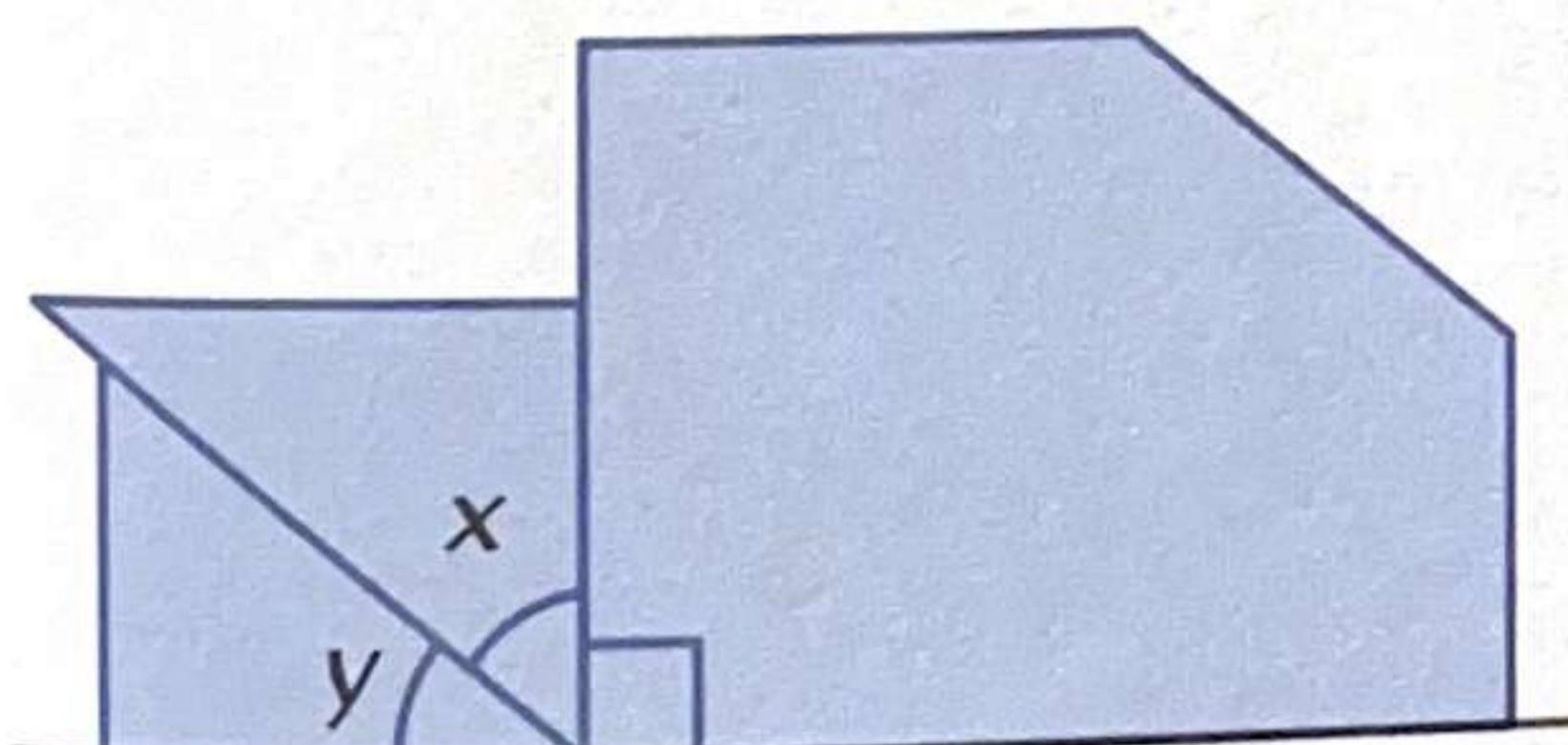
This is a right-angled triangle.



Cut the triangle along the dotted lines as shown.



Arrange and observe the 3 angles as shown.

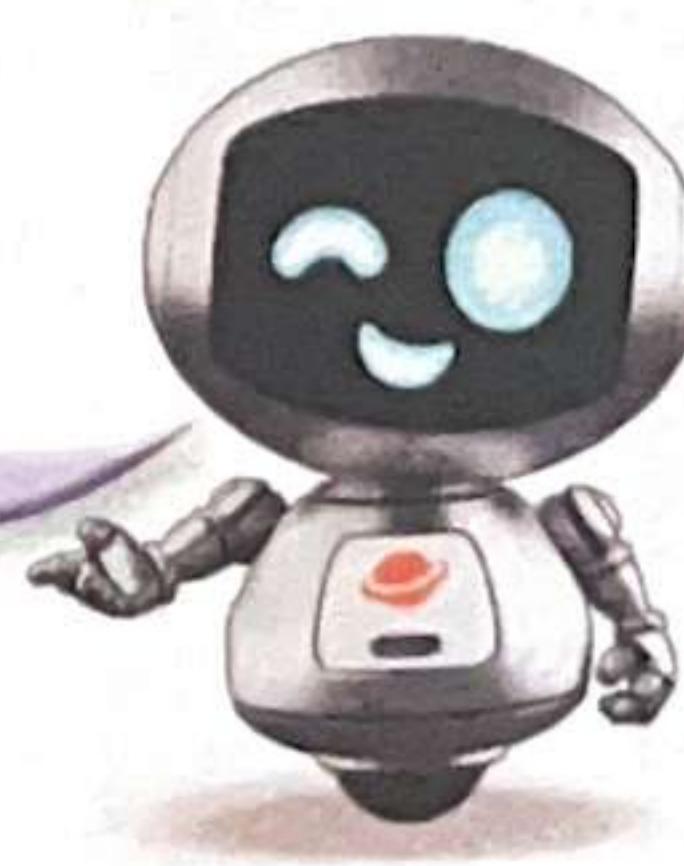


$$\angle x + \angle y + 90^\circ = 180^\circ$$

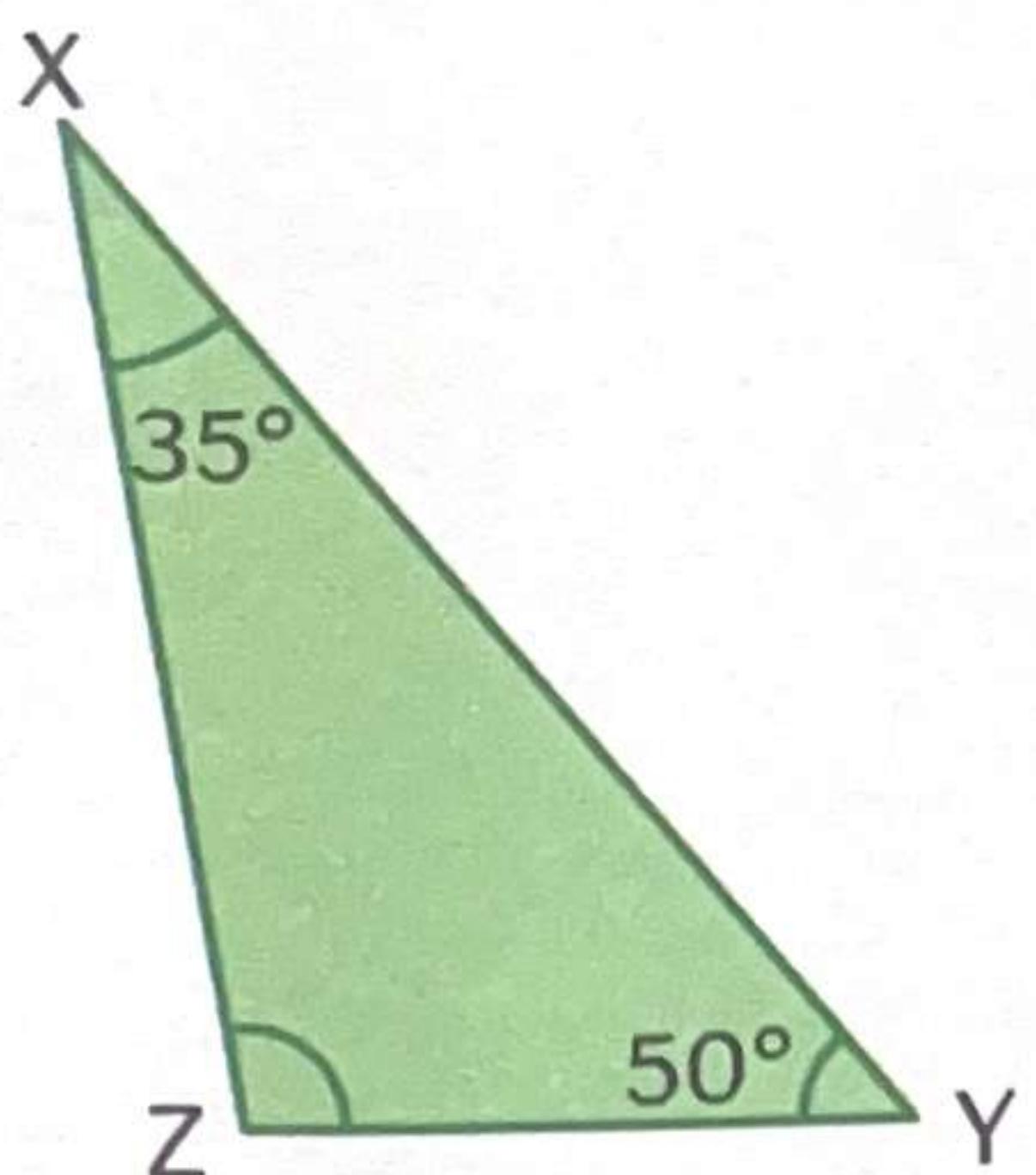
The sum of the angles in a triangle is  $180^\circ$ .



What can we say about the sum of the two acute angles in a right-angled triangle?



Find  $\angle XZY$ .

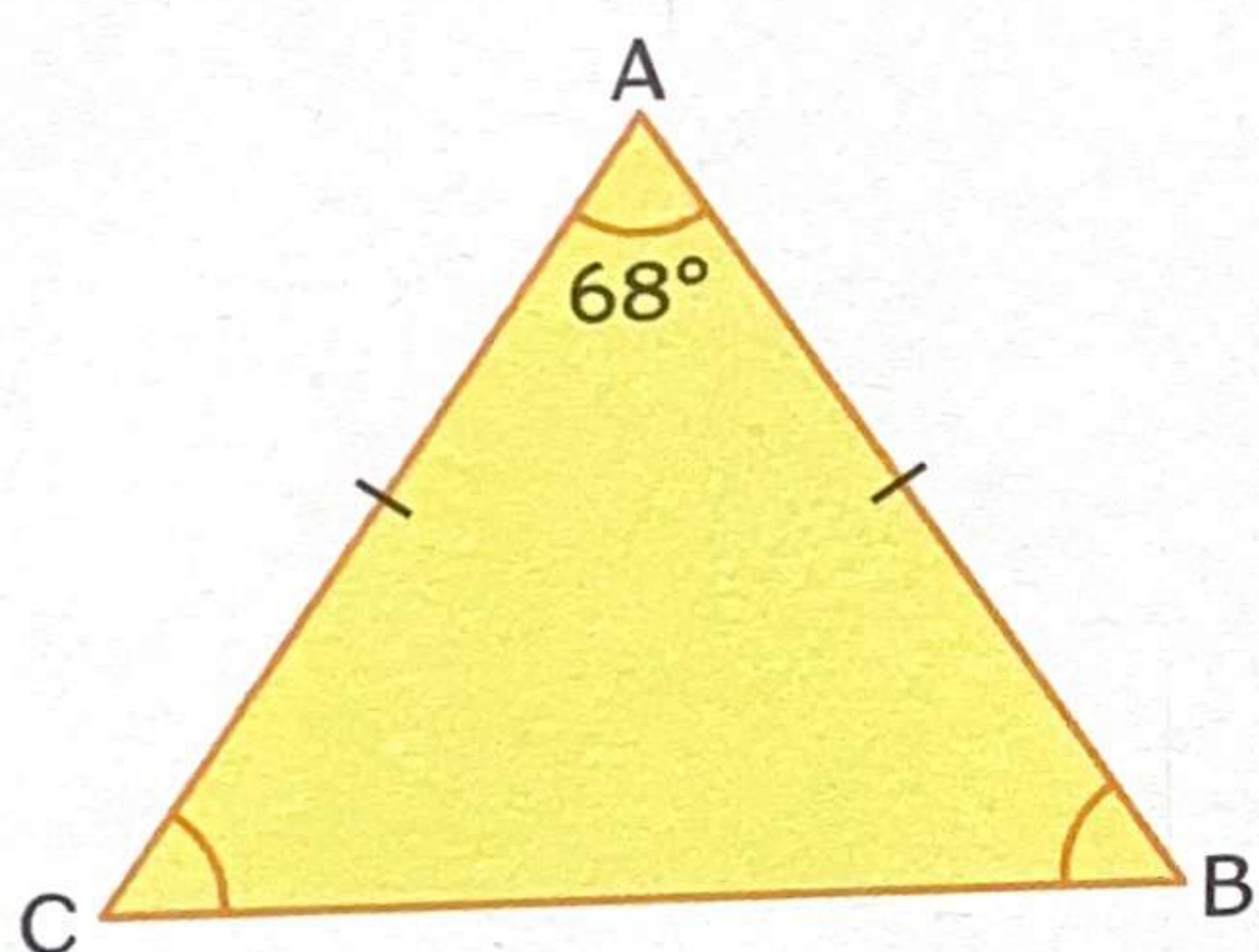


$$35^\circ + 50^\circ + \angle XZY = 180^\circ$$



$$\begin{aligned}\angle XZY &= 180^\circ - 35^\circ - 50^\circ \\ &= 95^\circ\end{aligned}$$

ABC is an isosceles triangle. Find  $\angle ACB$ .



In an isosceles triangle, the base angles that are opposite the two equal sides are equal.

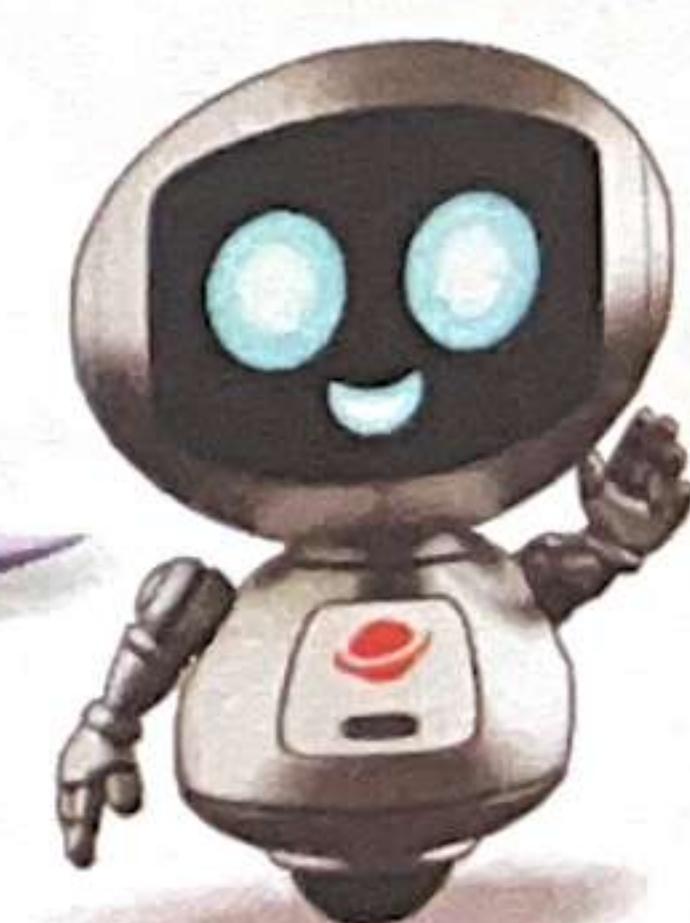
$$\angle ACB = \angle ABC$$

$$\begin{aligned}\angle ACB + \angle ABC &= 180^\circ - 68^\circ \\ &= 112^\circ\end{aligned}$$

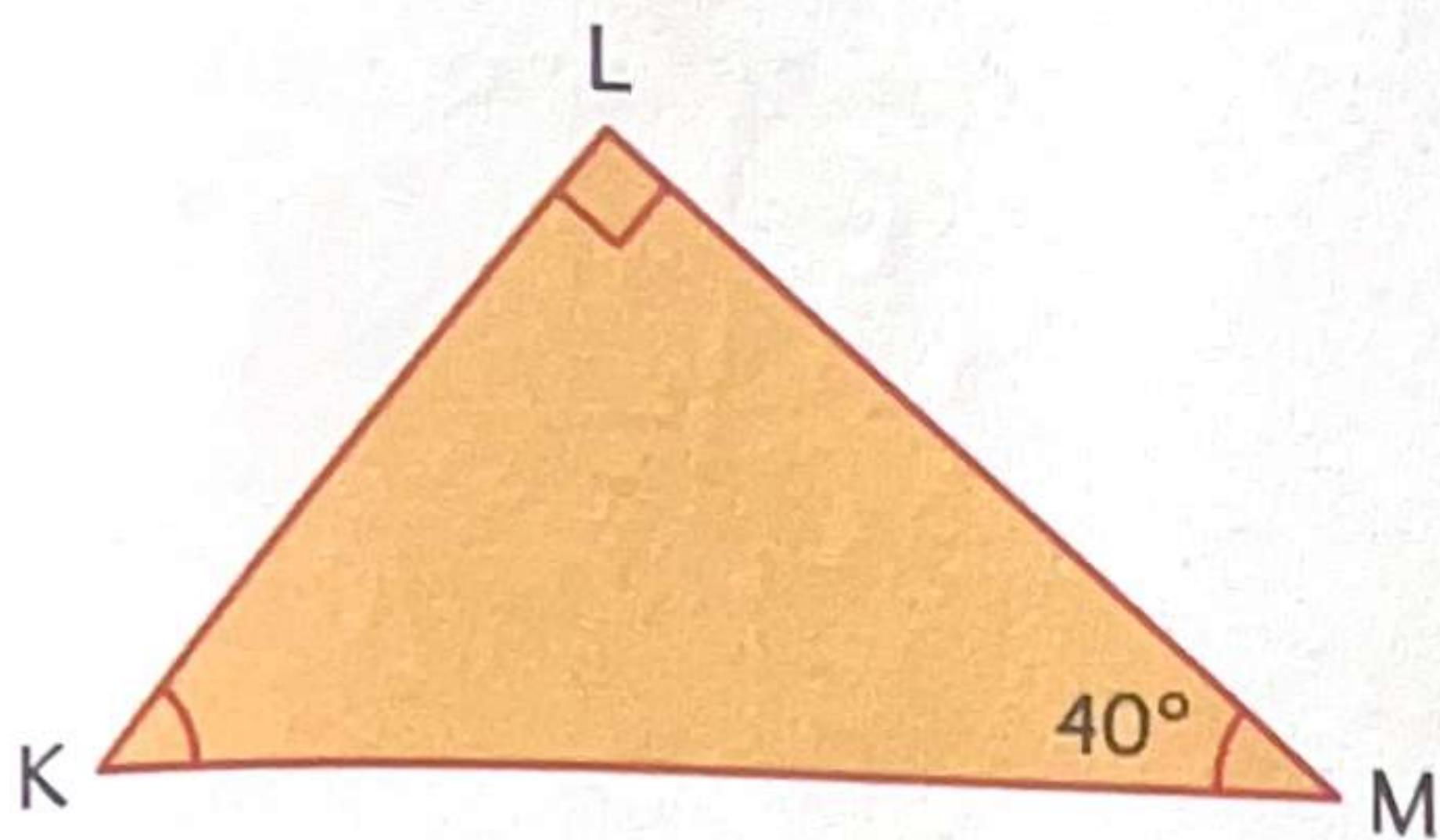
$$\begin{aligned}\angle ACB &= 112^\circ \div 2 \\ &= 56^\circ\end{aligned}$$



How can we use the sum of angles in a triangle to find the size of each angle in an equilateral triangle?



KLM is right-angled triangle.  $\angle LMK = 40^\circ$ .  
Find  $\angle MKL$ .



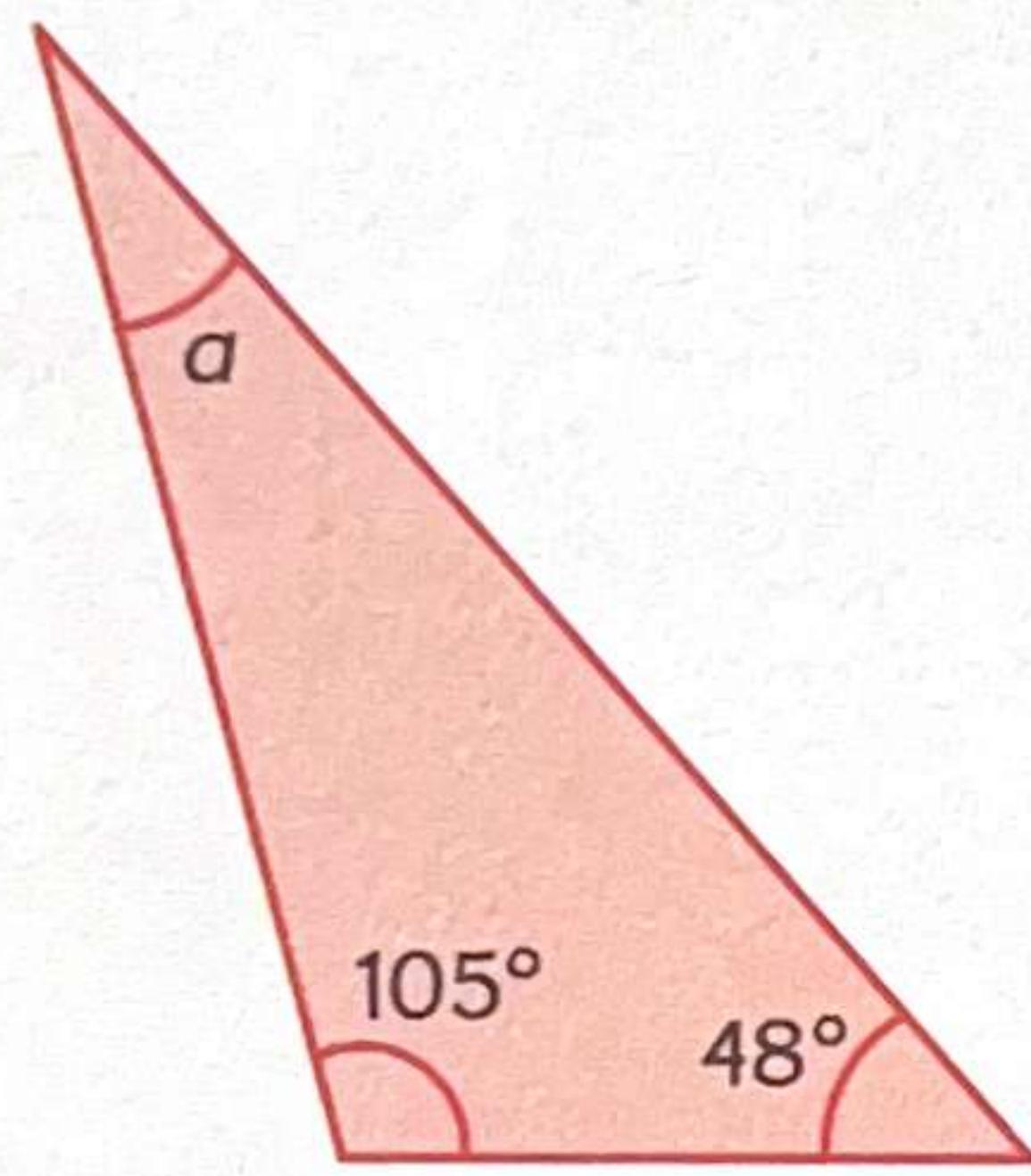
$$\begin{aligned}\angle MKL &= 180^\circ - 90^\circ - 40^\circ \\ &= 50^\circ\end{aligned}$$

### Let's Try!

2

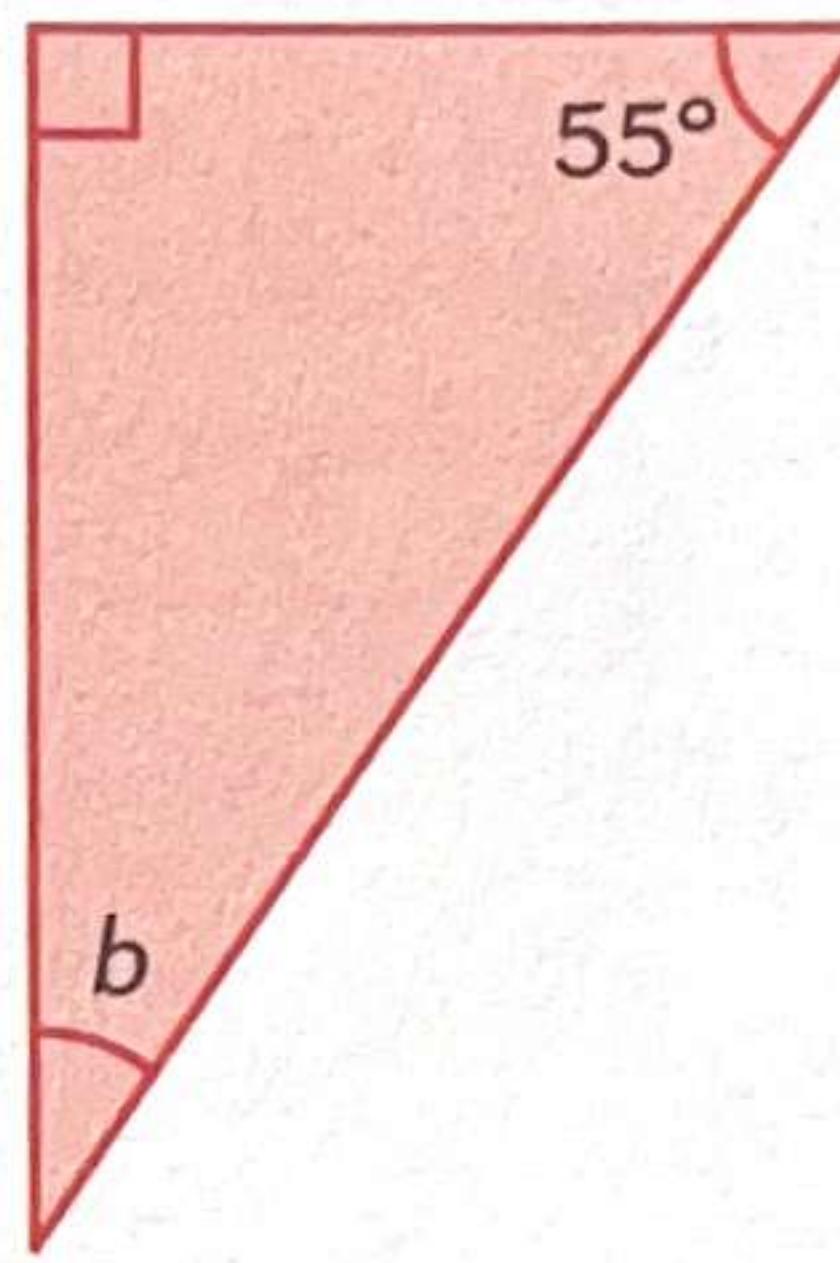
Find the unknown angle for each triangle.

(a)



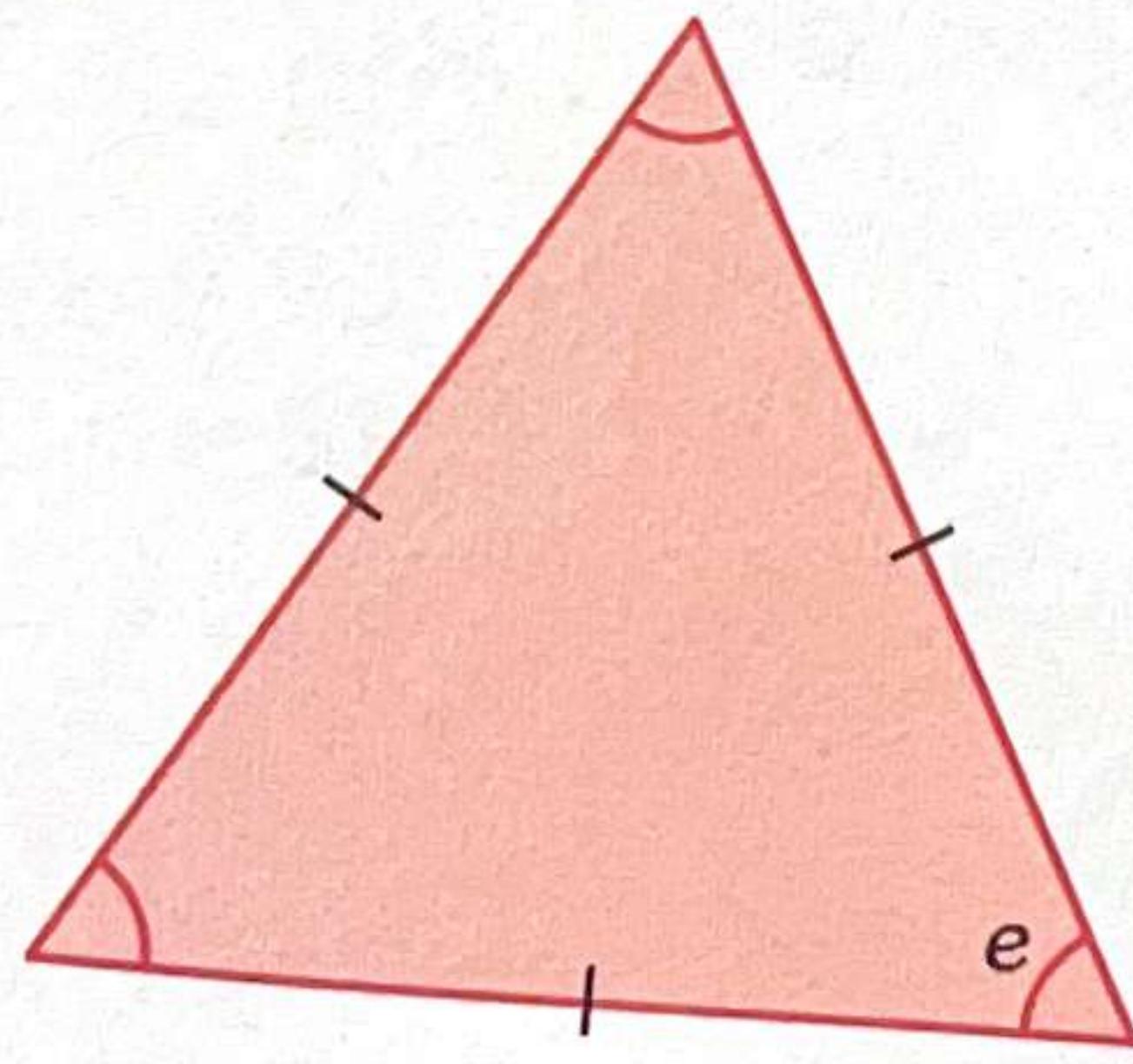
$$\angle a = \boxed{\phantom{00}}$$

(b)



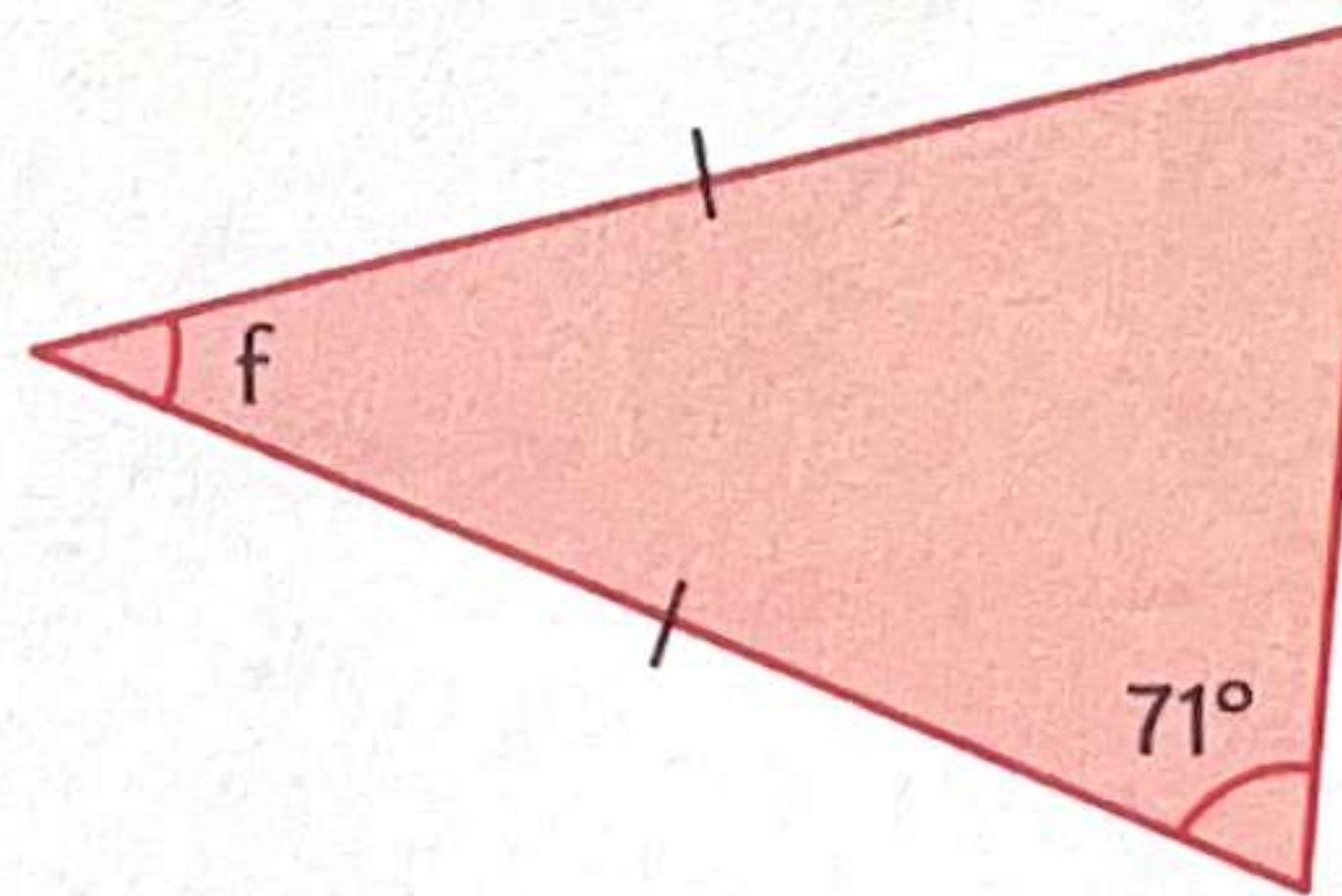
$$\angle b = \boxed{\phantom{00}}$$

(c)



$$\angle e = \boxed{\phantom{00}}$$

(d)



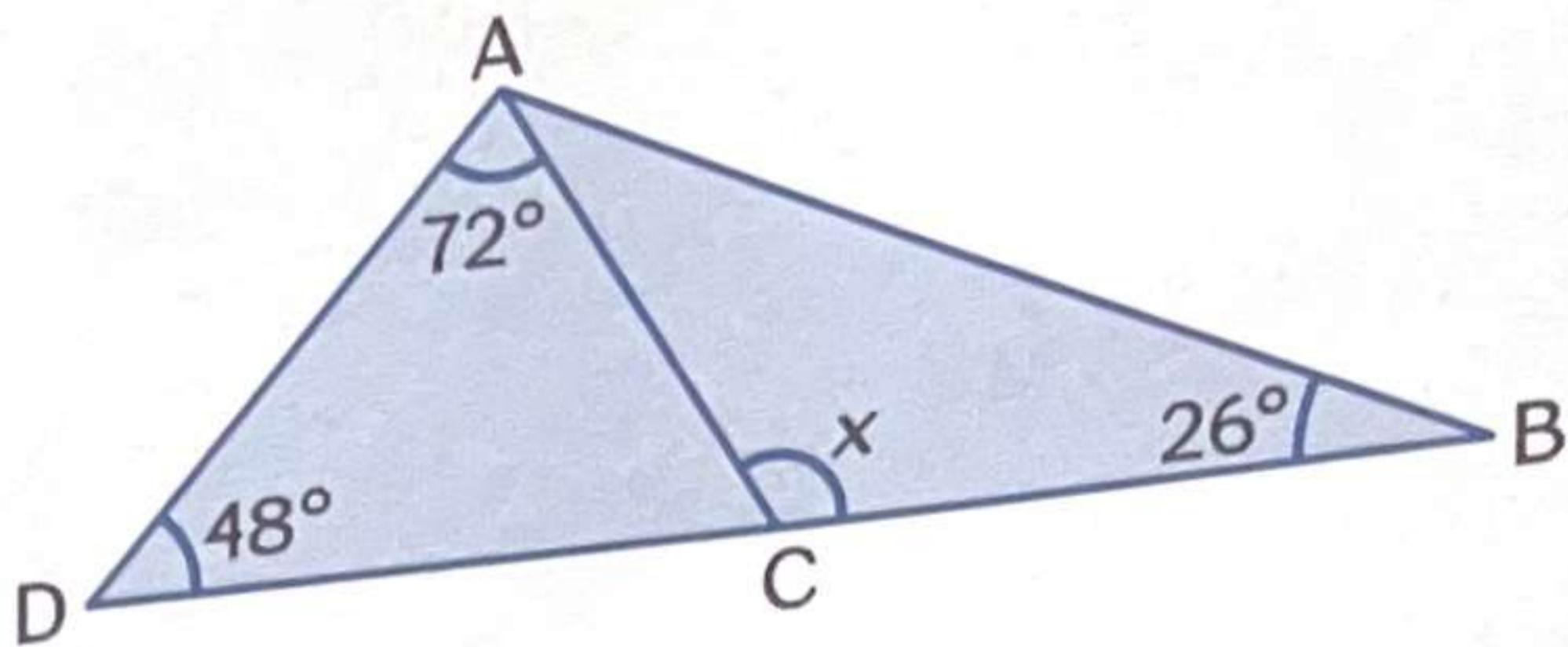
$$\angle f = \boxed{\phantom{00}}$$



# Finding Unknown Angles

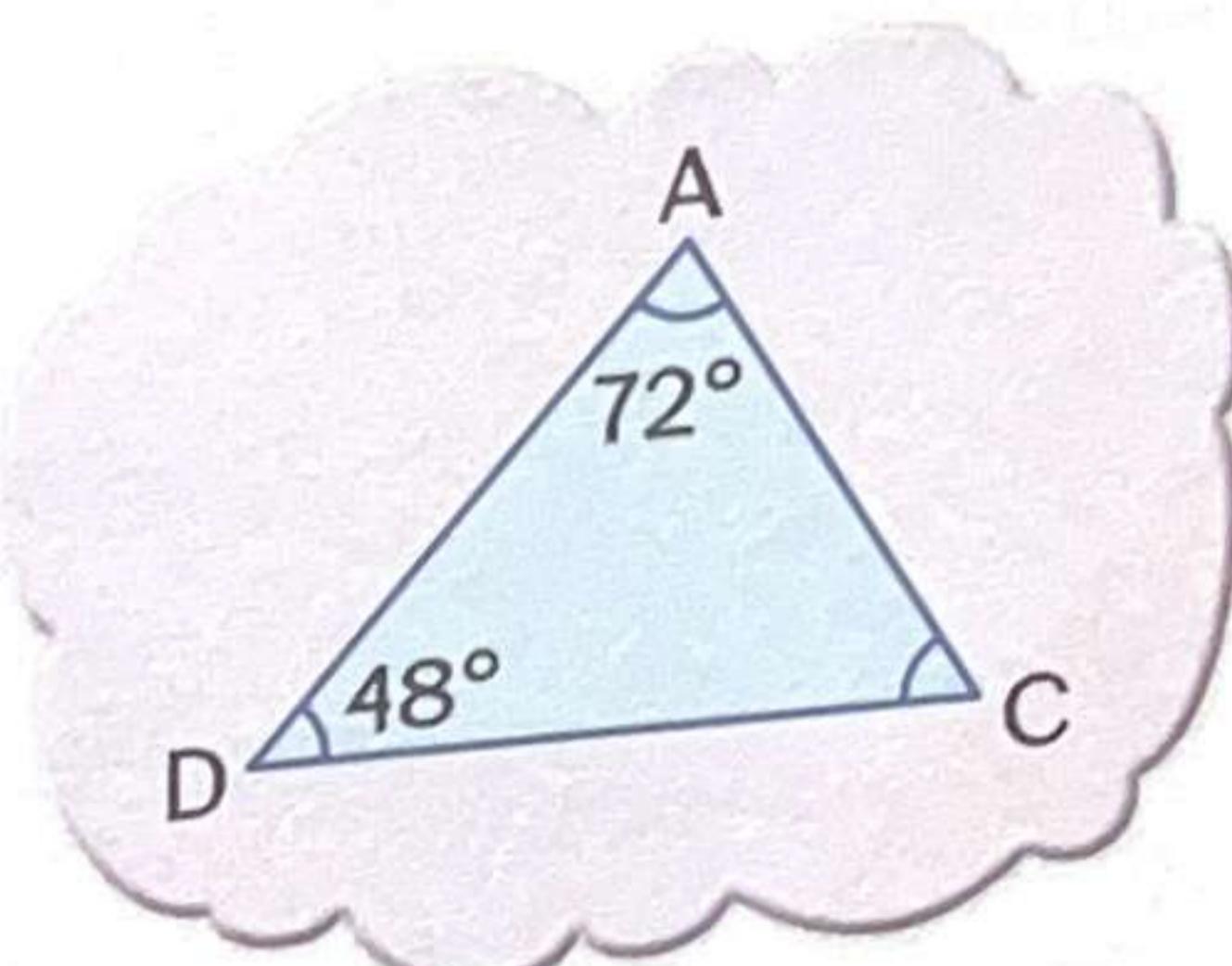
In the figure, BCD is a straight line.  $\angle DAC = 72^\circ$ ,  $\angle ADC = 48^\circ$  and  $\angle ABC = 26^\circ$ .

Find  $\angle x$ .



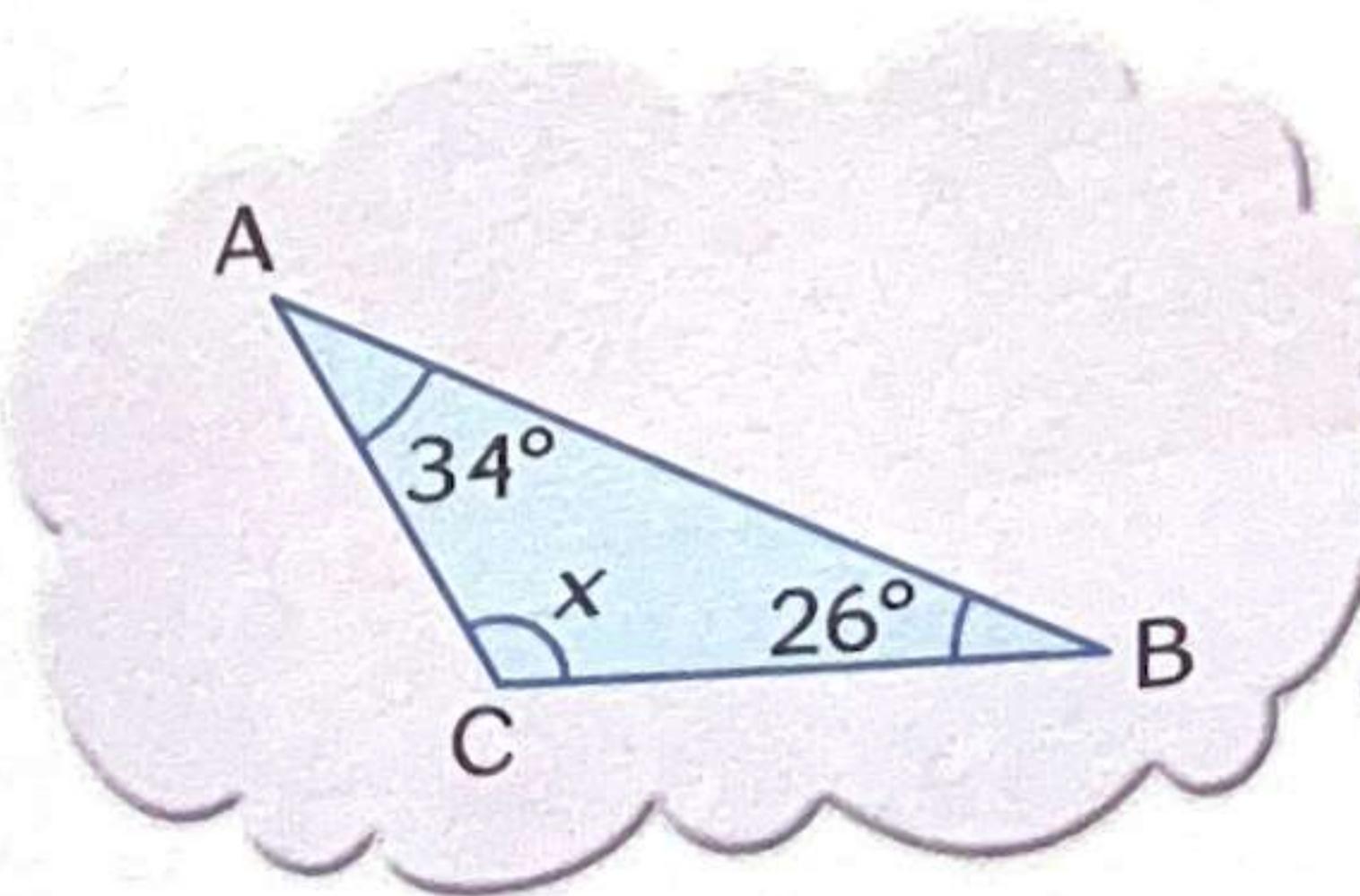
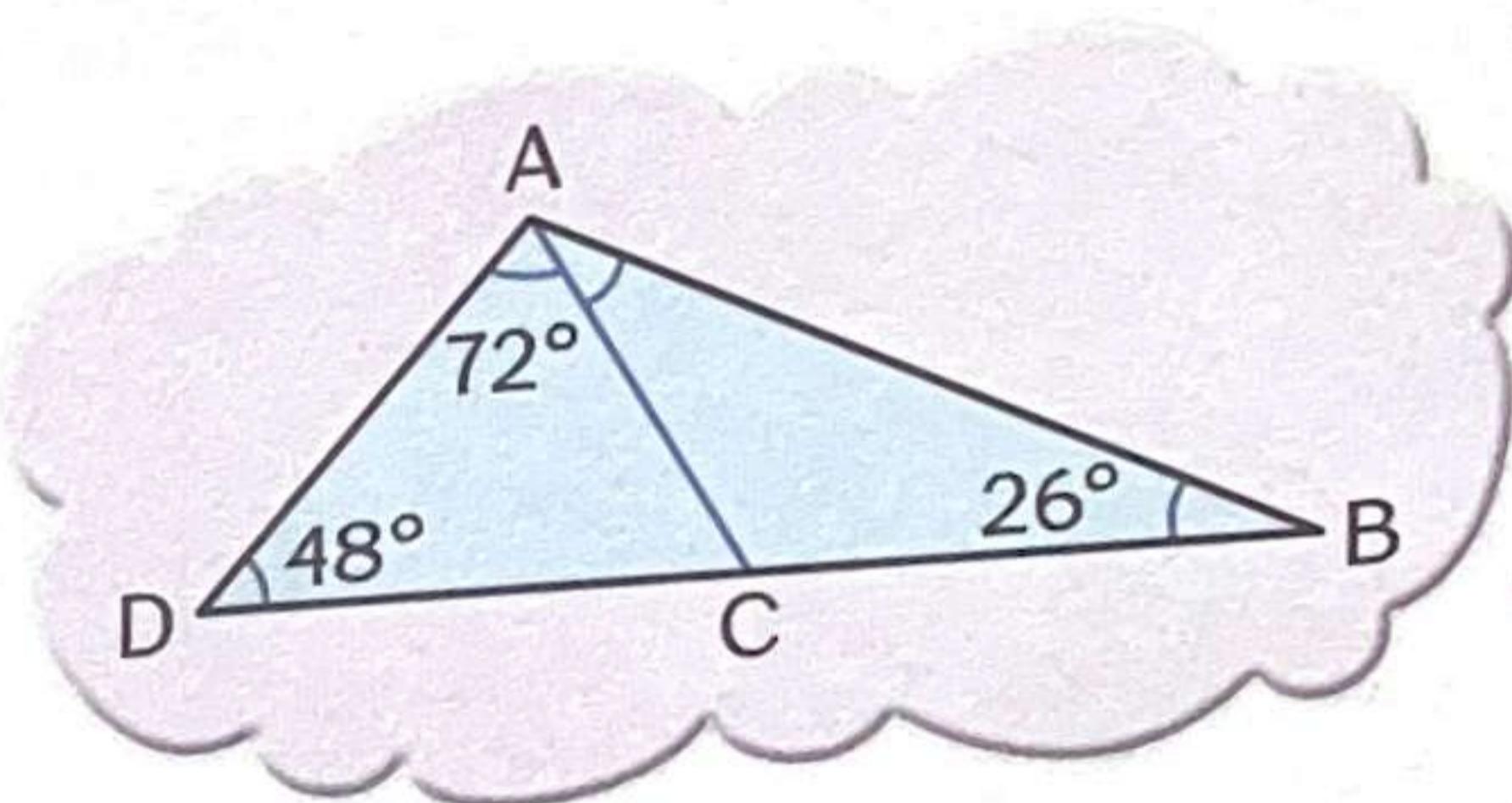
## Method 1

$$\begin{aligned}\angle ACD &= 180^\circ - 48^\circ - 72^\circ \\&= 60^\circ \\ \angle x &= 180^\circ - 60^\circ \\&= 120^\circ\end{aligned}$$



## Method 2

$$\begin{aligned}\angle CAB &= 180^\circ - 48^\circ - 26^\circ - 72^\circ \\&= 34^\circ \\ \angle x &= 180^\circ - 26^\circ - 34^\circ \\&= 120^\circ\end{aligned}$$

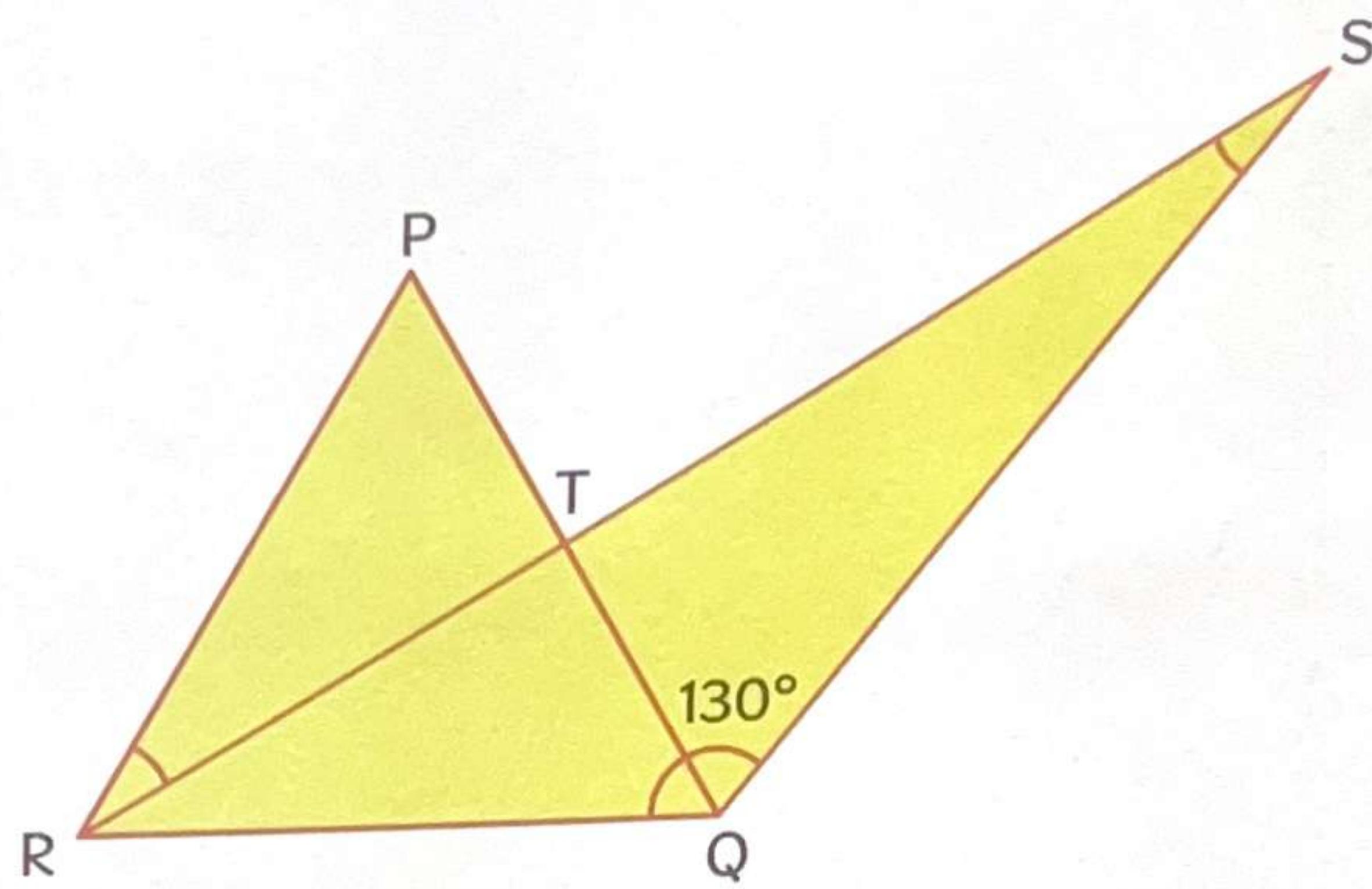


PQR is an equilateral triangle and QRS is a triangle.

$\angle PRT = \angle TRQ$ .  $\angle SQR = 130^\circ$ .

(a) Find  $\angle PRT$ .

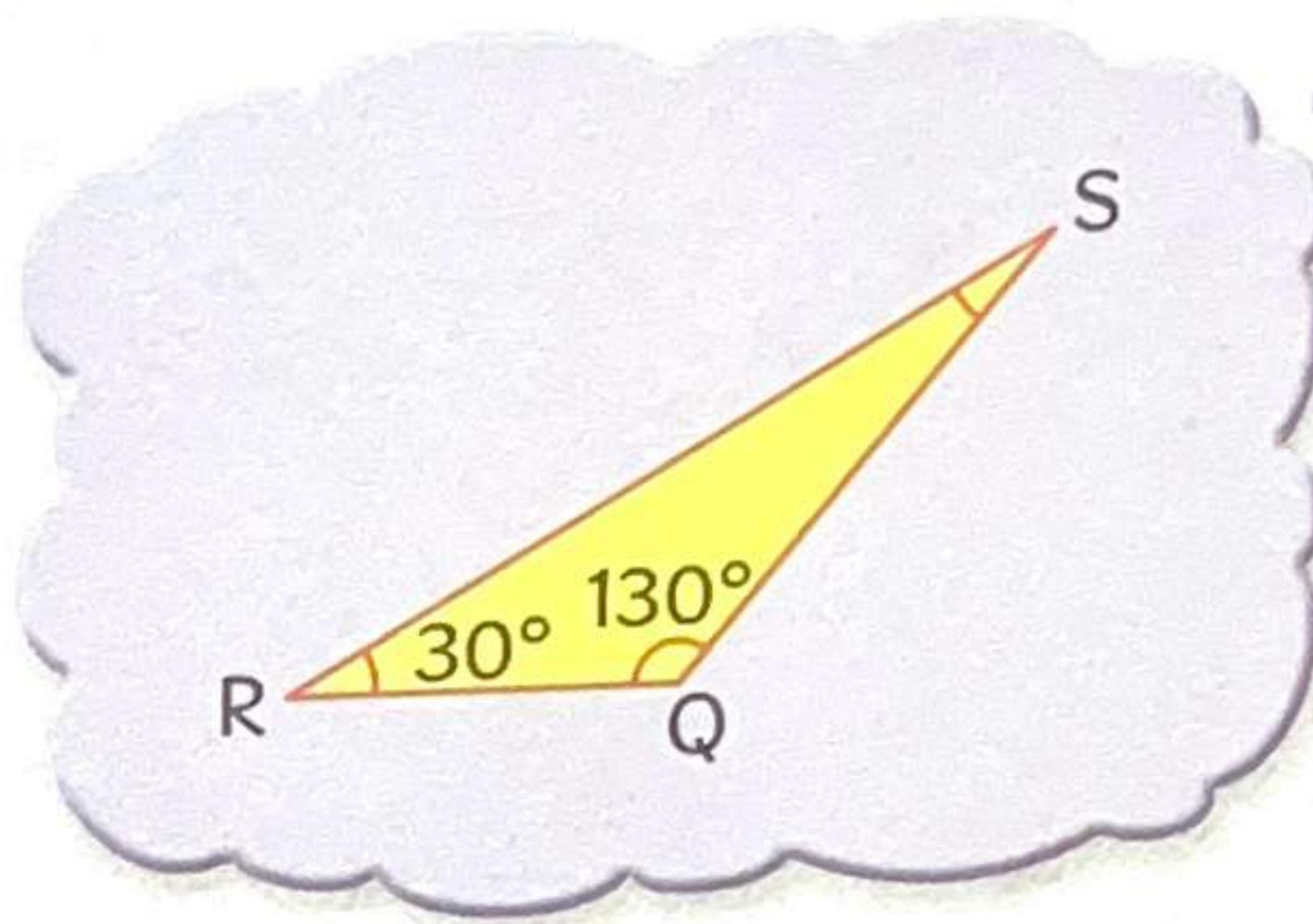
(b) Find  $\angle RSQ$ .



$$\begin{aligned}\text{(a)} \quad \angle PRT &= 60^\circ \div 2 \\ &= 30^\circ\end{aligned}$$

(b) **Method 1**

$$\begin{aligned}\angle TRQ &= \angle PRT = 30^\circ \\ \angle RSQ &= 180^\circ - 130^\circ - 30^\circ \\ &= 20^\circ\end{aligned}$$



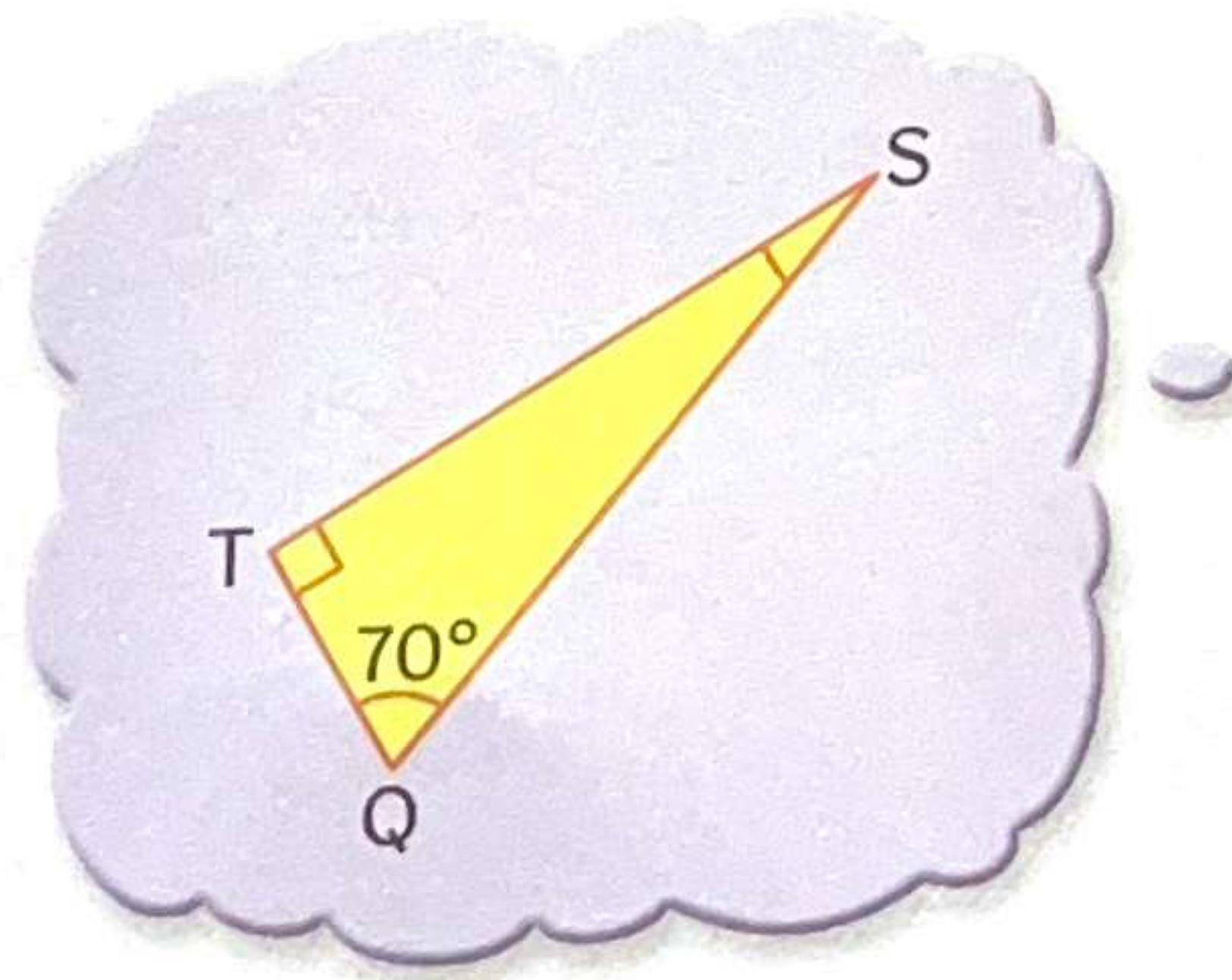
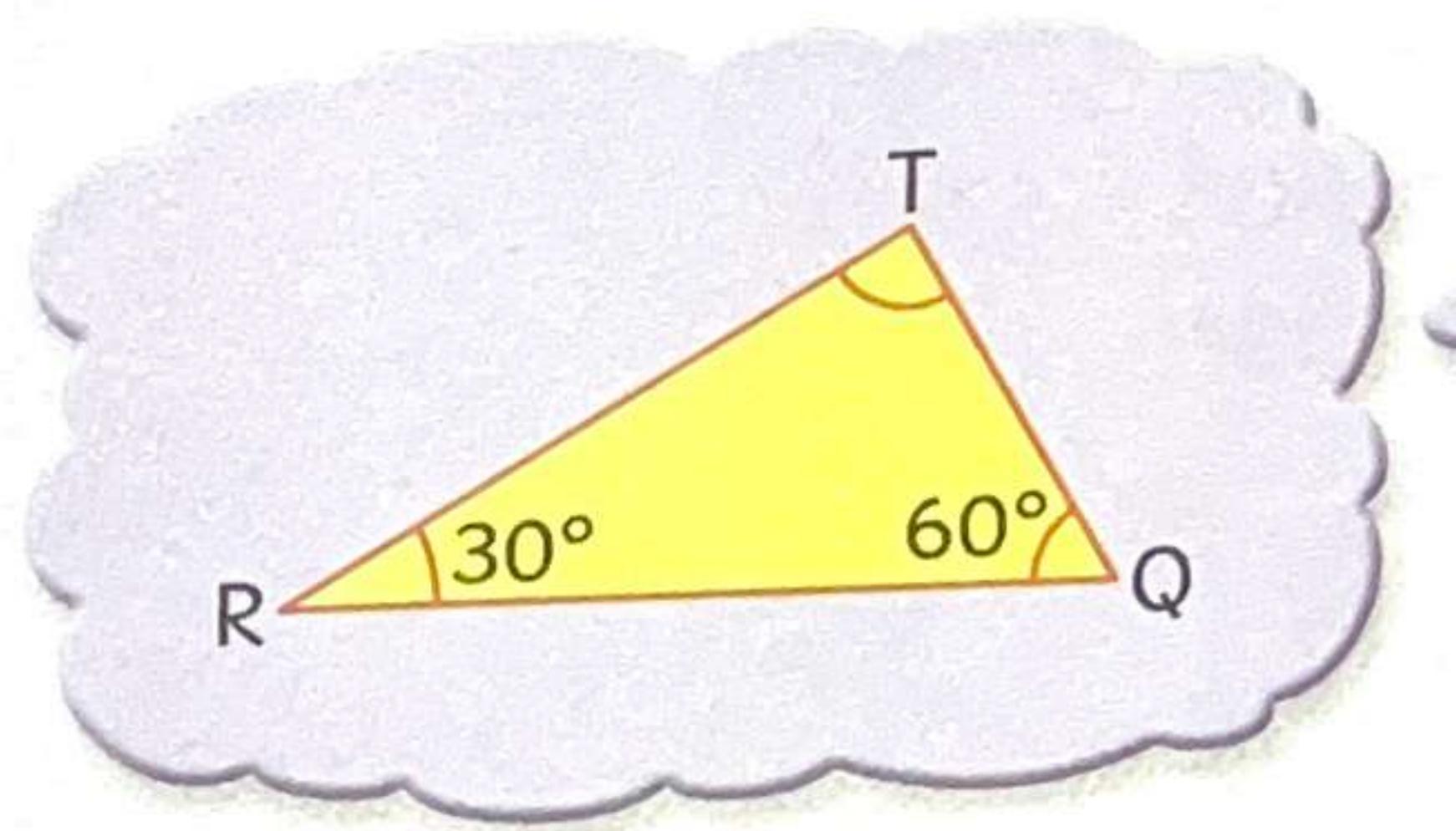
**Method 2**

$$\begin{aligned}\angle RTQ &= 180^\circ - 30^\circ - 60^\circ \\ &= 90^\circ\end{aligned}$$

$$\begin{aligned}\angle QTS &= 180^\circ - 90^\circ \\ &= 90^\circ\end{aligned}$$

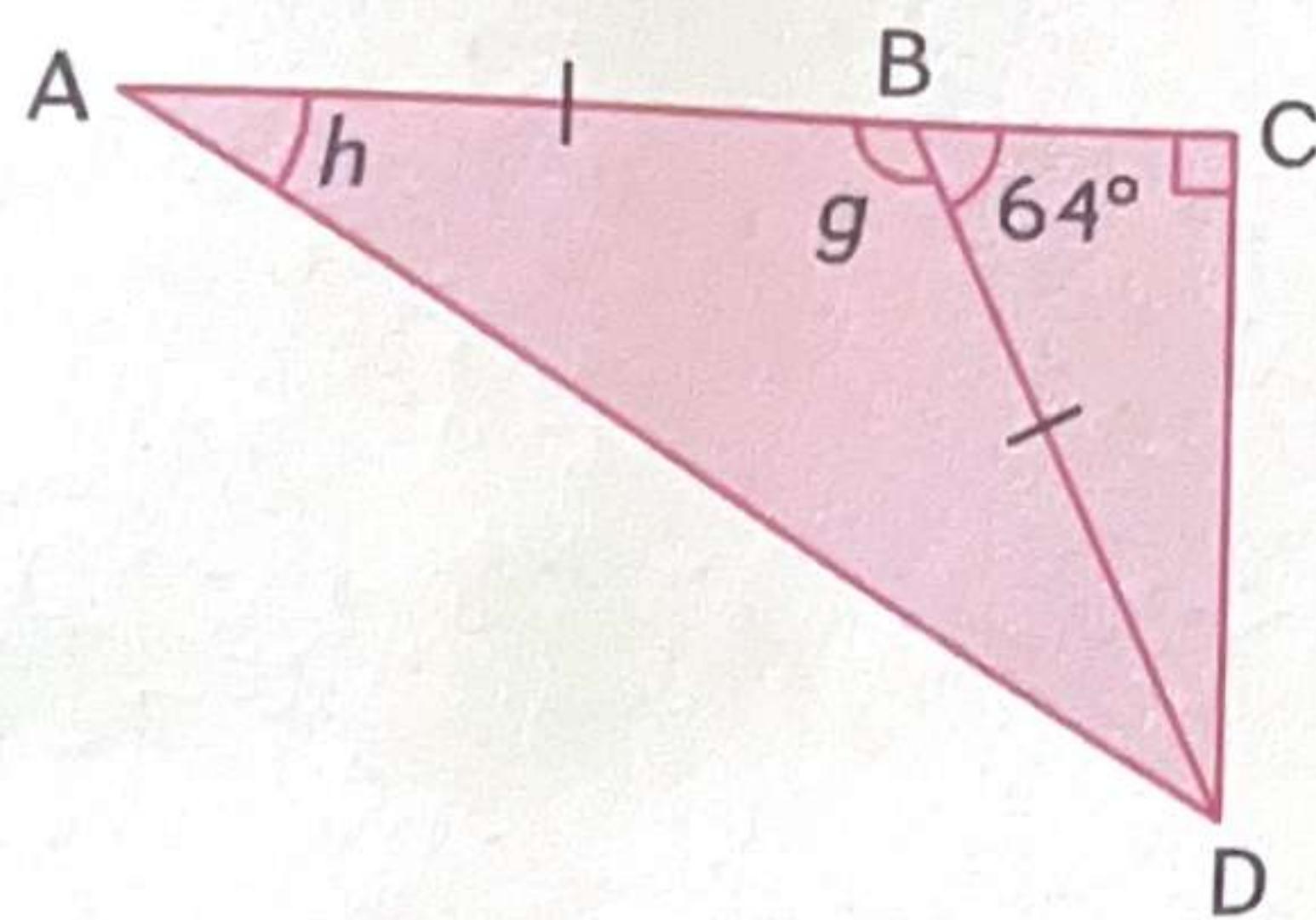
$$\begin{aligned}\angle TQS &= 130^\circ - 60^\circ \\ &= 70^\circ\end{aligned}$$

$$\begin{aligned}\angle RSQ &= \angle TSQ \\ &= 180^\circ - 90^\circ - 70^\circ \\ &= 20^\circ\end{aligned}$$

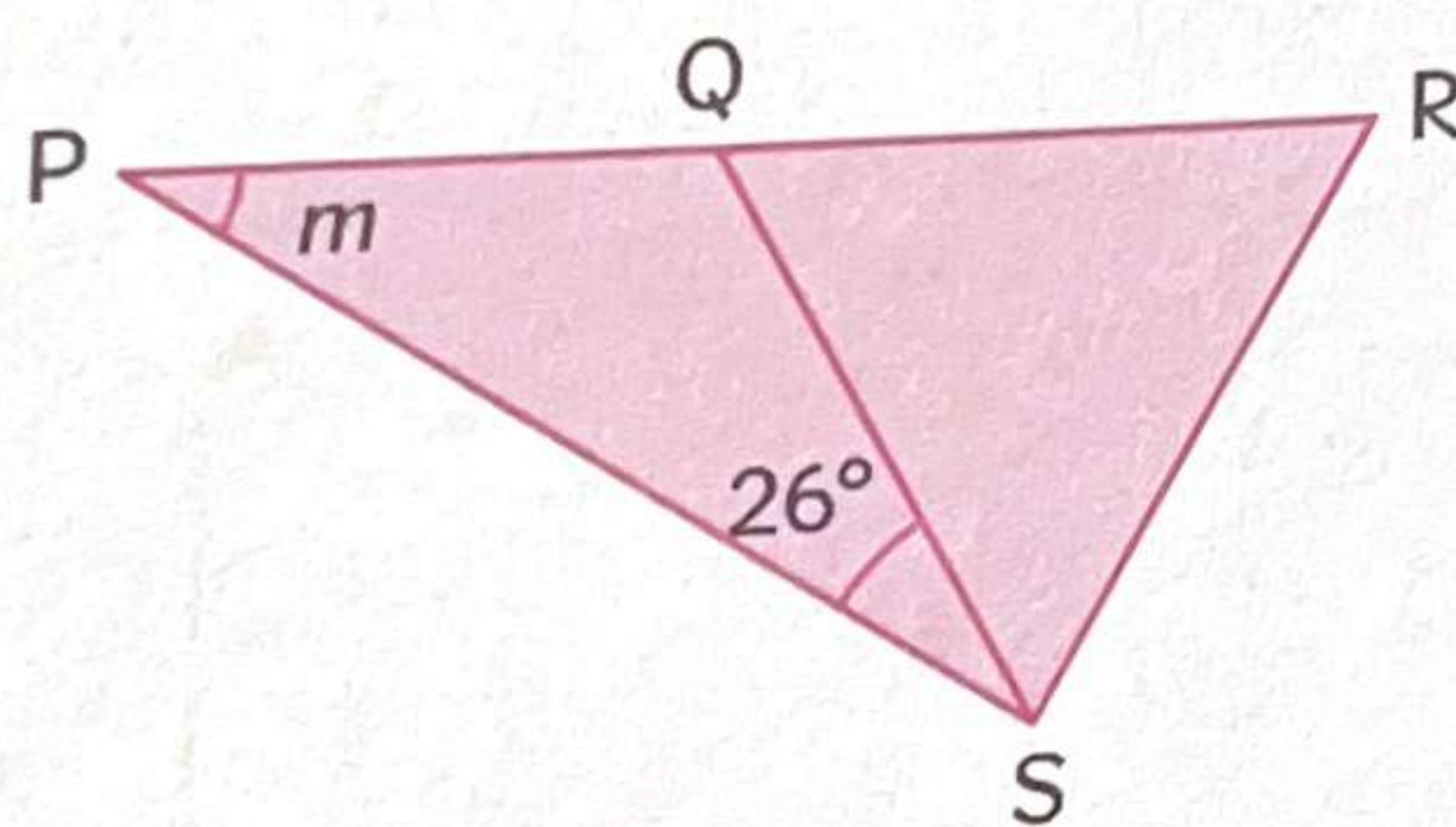


3

- (a) ABC is a straight line. ABD is an isosceles triangle.  $\angle DBC = 64^\circ$ .
- Find  $\angle g$ .
  - Find  $\angle h$ .



- (b) PQR is a straight line. QRS is an equilateral triangle.  $\angle QSP = 26^\circ$ .  
Find  $\angle m$ .



- (c) PRS is an isosceles triangle. PST is a right-angled triangle.  
 $\angle PRS = 50^\circ$ .  $\angle TPS = 12^\circ$ .
- Find  $\angle RPS$ .
  - Find  $\angle RST$ .

