

Programming Language Concepts, cs2104 Lecture 04 (2003-08-29)



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Overview

- Organization
- Course overview
- Introduction to programming concepts



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Organization



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Reading Suggestions



- Chapter 2
 - Sections 2.1 – 2.3 [careful]
 - Section 2.4 – 2.5 [careful]
 - Section 2.6 [careful]
- And of course the handouts!

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Organizational



- First assignment is due on Monday
- We could have a consultation session on Saturday from 10:00-13:00 in PC Lab2?

Reading Suggestions



- Chapter 2
 - Sections 2.1 – 2.5 [careful]
- And of course the handouts!

Last Lecture



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Our Roadmap



- Introduction **FINISHED**
 - Functions
 - Data structures
 - Recursion
 - Language syntax
- Declarative programming model
 - kernel language
 - language semantics

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Languages



- Kernel language
 - few constructs
 - sequence of instructions (statements)
 - geared at execution by machine
 - simple semantics, simple explanation
- Programming language
 - many constructs useful for programming
 - nested structure
 - geared at programming by humans
 - concise programming, rich language

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Kernel Language



- Statements
- Single assignment store
- Values and types
- Abstract machine
- Programming language translated to kernel language

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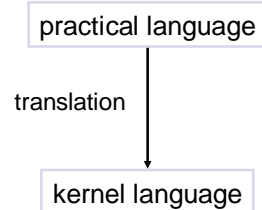
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Kernel Language Approach



- Provides useful abstractions for programmer
- Can be extended with linguistic abstractions



- Easy to understand and reason with
- Has a precise (formal) semantics

```
fun {sqr X} X*X end
B = {sqr {sqr A}}
```

```
proc {sqr X Y}
  { * X X Y}
end
local T in
  {sqr A T}
  {sqr T B}
end
```

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Linguistic Abstractions ⇔ Syntactic Sugar



- Linguistic abstractions: provide higher level concepts
- Syntactic sugar: short cuts and conveniences to improve readability

```
if N==1 then [1]
else
  local L in
    ...
  end
end
```

```
if N==1 then [1]
else L in
  ...
end
```

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Sequential Declarative Computation Model



- *Single assignment store*
 - declarative (dataflow) variables and values (together called entities)
 - values and their types
- *Kernel language syntax*
- *Environment*
 - maps textual variable names (variable identifiers) into entities in the store
- *Execution* of kernel language statements
 - execution stack of statements (defines control)
 - store
 - transforms store by sequence of steps

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Language Syntax



- Defines *legal* programs
 - programs that can be executed by machine
- Defined by *grammar rules*
 - define how to make 'sentences' out of 'words'
- For programming languages
 - sentences are called *statements*
 - words are called *tokens*
 - *grammar rules* describe tokens and statements

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Grammar Rules Constructs



- $\langle x \rangle$ nonterminal x
- $\langle x \rangle ::= Body$ $\langle x \rangle$ is defined by $Body$
- $\langle x \rangle \mid \langle y \rangle$ either $\langle x \rangle$ or $\langle y \rangle$ (choice)
- $\langle x \rangle \langle y \rangle$ the sequence $\langle x \rangle$ followed by $\langle y \rangle$
- $\{ \langle x \rangle \}$ sequence of zero or more occurrences of $\langle x \rangle$
- $\{ \langle x \rangle \}^+$ sequence of one or more occurrences of $\langle x \rangle$
- $[\langle x \rangle]$ zero or one occurrence of $\langle x \rangle$

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Kernel Language Syntax



$\langle s \rangle$ denotes a statement

- | | |
|--|----------------------------------|
| $\langle s \rangle ::= \text{skip}$ | <i>empty statement</i> |
| $\mid \langle x \rangle = \langle y \rangle$ | <i>variable-variable binding</i> |
| $\mid \langle x \rangle = \langle v \rangle$ | <i>variable-value binding</i> |
| $\mid \langle s_1 \rangle \langle s_2 \rangle$ | <i>sequential composition</i> |
| $\mid \text{local } \langle x \rangle \text{ in } \langle s_1 \rangle \text{ end}$ | <i>declaration</i> |
| $\mid \text{if } \langle x \rangle \text{ then } \langle s_1 \rangle \text{ else } \langle s_2 \rangle \text{ end}$ | <i>conditional</i> |
| $\mid \{ \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle \}$ | <i>procedural application</i> |
| $\mid \text{case } \langle x \rangle \text{ of } \langle \text{pattern} \rangle \text{ then } \langle s_1 \rangle \text{ else } \langle s_2 \rangle \text{ end}$ | <i>pattern matching</i> |

$\langle v \rangle ::= \dots$ *value expression*

$\langle \text{pattern} \rangle ::= \dots$

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Single Assignment Store



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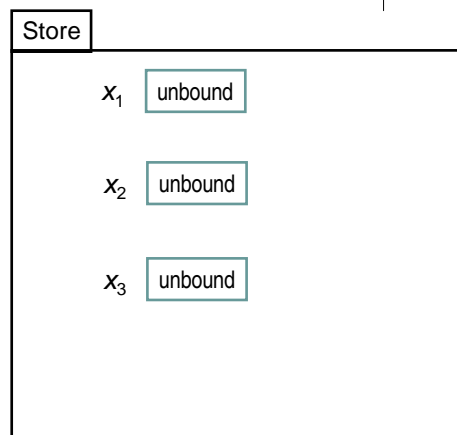
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Single Assignment Store



- Single assignment store is store (set) of variables
- Initially variables are unbound



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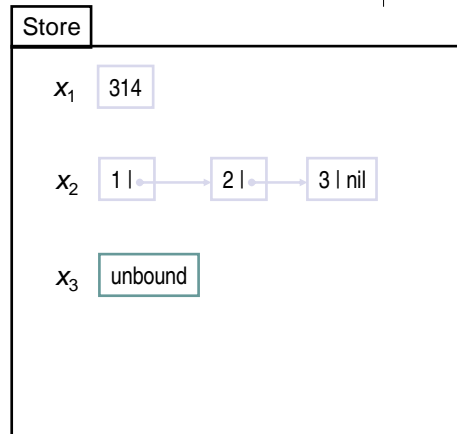
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Declarative (Single-Assignment) Variables



- Created as being *unbound*
- Can be *bound* to exactly one value
- Once bound, stays bound
 - indistinguishable from its value



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Store Operations



- Single assignment $\langle x \rangle = \langle v \rangle$
 - constructs value $\langle v \rangle$ in store
 - binds variable $\langle x \rangle$ to constructed value
 - if already bound, tests for compatibility
 - if not compatible, error raised
- Variable-variable binding $\langle x \rangle = \langle y \rangle$
 - binds variables to each other
 - variables form equivalence classes

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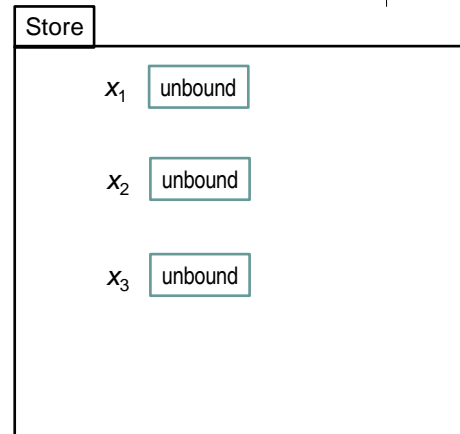
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Single Assignment Store



- Single assignment store is store (set) of variables
- Initially variables are unbound
- Example: store with three variables, x_1 , x_2 , and x_3
- $\{x_1, x_2, x_3\}$



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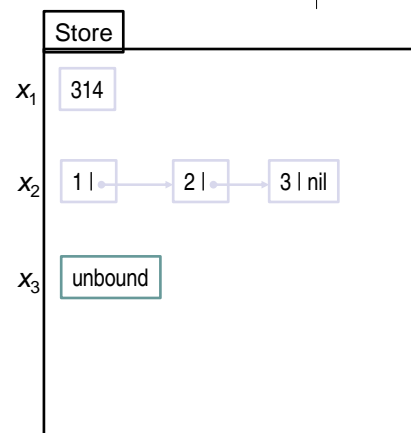
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Single Assignment Store (3)



- Variables in store may be bound to values
- Assume we allow as values
 - x_1 is bound to integer 314
 - x_2 is bound to list [1 2 3]
 - x_3 is still unbound
- $\{x_1=314, x_2=[1\ 2\ 3], x_3\}$



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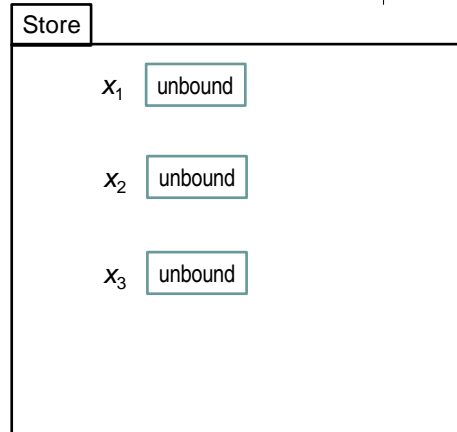
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Store Operations: Single Assignment



$\langle X \rangle = \langle V \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$
- Assumes that $\langle x \rangle$ is unbound



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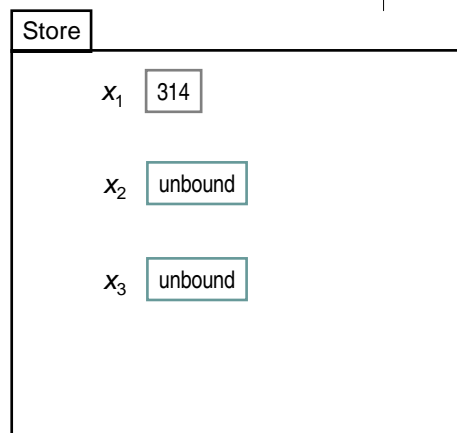
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Single Assignment



$\langle x \rangle = \langle \text{value} \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$



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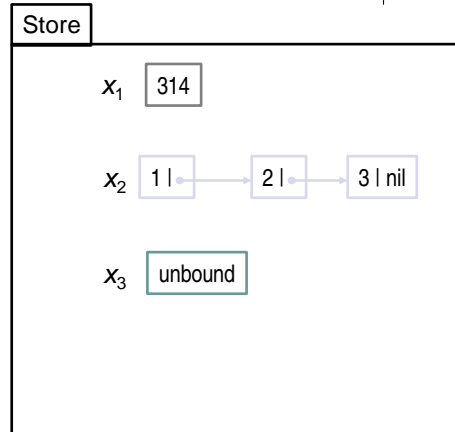
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Single Assignment



$\langle X \rangle = \langle V \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$
- *Single assignment operation* ('=')
 - constructs $\langle V \rangle$ in store
 - binds variable $\langle x \rangle$ to this value
- If variable already bound, operation tests compatibility of values
 - if test fails an error is raised



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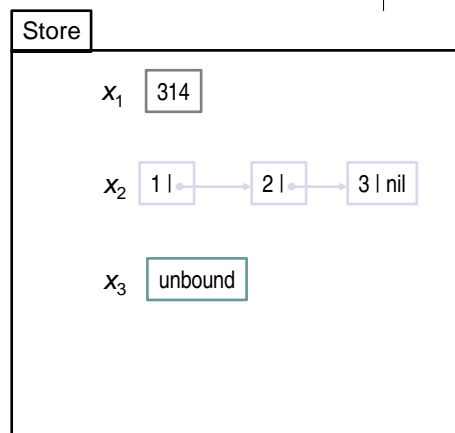
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Single Assignment



$\langle X \rangle = \langle V \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$
- *Single assignment operation* ('=')
 - constructs $\langle V \rangle$ in store
 - binds variable $\langle x \rangle$ to this value
- $\{x_1=314, x_2=[1\ 2\ 3], x_3\}$



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Single Assignment Store



- Can contain partial values
 - data structure with unbound variables
- Once variable is bound, indistinguishable from its value
 - *dereferencing*: traversing variable cell to get value
 - automatic and transparent to programmer

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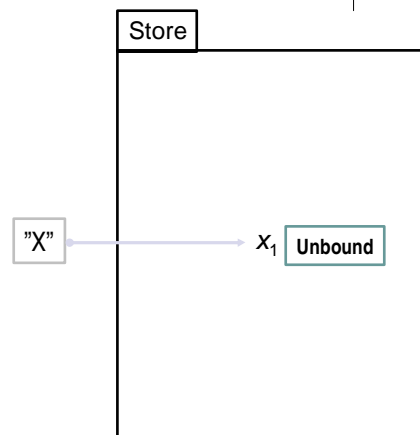
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Variable Identifiers



- Refer to store entities
- Environment maps variable identifiers to variables
 - declare X
 - local X in ...
- " X " is variable identifier
- Corresponds to 'environment' $\{ "X" \rightarrow x_1 \}$



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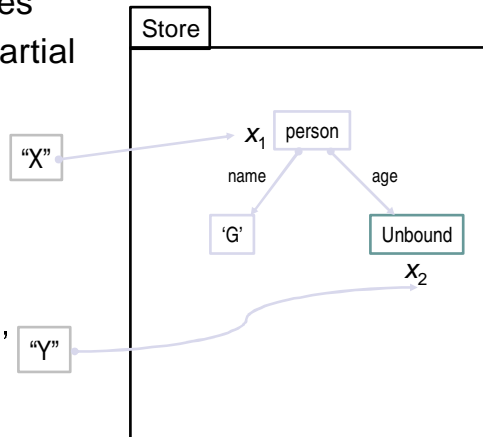
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Partial Values

- Data structure that may contain unbound variables
- The store contains the partial value:

person(name: 'G' age: x_2)

- declare Y X
X = person(name: george age: Y)
- The identifier 'Y' refers to x_2
- $S = \{x_1 = \text{person}(\text{name: 'G' age: } x_2), x_2\}$



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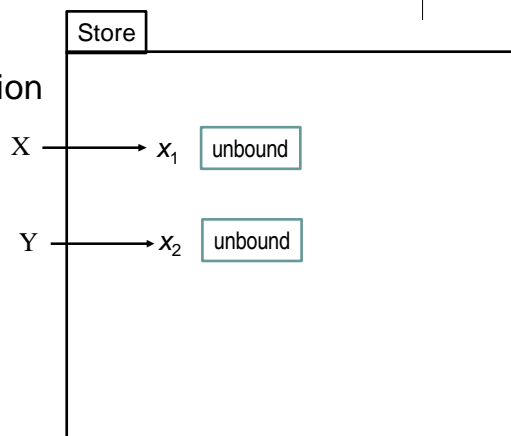
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Variable-variable Binding

$\langle x_1 \rangle = \langle x_2 \rangle$

- Performs bind operation between variables
- Example:
X = Y
- Operation equates (merges) the two variables
- $S = \{x_1, x_2\}$



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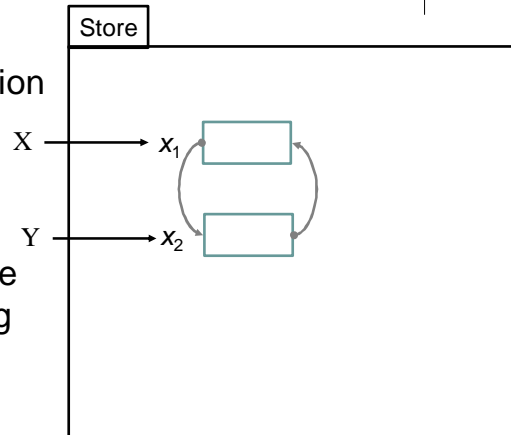
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Variable-variable Binding

$$\langle x_1 \rangle = \langle x_2 \rangle$$

- Performs bind operation between variables
- Example:
 $X = Y$
- Operation equates the two variables: forming an equivalence class
- $S = \{x_1 = x_2\}$



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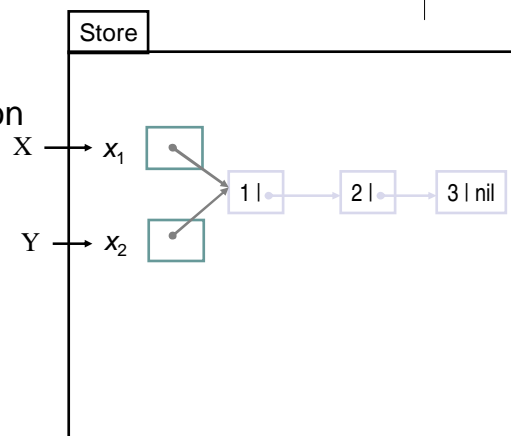
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Variable-variable Binding

$$\langle x_1 \rangle = \langle x_2 \rangle$$

- Performs bind operation between variables
- Example:
 $X = Y$
 $X = [1 \ 2 \ 3]$
- All variables (X and Y) are bound to **[1 2 3]**
- $S = \{x_1 = x_2 = [1 \ 2 \ 3]\}$



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Summary: Variables and Partial Values



- Declarative variable
 - resides in single-assignment store
 - is initially unbound
 - can be bound to exactly one (partial) value
 - can be bound to several (partial) values as long as they are compatible with each other
- Partial value
 - data-structure that may contain unbound variables
 - when one of the variables is bound, it is replaced by the (partial) value it is bound to
 - a complete value, or value for short is a data-structure that does not contain any unbound variable

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Kernel Language Syntax



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Variable Identifiers



- $\langle x \rangle$, $\langle y \rangle$, $\langle z \rangle$ stand for variables
- Concrete kernel language variables
 - begin with upper-case letter
 - followed by (possibly empty) sequence of alphanumeric characters or underscore
- Any sequence of characters within backquote
- Examples:
 - X, Y1
 - Hello_World
 - `hello this is a \$5 bill` (backquote)

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Kernel Language Syntax



$\langle s \rangle$ denotes a statement

$\langle s \rangle ::= \text{skip}$	<i>empty statement</i>
$\langle x \rangle = \langle y \rangle$	<i>variable-variable binding</i>
$\langle x \rangle = \langle v \rangle$	<i>variable-value binding</i>
$\langle s_1 \rangle \langle s_2 \rangle$	<i>sequential composition</i>
$\text{local } \langle x \rangle \text{ in } \langle s_1 \rangle \text{ end}$	<i>declaration</i>
$\text{if } \langle x \rangle \text{ then } \langle s_1 \rangle \text{ else } \langle s_2 \rangle \text{ end}$	<i>conditional</i>
$\{ \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle \}$	<i>procedural application</i>
$\text{case } \langle x \rangle \text{ of } \langle \text{pattern} \rangle \text{ then } \langle s_1 \rangle \text{ else } \langle s_2 \rangle \text{ end}$	<i>pattern matching</i>

$\langle v \rangle ::= \dots$	<i>value expression</i>
-------------------------------	-------------------------

$\langle \text{pattern} \rangle ::= \dots$	
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Value Expressions



$\langle v \rangle ::= \langle \text{record} \rangle \mid \langle \text{number} \rangle \mid \langle \text{procedure} \rangle$

$\langle \text{record} \rangle,$
 $\langle \text{pattern} \rangle ::= \langle \text{literal} \rangle$
 $\mid \langle \text{literal} \rangle (\langle \text{feature}_1 \rangle : \langle x_1 \rangle \dots \langle \text{feature}_n \rangle : \langle x_n \rangle)$

$\langle \text{literal} \rangle ::= \langle \text{atom} \rangle \mid \langle \text{bool} \rangle$
 $\langle \text{feature} \rangle ::= \langle \text{int} \rangle \mid \langle \text{atom} \rangle \mid \langle \text{bool} \rangle$

$\langle \text{bool} \rangle ::= \text{true} \mid \text{false}$

$\langle \text{number} \rangle ::= \langle \text{int} \rangle \mid \langle \text{float} \rangle$

$\langle \text{procedure} \rangle ::= \text{proc } \{ \$ \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end}$

Values and Types



Values and Types



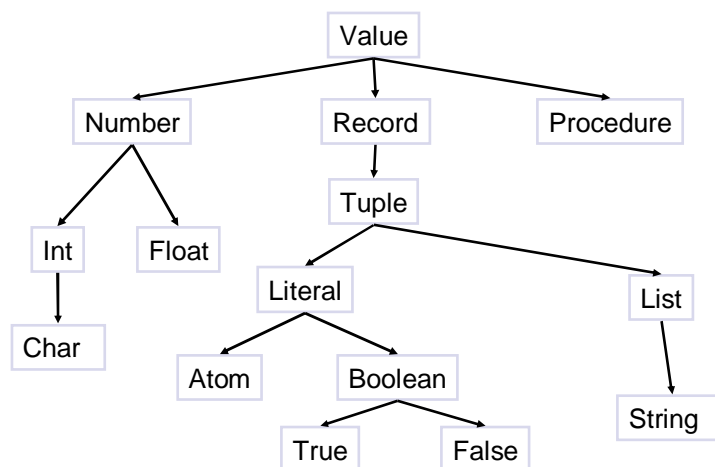
- *Data type*
 - set of values
 - set of associated operations
- Example: `Int` is data type "Integer"
 - set of all integer values
 - 1 is *of type* `Int`
 - has set of operations including `+`, `-`, `*`, `div`, etc
- Model comes with a set of basic types
- Programs can define other types
 - for example: *abstract data types* ADT

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Data Types

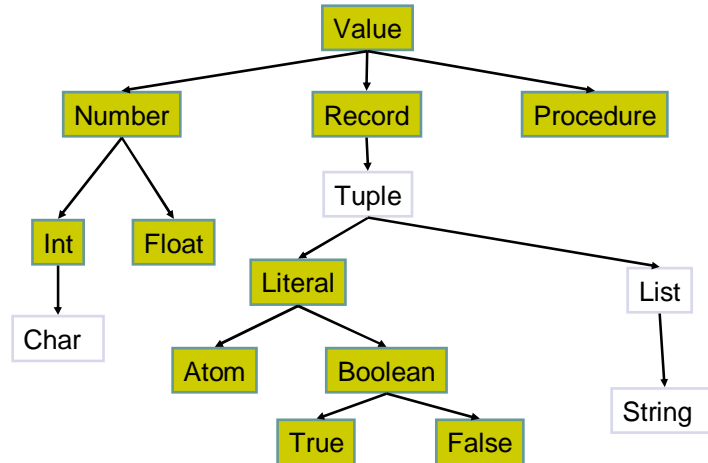


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Primitive Data Types



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Value Expressions

$\langle v \rangle ::= \langle \text{record} \rangle \mid \langle \text{number} \rangle \mid \langle \text{procedure} \rangle$

$\langle \text{record} \rangle,$
 $\langle \text{pattern} \rangle ::= \langle \text{literal} \rangle$
 $\mid \langle \text{literal} \rangle (\langle \text{feature}_1 \rangle : \langle x_1 \rangle \dots \langle \text{feature}_n \rangle : \langle x_n \rangle)$

$\langle \text{literal} \rangle ::= \langle \text{atom} \rangle \mid \langle \text{bool} \rangle$
 $\langle \text{feature} \rangle ::= \langle \text{int} \rangle \mid \langle \text{atom} \rangle \mid \langle \text{bool} \rangle$

$\langle \text{bool} \rangle ::= \text{true} \mid \text{false}$

$\langle \text{number} \rangle ::= \langle \text{int} \rangle \mid \langle \text{float} \rangle$

$\langle \text{procedure} \rangle ::= \text{proc } \{ \$ \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end}$

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Numbers



- Integers
 - 314, 0
 - ~10 (minus 10)
- Floats
 - 1.0, 3.4, 2.0e2, 2.0E2 (2×10^2)
- Number: either Integer or Float

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Atoms and Booleans



- A sequence starting with a lower-case character followed by characters or digits, ...
 - person, peter
 - 'Seif Haridi'
- Booleans
 - true
 - false
- Literal: atom or boolean

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Records



- Compound representation (data-structures)
 - $\langle l \rangle (\langle f_1 \rangle : \langle x_1 \rangle \dots \langle f_n \rangle : \langle x_n \rangle)$
 - $\langle l \rangle$ is a literal
- Examples
 - `person(age:X1 name:X2)`
 - `person(1:X1 2:X2)`
 - `'l'(1:H 2:T)`
- Syntactic sugar
 - tuples `f(a b)`
 - lists `a|Xr` `[a b c]`
 - pairs `a#b`

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Strings



- Is list of character codes enclosed with double quotes
 - example `"E=mc^2"`
 - same as `[69 61 109 99 94 50]`

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Procedure Declarations



- Kernel language
 $\langle x \rangle = \text{proc } \{ \$ \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end}$
is legal statement
 - binds $\langle x \rangle$ to procedure value
 - *declares* (introduces) a procedure
- Familiar syntactic variant
 $\text{proc } \{ \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle \}$
 $\langle s \rangle$
end
introduces (declares) the procedure $\langle x \rangle$

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Operations on Basic Types



- Numbers
 - floats: $+, -, *, /$
 - integers: $+, -, *, \text{div}, \text{mod}$
- Records
 - Arity, Label, Width, and ". "
 - $X = \text{person}(\text{name: "George" age: 25})$
 - $\{\text{Arity } X\} = [\text{age name}]$
 - $\{\text{Label } X\} = \text{person}, X.\text{age} = 25$
- Comparisons
 - equality: $==, \backslash=$
 - order: $=<, <, >=$
integers, floats, and atoms

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Value Expressions



$\langle v \rangle ::= \langle \text{procedure} \rangle \mid \langle \text{record} \rangle \mid \langle \text{number} \rangle \mid \langle \text{basicExpr} \rangle$

$\langle \text{basicExpr} \rangle ::= \dots \mid \langle \text{numberExpr} \rangle \mid \dots$

$\langle \text{numberExpr} \rangle ::= \langle x \rangle_1 + \langle x \rangle_2 \mid \dots$

.....

Summary: Values and Types



- For kernel language
 - numbers
 - literals
 - records
 - procedures
- Created by value expressions

Abstract Machine (Semantics)



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Concepts

- Single-assignment store
- Environment
- Semantic statement
- Execution state
- Computation



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Abstract Machine



- Performs a computation
- *Computation* is sequence of execution states
- *Execution state*
 - stack of semantic statements
 - single assignment store
- *Semantic statement*
 - statement
 - environment
- *Environment* maps variable identifiers to store entities

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Single Assignment Store



- Single assignment store σ
 - set of store variables
 - partitioned into
 - sets of variables that are equal but unbound
 - variables bound to value
- Example store $\{x_1, x_2=x_3, x_4=a|x_2\}$
 - x_1 unbound
 - x_2, x_3 equal and unbound
 - x_4 bound to partial value $a|x_2$

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Environment



- Environment E
 - maps variable identifiers to entities in store σ
 - written as set of pairs $X \rightarrow x$
 - variable identifier X
 - store variable x
- Example environment $\{ X \rightarrow x, Y \rightarrow y \}$
 - maps identifier X to store variable x
 - maps identifier Y to store variable y

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Environment and Store



- Given: environment E , store σ
- Looking up value for variable identifier X :
 - find store variable in environment $E(X)$
 - take value from σ for $E(X)$
- Example:
 - $\sigma = \{x_1, x_2 = x_3, x_4 = a | x_2\}$ $E = \{ X \rightarrow x_1, Y \rightarrow x_4 \}$
 - $E(X) = x_1$ and no information in σ on x_1
 - $E(Y) = x_4$ and σ binds x_4 to $a | x_2$

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Calculating with Environments



- Program execution looks up values
 - assume store σ
 - given variable identifier $\langle x \rangle$
 - $E(\langle x \rangle)$ is value in store σ
- Program execution modifies environments
 - for example: declaration
 - adding new mappings from identifiers
 - overwrite existing mappings
 - restricting mappings to sets of variables

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Environment Adjunction



- Given: Environment E
$$E + \{\langle x \rangle_1 \rightarrow x_1, \dots, \langle x \rangle_n \rightarrow x_n\}$$

is new environment E' with mappings added:
 - always take store entity from new mappings
 - might overwrite old mappings
- Obs: no name given in book!

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Environment Projection



- Given: Environment E

$$E \upharpoonright \{\langle x \rangle_1, \dots, \langle x \rangle_n\}$$

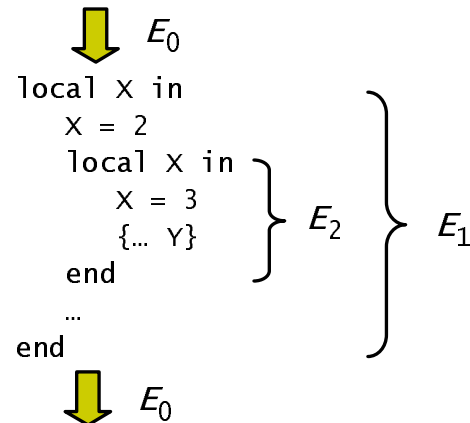
is new environment E' where only mappings for $\{\langle x \rangle_1, \dots, \langle x \rangle_n\}$ are retained from E

Adjunction Example



- $E_0 = \{ Y \rightarrow 1 \}$
- $E_1 = E_0 + \{ X \rightarrow 2 \}$
 - corresponds to $\{ X \rightarrow 2, Y \rightarrow 1 \}$
 - $E_1(X) = 2$
- $E_2 = E_1 + \{ X \rightarrow 3 \}$
 - corresponds to $\{ X \rightarrow 3, Y \rightarrow 1 \}$
 - $E_2(X) = 3$

Why Adjunction?



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Semantic Statements

- To actually execute statement:
 - environment to map identifiers
 - modified with execution of each statement
 - each statement has its own environment
 - store to find values
 - all statements modify same store
 - single store
- Semantic statement $(\langle s \rangle, E)$
 - pair of (statement, environment)

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Stacks of Statements



- Execution maintains stack of semantic statements ST

$[(\langle s \rangle_1, E_1), \dots, (\langle s \rangle_n, E_n)]$

- always topmost statement $(\langle s \rangle_1, E_1)$ executes first
 - rest of stack: what needs to be done
- Also called: *semantic stack*

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Execution State



- *Execution state* (ST, σ)
 - pair of (stack of semantic statements, store)

- *Computation*
 $(ST_1, \sigma_1) \Rightarrow (ST_2, \sigma_2) \Rightarrow (ST_3, \sigma_3) \Rightarrow \dots$
 - sequence of execution states

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Program Execution



- Initial execution state
 $([[\langle s \rangle, \emptyset]] , \emptyset)$
 - empty store \emptyset
 - stack with semantic statement $[[\langle s \rangle, \emptyset]]$
 - single statement $\langle s \rangle$, empty environment \emptyset
- At each execution step
 - pop topmost element of semantic stack
 - execute according to statement
- If semantic stack empty, execution stops

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Semantic Stack States



- Semantic stack can be in run-time states
 - *terminated* stack is empty
 - *runnable* can do execution step
 - *suspended* stack not empty, no execution step possible
- Statements
 - *non-suspending* can always execute
 - *suspending* need values from store
dataflow behavior

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Summary

- Single assignment store
- Environments
 - adjunction, projection
- Semantic statements
- Semantic stacks
- Execution state
- Program execution
 - runnable, terminated, suspended
- Statements
 - suspending, non-suspending

σ
 E
 $E + \{...\} \quad E \mid \{...\}$
 $(\langle s \rangle, E)$
 $[(\langle s \rangle, E) \dots]$
 (ST, σ)

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Statement Execution

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Plan



- Simple statements
 - skip and sequential composition
 - variable declaration
 - store manipulation
 - conditional
- Computing with procedures (next lecture)
 - lexical scoping
 - closures
 - procedures as values
 - procedure call

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Simple Statements



$\langle s \rangle$ denotes a statement

$\langle s \rangle ::=$ skip
| $\langle x \rangle = \langle y \rangle$
| $\langle x \rangle = \langle v \rangle$
| $\langle s_1 \rangle \langle s_2 \rangle$
| local $\langle x \rangle$ in $\langle s_1 \rangle$ end
| if $\langle x \rangle$ then $\langle s_1 \rangle$ else $\langle s_2 \rangle$ end

empty statement
variable-variable binding
variable-value binding
sequential composition
declaration
conditional

$\langle v \rangle ::=$...

value expression
(no records here)

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Executing skip



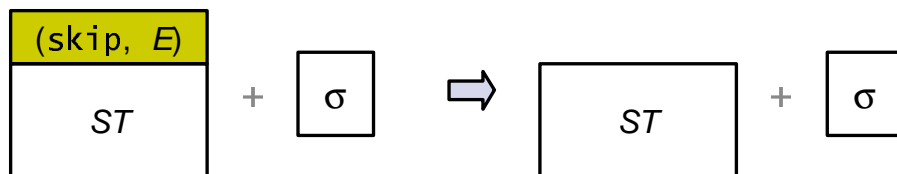
- Execution of semantic statement (skip, E)
- Do nothing
 - means: continue with next statement
 - non-suspending statement

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skip



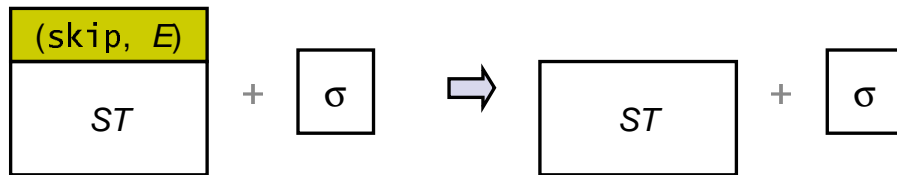
- No effect on store σ
- Non-suspending statement

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skip



- Remember: topmost statement is always popped!

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Executing Sequential Composition

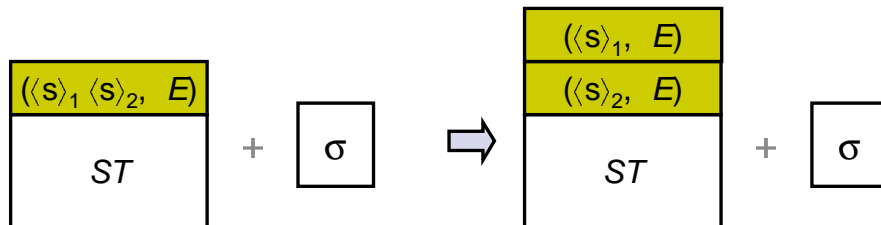
- Semantic statement is $(\langle s \rangle_1 \langle s \rangle_2, E)$
- Push in following order
 - $\langle s \rangle_2$ executes after
 - $\langle s \rangle_1$ executes next
- Statement is non-suspending

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Sequential Composition



- Decompose statement sequences
 - environment is given to both statements

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Executing local



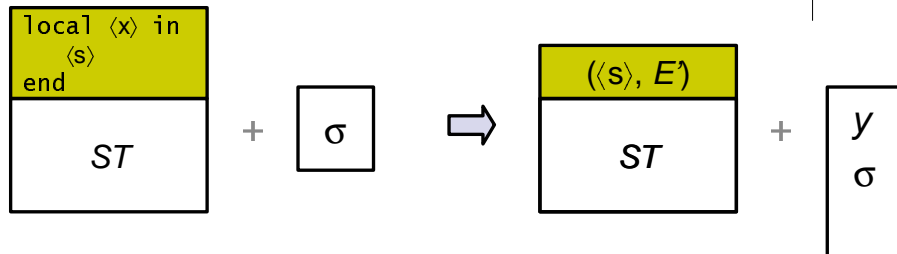
- Semantic statement is
 $(\text{local } \langle x \rangle \text{ in } \langle s \rangle \text{ end}, E)$
- Execute as follows
 - create new variable y in store
 - create new environment $E' = E + \{\langle x \rangle \rightarrow y\}$
 - push $(\langle s \rangle, E')$
- Statement is non-suspending

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local



- With $E = E + \{\langle x \rangle \rightarrow y\}$

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Variable-variable equality

- Semantic statement is $\langle \langle x \rangle = \langle y \rangle, E \rangle$
- Execute as follows
 - bind $E(\langle x \rangle)$ and $E(\langle y \rangle)$ in store
- Statement is non-suspending

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Variable-value equality



- Semantic statement is
$$(\langle x \rangle = \langle v \rangle, E)$$
with $\langle v \rangle$ number or record
- Execute as follows
 - create value $\langle v \rangle$ in store
 - use variables as defined by E
 - bind $E(\langle x \rangle)$ and $\langle v \rangle$ in store
- Statement is non-suspending

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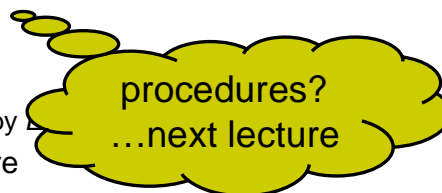
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Variable-value equality



- Semantic statement is
$$(\langle x \rangle = \langle v \rangle, E)$$
with $\langle v \rangle$ number or record
- Execute as follows
 - create value $\langle v \rangle$ in store
 - use variables as defined by E
 - bind $E(\langle x \rangle)$ and $\langle v \rangle$ in store
- Statement is non-suspending



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Suspending Statements



- All statements so far can always execute
 - non-suspending (or immediate)
- Conditional?
 - requires condition $\langle x \rangle$ to be bound variable
 - *activation condition*: $\langle x \rangle$ is bound (determined)

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Executing if



- Semantic statement is
 $(\text{if } \langle x \rangle \text{ then } \langle s \rangle_1 \text{ else } \langle s \rangle_2 \text{ end}, E)$
- If activation condition “ $\langle x \rangle$ bound” true
 - if $E(\langle x \rangle)$ bound to true push $\langle s \rangle_1$
 - if $E(\langle x \rangle)$ bound to false push $\langle s \rangle_2$
 - otherwise, raise error
- Otherwise, suspend...

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An Example

```
local x in
  local B in
    B=true
    if B then x=1 else skip end
  end
end
```

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Example: Initial State

```
((local x in
  local B in
    B=true
    if B then x=1 else skip end
  end
end, ∅)],
∅)
```

- Start with empty store and empty environment

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Example: local

```
(([local B in  
    B=true  
    if B then X=1 else skip end  
end,  
{X → x}]),  
{x})
```

- Create new store variable x
- Continue with new environment

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Example: local

```
(([B=true  
    if B then X=1 else skip end  
,  
{B → b, X → x}]),  
{b,x})
```

- Create new store variable b
- Continue with new environment

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Example: Sequential Composition



```
((B=true, {B → b, X → x}),  
  (if B then X=1  
    else skip end, {B → b, X → x})),  
 {b,x})
```

- Decompose to two statements
- Stack has now two semantic statements

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Example: Variable-Value Assignment



```
((if B then X=1  
  else skip end, {B → b, X → x}),  
 {b=true, x})
```

- Environment maps B to *b*
- Bind *b* to true

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Example: if

$([(X=1, \{B \rightarrow b, X \rightarrow x\})],$
 $\{b=\text{true}, x\})$

- Environment maps B to b
- Store binds b to true , continue with then

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Example: Variable-Value Assignment

$([],$
 $\{b=\text{true}, x=1\})$

- Environment maps X to x
- Binds x to 1
- Computation terminates as stack is empty

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Summary



- Semantic statement execute by
 - popping itself always
 - creating environment `local`
 - manipulating store `local, =`
 - pushing new statements `local, if`
sequential composition
- Semantic statement can suspend
 - activation condition
 - read store

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Homework



- Be an abstract machine!
- Execute something yourself!
- RTFB!

- See you next week!

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Our Roadmap

- Single assignment store
- Kernel language syntax
- Values and types
- Environments
- Execution



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Kernel Language Syntax



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Kernel Language Syntax



$\langle s \rangle$ denotes a statement

$\langle s \rangle ::=$	skip	<i>empty statement</i>
	$\langle x \rangle = \langle y \rangle$	<i>variable-variable binding</i>
	$\langle x \rangle = \langle v \rangle$	<i>variable-value binding</i>
	$\langle s_1 \rangle \langle s_2 \rangle$	<i>sequential composition</i>
	local $\langle x \rangle$ in $\langle s_1 \rangle$ end	<i>declaration</i>
	if $\langle x \rangle$ then $\langle s_1 \rangle$ else $\langle s_2 \rangle$ end	<i>conditional</i>
	$\{ \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle \}$	<i>procedural application</i>
	case $\langle x \rangle$ of $\langle \text{pattern} \rangle$ then $\langle s_1 \rangle$ else $\langle s_2 \rangle$ end	<i>pattern matching</i>

$\langle v \rangle ::=$...	<i>value expression</i>
-------------------------	-----	-------------------------

$\langle \text{pattern} \rangle ::=$...
--------------------------------------	-----