# Scaling

BIO401-01/598-02

2021-03-22 Mon

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## REVIEW: Git

### Concepts

- created by Linus Torvalds in 2005
- distributed version control : each directory as a full-fledged repo
- used for changes tracking and work coordination among collaborators

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### Concepts

- created by *Linus Torvalds* in 2005
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#### **Basic Practice**

- create a local copy of your SE.data repo
- git sync. with SE server
- local sync. with rsync

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## REVIEW: Git

### Concepts

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#### **Basic Practice**

- create a local copy of your SE.data repo
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#### Advanced

- git repo setup
- good for professional development
- good for collaboration

## Git Procedure

## Local Synchronisation

\$ cd ~/SE\_data

```
routine after the first time
```

```
$ git pull # (sync. w/ server)
$ rsync -hvrPt --ignore-existing ~/SE_data/* \
   /media/sf_LVM_Shared/my_SE_data
#(sync. only new files)
$ cd /media/sf_LVM_Shared/my_SE_data # (work here)
```

## Git Procedure

# Replacement (only when needed)

example: replacing the exising copy

```
$ cp ~/SE_data/exercise/05_R_Intro.ipynb \
   /media/sf_LVM_Shared/my_SE_data/exercise

or, if you want to keep the old copy

$ myPath=/media/sf_LVM_Shared/my_SE_data/exercise
$ mv ${myPath}/05_R_Intro.ipynb \
   ${myPath}/05_R_Intro.ipynb
$ cp ~/SE_data/exercise/05_R_Intro.ipynb ${myPath}
```

## about the Course

• methodology instead of recipe

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- active role

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### about the Course

- methodology instead of recipe
- active role
- efficiency and effectiveness

# CW Case: setup

### objectives

- modelling Canada Warbler (CW) abundance
- scaling effects

### landscape variables

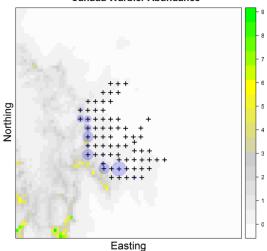
- elevation : CW high elevation
- evergreen coverage (NDVI): understory thickets



R. Chandler and J. Hepinstall-Cymerman, Landscape. Ecol. (2016) doi :  $10.1007/\mathrm{s}10980\text{-}016\text{-}0380\text{-}z$ 

# CW Case: output

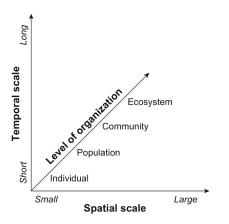




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# Scale in Ecology

describes the spatiotemporal dimension of a pattern or process





Spatial Ecology and Conservation Modeling Applications with R, Robert Fletcher, Marie-Josée Fortin (2018)

## CW Case: methods

#### Scale effect

- spatial extent at which each landscape covariate mostly highly correlated with the response variable
- landscape-level covariate covering the entire region while abundance data only available at sampled sites

#### Goal

- coordinates of a site : x
- abundance data at the site : N(x)
- $E(N(\mathbf{x})) = \lambda(\mathbf{x}) = z(\mathbf{x})$

### Spatial smoothing

- ullet unknown : scale at which the surrounding landscape effecting  $N(oldsymbol{x})$
- effects diminish with distance

$$s(z(\mathbf{x}), \sigma) = \sum_{(\mathbf{x}_j \neq \mathbf{x}_i) \in S} z(\mathbf{x}_j) w(\mathbf{x}_i, \mathbf{x}_j, \sigma)$$

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# CW Case: methods (contd.)

weighting function w

$$w(\mathbf{x}_i, \mathbf{x}_j, \sigma) = \frac{\exp(-||\mathbf{x}_i - \mathbf{x}_j||^2/(2\sigma)^2)}{\sum_{(\mathbf{x}_i \neq \mathbf{x}_i) \in S} \exp(-||\mathbf{x}_i - \mathbf{x}_j||^2/(2\sigma)^2)}$$

log-linear model

$$log(\lambda(\mathbf{x})) = \sum_{i=1}^{p} \beta_{i} s_{i} (z_{i}(\mathbf{x}_{i}), \sigma_{i})^{i-1}$$

Poisson model :  $N(x_i) \sim Poisson(\lambda(x_i))$ 

$$\mathcal{L}(\boldsymbol{\beta}, \sigma; \{N(\mathbf{x}_i)\}) = \prod_{i=1}^{R} \frac{\lambda(\mathbf{x}_i)^{N(\mathbf{x}_i)} \exp(-\lambda(\mathbf{x}_i))}{N(\mathbf{x}_i)!}$$

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# Probability: Basic Definitions

## Sample Space

The set of all possible outcomes in a random experiment is called the sample space, denoted S.

Example: a six-sided dice

$$S = \{1, 2, 3, 4, 5, 6\}$$

#### **Event**

A subset of S (A  $\subseteq$  S) is called an event.

Example (continued)

$$A = \{1, 2\}$$

$$A = \{3, 4, 5, 6\}$$

$$A = \{1, 3, 5\}$$

# Probability: Axioms and Propositions

### **Axioms**

A probability measure is a function P, which assigns to each event A a number P(A) satisfying

- (1)  $0 \le P(A) \le 1$
- (2) P(S) = 1
- (3) let A<sub>i</sub> be a sequence of disjoint events

$$P(\bigcup_{k=1}^{\infty} A_k) = \sum_{k=1}^{\infty} P(A_k)$$

## **Propositions**

Let P be a probability measure in some sample space S and let A and B be events

- (1)  $P(A^c) = 1 P(A)$
- (2)  $P(A \setminus B) = P(A) P(A \cap B)$
- (3)  $P(A \cup B) = P(A) + P(B) P(A \cap B)$

### **Exercises**

Please point out the error in the statement below.

"There will be 50% chance of rain on Sat. and 50% chance of rain on Sun. Therefore, there will be 100% chance of rain this weekend."

# Conditional Probability

#### Definition

Given a non-empty event B, the probability of A given B is defined as

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

### Example:

Suppose the chance of rain for this Sat. and Sun. is 50% and the chance of two rainy days in a row is 60%. What's the probability of rain this weekend?

#### Solution:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$
  
$$P(A \cap B) = P(B|A)P(A) = 0.3$$

So, 
$$P(A \cup B) = 0.7$$

# Independent Events

#### Definition

If A and B are two events satisfying

$$P(A \cap B) = P(A)P(B)$$

then they are said to be independent.

### Example:

Suppose the chance of rain for this Sat. and Sun. is 50% and rainy days are independent. What's the probability of rain this weekend?

### Solution:

$$P(A \cap B) = P(A)P(B) = 0.25$$
  
So,  $P(A \cup B) = 0.75$ 

# Law of Total Probability

## Law of Total Probability

Let  $A_i$  be a sequence of events that partition the sample space. i.e.  $S = \bigcup A_i$ . Then, for any event B in the same sample space,

$$P(B) = \sum_{i=1}^{\infty} P(B|A_i)P(A_i)$$

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# Example

Suppose that two factories supply light bulbs to the market. Factory X's bulbs work for over 5000 hours in 99% of cases, whereas factory Y's bulbs work for over 5000 hours in 95% of cases. It is known that factory X supplies 60% of the total bulbs available and Y supplies 40% of the total bulbs available. What is the chance that a purchased bulb will work for longer than 5000 hours?

$$P(L > 5000) = P(L > 5000|F_X)P(F_X) + P(L > 5000|B_Y)P(B_Y)$$
  
= 0.99 \times 0.6 + 0.95 \times 0.4 = 97.4%



https://en.wikipedia.org/wiki/Law of total probability

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