



Track based Alignment of the CMS Silicon Tracker



Frank-Peter Schilling (CERN)

Univ. Karlsruhe, 15/09/2006

- Personal Introduction
- Impact of misalignment
- Data samples
- Alignment strategy
- Alignment algorithms
 - HIP
 - Kalman Filter
 - Millepede-II

Personal Introduction

1998-2001: Ph.D. thesis, Univ. Heidelberg (H1 @ HERA, DESY)

- **Analysis: Measurement of jet cross sections in “diffractive” deep-inelastic scattering**
 - ❑ Published in **H1 Coll., Eur. Phys. J. C20 (2001) 29**
- **Hardware: H1 Backward Drift Chamber detector**
 - ❑ Maintenance, data quality, 24/7 “on-call” service
- **Data taking as shift leader**

2001-2004: Post-Doc at DESY (H1 Experiment)

- **Analysis: Measurement and QCD analysis of the inclusive diffractive structure function $F_2^{D(3)}(x_{IP}, x, Q^2)$**
 - ❑ Published in **H1 Coll., acc. by Eur. Phys. J. C, hep-ex/0606004**
- **Convenor of the Diffractive Physics Working Group of H1 (2001-2003)**
- **H1 Trigger Coordinator (2003-2004)**
 - ❑ Optimization of trigger budgets in coordination with physics groups
 - ❑ Integration of new trigger systems
 - ❑ Trigger setup for HERA-II phase (high lumi, initially high backgrounds)
 - o Reject beam induced backgrounds at L1
 - o Increase trigger thresholds
- **Data taking as Run Coordinator (2 week coordination of data taking)**

Since 10/2004: CERN research fellow (CMS Experiment)

- **Track based alignment of the CMS silicon tracker**
 - ❑ Implementation of a **common software framework** for track based alignment algorithms in ORCA
 - o CMS IN 2005/051
 - ❑ Implementation of the **HIP alignment algorithm** and alignment studies of the CMS pixel detector
 - o CMS Note 2006/018
 - ❑ **Co-editor of Physics TDR, Vol. 1, section 6.6: Alignment**
 - o CMS/LHCC 2006/001
 - ❑ Coordination of the **migration of the CMS alignment software to CMSSW**
 - ❑ Coordination of the “Alignment Exercise” in the coming **CSA06**
 - ❑ Development of **alignment strategies** for the CMS startup
 - ❑ Since 06/2006 **co-convenor of the PRS b/tau alignment group** (with O. Buchmueller)
- **Reconstruction of K0s in the CMS tracker (Energy flow group)**
 - ❑ Development of a dedicated **seeding in outer layers** of strip tracker
 - ❑ Development of a dedicated **V0 track finder**

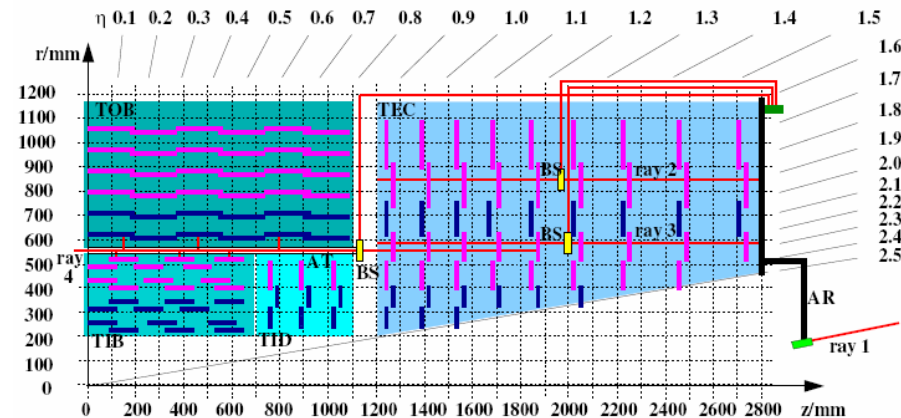
The CMS Tracker Alignment Challenge

O(16k) modules of Pixel and Strip tracker to be aligned to equal or better precision than intrinsic resolution of 10...50 μ

- **Determination of O(100k) alignment parameters**
- **Critical for performance of CMS tracker (e.g. b-tagging, W-mass)**
 - Example: $\sigma(M_W) \sim 15 \text{ MeV} \rightarrow$ alignment 10 μm in $r\phi$

Basic ingredients

- **Measurements from Construction**
 - Initial positions of modules and structures known to O(few 100 μ)
- **Laser Alignment System**
 - Can monitor only larger structures (TEC discs, TIB, TOB)
 - Pixel and TID not included!
- **Track based alignment**
 - Only way to carry out full alignment at sensor level
 - Requires large samples of tracks with different topologies (CPU, memory intensive, may require dedicated hardware)



- Misalignment implemented at reconstruction level by moving/rotating modules/layers etc
- Can be studied even at DST/RECO level using track refitter

Two misalignment scenarios developed for PTDR studies:

- **“first data” scenario**
 - ❑ Situation at LHC start-up (first few 100 pb⁻¹)
 - ❑ Construction information, LAS, pixel aligned with tracks
- **“long term” scenario**
 - ❑ After first few fb⁻¹ have been taken
 - ❑ Tracker aligned at the sensor level to ~20 μm

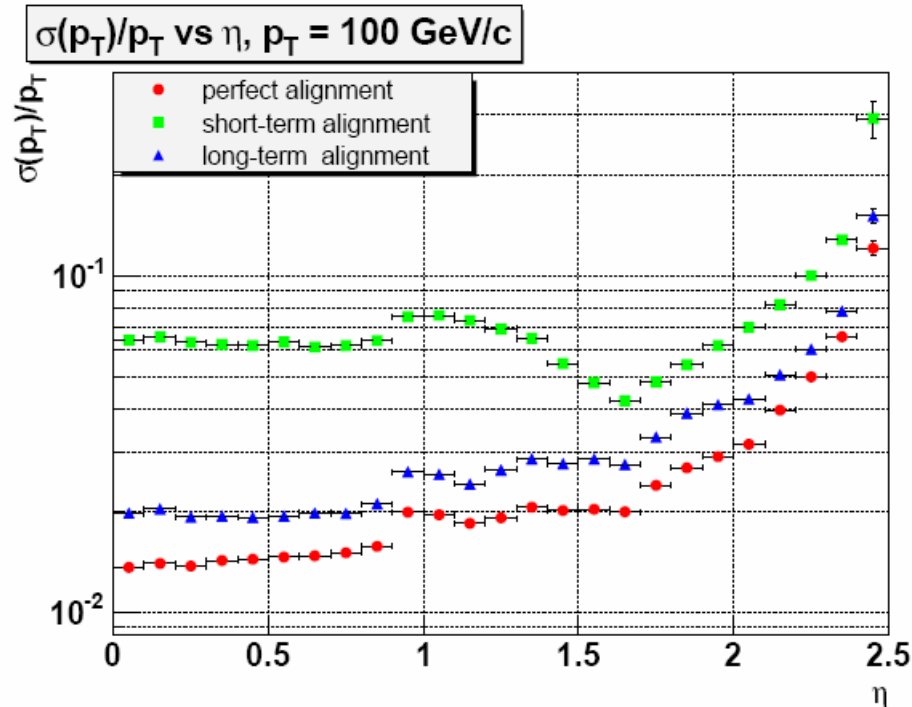
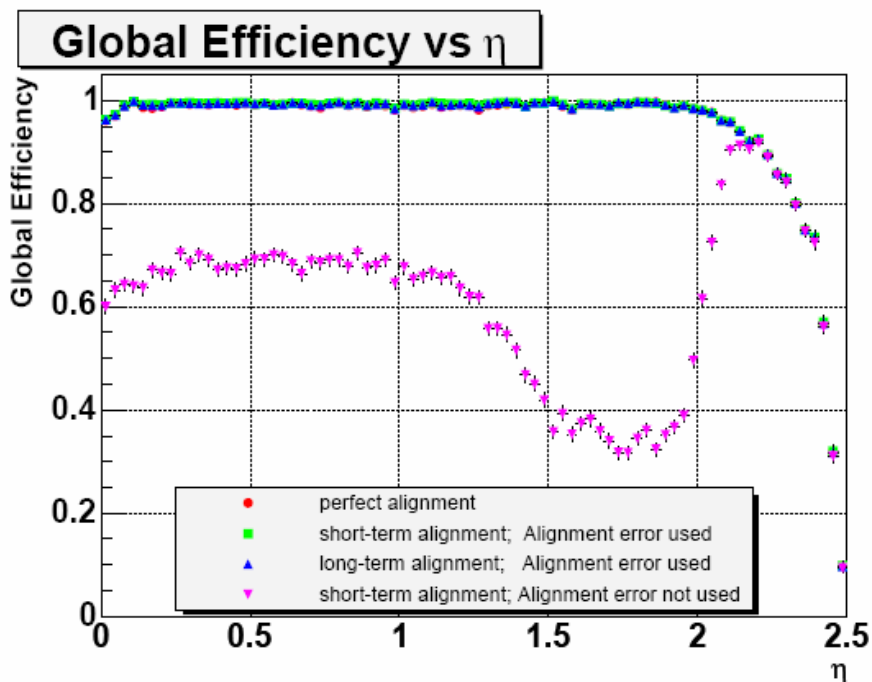
	Pixel		Silicon Strip			
	Barrel	Endcap	Inner Barrel	Outer Barrel	Inner Disk	Endcap
First Data Taking Scenario						
Modules	13	2.5	200	100	100	50
Ladders/Rods/Rings/Petals	5	5	200	100	300	100
Long Term Scenario						
Modules	13	2.5	20	10	10	5
Ladders/Rods/Rings/Petals	5	5	20	10	30	10

CMS-Note-2006/008

CMS-Note-2006/029

Impact of Misalignment

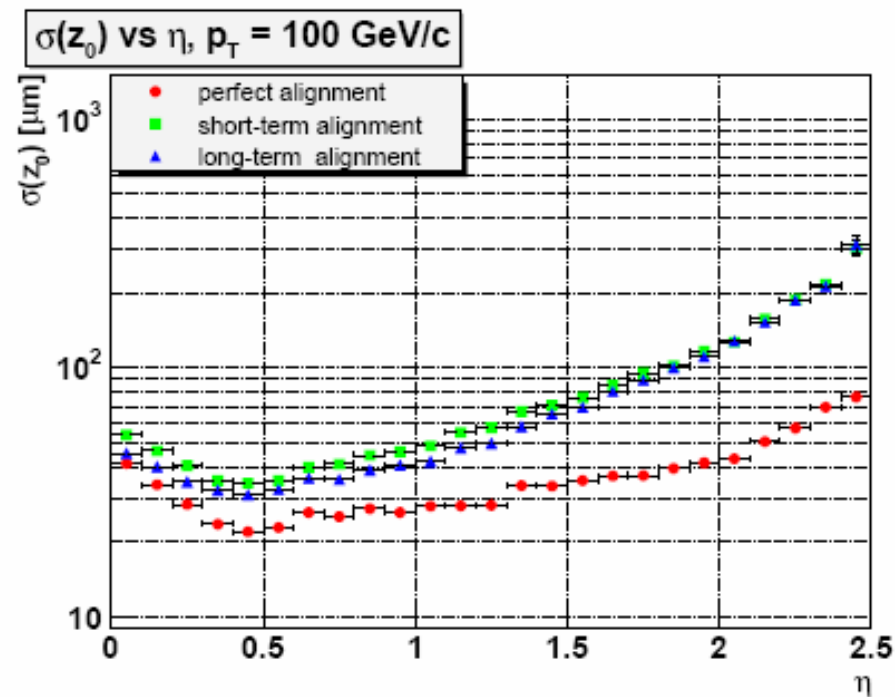
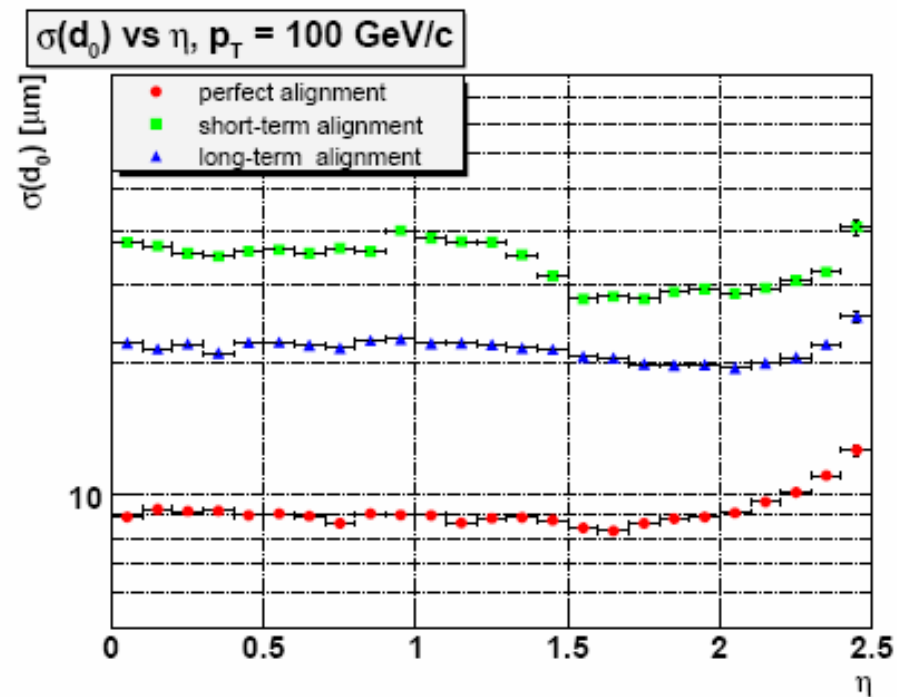
- Single muons with $P_t=100$ GeV (typical scale for LHC physics, resolutions not dominated by multiple scattering)



- Inefficiency in barrel, if alignment unc. not added to meas. error
- Worse in TID region (larger initial uncertainty from mounting)
- P_t resolution worse by factor ~ 5 for short-term scenario

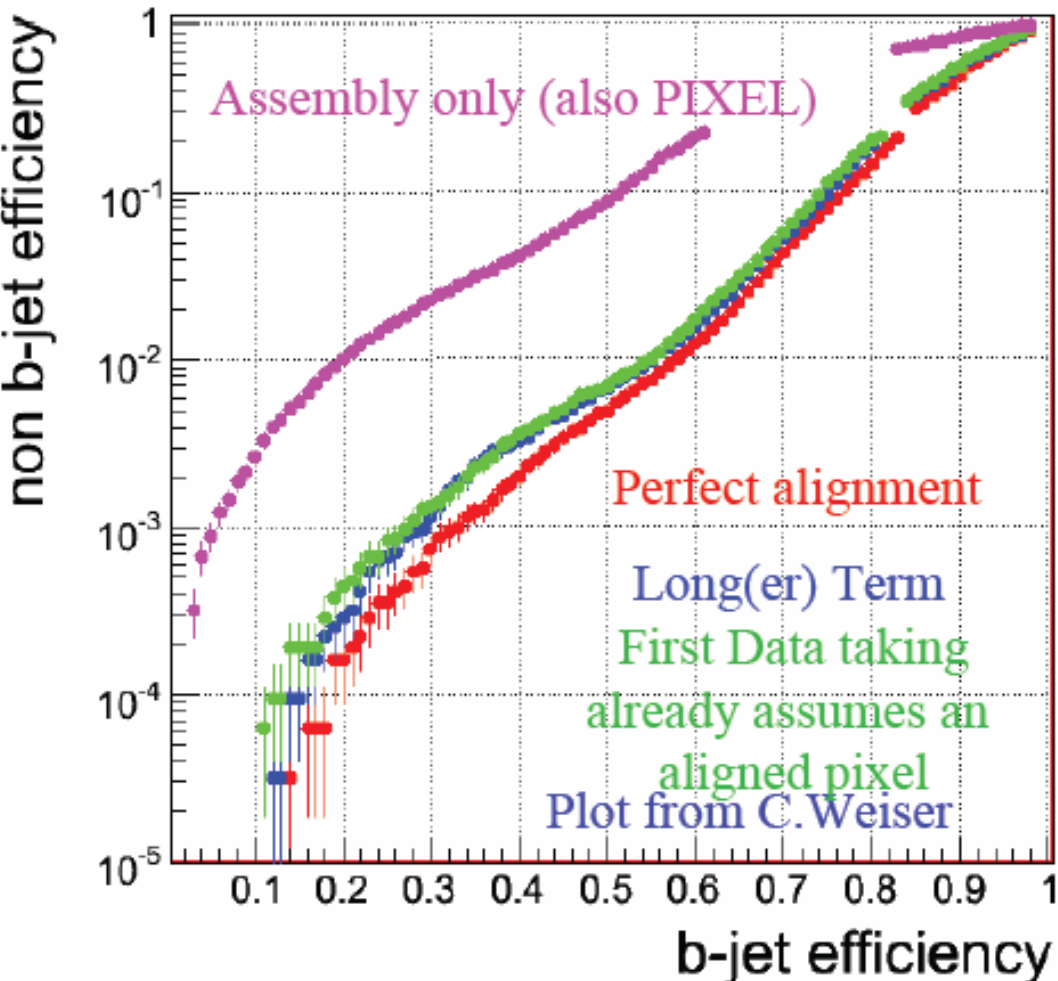
Impact of Misalignment

- Transverse and longit. Impact parameter resolution



- d_0 resolution $\sim 9, 35, 20$ μm (ideal, short term, long term)
- Note: Pixel detector assumed aligned even in short term scenario

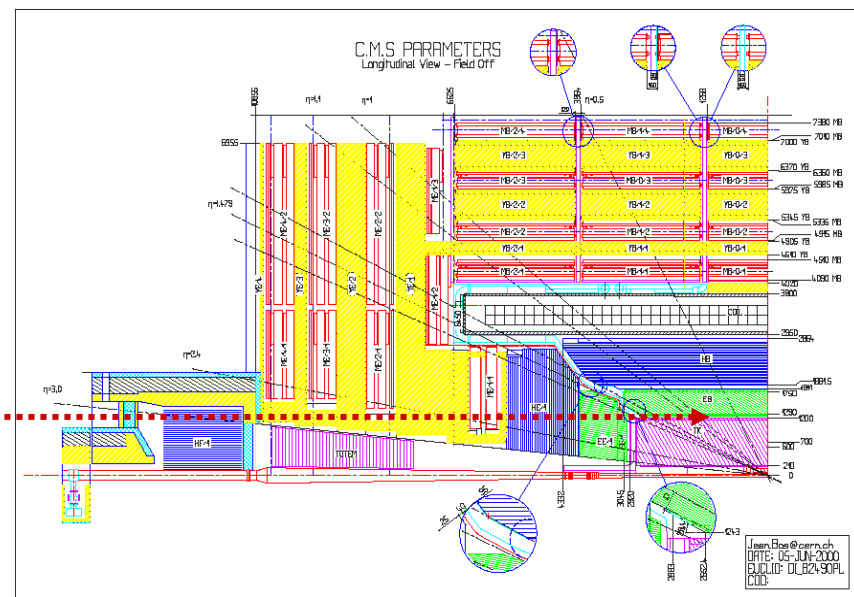
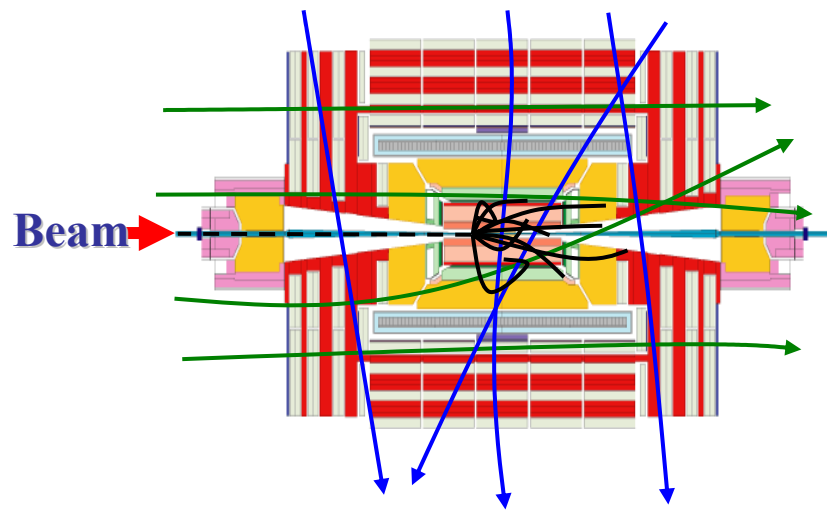
Impact of Misalignment



- No b-tagging performance with currently assumed assembly precision for pixel
- Fast Pixel alignment mandatory (also to provide reference for strip alignment)!

- Large number of alignment parameters (~100,000 in tracker) requires novel techniques
- Three different alignment algorithms implemented in CMS reconstruction software (now transition from “ORCA” to “CMSSW”)
 - ❑ Kalman Filter, Millepede-II, HIP Algorithm
 - ❑ Cross check results using different algorithms with different approaches and systematics
 - ❑ Supported by common software infrastructure
- Alignment using different data sets (dedicated MC generators)
 - ❑ Muons from Z,W; Cosmics; beam halo; muons from J/ψ, B; high pt QCD tracks
- Reduced data format (AlCaReco)
 - ❑ Development of fast Alignment stream (Z,W) produced during prompt reconstruction at Tier-0
- Combine track based alignment with laser alignment and survey data
- Employ mass and vertex constraints; use of overlaps
- Develop observables sensitive to misalignment other than χ^2
 - ❑ Monitoring, fix χ^2 invariant mode
- CMS alignment group ~20 people from ~8 institutes (Germany: Aachen, Hamburg)

- **High p_T muons from Z,W decays**
 - ❑ **Rate:** 20k $Z \rightarrow \mu\mu$, 100k $W \rightarrow \mu\nu$ per day at $L=2 \times 10^{33}$
 - ❑ **Gold plated for tracker alignment (small multiple scattering)**
 - ❑ **Exploit Z^0 mass constraint**
- **Cosmic Muons**
 - ❑ **~400Hz after L1 and s.a. muon reco.**
- **Beam Halo Muons**
 - ❑ **~5 kHz per side after L1 and s.a. muon**
 - ❑ **Problem: Muon endcap trigger outside tracker acceptance in R!**
 - ❑ **Potentially install scintillators (for startup) or use TOTEM T1**
- **Muons from J/ψ and inclusive B decays**
 - ❑ **J/ψ mass constraint**
- **Min. bias, high pt hadrons from QCD events**
 - ❑ **Potentially useful for pixel alignment**



Basic scetch:

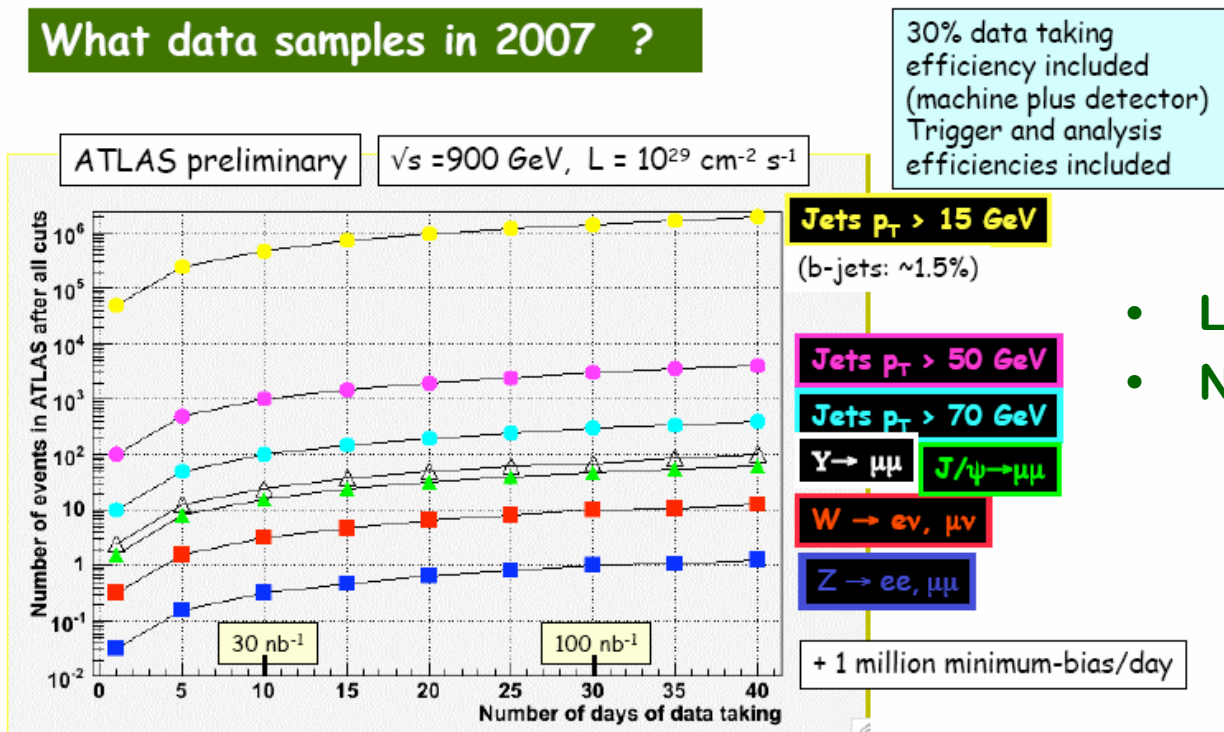
- 2007: Before beams:
 - ❑ Cosmics (+laser alignment and survey measurements)
- 2007: single beams
 - ❑ add beam halo muons
- 2007: Pilot run, pixel detector not installed (except few test modules)
 - ❑ Cosmics, beam halo muons
 - ❑ add available high pt muons, tracks
 - ❑ Initial alignment of high level strip tracker structur (layers, rods)?
- 2008: Two-step approach:
 - ❑ Add Larger statistics of muons from Z,W
 - ❑ 1. Standalone alignment of pixel detector
 - ❑ 2. Alignment of strip tracker, using pixel as reference
- To be laid out in more detail ...

See next slides
for rate estimates

Expected event rates

- Pilot run 2007 @ 900 GeV, $L \sim 10^{29}$

What data samples in 2007 ?



F. Gianotti (ICHEP 2006)

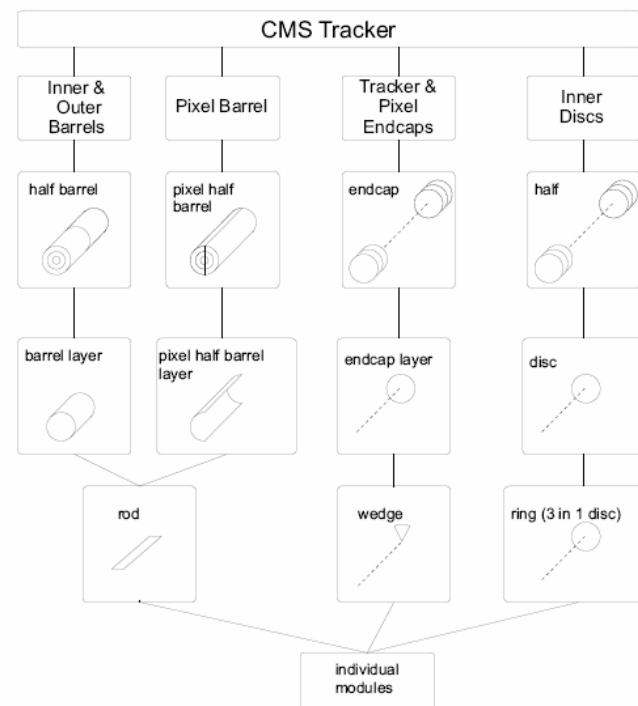
- Loads of min. bias, QCD jets
- Not much of anything else ...

- Physics Run 2008 @ 14 TeV, $L \sim 10^{32...33}$

Luminosity	$10^{32} \text{ cm}^{-2} \text{ s}^{-1}$		$2 * 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$		
Time	few weeks	6 months	1 day	few weeks	one year
Int. Luminosity	100 pb^{-1}	1 fb^{-1}		1 fb^{-1}	10 fb^{-1}
$W^\pm \rightarrow \mu^\pm \nu$	700K	7M	100K	7M	70M
$Z^0 \rightarrow \mu^+ \mu^-$	100K	1M	20K	1M	10M

- Large statistics of high p_T muons within few weeks!

- (MIs)alignment implemented at reconstruction level:
 - ❑ “Misalignment tools”, move and rotate modules or higher level structures
- Dedicated “Misalignment Scenarios”
 - ❑ Short term scenario
 - o First data taking (few 100 pb^{-1})
 - o Pixel already aligned
 - o Strip tracker misaligned, only survey and laser alignment
 - ❑ Long term scenario
 - o Few fb^{-1} accumulated
 - o Full alignment performed, residual misalignments $\sim 20 \mu\text{m}$
- Fast track refit (without redoing pattern recognition)
- Reduced data format containing only alignment tracks
 - ❑ Small file size, fast processing



- Algorithms implemented in standard CMS reconstruction software using a **common layer of general functionality**
 - ❑ Management of parameters and covariances
 - ❑ Derivatives wrt track and alignment parameters
 - ❑ I/O, Database connection

HIP Algorithm: Formalism

- Minimization of track impact point (x) - hit (m) residuals in local sensor plane as function of alignment parameters

$$\epsilon = \begin{pmatrix} \epsilon_u \\ \epsilon_v \end{pmatrix} = \begin{pmatrix} u_x - u_m \\ v_x - v_m \end{pmatrix}$$

- χ^2 function to be minimized on each sensor (after many tracks per sensor accumulated)

$$\chi^2 = \sum_i \epsilon_i^T V_i^{-1} \epsilon_i$$

□ V: covariance matrix of measurement

- Linearized χ^2 solution:

□ δp : vector of alignment parameters

$\delta p = (\delta u, \delta v, \delta w, \delta \alpha, \delta \beta, \delta \gamma)$

□ J_i : derivative of residuals w.r.t. alignment parameters

$$\delta p = \left[\sum_i J_i V_i^{-1} J_i^T \right]^{-1} \left[\sum_i J_i V_i^{-1} \epsilon_i \right]$$

- Local solution on each “alignable object”

□ Only inversion of small (6x6) matrices, computationally light

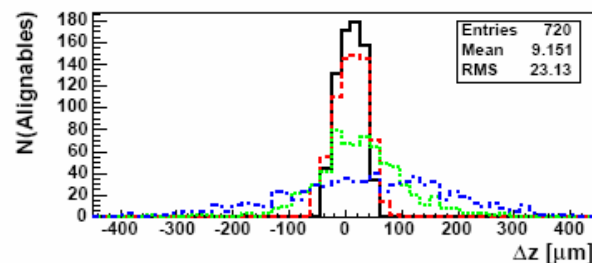
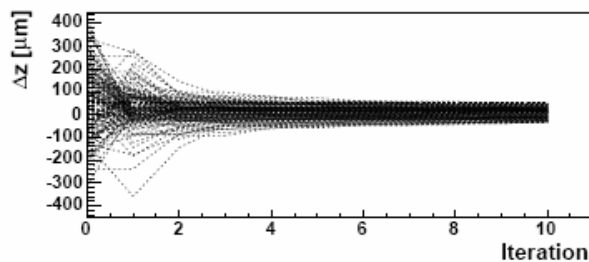
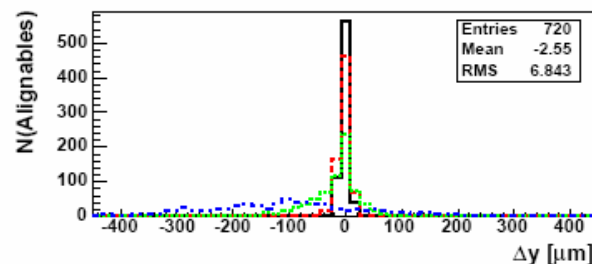
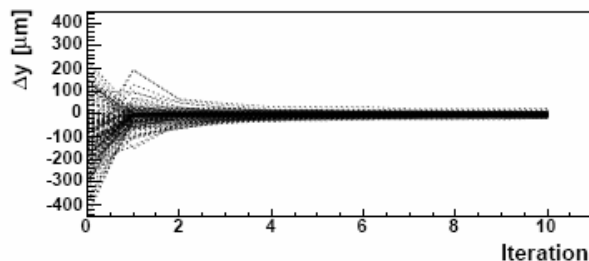
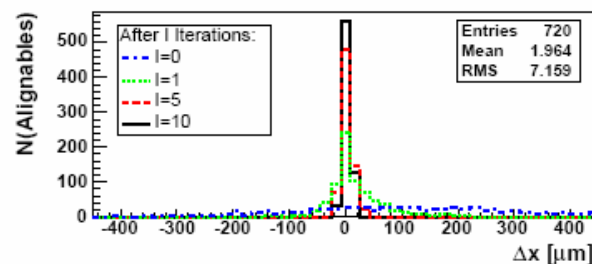
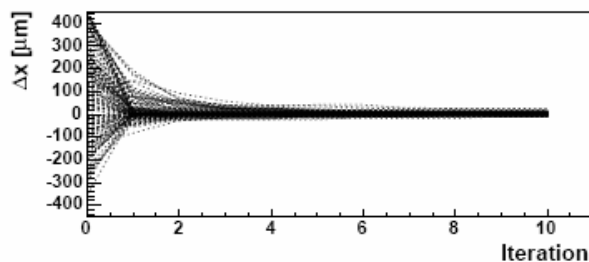
CMS Note 2006/018

- o Formalism extended to **alignment of composite detector structures** (ladders, disks, layers etc.)
 - o Minimize χ^2 using all tracks crossing sensors of composite object with respect to alignment parameters of composite object
 - o Implemented using chain rule
- o Correlations between modules not included explicitly
- Implicitly included through iterations
- Large statistics \rightarrow **parallel processing**:
 - ❑ Run on N cpu's processing 1/N of the full sample each
 - ❑ Combine results from all CPUs, compute alignment corrections
 - ❑ Start next iteration on N cpu's

$$\frac{\delta \epsilon_i^S}{\delta p_i^C} = \frac{\delta \epsilon_i^S}{\delta p_i^S} \times \frac{\delta p_i^S}{\delta p_i^C}$$

- **Example: 1M $Z \rightarrow \mu\mu$ events:**
 - ❑ reduced DST format keeps only muon tracks
 - ❑ Refit track, don't re-reconstruct
 - ❑ With 20 CPUs in parallel, **one iteration: ~45'**

- Alignment of 720 CMS Pixel Barrel modules
- “First data taking” misalignment scenario
 - Includes correlated misalignments
- 200K $Z^0 \rightarrow \mu^+ \mu^-$ events, 10 iterations



- Good convergence: RMS $\sim 7\mu\text{m}$ in x, y $\sim 23\mu\text{m}$ in z

- Caveat: Alignment w.r.t ideal strip tracker

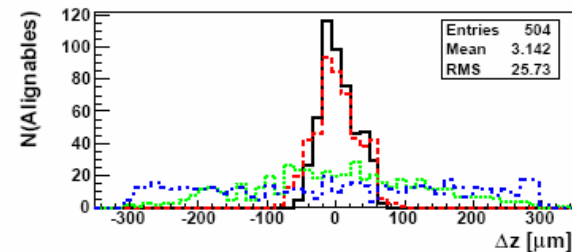
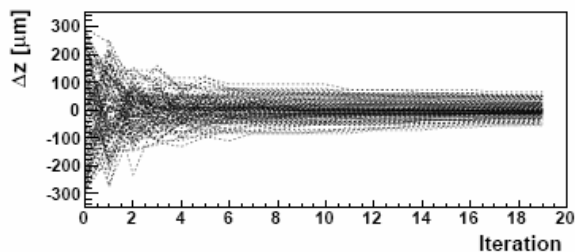
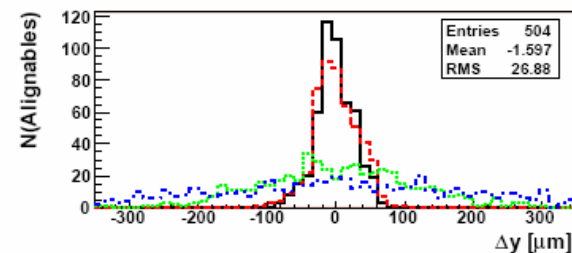
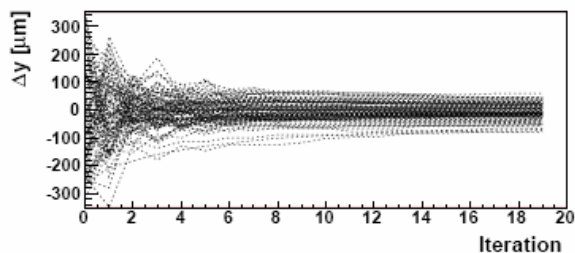
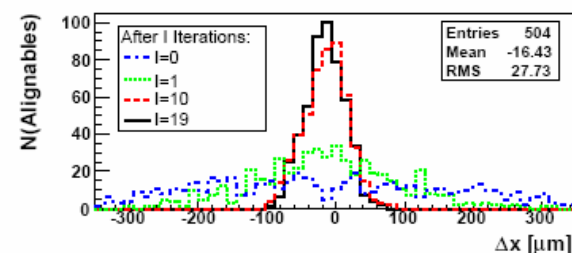
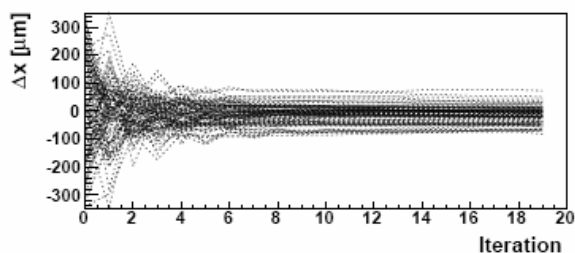
CMS Note 2006/018

- Standalone alignment of pixel modules
- Minimize influence of misaligned strip detector:

- ❑ refitting only pixel hits of the tracks
- ❑ use momentum constraint from full track (significantly improves convergence)

- Two muons from $Z^0 \rightarrow \mu^+ \mu^-$ are fitted to common vertex
- Flat misalignment $\pm 300 \mu\text{m}$ in x,y,z
- 500k events, 19 iterations

- Reasonable convergence, RMS $\sim 25 \mu\text{m}$ in all coordinates



CMS Note 2006/018

- Method for global alignment derived from Kalman Filter track fitter
- Ansatz:
 - ❑ measurements m depend via track model f not only on track parameters x , but also on alignment parameters d :

$$m = f(x, d) + \epsilon \quad \text{COV}(\epsilon) = V$$

- ❑ Update equation of Kalman Filter:

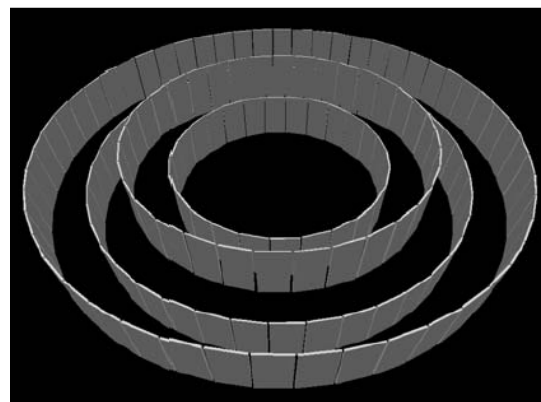
$$\begin{pmatrix} \hat{d} \\ \hat{x} \end{pmatrix} = \begin{pmatrix} d \\ x \end{pmatrix} + K(m - c - Ad - Bx)$$

- Iterative: Alignment Parameters updated after each track
- Global: Update not restricted to modules crossed by track
 - ❑ Update can be limited to those modules having significant correlations with the ones in current trajectory
 - ❑ Requires some bookkeeping
 - ❑ No large matrices to be inverted!
- Possibility to use prior information (e.g. survey data, laser al.)
- Can add mass / vertex constraints

CMS Note 2006/022

Kalman Filter Alignment (cont.)

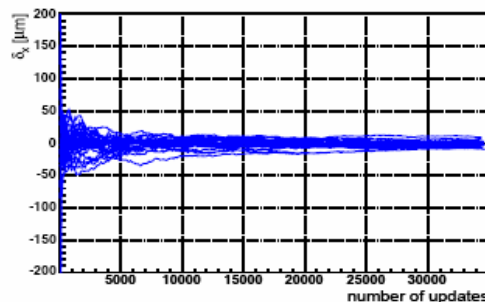
- Wheel-like setup: (part of CMS tracker: 156 TIB modules)
- Pixel detector as reference
- Misalignment:
 - local x, y $\sigma = 100 \mu\text{m}$



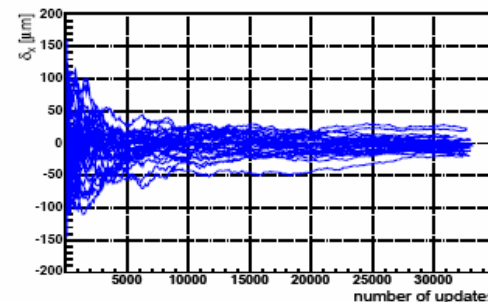
- Single muons $p_T = 100 \text{ GeV}$

- Convergence slower in outer layers (distance from reference system, less track statistics)

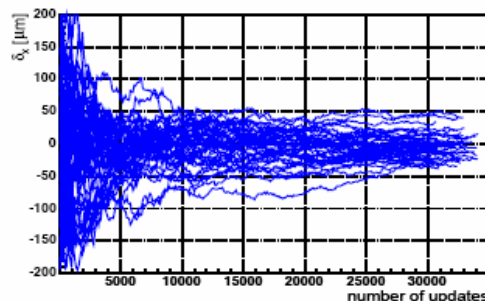
Layer 1



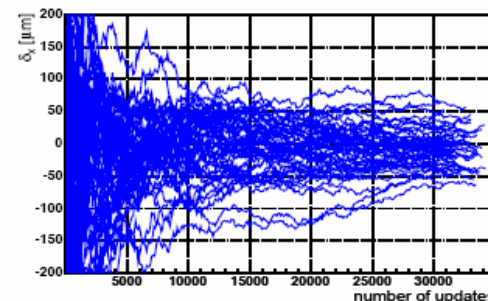
Layer 2



Layer 3

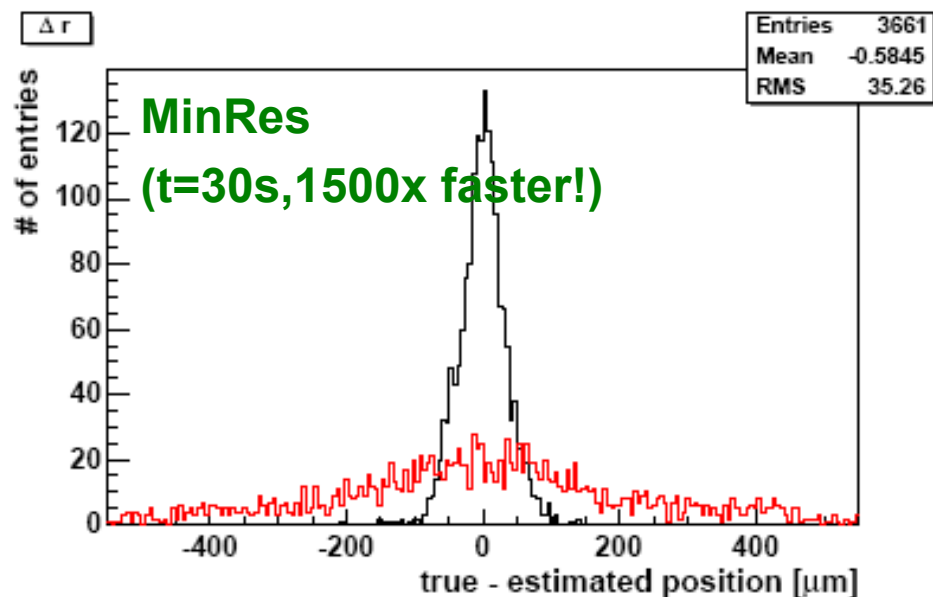
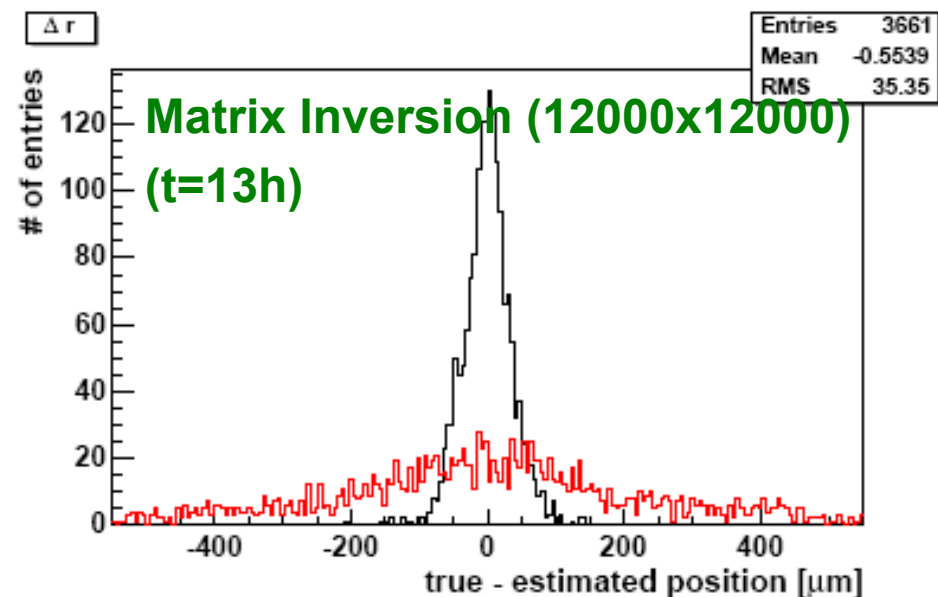


Layer 4

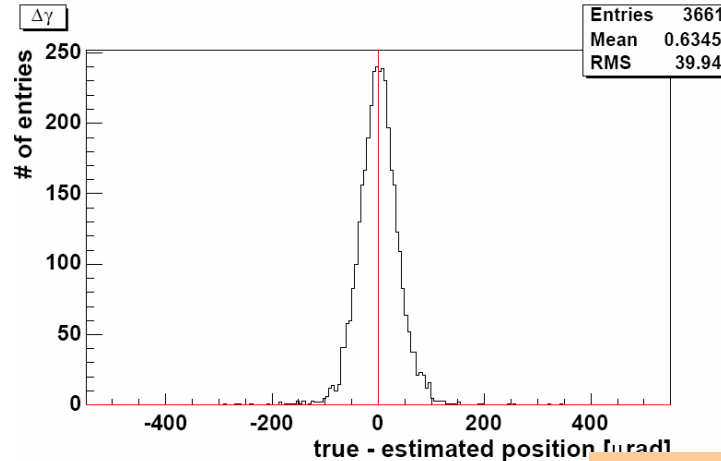
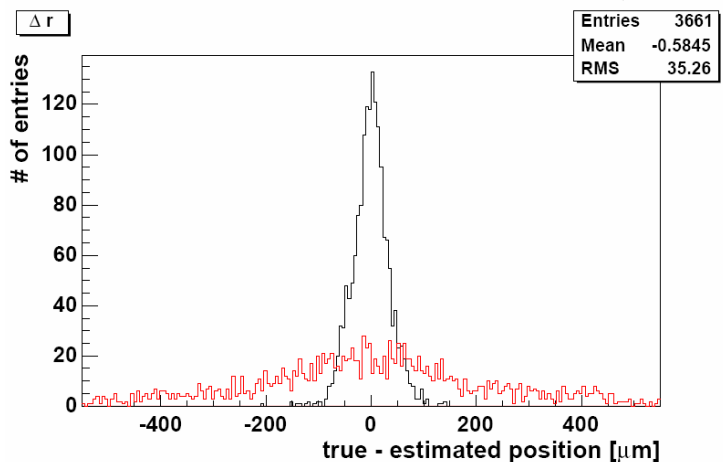
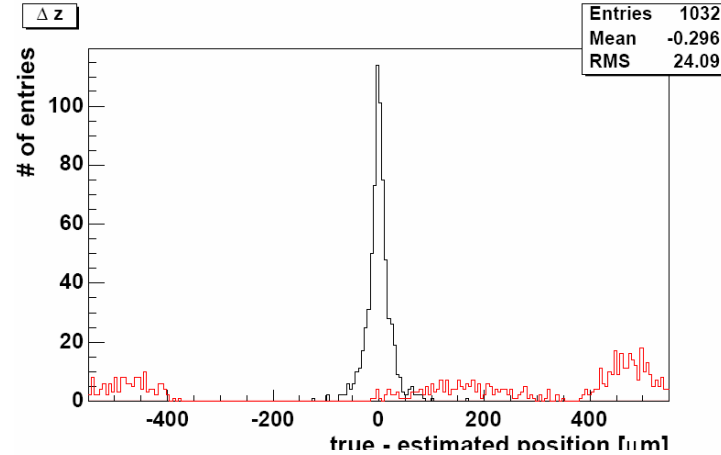
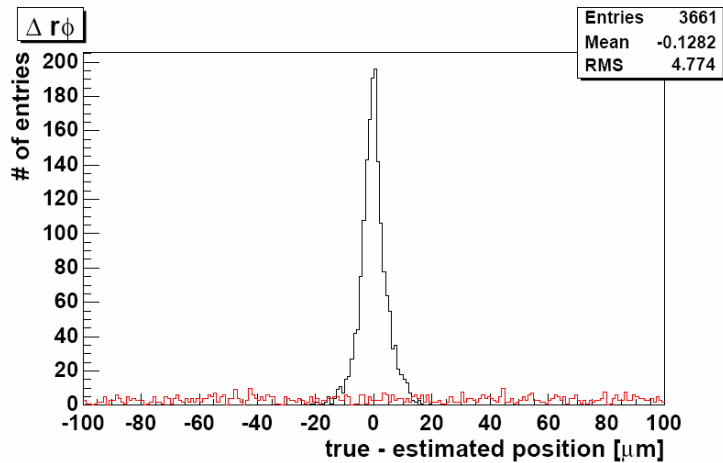


CMS Note 2006/022

- **Global chi2 minimization, fitting (local) track and (global) alignment parameters at once**
 - Correlations between modules included
 - No iterations needed
- **Original Millepede method solves matrix eqn. $Ax = B$, by inverting huge matrix A. Can only be done for <12000 alignment parameters**
- **New Millepede II method instead minimises $|Ax - B|$. Expected to work for ~100000 alignment parameters (i.e. for full CMS at sensor level)**

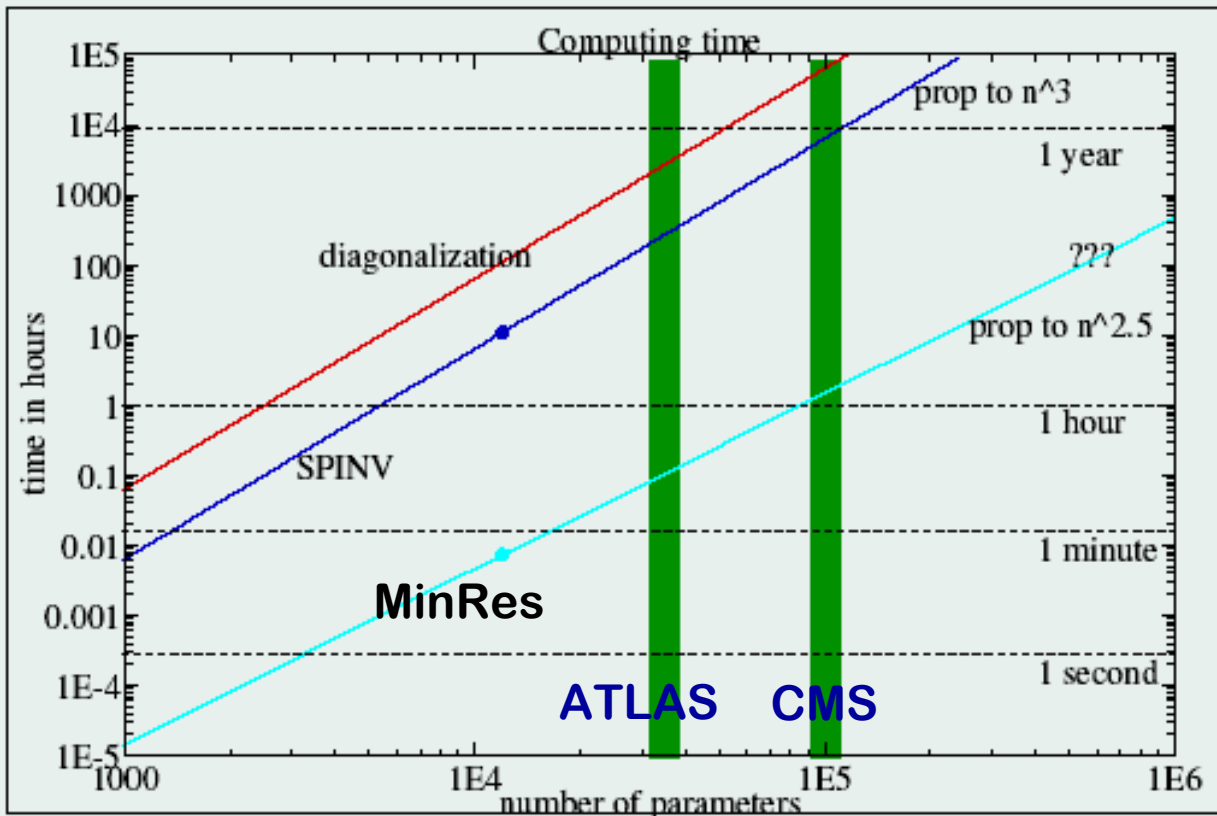


- Alignment of the strip tracker at sensor level
- Barrel region, $|\eta| < 0.9$, 12015 alignment parameters
- (Mis)alignment in $r\phi$, r , z , γ at half-barrel / layer / rod / module levels



CMS Note 2006/011

CPU time in hours as a function of number of parameters



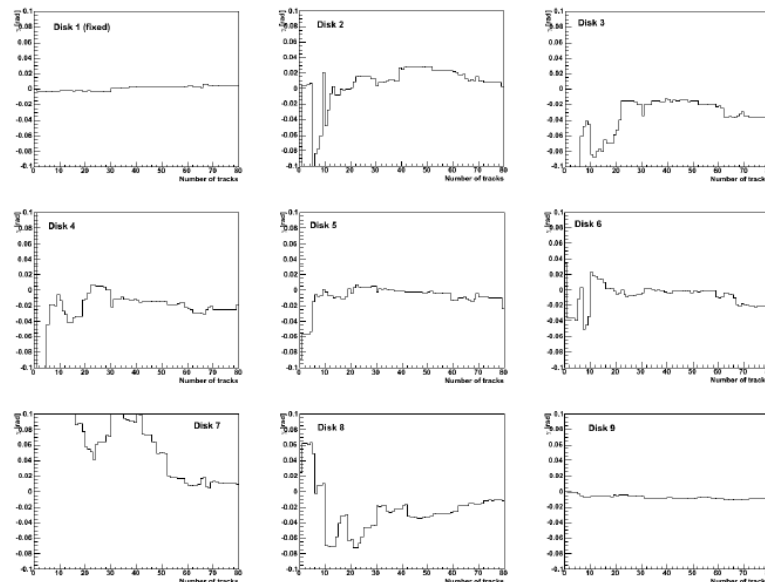
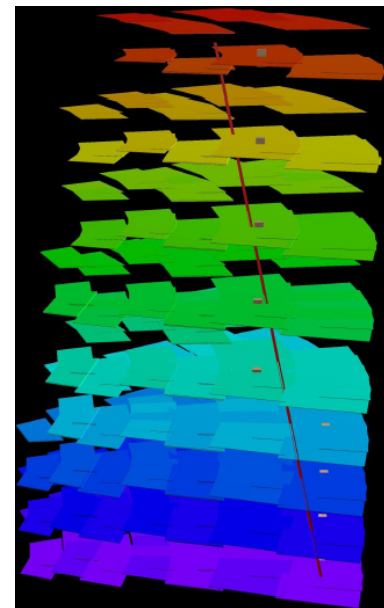
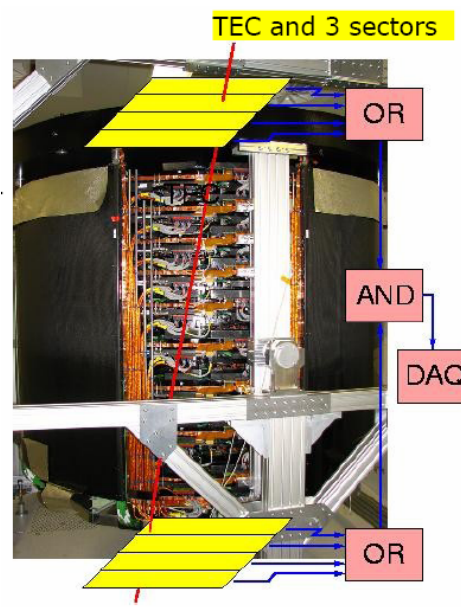
CPU Time for CMS (100k parameters):

- **Diagonalization**
~10 year on one CPU
- **Inversion**:
~1 year on one CPU
- **Iteration**:
~1 h at one CPU

- **New Millepede-II (iterative method) scalable to full CMS problem**
- **Alternative: massively parallel algorithm (difficult to implement)**
- **Memory needs (dep. on sparseness of matrix) under study...**

- **Aachen (L. Feld, F. Raupach, M. Weber):**
 - ❑ 2nd Implementation of the Kalman filter algorithm
 - ❑ Alignment studies of TEC+ with cosmics
- **Hamburg (G. Flucke, P. Schleper, G. Steinbrueck, M. Stoye):**
 - ❑ Close collaboration with V. Blobel (MillePede developer)
 - ❑ Implementation of MillePede I and II for CMS
 - ❑ Alignment studies for PTDR-I
 - ❑ Alignment with simulated cosmics
 - ❑ Study of monitoring observables other than χ^2 (e.g. sensitive to global distortions)
- **Aachen+CERN**
 - ❑ **Prepare proposal for Alignment @ TIF**
 - o Validate alignment software with real data and real geometry
 - o Balance against many constraints (schedule, lead thickness below ST etc)

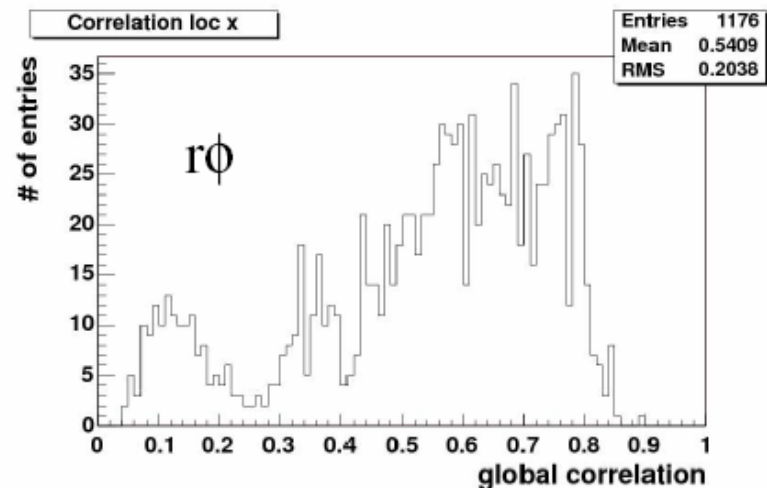
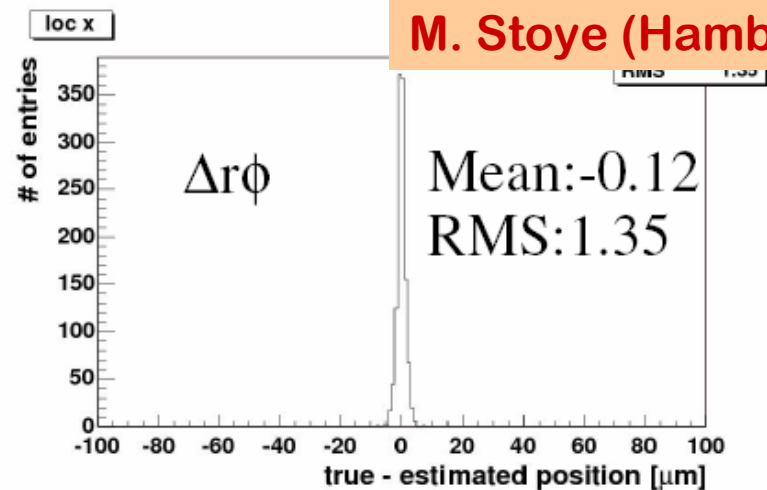
- Updating/debugging geometry
- Kalman Filter alignment algorithm implemented
- First results obtained with small statistics, ongoing ...
- Plans:
 - ❑ Compare alignment with LAS
 - ❑ Implement Millepede and compare with Kalman filter
- First low statistics results aligning disks 2-8 (1,9 fixed)



Importance of using "complete" datasets (Hamburg)

- Collision tracks and cosmics populate different parts of global covariance matrix → **reduce global correlations!**
- Example: Alignment of CMS strip barrel rods and layers
 - ❑ Only one layer fixed
 - ❑ 500k $Z^0 \rightarrow \mu\mu$ with vertex constraint
 - ❑ 100k Cosmics
- Use Z^0 tracks only:
 - ❑ No solution
 - ❑ Matrix singular
- Use Z^0 and Cosmics:
 - ❑ Problem solvable
 - ❑ Reasonable correlations

M. Stoye (Hamburg)



**Simplified simulation and scenario,
Now look at realistic study ...**

χ^2 invariant deformations (Hamburg)

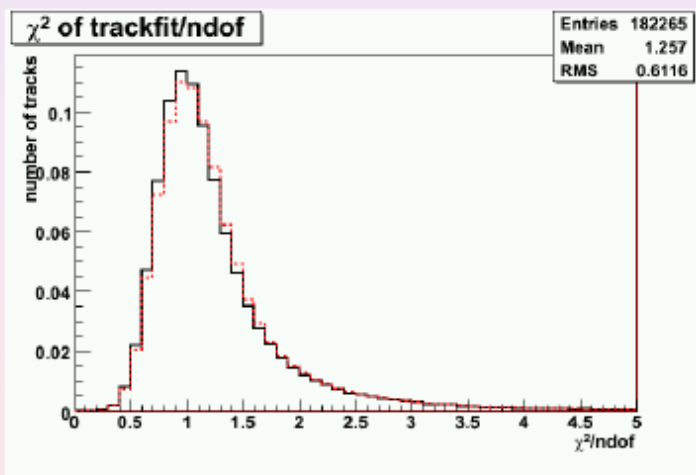
Motivation
 χ^2 Invariant Deformations

The Deformations
Fixing the Deformations

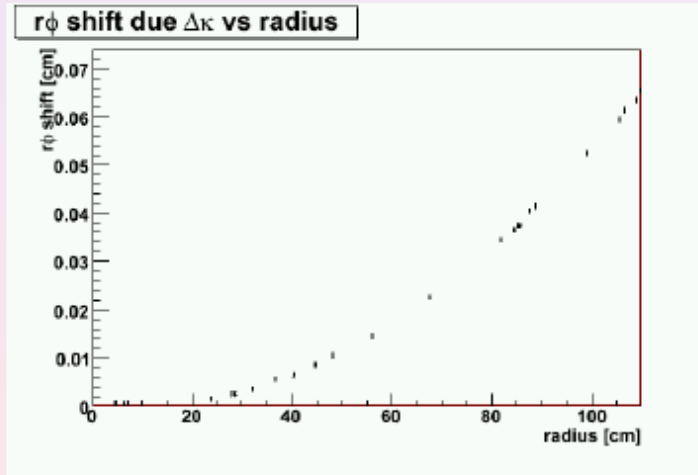
Example: Curvature

The average curvature is changed via misalignment

The difference in the $\frac{\chi^2}{ndof}$ is very small, the shift due to misalignment up to 700 μm



black: ideal
red: misaligned







misalignment in $r\phi$ vs radius of sensor position

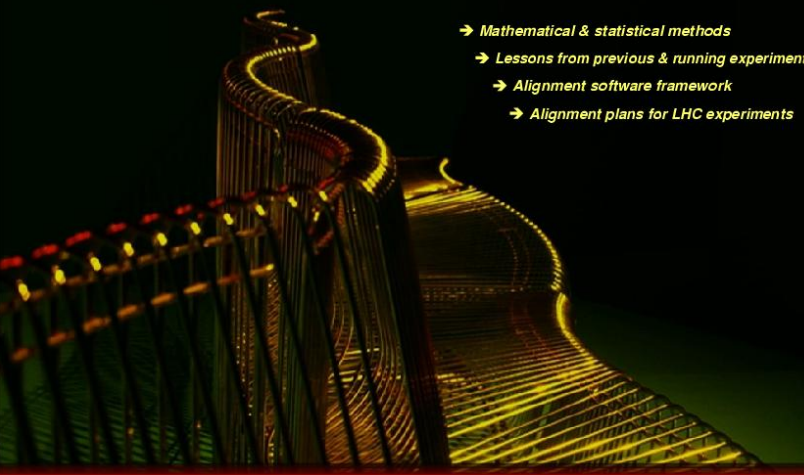
1st

LHC Detector Alignment Workshop

4-6 September 2006
CERN, Geneva

The aim of the workshop is to exchange ideas and information on the issues related to alignment of detectors





- Mathematical & statistical methods
- Lessons from previous & running experiments
- Alignment software framework
- Alignment plans for LHC experiments

More Information : <http://lhc-detector-alignment-workshop.web.cern.ch>

Organising Committee :

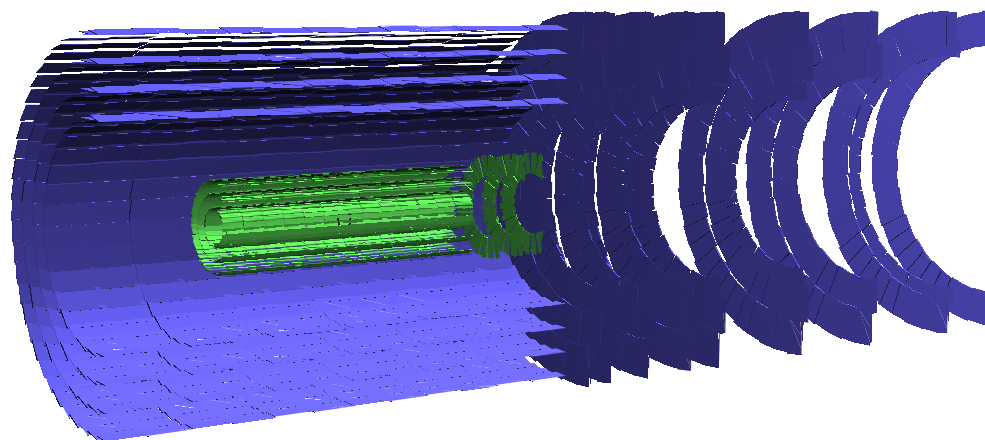
S. Blusk	(Syracuse)
O. Buchmuller	(CERN)
A. Jacholkowski	(Catania)
S. Marti i Garcia	(Valencia)
T. Ruf	(CERN)
K. Safarik	(CERN)
J. Schieck	(Munich)
S. Viret	(Glasgow)

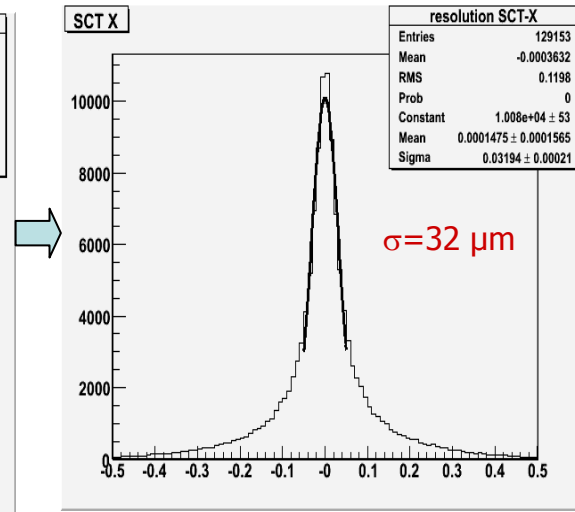
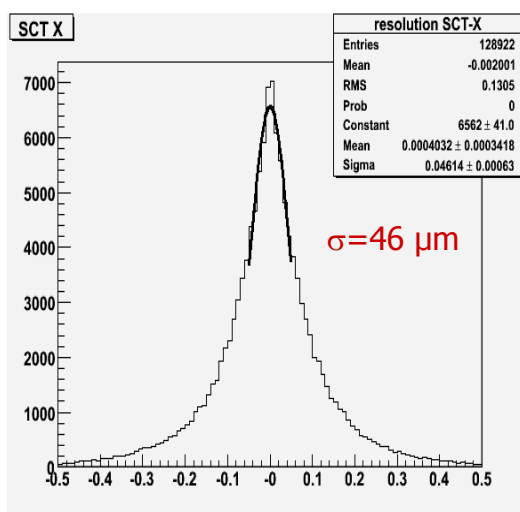
Sponsored by LCG and CERN PH department

- CMS initiative
- Alignment strategies of 4 LHC experiments
- Experience from other experiments
- External algorithm experts (V. Blobel, R. Fruehwirth)
- Workshop page
<http://physics.syr.edu/~lhcb/public/alignment/LHCAlignmentWorkshop/>
- Featured in this week's CMS times
http://cmsinfo.cern.ch/outreach/CMS/2006/09_11/index.html

- Atlas Inner Detector: Pixel+SCT+TRT
 - “only”~36000 parameters
- Three algorithms considered
 - “Robust alignment”
 - Minimization of residuals, overlaps
 - Local chi2 approach
 - Equivalent to CMS HIP algorithm
 - Global chi2 approach
 - Equivalent to MillePede-I
 - ~32 nodes in parallel
- Misalignment only possible at simulation level (cpu intensive)
- More experience with real data
 - 2004 Combined test beam
 - Cosmics at surface build.

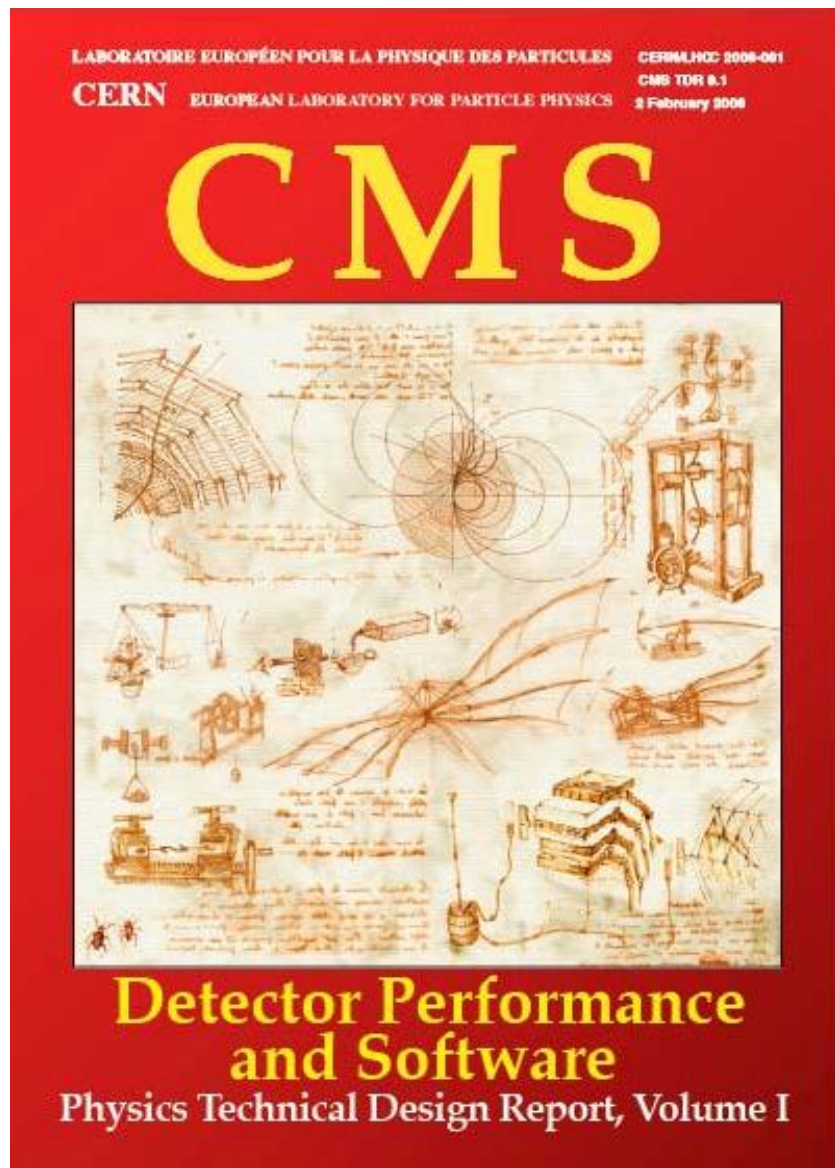


- Global chi2 with 250k SR1 tracks



- **Alignment of the CMS tracker and muon system is a challenge**
 - ❑ Large number of parameters (~100,000 in tracker)
 - ❑ High intrinsic resolution of devices
- **A lot of ongoing work on track based alignment already now**
 - ❑ Implementation and further development of algorithms
 - o Initial results promising
 - o Not yet demonstrated realistic alignment of full tracker at sensor level
 - ❑ Alignment studies using various MC data sets
 - ❑ Dedicated HLT alignment stream
 - ❑ Use of overlaps, mass and vertex constraints
 - ❑ How to combine with Laser Alignment and Survey?
 - ❑ Define monitoring observables other than χ^2 (“global modes”)
 - ❑ Condition Database infrastructure
- **Alignment of test beam and cosmics data**
 - ❑ Tracker “Cosmic Rack” test structure
 - ❑ Magnet Test & Cosmic Challenge (MTCC) data
- **Aim for having all ingredients in place when data will arrive!**

BACKUP



- **Section 6.6 “Alignment”**
 - ❑ 14 pages summary of work done so far (Feb 2006)
- **8 accompanying CMS Notes**
- **Contents**
 - ❑ Alignment strategy and data samples
 - ❑ Simulation and impact of misalignment
 - ❑ Track based alignment algorithm studies
 - ❑ Alignment of test beam data
- **Impact of misalignment also studied in several physics analyses documented in Vol.2**

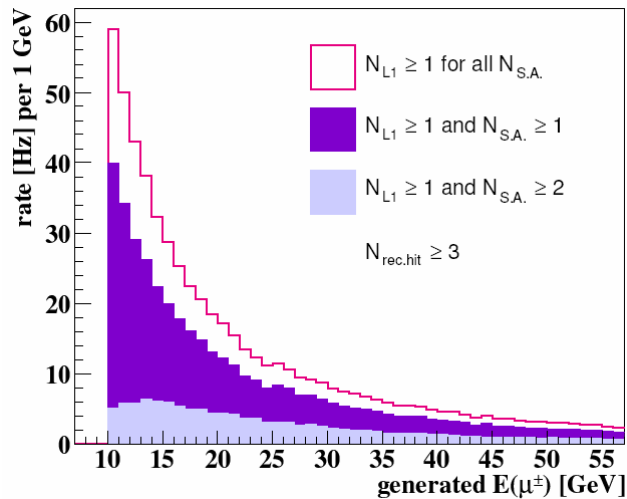
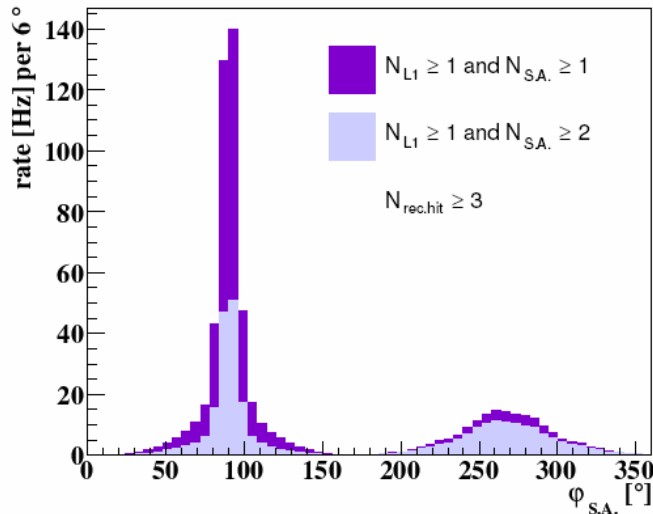
- A lot of effort of work and documentation by many groups
- Algorithms and applications
 - ❑ CMS 2006/022 -- A Kalman Filter for Track Based Alignment
 - ❑ CMS 2006/018 -- The HIP Algorithm for Track Based Alignment and its Application to the CMS Pixel Detector
 - ❑ CMS 2006/006 -- Alignment of the Cosmic Rack with the HIP Algorithm
 - ❑ CMS 2006/011 -- Software Alignment of the CMS Tracker using MILLEPEDE II
 - ❑ CMS 2006/016 -- Muon System alignment with tracks
- Misalignment simulation and Physics Impact
 - ❑ CMS 2006/008 -- Simulation of Misalignment Scenarios for CMS Tracking Devices
 - ❑ CMS 2006/029 -- Impact of CMS Silicon Tracker Misalignment on Track and Vertex Reconstruction
 - ❑ CMS 2006/017 -- Influence of Misalignment Scenarios on Muon reconstruction

Three algorithms being studied in CMS (using common software):

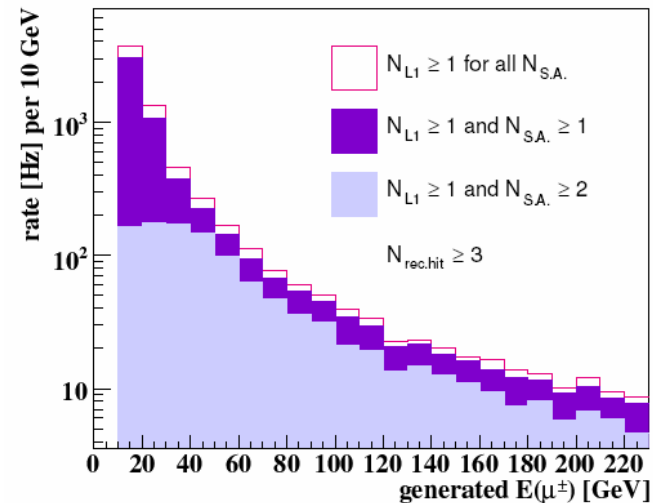
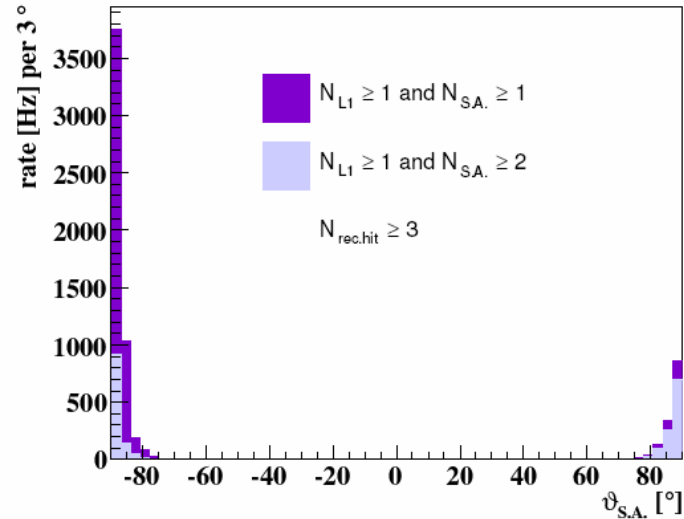
- **Kalman filter (Vienna, Aachen) CMS-Note-2006/022**
 - ☐ Parameters and correlations updated after each track
 - ☐ No large matrix inversions, but book-keeping of relevant correlations
- **Millepede (Hamburg) CMS-Note-2006/011**
 - ☐ Used successfully in other experiments (e.g. CDF, H1)
 - ☐ New version Millepede-II, expected to be scaleable to CMS problem (see next slides)
- **HIP Algorithm (Helsinki, CERN) CMS-Note-2006/018**
 - ☐ Robust approach, no large matrices (ignores module correlations)
 - ☐ Pixel alignment
- **Successfully used to align**
 - ☐ parts of CMS tracker in simulation
 - ☐ the TOB Cosmic Rack with real data
 - ☐ Working on demonstrating scaleability to full CMS tracker

Simulation of Cosmics and Beam halo muons in CMS

- Cosmic muons: 400 Hz**

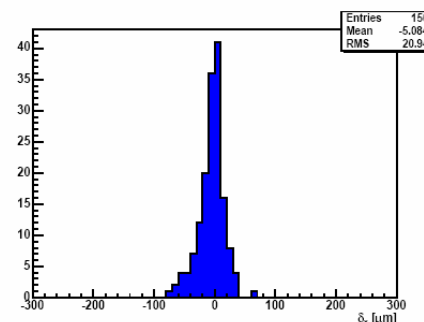
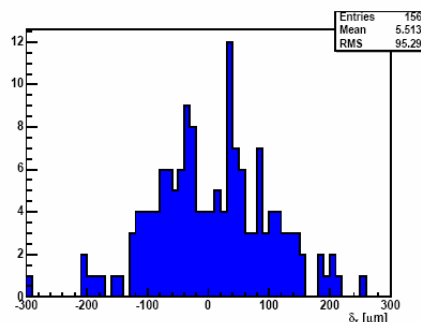


- Beam halo muons: 5 kHz per side**



Kalman Filter Alignment (cont.)

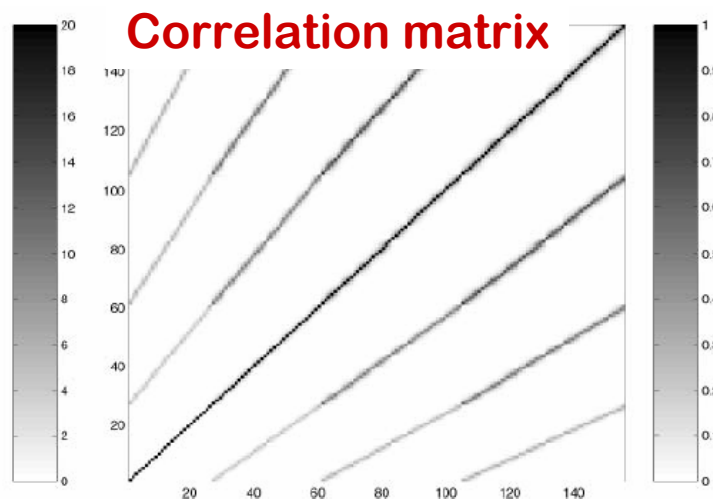
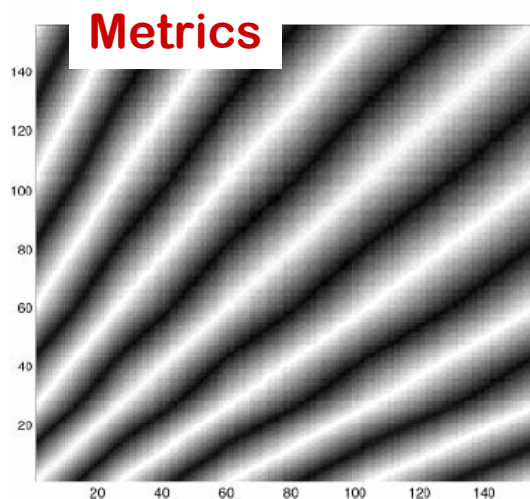
- Overall RMS $\sim 21\mu\text{m}$ after alignment



- Dependence of RMS and CPU time on d_{max}

d_{max}	1	2	3	4	5	6
σ [μm]	24.75	21.38	20.97	20.95	20.94	20.94
T [s]	472	604	723	936	1152	1319

- $d_{\text{max}}=6$ does not exclude modules with relevant correlations



CMS Note 2006/022

M. Stoye (Hamburg)

- Realistic alignment scenario of the CMS pixel and strip barrel studied
- Datasets and prior information:
 - ❑ 250k $Z^0 \rightarrow \mu\mu$ with vertex constraint
 - ❑ 500k Cosmics
 - ❑ Survey information
- Global correlations of alignment parameters high (can be >99%)
 - ❑ Independent of alignment algorithm!
- Cosmics (and beam halo, shifted vertex?!) very important to decrease global correlations!

Correlations of translations in x

- layers/halfbarrels and
- halfbarrels/CMS

