# Reserve Accumulation and the Currency Composition of Sovereign Debt

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### A puzzle in risk

#### Three facts

- 1. International reserves help central banks hedge risks
- 2. Local-currency debt mitigates risks by promising lower real payments in bad times
- 3. Countries which issue LC debt also hold more reserves

How to make sense of this?

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### Local currency debt is a two-edged sword

#### Two effects

#### LC debt reacts to RER

- · RER depreciates in recessions
- ⇒ LC debt builds in state-contingency

#### Gov't can affect RER

- · Planner modulates demand
- ⇒ LC debt boosts these incentives

- Affecting the RER costly: prefer to pay with reserves
- Affecting the RER costly ex-ante: prefer to accumulate reserves

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### A model of LC sovereign debt and reserves

#### Ingredients

- Small-open economy borrowing from RoW
- · Two-sector structure, nominal rigidities
  - Aggregate-demand externality
  - · Modulate labor demand (in all sectors) through consumption (of tradables)
- Government issues long-term debt, accumulates reserves
- · No commitment to (i) repayment, (ii) future borrowing decisions
- Debt in domestic or foreign currency
- Compare with synthetic LC debt

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### Main findings

- 1. Significant reserve holdings to curtail time-inconsistency
  - · Synthetic LC debt issuer holds twice as many reserves as LC debt issuer
- 2. Incentives vs. insurance
  - FC debt  $\rightarrow$  LC debt  $\sim$  0.15% of permanent consumption
  - · 0.46% to move to synthetic LC debt

#### Relation to the literature

· Sovereign debt and default

· Reserves for macroeconomic stabilization

· Currency composition of sovereign debt .

### Roadmap

Evidence

Model

Quantitative Results Synthetic Debt

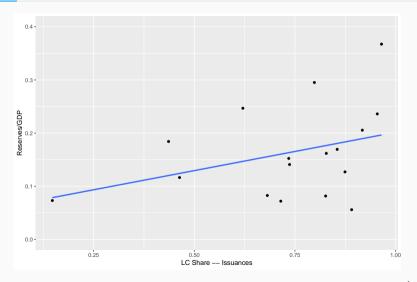
**Concluding Remarks** 

## Evidence

### Local currency debt and reserves

Local currency share of debt issued from Ottonello and Perez (2019)

FX reserve holdings from IFS



## Model

### Two-sector small-open economy structure

### Supply

- Traded goods
  - Exogenous endowment  $y_T = \exp(z)$ , can be exported/imported

$$z' = \rho_z z + (1 - \rho_z)\mu_z + \sigma_z \epsilon'$$

with 
$$\epsilon \stackrel{\textit{iid}}{\sim} \mathcal{N}(0,1)$$

Nontraded goods, produced

$$y_N = h^{\alpha}$$

with labor supply h (inelastic up to  $ar{h}$ ) =1

#### Demand

- Households consume both goods
  - Standard CRRA preferences  $\frac{c^{1-\gamma}-1}{1-\gamma}$
  - CES aggregator

$$c = \mathcal{C}(c_N, c_T) = \left[\varpi_N c_N^{-\eta} + \varpi_T c_T^{-\eta}\right]^{-\frac{1}{\eta}}$$

Intratemporal FOC gives relative price

$$p_{N} = \frac{\varpi_{N}}{\varpi_{T}} \left(\frac{c_{T}}{c_{N}}\right)^{1+\eta} p_{T}$$

with  $p_T = 1$ 

### Two-sector small-open economy structure

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#### Aggregate constraint: $w \geq \bar{w}$

· Labor demand of firms

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· In equilibrium,  $c_N = y_N$ , and

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  - $\kappa(s)$  in t+1, state s
  - $(1-\delta)\kappa(s)$  in t+2
  - $\cdot (1-\delta)^2 \kappa(s) \operatorname{in} t + 3$
  - . ...
    - $(1-\delta)^{k-1}\kappa(s)$  in t+k
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#### Geometrically decaying coupons with currency

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### The planner's problem: choosing default

Planner receives iid EV1 preference shocks for repayment and default so that

$$\mathcal{P}(b, a, \mathbf{s}) = \frac{\exp(\mathsf{V}^\mathsf{D}((1 - \hbar)b, a, \mathbf{s})/\sigma_\mathsf{V})}{\exp(\mathsf{V}^\mathsf{D}((1 - \hbar)b, a, \mathbf{s})/\sigma_\mathsf{V}) + \exp(\mathsf{V}^\mathsf{R}(b, a, \mathbf{s})/\sigma_\mathsf{V})}$$

and

$$\begin{split} \mathcal{V}(b, a, \mathbf{s}) &= \max \left\{ \mathbf{V}^{R}(b, a, \mathbf{s}) + \epsilon_{R}, \mathbf{V}^{D}((1 - \hbar)b, a, \mathbf{s}) + \epsilon_{D} \right\} \\ &= \sigma_{V} \log \left[ \exp \left( \mathbf{V}^{R}(b, a, \mathbf{s}) / \sigma_{V} \right) + \exp \left( \mathbf{V}^{D}((1 - \hbar)b, a, \mathbf{s}) / \sigma_{V} \right) \right] \end{split}$$

### Foreign lenders

Risk-averse lenders with stochastic discount factor

$$m(\mathsf{s},\mathsf{s}') = \exp\left(-r - \nu(\psi\epsilon' + 0.5\psi^2\sigma_\epsilon^2)\right)$$

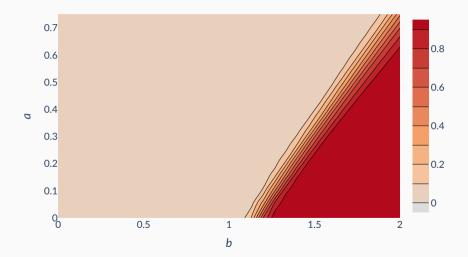
- $\nu$  follows a Markov chain with support  $\{0, 1\}$
- $\cdot$   $\epsilon$  is the innovation in tradable output

Price bonds as

$$q_b(b', a', s) = \mathbb{E}\left[m(s, s')\left(\mathbb{1}_{\mathcal{D}'}(1 - \hbar)q_b^D((1 - \hbar)b', a'', s') + (1 - \mathbb{1}_{\mathcal{D}'})(\kappa(s') + (1 - \delta)q_b(b'', a'', s'))\right)\right]$$

**Quantitative Results** 

### **Default Sets**



#### Price of Debt

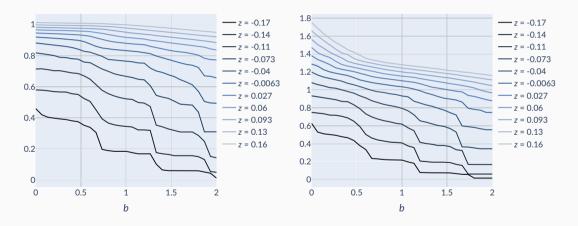


Figure: *q<sub>b</sub>* for dollar debt (left) and peso debt (right)

### Real Exchange Rate

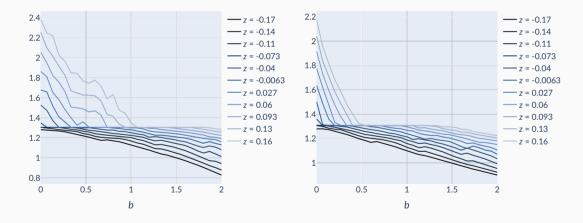


Figure:  $p_N$  for dollar debt (left) and peso debt (right)

### A synthesized LC bond

Idea: fix the hedging properties of LC debt while taking out incentives

- 1. Solve the model with FC debt
- 2. Record the state-dependent payments

$$\kappa^{\text{synth}}(b, a, s) = (r + \delta)p_N(b, a, s)$$

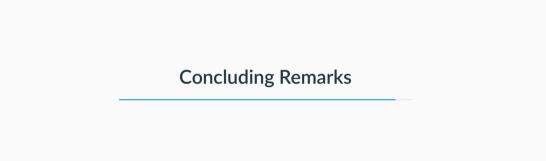
or

$$\kappa^{exog}(b, a, s) = (r + \delta)p_N(0, 0, s)$$

3. Fix the state-contingent bond with coupon payments  $\kappa^i$  and resolve

### **Comparative statics**

Statistic	Dollar debt	Peso debt	Exogenous SCI	Full SCI
mean a/y	9.98%	4.57%	2.32%	2.79%
mean b/y	23.9%	12.8%	9.76%	10.3%
mean ds/y	13.5%	18.7%	13.3%	13.2%
mean a/ds	75.4%	24.7%	18.8%	20.5%
corr c,y	75.9%	27.1%	64.2%	73.7%
vol c/vol y	25.8%	21.2%	23.7%	20.5%
std RER	18.9%	20.2%	19.4%	21.2%
mean unemp	2.4%	2.55%	1.94%	1.98%
default freq	2.32%	2.26%	2.13%	2.04%
$\mathcal{V}$	-8.089	-8.0738	-8.0425	-8.0572
Welfare gain	-	0.15%	0.46%	0.31%



### **Concluding Remarks**

- · Motivated by empirical association between high reserves and local-currency debt
- · Model emphasizes dual role of LC debt
- · Time-inconsistency erodes most of the gains from indexation
  - $\dots$  and induces high reserves compared to synthetic SCIs