Risk Aversion in Sovereign Debt and Default

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Macro-financial separation

- · In most RBC models, macro-financial separation holds
 - Elasticity of intertemporal substitution determines allocations
 - · Risk aversion determines asset prices
- · Sovereign debt literature typically inherits this line of thinking
 - · CRRA preferences frequent, typically $\gamma=2$
- · If MFS holds in sovereign debt, macro outcomes robust to different preferences
 - · In particular, calibration of output/utility costs of default
 - · Less clear about welfare effects
 - ... losses from default, debt dilution
 - ... welfare effects of banning debt, introducing state-contingent bonds

Wanting risk prices in sovereign debt

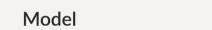
This paper

- · Show that macro-financial separation breaks in the sovereign debt model
- · Understand the impact of preferences consistent with significant risk premia
- Risk aversion
 - 1. affects higher-order moments of equilibrium
 - ... cautious behavior: stay away from default but use debt for insurance
 - 2. has limited impact on welfare comparisons
 - ... default costs adjust in calibration
 - has some impact on optimal fiscal rules

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 - ... default costs adjust in calibration
 - 3. has some impact on optimal fiscal rules



Framework

· Sovereign default model without default [reduces to an income-fluctuations problem]

$$\begin{aligned} \mathbf{v}(\mathbf{b},\mathbf{z}) &= \max_{\mathbf{b}'} \mathbf{u}^{-1} \left((1-\beta)\mathbf{u}(\mathbf{c}) + \beta \mathbf{u} \bigg(\underbrace{\mathbf{g}^{-1} \left(\mathbb{E} \left[\mathbf{g} \left(\mathbf{v}(\mathbf{b}',\mathbf{z}') \right) \mid \mathbf{z} \right] \right)}_{= \mathbb{T}(\mathbf{v}(\mathbf{b}',\mathbf{z}')|\mathbf{z})} \right) \right) \\ \text{subject to} \quad c + \kappa \mathbf{b} &= q(\mathbf{b}',\mathbf{z})(\mathbf{b}' - (1-\delta)\mathbf{b}) + \mathbf{y}(\mathbf{z}) \\ \quad \mathbf{b}' \leq \bar{\mathbf{b}} \\ \text{with} \quad q(\mathbf{b}',\mathbf{z}) &= 1 \\ \kappa = r + \delta \end{aligned}$$

· We consider parametrizations of the model to vary risk aversion

... with CRRA preferences
$$g(x) = u(x) = x^{1-\sigma}$$
 so $\mathbb{T} = \mathbb{E}$
... with robustness, $u(c) = \log c$; $g(x) = x^{1-\gamma}$, so that $\mathbb{T}[X \mid \mathcal{F}] = \mathbb{E}\left[X^{1-\gamma} \mid \mathcal{F}\right]^{\frac{1}{1-\gamma}}$

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Domestic risk premia

• Price of Lucas tree [dividend y(z)]:

$$q_{L}(b,z;d) = \beta \mathbb{E}\left[\left(\frac{c(b',z';d')}{c(b,z;d)}\right)^{-\sigma} \left(\frac{v(b',z';d')}{\mathbb{T}\left[v(b',z';d')\mid z,d\right]}\right)^{\sigma-\gamma} \left(y(z';d') + q_{L}(b',z';d')\right)\mid z,d\right]$$

· Turn into yields

$$r(b',z';d') = \frac{y(z';d') + q_L(b',z';d')}{q_L(b,z;d)}$$

· Compare with the yield of a risk-free asset [dividend 1]

Macro-financial separation without default



· Start from log-log [$\sigma=\gamma=1$]: RA moves asset prices and welfare, not the macro

| | loglog | $\gamma=$ 2 | $\gamma = 5$ | $\gamma=$ 10 | $\gamma=$ 15 |
|----------------------|--------|-------------|--------------|--------------|--------------|
| Corr. NX, y (%) | -2.02 | -2.01 | -1.98 | -1.92 | -1.86 |
| Rel. vol. cons | 1.1 | 1.1 | 1.1 | 1.1 | 1.11 |
| Risk premium (p.p.) | 1.03 | 1.1 | 1.29 | 1.63 | 1.97 |
| Debt-to-GDP (%) | 30.5 | 30.5 | 30.5 | 30.5 | 30.5 |
| Corr. deficit, y (%) | -1.64 | -1.65 | -1.68 | -1.73 | -1.78 |
| Default freq. (%) | 0 | 0 | 0 | 0 | 0 |
| Welfare | 1.028 | 1.027 | 1.024 | 1.019 | 1.015 |

^{...} welfare in autarky at $\gamma=$ 15 is 1.5pp lower than loglog or CRRA

Models with default

Option value of default (with small pref. shocks for numerical performance)

$$\mathcal{V}(b, z) = \max\{v_R(b, z) + \epsilon_R, v_D(b, z) + \epsilon_D\}$$

· Similar equation for value of repayment v_R , debt prices reflect default probabilities

$$q(b',z) = \frac{1}{1+r} \mathbb{E}\left[(1 - \mathbb{1}_{\mathcal{D}'}) \left(\kappa + (1-\delta)q(b'',z') \right) \mid z \right]$$

Costs of default

$$v_{D}(b,z) = u^{-1} \left((1 - \beta) u(h(y(z))) + \beta \mathbb{T} \left[\mathbb{1}_{R} \mathcal{V}(B(b,z'),z') + (1 - \mathbb{1}_{R}) v_{D}(b,z') \mid z \right] \right)$$

$$h(y) = y(1 - d_{0} - d_{1}y)$$

· Risk aversion \implies lack of smoothing in default costly \implies no macro-fin separation

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6

Quantitative properties

Comparative statics: robustness

· Increasing RA: lower debt tolerance, slightly lower volatilities

| | loglog | $\gamma=$ 2 | $\gamma=5$ | $\gamma=$ 10 | $\gamma =$ 15 |
|-------------------------|--------|-------------|------------|--------------|---------------|
| Avg. spread (bps) | 746 | 760 | 800 | 873 | 884 |
| Corr. NX, y (%) | -21.1 | -20.7 | -19.2 | -15.1 | -9.71 |
| Rel. vol. cons | 1.29 | 1.29 | 1.27 | 1.24 | 1.19 |
| Risk premium (p.p.) | 2.43 | 2.55 | 2.96 | 3.54 | 3.72 |
| Debt-to-GDP (%) | 17.5 | 17.3 | 16.7 | 15.5 | 13.3 |
| Corr. deficit, y (%) | 41.9 | 41.5 | 39.8 | 36.7 | 33.5 |
| Default freq. (%) | 8.33 | 8.47 | 9 | 10.1 | 11.5 |
| Std. dev. spreads (bps) | 311 | 321 | 351 | 408 | 447 |
| Welfare | 1.009 | 1.008 | 1.004 | 0.9988 | 0.9935 |

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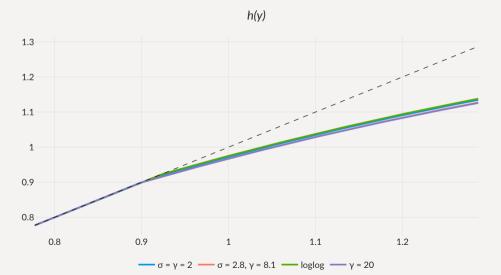
Calibration

· Add moments as more free parameters are included

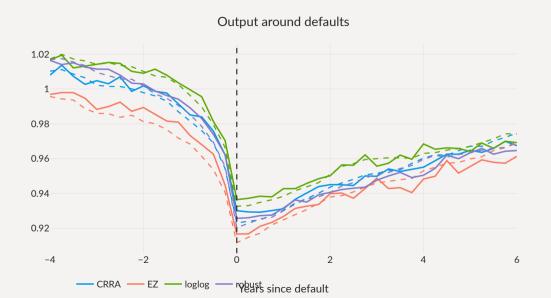
| | Parameter | loglog | CRRA | robust | EZ |
|--------------------------------|-----------|---------|---------|---------|---------|
| Sovereign's discount factor | β | 0.9665 | 0.9671 | 0.9711 | 0.9685 |
| Sovereign's risk aversion | γ | 1 | 2 | 19.78 | 8.145 |
| Sovereign's EIS | σ | 1 | 2 | 1 | 2.813 |
| Default output cost: linear | d_1 | -0.2923 | -0.2891 | -0.2896 | -0.2859 |
| Default output cost: quadratic | d_2 | 0.3171 | 0.3168 | 0.3224 | 0.3186 |
| | Data | loglog | CRRA | robust | EZ |
| Avg. spread (bps) | 815 | 834 | 800 | 783 | 722 |
| Rel. vol. cons | 0.94 | 1.47 | 1.32 | 1.43 | 1.21 |
| Risk premium (p.p.) | 3 | 1.03 | 1.82 | 2.78 | 2.93 |
| Debt-to-GDP (%) | 17.4 | 17.2 | 17.4 | 18.4 | 17.5 |
| Std. dev. spreads (bps) | 443 | 402 | 461 | 497 | 529 |

Calibrated output costs of default with robustness

· Calibrations with risk aversion need higher costs



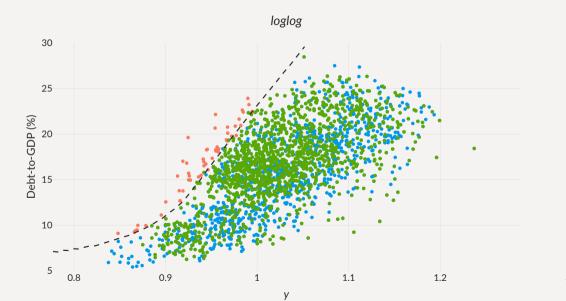
Event-study of defaults

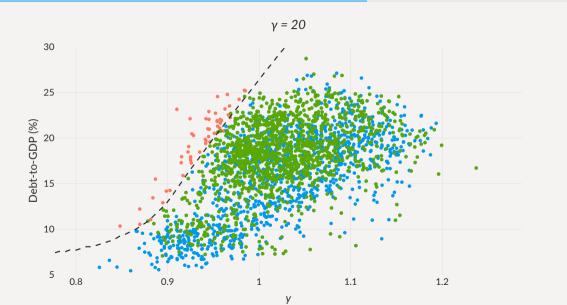


Untargeted moments

· Calibrations with robustness: not really helpful with untargeted moments

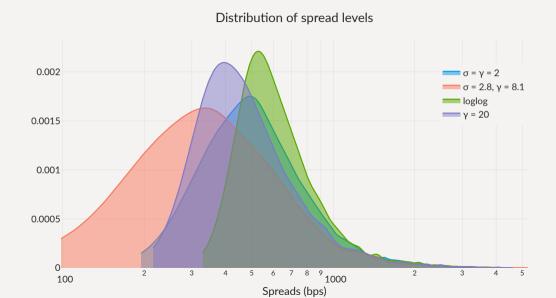
| | Data | loglog | CRRA | robust | EZ |
|------------------|------|--------|-------|--------|-------|
| Corr. NX,y (%) | -69 | -31 | -28.8 | -22.2 | -16.9 |
| Std. NX (%) | 1.35 | 2.6 | 2.06 | 2.72 | 1.82 |
| Corr. spr,y (%) | -65 | -65.4 | -78.7 | -71.5 | -81.3 |
| Corr. c,y (%) | 97 | 84.9 | 88.7 | 82.2 | 89.7 |
| Corr. spr,NX (%) | 56 | 23.5 | 21 | 11.7 | 10.3 |





Ergodic distribution for spreads





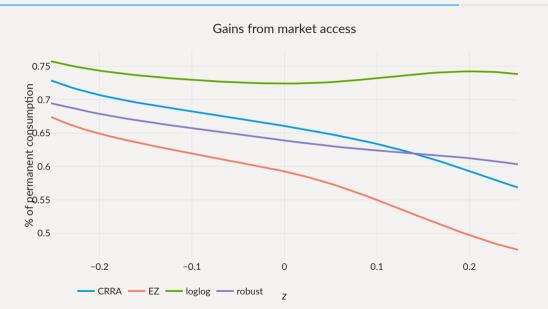
Takeaways

With preferences consistent with significant risk premia

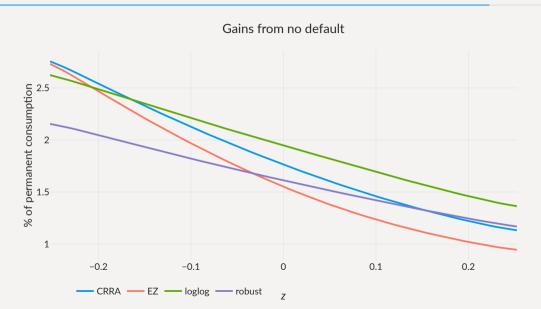
- Lower debt tolerance
 - ... Larger default costs required
- · Less staying at the edge of default
 - ... More skewness in the distribution of debt and spreads
 - ... Larger differences between ergodic distribution and pre-default samples
- · More use of the debt for insurance
 - ... Larger swings in debt to smooth shocks



Welfare effects of access to debt



Welfare effects of banning defaults



Fiscal rules

· Overall deficit [= current account]

$$d_t = c_t + \kappa b_t - y_t$$

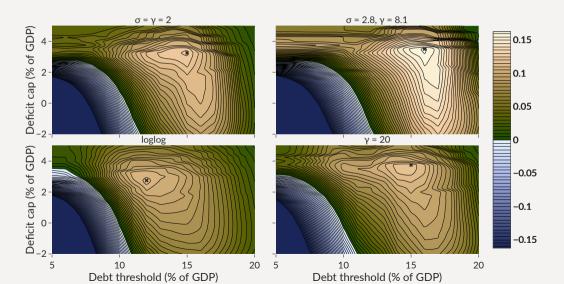
= $q_t(b_{t+1} - (1 - \delta)b_t)$

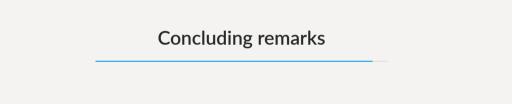
· Consider rules of the form

$$d_t \leq d^\star \mathbb{1}_{rac{b_t}{y_t} \geq b^\star}$$

Optimal fiscal rules







Risk aversion in the sovereign debt model

- · Risk aversion matters for macro outcomes in the sovereign debt model
 - ... raises questions about inference, policy evaluation based on CRRA preferences
- Effect of robustness concentrated at higher-order moments
 - ... makes crises look like more abrupt events
- · Welfare effects of market access and default unchanged from standard preferences
 - ... re-calibration of default costs weighs against change in risk attitudes
- Optimal fiscal rules affected by underlying preferences
 - ... more risk aversion \implies looser fiscal rules
- · No long-run risk

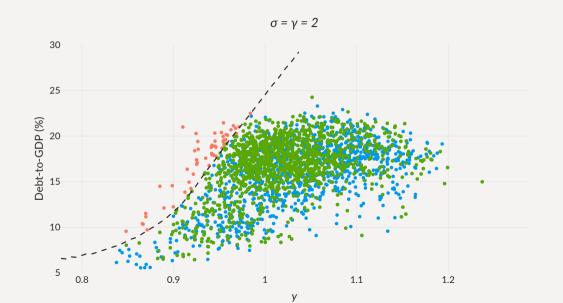
Macro-finanical separation without default



| | CRRA | $\gamma = 5$ | $\gamma=$ 10 | $\gamma =$ 15 |
|----------------------|-------|--------------|--------------|---------------|
| Corr. NX, y (%) | -1.68 | -1.58 | -1.41 | -1.22 |
| Rel. vol. cons | 1.06 | 1.06 | 1.06 | 1.06 |
| Risk premium (p.p.) | 2.26 | 2.58 | 3.05 | 3.53 |
| Debt-to-GDP (%) | 30.5 | 30.5 | 30.5 | 30.5 |
| Corr. deficit, y (%) | -3.73 | -3.85 | -4.07 | -4.32 |
| Default freq. (%) | 0 | 0 | 0 | 0 |
| Welfare | 1.024 | 1.021 | 1.016 | 1.011 |
| | | | | |

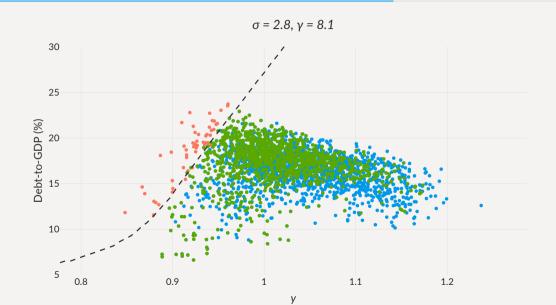
Ergodic distribution for debt





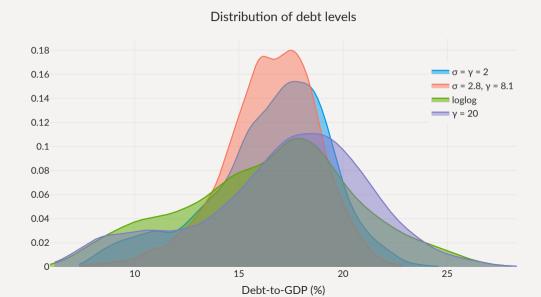
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Optimal fiscal rules



