The Perils of Bilateral Sovereign Debt

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Official Sovereign Debt

- · A large share of sovereign borrowing takes the form of official debt
 - ... Multilaterals, development banks, other governments
- Emergence of new bilateral creditors outside the Paris Club



... with claims to seniority and sometimes opaque terms

Questions

- How does the presence of a large senior lender affect sovereign debt markets?
- What are its welfare implications for borrowing governments?

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Evaluating Senior Official Creditors

Quantitative sovereign debt model with

- Competitive creditors in private markets (bondholders)
- Large bilateral lender
 - 1. Superior enforcement technology
 - 2. Bargained borrowing terms (price and quantity)
 - 3. Short-maturity loans
- Prime example: Central Bank swap lines (Horn et al., 2021)
 - ... also perhaps CB deposits, loans with non-monetary payment, IMF programs...
- · Focus on the interaction between both funding sources
 - ... presence of bilateral lender affects government behavior in debt markets
 - ... outcomes in debt markets affect threat points in bargaining

Main findings

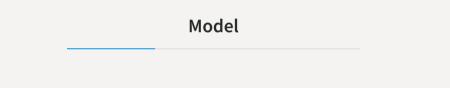
- Bilateral loans have significant effects on equilibrium outcomes
 - ... provide funding when other sources dry up (e.g. because of default risk)
 - ... can also incentivize more risk-taking
- If the rate on bilateral loans is decreasing in *market* debt [cross-elasticity]
 - ... government issues debt more quickly, delevers more slowly
 - ... spends longer in the risky region
 - ... defaults more frequently
- Cross-elasticity emerges endogenously from bargaining
 - ... at plausible values for bargaining weights
 - ... increased frequency of defaults dominates extra liquidity
 - ... welfare losses for the government

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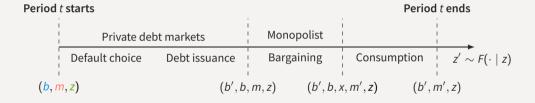
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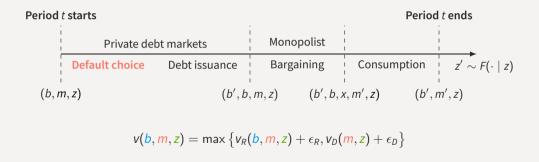
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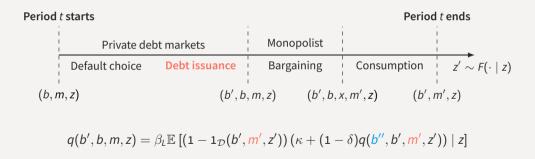
• Enter period t owing b to bondholders, m to monopolist, income y(z)



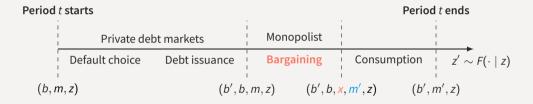
· Choose to repay or default the market debt subject to convex output costs



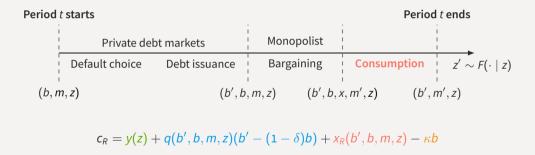
If repaid, issue new debt b' in markets at price q



· Meet with senior lender, decide any transfers x and new/remaining balance m'



· Consume output plus revenues from debt issuance plus transfers minus debt service



Exogenous Bilateral Terms

Programming the Large Lender: Possible Rules

• Explore interest rate rules of the form

$$r(b', m') = \max\{r^*, \alpha_0 + \alpha_b b' + \alpha_m m'\}$$

Two versions

Size-dependent

$$\alpha_0 > 0, \alpha_b = 0, \alpha_m > 0$$

Risk-inducing

$$\alpha_0 > 0, \alpha_b < 0, \alpha_m = 0$$

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Equilibrium with Exogenous Rules

	Only market	Size dependent r	Risk inducing <i>r</i>
Avg spread (bps)	714	623	921
Std spread (bps)	399	315	552
$\sigma(c)/\sigma(y)$ (%)	113	115	115
Debt to GDP (%)	22.5	23.5	22.8
Loan to GDP (%)	0	0.71	0.972
Loan spread (bps)	-	682	1,264
Corr. loan & spreads (%)	-	62.5	48.1
Default frequency (%)	5.72	5.13	6.92
Welfare gains (rep)	_	0.21%	-0.079%

Endogenous Bargaining

Bargaining Stage with Monopolist

· At state z, owing debt b bonds and m on the loan and having issued b'

$$\max_{x,m} \mathcal{L}_R(b',x,m,m',z)^\theta \times \mathcal{B}_R(b',b,x,m,m',z)^{1-\theta}$$
 Lender surplus

Lender's surplus

$$\mathcal{L}_{R}(b',x,m,m',z) = \underbrace{(a-x+\beta_{L}\mathbb{E}\left[h(b',m',z')\mid z\right])}_{\text{agreement}} - \underbrace{(a+m+\beta_{L}\mathbb{E}\left[h(b',0,z')\mid z\right])}_{\text{threat point}}$$

Government's surplus

$$\mathcal{B}_{R}(b',b,x,m,m',z) = \underbrace{u\big(y(z) + B(b',b,m,z) + x\big) + \beta \mathbb{E}\left[v(b',m',z') \mid z\right]}_{\text{agreement}} - \underbrace{\big(u\big(y(z) + B(b',b,m,z) - m\big) + \beta \mathbb{E}\left[v(b',0,z') \mid z\right]\big)}_{\text{threat point}}$$

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- Revenues from debt issuance B(b', b, m, z) modulate the value of the threat point
 - After large revenues (high q, high b'), gov't flush with cash, strong in bargaining
 - · After bad issuance (low q or low b'), gov't weak in bargaining
- Strongly negative cross-elasticity of bilateral terms to market debt
 goes against market discipline of spreads

$$u'(c)\left(q+\frac{\partial q}{\partial b'}i+\frac{1}{1+r_b}\frac{\partial m'}{\partial b'}+\frac{\partial\frac{1}{1+r_b}}{\partial b'}m'\right)=\beta\mathbb{E}\left[u'(c)(1-\mathbb{I}_{\mathcal{D}})\left(\kappa+(1-\delta)q'+\ldots\right)\right]$$

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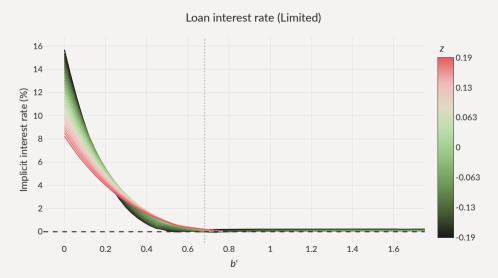
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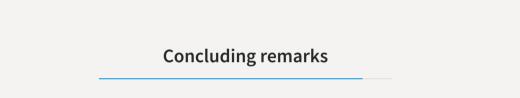
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Risk-taking Incentives



Surplus on loan requires spreads > 0: monopolist provides incentives for risk taking





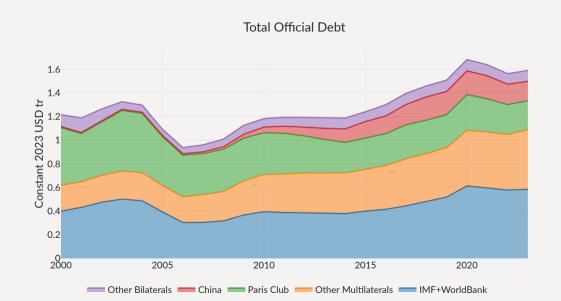
The Perils of Bilateral Sovereign Debt

- · Simple model of borrowing from markets and a senior bilateral lender
 - ... Dangerous when bilateral interest rate responds negatively to market debt
 - ... Bargaining as an example of situation where cross-elasticity emerges
- · Strong interaction between two markets for sovereign debt
 - ... cross-elasticity induces risk-taking, more defaults, welfare losses
 - ... even if bilateral loans are **not** used intensely on the equilibrium path
- · Cross-elasticity constitutes a simple test to assess welfare gains of new instruments
 - ... or a boost to the gains of fiscal rules, state-contingent debt...



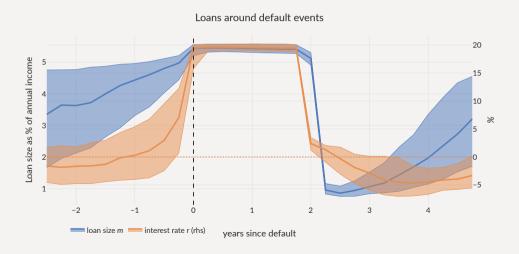
Scan to find the paper







· Further conditioning on default events lasting exactly two years





• With Limited: $\Gamma(m) = m$

