# Central Bank Swap Lines as Bilateral Sovereign Debt

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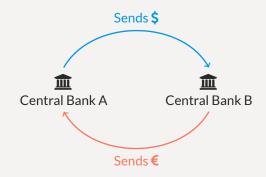
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# What is a Central Bank swap?

# Swaps are symmetric currency exchanges

- A swap line is a contract between two Central Banks
- When activated, each institution provides an amount of its currency to the counterparty
- · At maturity, positions are undone



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  - ... Symmetric swaps better understood, growing number of asymmetric ones

# What is a Central Bank swap?



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- The Fed doesn't really want Mexico's pesos
  - ... treats them more like collateral
- Mexican authorities may need dollars for their BoP
  - ... more similar to borrowed reserves
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### How are Central Bank Swap Lines different from Sovereign Debt?

#### For an EM using the swap line to borrow from an AE

#### Regular debt (bond markets)

- Defaultable
- Many different lenders
- Interest rate (spreads) mainly reflects default risk

#### Bilateral loan (swap line)

- Non-defaulteable (Central Bank)
- · No coordination issues
- · Can be used to curb default risk
- Interest rate?

## How do Central Bank Swap Lines interact with Sovereign Debt?

#### Main findings

- · One type of debt affects borrowing conditions for the other
  - · Borrowing from the market serves as threat in swap negotiations
  - · Swap can be used when spreads on the market are high
- · Lending around or in default maximizes surplus for bilateral loans
  - · Without restricting swaps in default, welfare losses for government
- Swaps worsen the debt dilution problem

#### Literature

- · Central Bank swaps among advanced economies
  - ... Bahaj and Reis (2021); Cesa-Bianchi, Eguren-Martin, and Ferrero (2022)
- · Data on Central Bank swaps
  - ... Perks, Rao, Shin, and Tokuoka (2021); Horn, Parks, Reinhart, and Trebesch (2023)
- · Sovereign debt/default with non-defaultable debt
  - ... Hatchondo, Martinez, and Onder (2014)

# Roadmap

Model with Swaps only

Model with Swaps and Debt

Concluding remarks

Model with Swaps only

#### **Environment**

#### The government of a small open economy borrows from a monopolist

- · Income  $y(z_t)$  follows an AR(1) process in logs
- · Renegotiate the swap *m* each period
  - ... Involves a transfer x and a new loan size m'
- · The swap is non-defaultable
  - ... Repaying the whole amount is a natural threat point
- Should expect
  - ... Interest rate to vary over time
  - ... Interest rate to reflect market power
  - ... Interest rate to reflect outside options

$$x = \frac{1}{1+r}m' - m$$

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5

· At income state z and loan m, solve

$$\max_{x,m'} \mathcal{L}(x,m,m',z)^{\theta} \times \mathcal{B}(x,m,m',z)^{1-\theta}$$

Government (borrower) surplus

$$\mathcal{B}(x,m,m',z) = \underbrace{u(y(z)+x) + \beta \mathbb{E}\left[v(m',z')\mid z\right]}_{\text{agreement: receive } x, \text{ owe } m'} - \underbrace{\left(u(y(z)-m) + \beta \mathbb{E}\left[v(0,z')\mid z\right]\right)}_{\text{threat point: repay } m, \text{ clean slate}}$$

Lender surplus

$$\mathcal{L}(x, m, m', z) = \underbrace{a - x + \beta_L \mathbb{E}\left[h(m', z') \mid z\right]}_{\text{agreement}} - \underbrace{\left(a + m + \beta_L \mathbb{E}\left[h(0, z') \mid z\right]\right)}_{\text{threat point}}$$

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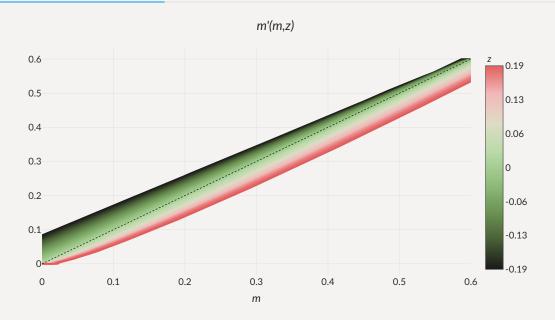
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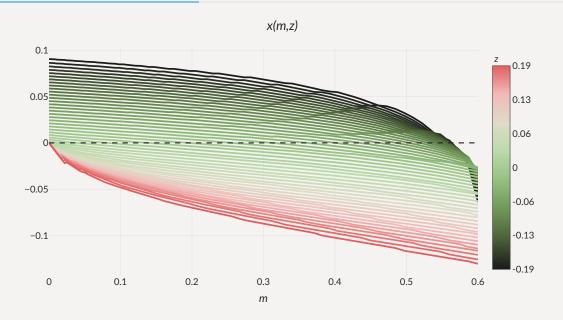
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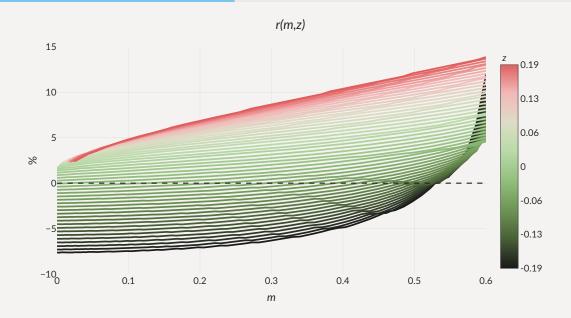
# **Swap Line Terms: Loan Dynamics**



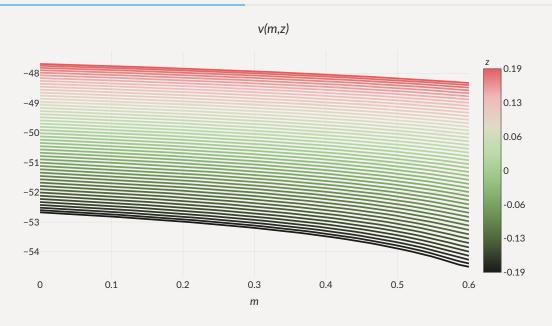
# **Swap Line Terms: Transfers**



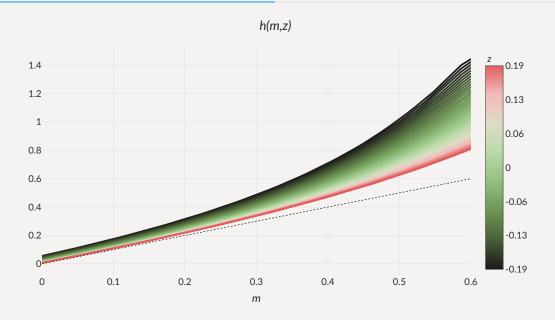
# **Swap Line Terms: Interest rate**



# Swap Line Terms: Borrower's value function



# Swap Line Terms: Lender's value function



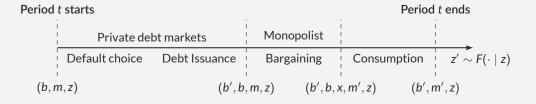
**Swap Line Terms: Takeaways** 

#### The threat point is less 'credible' when m is large

- · This creates convexity in the lender's value function
  - ... making the lender act 'as if' risk-loving
- · The lender initially subsidizes the loan to induce indebtedness and high profits
  - Gamble for debt overhang
- · Initial subsidy and high rates consistent with B's risk aversion 'Participation constraint'

Model with Swaps and Debt

#### Timeline of events



#### Borrowing from markets

· Debt is a geometrically-decaying coupon

... get 1, pay 
$$\kappa$$
,  $(1-\rho)\kappa$ , ...  $(1-\rho)^{s-1}\kappa$ 

· Government enters first stage owing b in debt, m in swaps, income state z

$$v(b, m, z) = \max \{v_R(b, m, z) + \epsilon_R, v_D(m, z) + \epsilon_D\}$$
$$v_R(b, m, z) = \max_{b'} w_R(b', b, m, z)$$

Lenders in competitive markets need to anticipate interactions with the monopolist

$$\begin{aligned} q(b',b,m,z) &= \beta_{L} \mathbb{E} \left[ (1 - 1_{\mathcal{D}}(b',m',z')) \left( \kappa + (1 - \rho) q(b'',b',m',z') \right) \mid z \right] \\ m' &= m'(b',b,m,z) \\ b'' &= b'(b',m',z') \end{aligned}$$

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## Bargaining stage

• Similar to the case with swaps only with extra state variables (b, b')

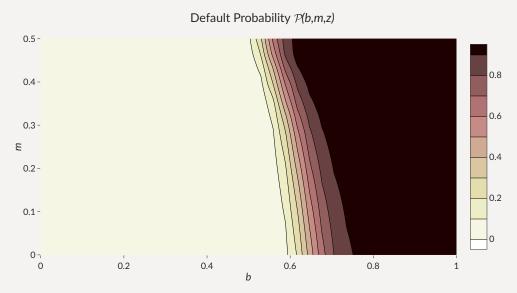
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$$\mathcal{B}_{R}(b', b, x, m, m', z) = u(y(z) + B(b', b, m, z) + x) + \beta\mathbb{E} [v(b', m', z') \mid z] - (u(y(z) + B(b', b, m, z) - m) + \beta\mathbb{E} [v(b', 0, z') \mid z])$$

$$B(b', b, m, z) = q(b', b, m, z)(b' - (1 - \rho)b) - \kappa b$$

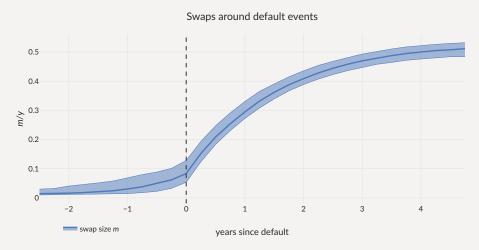
# Default probability

## Both types of debt are clearly complements



### When is the Swap Used?

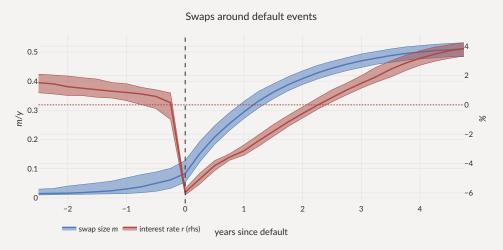
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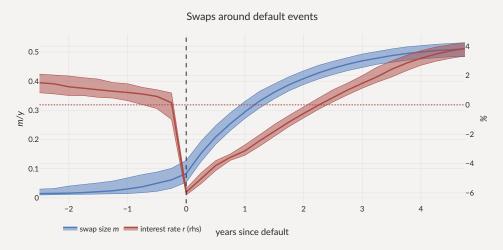
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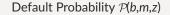
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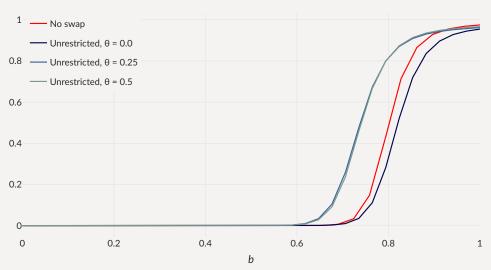


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## **Debt Tolerance with Swaps**

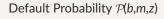
More repayment with Limited and with bargaining power

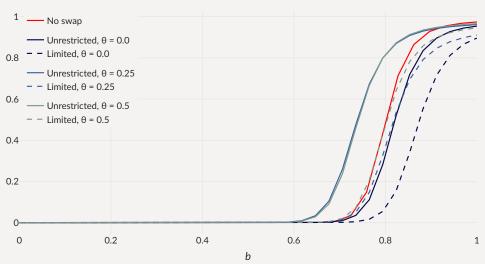




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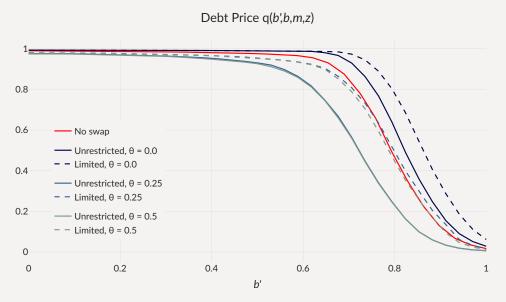
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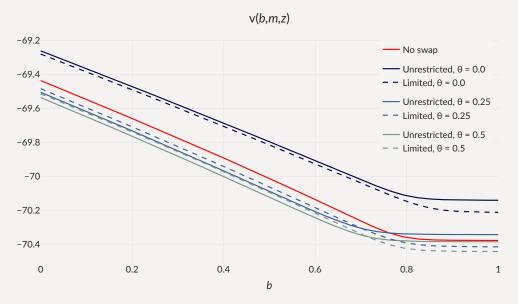
### **Debt Prices with Swaps**

More repayment with Limited but still lower prices — Tell-tale sign of debt dilution



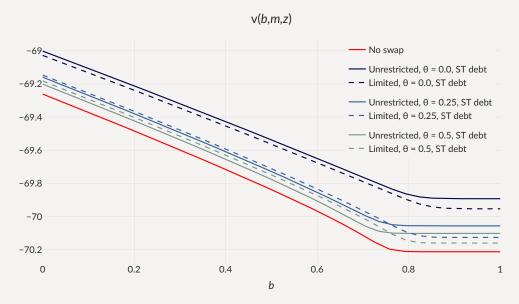
## Welfare effects of swap lines

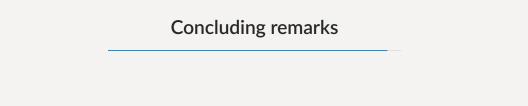
with interior bargaining power, Limited  $\succcurlyeq$  Unrestricted, but...



# Welfare effects of swap lines — Debt dilution

Solving model with short-term debt: gains of swaps





## Concluding remarks

- Simple model with monopolist/fringe structure
- · Strong interaction between two markets for sovereign debt
  - ... even if swaps are **not** used intensely on the equilibrium path
- · Market power crucial in model
  - ... how to discipline in model?
  - ... how to affect in reality?
- Large welfare effects, policy challenges
  - · How to limit their use during defaults?
  - Strengthen debt dilution more gains from fiscal rules, state-contingent debt?