# Credibility Dynamics and Disinflation Plans[*]

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### Abstract

We study the optimal design of a disinflation plan by a planner who lacks commitment and has imperfect control over inflation. The government's reputation for being committed to the plan evolves as the public compares realized inflation to the announced targets. Reputation is valuable as it helps curb inflation expectations. At the same time, some plans create more temptation to break them, leading to larger expected reputational losses in the ensuing equilibrium. Taking these dynamics into consideration, the government announces a plan which balances promises of low inflation with dynamic incentives that make them credible. We find that, despite the absence of inflation inertia in the private economy, a gradual disinflation is preferred even in the zero-reputation limit.

## Introduction

Macroeconomic models give expectations about future policy a large role in the determination of current outcomes. Policy is then generally set under one of two assumptions: commitment to future actions or discretion. Attempts to model policy departing from these extreme cases have found limited success.

However, governments actively attempt to influence beliefs about future policy. Examples include forward guidance and inflation targets but also fiscal rules and the timing of introduction of policies. Such promises rarely constrain future choices, yet they can shift expectations substantially. Standard macroeconomic models cannot capture this idea directly, as expectations of the public are fully determined by the policy chosen with commitment, or with discretion as part of an equilibrium. In both cases the public understands that announcements do not bind the government in any way. Announcements do not grant any additional credibility to the policy maker, as the public is convinced of her course of action.

In this paper we develop a rational-expectations theory of government credibility and apply it to policy design questions. Our notion of credibility is based on the concept of reputation in game theory (Kreps and Wilson, 1982; Milgrom and Roberts, 1982). In our model, the government (or central bank, or planner) could be rational and strategic, or one of many possible behavioral types described by a policy that they stubbornly follow. The public is uninformed about the government's type and makes statistical inference about it after observing the government's announcements and actions. This inference is central to our analysis because it turns out to be in the best interest of the rational type to pretend to be one of the behavioral types.

We consider a stylized environment. In the initial period, the government makes an announcement of its policy targets and is then free to choose policy. However, the private sector knows that if the government is behavioral it announced exactly what it will implement. As a consequence, the rational type has an ex-post incentive to stay close to any announced targets, which might earn it a reputation for being committed to them. The incentive exists at any positive level of reputation, though its strength depends on the announced targets. In anticipation of these interactions, the rational type chooses carefully which targets to announce. Our main question

concerns the optimal policy announcement in the presence of these reputational concerns.

We set our model of reputation in a modern version of the classic environment of Barro (1986) and Backus and Driffill (1985), where a central bank sets inflation subject to an expectations-augmented Phillips curve. The monetary authority dislikes inflation but constantly faces an opportunity to engineer surprise inflation, which would deliver output closer to potential. We model these features through the standard, cashless-limit New Keynesian setup for the private economy. To focus on incentives and reputation dynamics, we abstract from an IS curve and let the government control inflation directly.

A natural definition of the government's reputation is the private sector's belief that the government is indeed the behavioral type whose plan was announced. The credibility of a plan measures the proximity of expected inflation to the targets. We refer to the total, ex-ante probability of the behavioral types as the government's initial reputation. While credibility generally increases with reputation, the insights of the reputation literature mean in our case that credibility need not converge to zero as reputation vanishes.

A key assumption we introduce is that the government exerts imperfect control over inflation, perhaps due to underlying shocks to money demand. Imperfect control masks the government's choice of policy: the private sector understands that realized inflation is only an imperfect signal of intended inflation. We consider additive and normally distributed noise which implies that the public can never be certain of the government's action. This assumption distinguishes us in technical terms from the early studies of reputation in monetary policy referenced above, where the public perfectly observes the inflation chosen by the government. But, crucially, it also creates a smooth tradeoff for the government: overshooting the target by more creates, in expectation, a larger boom but also larger reputational losses.

When designing policy, the planner takes into account its own future behavior, which it can influence but not control. 'Future' governments have complete freedom and will only respect promises made at time 0 to the extent that it suits them. Preserving reputation turns out to be a powerful disciplining force for the planner's future self. Crucially, the value of reputation depends on the plan in place. Plans differ in the outcomes they intend to deliver and in their credibility, how closely they are expected to be followed in the future. Both features contribute

to current outcomes through the private sector's expectations. These forces lead the planner to weigh a plan's intended outcomes against the reputation dynamics it generates.

Our main result is that the government chooses a policy under which inflation starts high and diminishes gradually. Plans with gradual disinflation are more credible: having a higher target for today than tomorrow boosts the gains from sticking to the plan. This slows down the pace of reputational losses sufficiently to offset the negative effect of higher announcements on expected inflation. In contrast, the reputation literature typically considers the limit as the long-lived player becomes arbitrarily patient (Fudenberg and Levine, 1989). In that case, the government can obtain a payoff arbitrarily close to its commitment payoff by announcing a static plan with zero inflation in every period.

The gradualism of our optimal policy might lead an outside observer to conclude that there is substantial inflation inertia in the economy and that the government avoids a costly recession when bringing inflation down. However, in our model past inflation does not enter the Phillips curve. Instead, gradual disinflation is a result of the dynamic incentives of the government.

A second result concerns the limit as initial reputation becomes arbitrarily small. At zero initial reputation, the only Markov equilibrium is a repetition of the static Nash equilibrium with high inflation and output at the natural level. However, as is usual in the reputation literature, even a small amount of reputation creates a large departure in behavior from the Nash equilibrium. In particular, we show that the gradualist nature of optimal announcements and the corresponding credibility dynamics are preserved at arbitrarily low levels of initial reputation. In addition, the limiting announcement, which can be interpreted as the announcement in a fully rational model where the government has mild credibility concerns, also exhibits gradualism.

**Discussion of the Literature**   We contribute to a long literature dealing with commitment, imperfect credibility, and reputation. The time-inconsistency of optimal policy (Kydland and Prescott, 1977) has long been recognized by researchers, who have set out to ask whether reputation can be a substitute for commitment.

Barro (1986) and Backus and Driffill (1985) were the first studies of monetary policy to introduce reputation via behavioral types committed to a certain policy. These and many subsequent

studies (Cukierman and Liviatan, 1991; Sleet and Yeltekin, 2007; King et al., 2008; Dovis and Kirpalani, 2019) assume the government has perfect control of inflation. Thus, any deviations are detected by the private sector and fully destroy the government's reputation. In contrast, the assumption of imperfect control in our paper enables distinct tradeoffs that shape the gradualism of optimal plans.

Another tradition studies monetary policy with imperfect control by considering uncertainty about the preferences of the planner which is distinct from reputation (Cukierman and Meltzer, 1986; Faust and Svensson, 2001; Phelan, 2006). We view reputation as more directly suited to address optimal announcements, which was not the goal of the above papers.

Most closely related is the work of Lu, King, and Pastén (2016) and King and Lu (2020) who consider reputational models with imperfect control. The main distinction is that in our model the type that lacks commitment is rational and forward looking. The commitment type follows a fixed rule in Lu, King, and Pastén (2016), and behaves myopically in King and Lu (2020). Because of this reversal of roles, they recover the model without reputation in the zero-reputation limit.

An alternative view of reputation is given by the notion of sustainable plans (Chari and Kehoe, 1990; Phelan and Stacchetti, 2001). This literature considers subgame perfect equilibria in games between the government and the private sector applying the tools of Abreu, Pearce, and Stacchetti (1990). However, this typically generates a large set of equilibria. In fact, reputational models are often used to refine the equilibrium set. Faingold and Sannikov (2011) study a general model of reputation in continuous time which applies to our framework of monetary policy with imperfect control, with the important exception that behavioral types are limited to static plans. Hence, their model cannot address the gradualism of announcements we are interested in. Faingold and Sannikov (2011) find conditions for a unique equilibrium which is Markovian in reputation, which informs our restriction to Markovian equilibria.

Even though the announcements in our model do not constrain the actions of the rational government, they are not cheap talk, as they can be sent by only one of the behavioral types. This distinguishes us from cheap talk models of monetary policy such as Stein (1989) and Turdaliev (2010).

**Layout**    The rest of the paper is structured as follows. Section 2 introduces our model of reputation. Notions of equilibrium are defined and discussed in Section 3. Section 4 lays out our main results and Section 5 discusses how optimal plans depend on parameters. Section 6 relates our results to other salient models. Finally, Section 7 concludes.

## 2. Model

We consider a government which dislikes inflation and deviations of output from a target $y^\star$ according to a loss function

$$L_0 = \mathbb{E}_0 \left[ \sum_{t=0}^{\infty} \beta^t \left[ (y^\star - y_t)^2 + \gamma \pi_t^2 \right] \right], \tag{1}$$

where $y_t, \pi_t$ denote output and inflation at time $t$, $\gamma \geq 0$ is the relative weight on inflation, and $\beta \in (0, 1)$ is a discount factor. A Phillips curve relates current output to current and expected inflation:

$$\pi_t = \kappa y_t + \beta \mathbb{E}_t \left[ \pi_{t+1} \right], \tag{2}$$

where $\mathbb{E}_t$ represents the expectations operator based on information up to time $t$ (including $\pi_t$) and $\kappa \geq 0$ is the slope of the Phillips curve. The government has imperfect control over inflation. At time $t$ it chooses $g_t$, and realized inflation is

$$\pi_t = g_t + \sigma \epsilon_t, \tag{3}$$

where $\epsilon_t \overset{iid}{\sim} \mathcal{N}(0, 1)$ is realized after the governments has made its choice and $\sigma > 0$.

### 2.1    Announcements and behavioral types

An announcement is a sequence $(a_t)_{t=0}^{\infty}$, where $a_t$ is an inflation target for time $t$. Inflation targets are in the interval $A = [0, \pi^N]$, where $\pi^N$ is inflation in the unique Nash equilibrium of the static game. Consequently, the space of announcements is $\mathcal{A} = A^{\infty}$.

The government is either rational or one of many behavioral types indexed by a set $\mathcal{C} \subseteq \mathcal{A}$. A behavioral type $c \in \mathcal{C}$ is committed to making an announcement $c$ and following it. The

announcement of each behavioral type $c$ is denoted by $(a_t^c)_{t=0}^\infty$ and satisfies

$$a_t^c = \chi + (a_0 - \chi) \, e^{-\omega t}$$

for some parameters $(a_0, \omega, \chi)$. This parametrization makes $\mathcal{C}$ finite-dimensional and allows us to write each plan recursively as $a_{t+1}^c = \varphi_c(a_t^c)$, where

$$\varphi_c(a) = \chi + e^{-\omega} (a - \chi) \, .$$

The set $\mathcal{C}$ contains constant, decreasing, and increasing paths (Figure 1). Paths start at $a_0$ and converge towards $\chi$ with a exponential decay rate of $\omega$.
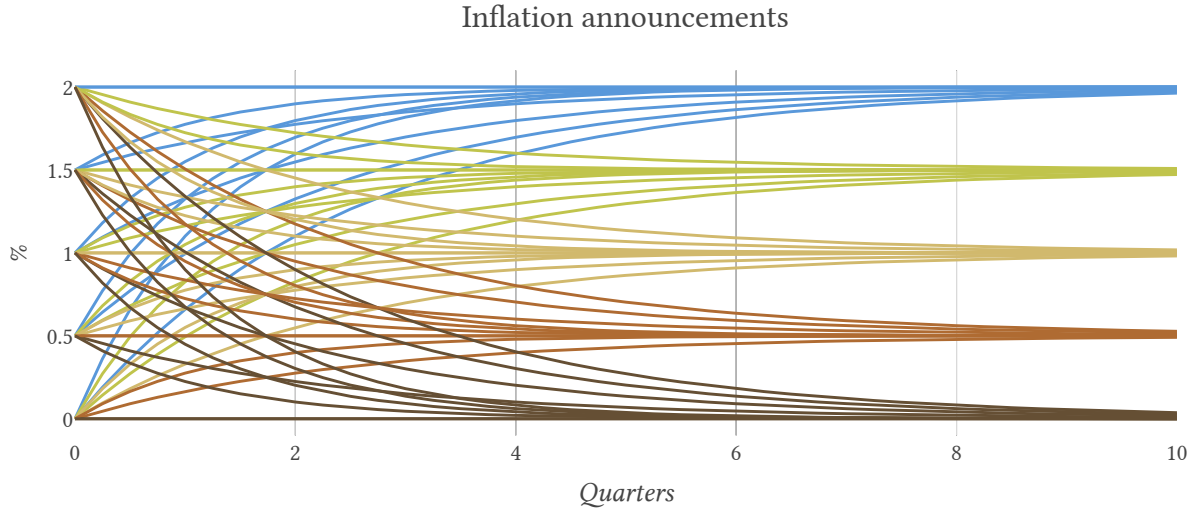


Inflation announcements

FIGURE 1: POSSIBLE BEHAVIORAL TYPES' ANNOUNCEMENTS

We assume that the government is rational with probability $1 - z$. A probability distribution on $\mathcal{C}$ with density $v$ describes the distribution of possible behavioral types, which have total probability $z$.

## 2.2 Timing of play

At time 0 the government announces an inflation plan $a \in \mathcal{A}$. Then at each $t \geq 0$, the government chooses $g_t$ and inflation $\pi_t$ is given by (3). After seeing inflation, beliefs are updated (see below) and output is determined.

If the government is a behavioral type $c \in \mathcal{C}$, it announces $(a_t^c)_t$ and follows the announcement by setting $g_t = a_t^c$ at each time $t$. A rational government instead makes a strategic choice of announcement $r \in \mathcal{A}$ and is also free to choose any action $g_t$ at time $t$ based on time-$t$ information, regardless of what $a_t^r$ calls for.

## 2.3  Beliefs

We refer to the probability the private sector attaches to the government being a behavioral type as its *reputation*. Reputation evolves as the private sector updates its beliefs via Bayes' rule following the initial announcement of targets at time 0 as well as realized inflation at each time $t$.

Consider the posterior beliefs following an announcement $a \in \mathcal{A}$. If $a \notin \mathcal{C}$ the private sector infers that the government is rational. If $a \in \mathcal{C}$, the government can be either rational or the behavioral type $c$. Suppose that in equilibrium the rational type announces $c$ with density $\mu(c)$. Then the posterior probability that the government is behavioral conditional on an announcement $c$ with $\mu(c) > 0$ is given by

$$p_0(c; z, \mu) = \frac{zv(c)}{zv(c) + (1 - z)\mu(c)}. \tag{4}$$

At time $t$, the private sector's posterior of the government being a behavioral type $c$ is formed by applying Bayes' rule to the private sector's information. Suppose that inflation $\pi_t$ is realized at time $t$. If the government is behavioral of type $c$, then it must have chosen $g_t = a_t^c$ and the current shock must have been $\epsilon_t = \pi_t - a_t^c$, which has density $f_\epsilon(\pi_t - a_t^c)$. Let $g_t^\star$ denote the rational type's equilibrium strategy. Then if the government is rational, it must have chosen $g_t = g_t^\star$ so the shock must have been $\epsilon_t = \pi_t - g_t^\star$. Therefore, updating from a prior belief of $p_t$, we have that

$$p_{t+1} = \frac{p_t \cdot f_\epsilon(\pi_t - a_t)}{p_t \cdot f_\epsilon(\pi_t - a_t) + (1 - p_t) \cdot f_\epsilon(\pi_t - g_t^\star)}$$

It is useful to rewrite this condition as

$$p_{t+1} = p_t + p_t(1 - p_t)\frac{f_\epsilon(\pi_t - a_t) - f_\epsilon(\pi_t - g_t^\star)}{p_t f_\epsilon(\pi_t - a_t) + (1 - p_t)f_\epsilon(\pi_t - g_t^\star)} \tag{5}$$

which shows that reputation moves slowly when it started away from 0 and 1. Large increases in reputation occur when realized inflation is much closer to the target than to the rational type's

strategy, and large decreases in reputation require the converse. Consequently, large movements in reputation are more likely when the target differs significantly from the expected behavior of the rational type.

## 2.4 Bellman equations after an announcement

Given an announcement $c$, the problem of the rational type is to choose mean inflation $g_t$ in period $t$ to maximize (1) subject to (2), (3), and (5). The time-$t$ government makes its choices taking as given its reputation $p_t$, its continuation equilibrium strategy $g_t^\star$, and the private sector's expectations. We focus on Markovian strategies with $g_t^\star = g^\star(p_t, a_t^c)$. Thus, at time $t$ the private sector expects the behavioral type to choose $a_t^c$ and the rational type to choose $g^\star(p_t, a_t^c)$. This allows us to write the rational government's problem recursively as

$$\mathcal{L}^c(p, a) = \min_g \mathbb{E}\left[(y^\star - y)^2 + \gamma \pi^2 + \beta \mathcal{L}^c(p', \varphi_c(a))\right] \tag{6}$$

$$\text{subject to } \pi = g + \epsilon$$

$$\pi = \kappa y + \beta\left[p'\varphi_c(a) + (1 - p')g^\star(p', \varphi_c(a))\right]$$

$$p' = p + p(1 - p)\frac{f_\epsilon(\pi - a) - f_\epsilon(\pi - g^\star(p, a))}{pf_\epsilon(\pi - a) + (1 - p)f_\epsilon(\pi - g^\star(p, a))}$$

Problem (6) illustrates the government's reputation-building incentives. By controlling current inflation, the rational type can, on average, affect its future reputation $p'$. This changes the continuation value $\mathcal{L}^c(p', \varphi_c(a))$ as well as current output (through the Phillips curve). Expected inflation is a reputation-weighted average between the behavioral type's target $\varphi_c(a)$, and the equilibrium choice of the rational type $g^\star(p', \varphi_c(a))$. A higher reputation $p'$ shifts expectations away from the expected action of the rational type and towards the target $\varphi_c(a)$. It also enters the rational type's choice $g^\star(p', \varphi_c(a))$ directly.

At low levels of initial reputation $p$, inflation expectations place most of the weight on the rational type's action $g^\star(p', \varphi_c(a))$. If future governments are expected to value their reputation and choose inflation close to the target, then the current government has an incentive to conserve its reputation and, therefore, also stay close to its announcement.

# 3. EXPECTATIONS AND EQUILIBRIUM

A solution to (6) describes the government's choices $g(p, a)$ as a function of $g^\star$, the private sector's expectations of its actions. An equilibrium requires finding a fixed point of this function, making the expectations rational.

**Definition** Given an announcement $c \in \mathcal{C}$, a *continuation equilibrium* consists of a loss function $\mathcal{L}^c : [0, 1] \times \mathcal{A} \to \mathbb{R}$ and a policy function $g_c^\star : [0, 1] \times \mathcal{A} \to \mathbb{R}$ such that

1. The loss function $\mathcal{L}^c$ solves the government's Bellman equation (6) taking as given expectations $g_c^\star$.

2. $g_c^\star$ is the policy function that corresponds to the solution of (6).

A useful property of continuation equilibria follows from close observation of problem (6): given the decay and asymptote parameters, it is equivalent to start the plan at a different initial announcement $a$ or to just have arrived at a current announcement $a$ as the continuation equilibrium unfolded.

**Observation** Suppose $(\mathcal{L}, g^\star)$ is a continuation equilibrium for announcement $c = (a_0, \chi, \omega) \in \mathcal{C}$. Then for any $b_0$, the same pair $(\mathcal{L}, g^\star)$ is a continuation equilibrium for plan $c' = (b_0, \chi, \omega)$.

Another immediate property of equilibrium is that the government cannot design an inflation plan that will increase its reputation over time. If the rational government follows the announcement exactly, i.e. $g^\star(p, a) = a$, its reputation will stay unchanged because inflation is not a signal of its type. Any if the equilibrium strategy calls for deviations from the plan, reputation will decline on average over time. In other words, rational expectations do not allow the planner to accumulate reputation by consistently delivering on its promises, as such compliance would be anticipated by the private sector. What the planner can do is to design its plan in a way that provides incentives to deliver on it.

**Observation**    In any continuation equilibrium, the rational type's reputation is a supermartingale:

$$\mathbb{E}\left[p_{t+1} \mid \text{rational}, \mathcal{F}_t\right] \leq p_t,$$

where $\mathcal{F}_t$ denotes information up to time $t$. Thus, the planner cannot design a policy that generates expected reputational gains.

We proceed by defining equilibrium from the announcement stage, i.e. the beginning of the game.

**Definition**    Given an initial reputation $z$, a *reputational equilibrium* is a distribution $\mu_z$ on $\mathcal{C}$ along with continuation equilibria $\{\mathcal{L}^c, g_c^\star\}_{c \in \mathcal{C}}$ and a posterior reputation $p_0 : \mathcal{C} \to [0, 1]$ such that

1. Posterior reputation is set according to Bayes' rule (4) given the distribution $\mu_z$.

2. The distribution of mimicked types $\mu_z$ minimizes the posterior reputation-adjusted loss function

$$\mathcal{L}^\star(\mu_z, z) = \int_{\mathcal{C}} \mathcal{L}^c(p_0(c), a_0^c) d\mu_z(c)$$

taking as given the posterior reputation function $p_0$.

The second part of the definition implies that the planner is indifferent among plans in the support of $\mu_z$ and prefers them to other plans:

$$\mathcal{L}^c(p_0(c), a_0^c) = \mathcal{L}^{c'}(p_0(c'), a_0^{c'}) \qquad\qquad \text{for } c, c' \in \text{supp}(\mu_z)$$

$$\mathcal{L}^c(p_0(c), a_0^c) \leq \mathcal{L}^{c'}(1, a_0^{c'}) \qquad\quad \text{for } c \in \text{supp}(\mu_z), c' \notin \text{supp}(\mu_z),$$

where we highlight the fact that announcements which are not made in equilibrium grant full reputation: $p_0(c) = 1$ for all $c \notin \text{supp}(\mu_z)$.

**Definition**    An *equilibrium with vanishingly small reputation* is the limit of reputational equilibria as $z \to 0$.

$$\mu^\star = \lim_{z \to 0} \mu_z$$

An alternative definition of equilibrium follows Kambe (1999) and does away with the initial inference by the private sector. Instead, it corresponds to the case where the government first announces a plan $c$ and subsequently becomes committed to following it with some exogenous probability $p_0$, independent of $c$.

**Definition** For given $p_0 \in [0, 1]$, a K-*equilibrium* is an announcement $c_K^\star(p_0)$ and continuation equilibria $\{\mathcal{L}^c, g_c^\star\}_{c \in \mathcal{C}}$ such that

$$c_K^\star(p_0) = \arg\min_c \mathcal{L}^c(p_0, a_0^c)$$

Similarly to reputational equilibria, we are especially interested in the limiting announcement $c_K^\star(p_0)$ as $p_0 \to 0$.

Finding a $K$-equilibrium is simple. For a given plan $c$ and reputation $p_0$, the value of starting plan $c$ at reputation $p_0$, $\mathcal{L}^c(p_0, a_0^c)$ can be found applying our previous discussion. We then optimize over this function by choosing $c$ in $\mathcal{C}$, keeping $p_0$ fixed.

To find a reputational equilibrium, we proceed as follows: given $k \in \mathbb{R}$, we partition the space of plans according to whether

$$\mathcal{L}(1, c) \lessgtr k$$

Plans that have a loss greater than $k$ are assigned probability zero, $\mu(c) = 0$. For the remainder of plans, we find a probability $p_0(c)$ that delivers $k$ by requiring

$$\mathcal{L}(p_0(c), c) = k$$

For plan $c$ to start with a reputation of $p_0(c)$, the initial application of Bayes' rule (4) tells us that $c$ must be played with a probability $\mu(c)$ such that

$$p_0(c) = \frac{z\nu(c)}{z\nu(c) + (1 - z)\mu(c)}$$

Finally, the planner's strategy is required to be a probability distribution. Therefore, we pin down $k$ by requiring that at the end of this process the non-negative function $\mu(c)$ integrates to 1 over the set of possible plans $\mathcal{C}$.

## 3.1 Reputation-building incentives

First-order conditions in the government's problem involve critically the marginal effect of inflation on output and on future reputation. Rearraging the Phillips curve yields that output is affected by inflation according to

$$\frac{\partial y}{\partial \pi} = \frac{1}{\kappa}\left[1 - \beta\frac{\partial p'}{\partial \pi}\left(\varphi_c(a) - g^\star(p', \varphi_c(a)) + (1 - p')\frac{\partial g^\star(p', \varphi_c(a))}{\partial p'}\right)\right] \tag{7}$$

Inflation affects current output through three different channels, corresponding to three terms in equation (7). The first term, $\frac{1}{\kappa} \cdot 1$, describes the standard, direct effect of inflation on output.

The second term, $\beta\frac{1}{\kappa}\left(-\frac{\partial p'}{\partial \pi}\right)(\varphi_c(a) - g^\star(p', \varphi_c(a)))$, describes an expectation-shifting effect by which more inflation reduces the posterior $p'$ and therefore moves expectations of future inflation away from the target $\varphi_c(a)$ and toward the expected choice of the rational type $g^\star(p', \varphi_c(a))$.

Finally, the third effect is given by $\beta\frac{1}{\kappa}\left(-\frac{\partial p'}{\partial \pi}\right)(1 - p')\frac{\partial g^\star(p', \varphi_c(a))}{\partial p'}$. It describes how more inflation today moves the expected choice of future rational governments through its effect on their reputation.

## 3.2 Reputation and credibility

Let $\pi^N$ be the (mean) level of inflation in the Nash equilibrium of the stage game or, equivalently, in a Markov equilibrium when $p = 0$. First-order conditions of the government's choice in this case imply that

$$\pi^N = y^\star\frac{\kappa}{1 - \beta + \kappa^2\gamma}$$

**Observation** In any continuation equilibrium, the rational type's choice of inflation is bounded above by the choice in the Nash equilibrium of the stage game:

$$\forall c \in \mathcal{C} : \qquad g_c^\star(p, a) \leq \pi^N$$

We define the credibility of a plan as the ratio of announced and (expected) realized inflation, normalized by their distance from Nash inflation.

**Definition** Given a plan $c$, its *remaining credibility* in state $(p, a)$ is

$$C(p, a; c) = \mathbb{E}\left[(1 - \beta)\frac{\pi^N - \pi}{\pi^N - a} + \beta C(p'_c(p, a), \varphi_c(a))\right] \tag{8}$$

$$= (1 - \beta)\frac{\pi^N - [pa + (1 - p)g^\star_c(p, a)]}{\pi^N - a} + \beta\mathbb{E}\left[C(p'_c(p, a), \varphi_c(a))\right]$$

where $\pi^N$ is Nash inflation. The *credibility* of a plan in a $K$-equilibrium is then given by

$$C^K(c) = \lim_{p \to 0} C(p, a_0(c); c)$$

while in a reputational equilibrium it is

$$C^\star(c) = \lim_{z \to 0}\int C(p_0(c), a_0(c); c)d\mu_z(c)$$

## 4. Analysis and Numerical Results

We solve the model numerically for different announcements $c \in \mathcal{C}$.

### 4.1 Parametrization

We parametrize our model following Lu, King, and Pastén (2016) and pick our preference and technology parameters $\gamma, \kappa, y^\star$ consistently with the planner's objective function and Phillips curve in a standard New Keynesian economy calibrated to US data (Galí, 2015; Galí and Gertler, 1999). Table 1 summarizes our parameter choices.

Table 1: Benchmark calibration

| Parameter | Value | Definition | Source / Target |
|-----------|-------|------------|-----------------|
| $\beta$ | 0.995 | Discount factor | 2% real interest rate |
| $\gamma$ | 60 | Inflation weight | Lu, King, and Pastén (2016) |
| $\sigma$ | 1% | Std of control shock | Lu, King, and Pastén (2016) |
| $\kappa$ | 0.17 | Slope of Phillips curve | Lu, King, and Pastén (2016) |
| $y^\star$ | 5% | Output target | Lu, King, and Pastén (2016) |

## 4.2    Continuation equilibrium after announcement c

Figure 2 shows a typical value function $\mathcal{L}^c(p, a)$ for an arbitrary plan $c$. All plots have current reputation $p$ in the $x$-axis. Darker lines correspond to lower current announcements $a$.
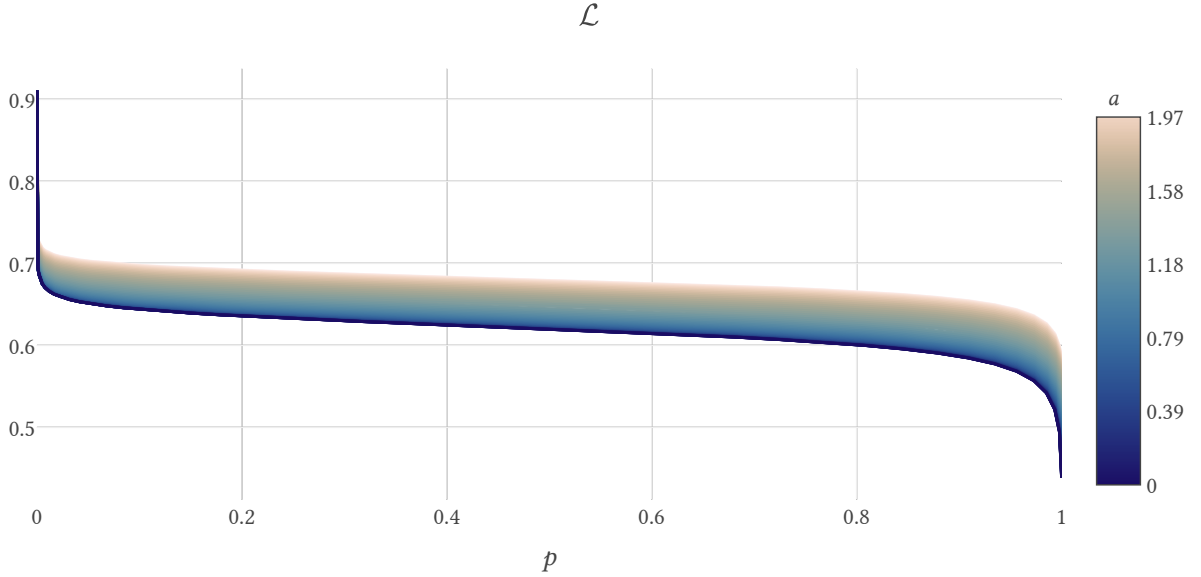


FIGURE 2: LOSS FUNCTION AFTER ANNOUNCEMENT $c$

There are three observations to make. First, $\mathcal{L}$ is decreasing in $p$. An increase in reputation generally decreases expected inflation leading to higher current output.

Second, the loss function has a convex-concave shape, which reflects the dynamics of reputation. A value close to either 0 or 1 for reputation means that the public is confident in its assessment of who it faces. As reputation approaches the bounds, more evidence is required to make it move. An increase (decrease) of the same magnitude is hard to revert when reputation is close to 1 (0), which makes the government attach a larger value to it.

Finally, at high levels of reputation, a lower current target $a$ is unambiguously good. When $p$ is high, lower $a$ mostly means lower inflation expectations. However, when $p$ is small a lower $a$ also means a larger expected loss of reputation (as a more ambitious target fosters a larger deviation), which makes more modest targets preferable.

On the other hand, as reputation decreases, the gap between $a$-lines shrinks as two effects arise. The first effect is that with lower reputation the current announcement becomes less rele-

vant as its weight in expected inflation decreases. The second effect concerns the government's choice and how close to $a$ it chooses to set mean inflation. If at low reputation the government chooses to deviate more from lower announcements, this second force might make it prefer a higher announcement today. This is indeed the case: for most plans, at low values of $p$ the loss function is minimized at an interior value for $a$.

Figure 3 shows deviations from the current target as a function of current reputation and target. It shows that the deviation $g^\star - a$ is generally decreasing in reputation, except when both reputation and the announcement are near zero. The figure also reveals a discontinuity at zero reputation, where the government reverts to Nash inflation regardless of announcements. When reputation is exactly zero, Bayes' rule prevents it from moving. This makes the government entirely disregard the plan. By the same logic, a planner with zero reputation is indifferent across all plans, as they all yield the stage Nash payoff at $p = 0$.
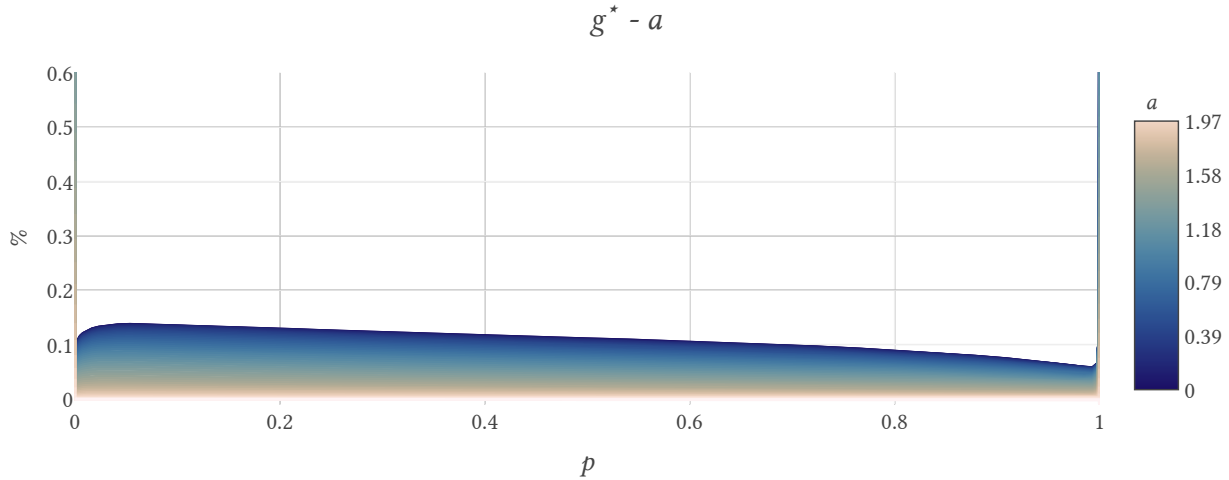


FIGURE 3: INFLATION DEVIATIONS

The effect of reputation $p$ on the deviation $g^\star(p, a) - a$ is complicated and arises from the sum of many forces. On the one hand, a larger stock of reputation makes the planner more inclined to spend it. Moreover, at higher levels of reputation Bayes' rule implies that reputation is more difficult to lose, which increases incentives to gamble. But on the other hand, at higher reputation delivering on the announcement is less costly, especially when the current announcement is also high.

A higher current announcement $a$ has a more clear effect on the deviation: the lower $a$, the

further away from it will the rational type set inflation. The reason is simple: getting inflation close to target rewards the government in roughly the same way, but it is more costly to set inflation close to target when the target is lower.

Figure 4 shows average reputation $p'$ as function of current reputation $p$ and announcement $a$. First, $\mathbb{E}[p']$ is always below $p$, as predicted by Lemma ??. At the highest announcement we consider, which coincides with the Nash equilibrium of the stage game, by definition the government has no incentives to deviate so it chooses $g = a$ for all levels of $p$. As a result, reputation does not move. For all announcements lower than Nash inflation, reputation falls on average.
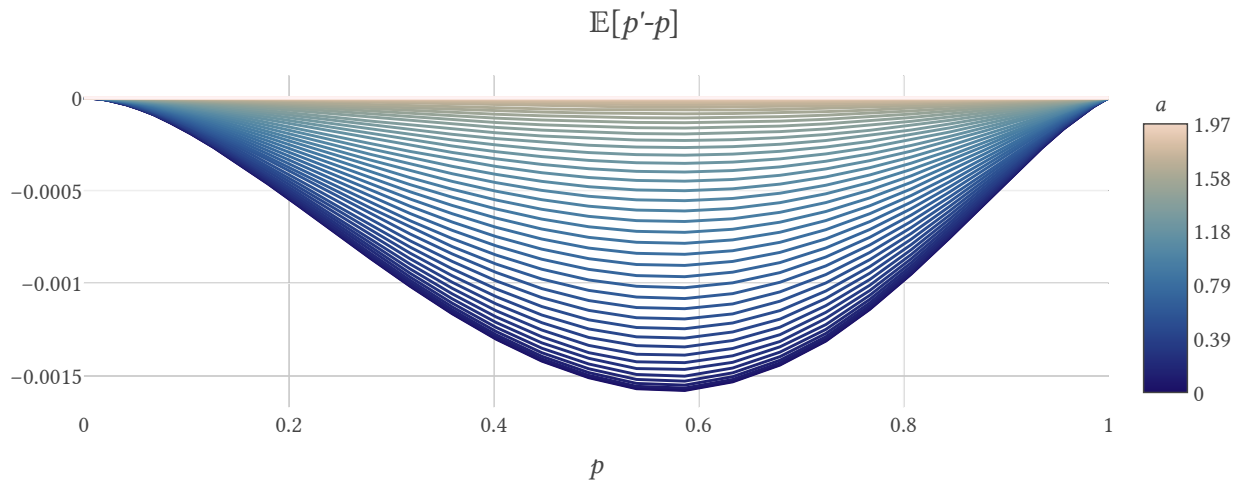


FIGURE 4: EXPECTED REPUTATION LOSSES

Second, lower announcements are associated with a larger expected reputation loss. Lower current announcements generate weaker incentives to deliver target inflation: as the temptation to inflate grows larger, the government prefers to spend more of its reputation to achieve more output.

Third, Bayes' rule forces $p'$ to be close to $p$ when $p$ is close to either 0 or 1. However, the picture looks skewed to the right, which means that the government 'spends' more reputation when it has more of it. This is especially true at high levels of $p$, consistent with Figure 3. At low levels of reputation, the government expects to lose more reputation when its current target $a$ is lower.

## 4.3   Announcements in the K-equilibrium

Figure 5 shows the $K$-equilibrium as a function of $p_0$, which is simply the loss-minimizing plan conditional on starting with reputation $p_0$. The top panel shows the decay rate $1 - e^{-\omega}$ (in percent terms) while the bottom panel shows the choice of initial inflation $a_0$ and asymptote $\chi$.
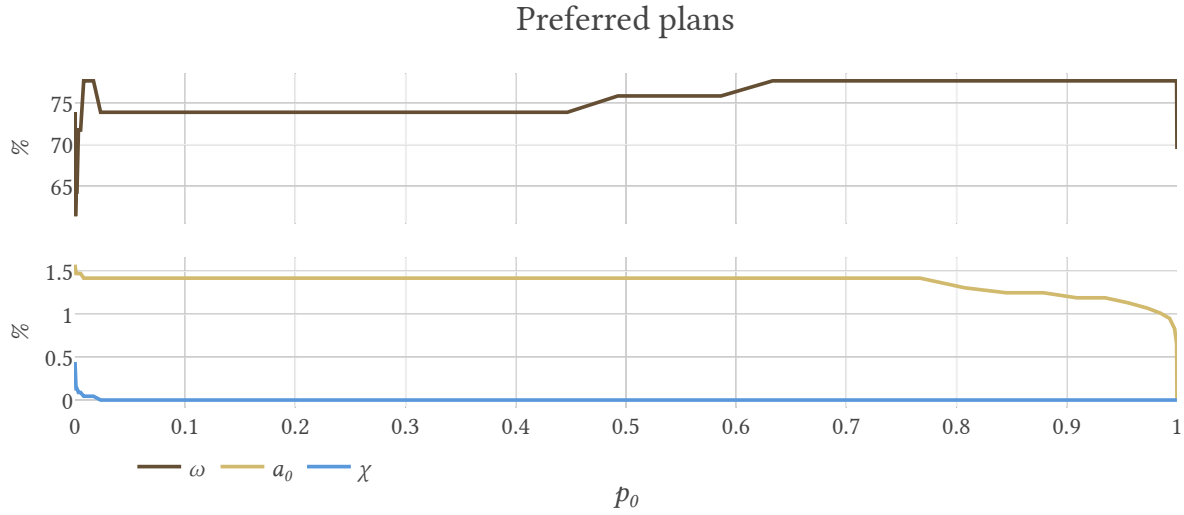


Preferred plans

FIGURE 5: PREFERRED PLANS WITH DIFFERENT $p_0$

At $p_0 = 1$, any announcement is believed by the private sector, regardless of expectations about the behavior of the rational type. The planner sets expectations at their most advantageous level by promising zero inflation throughout. The rational type intends to break this promise, given that at full reputation the private sector never learns. As soon as the initial posterior $p_0$ is less than one, the planner starts caring about incentivizing its future selves to behave and conserve reputation. This leads the planner to prefer plans that have a higher initial inflation $a_0$. The planner also chooses plans that make inflation decrease over time by setting $a_0 > \chi$, meaning that the planner attempts a gradual disinflation. This property holds even as $p_0$ approaches zero.

Figure 6 shows the determination of the $K$-equilibrium when $p_0$ is small. For each decay $\omega$ and asymptote $\chi$ we plot the minimized loss function $\min_{a_0} \mathcal{L}(p_0, (a_0, \omega, \chi))$. The $x$-axis moves $\omega$ while different curves plot different values of $\chi$.

Some patterns are evident from Figure 6. The overall minimum is achieved at a point with both $\omega, \chi > 0$: the $K$-equilibrium has the initial planner promise a gradual disinflation that does

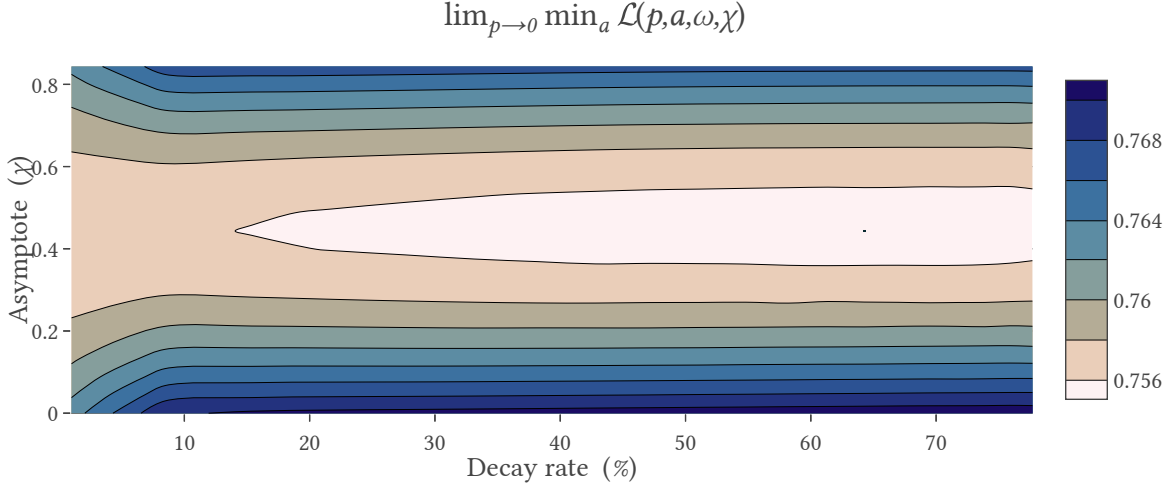not converge to the first best level of zero inflation.

$$\lim_{p \to 0} \min_a \mathcal{L}(p, a, \omega, \chi)$$



FIGURE 6: LOSS FUNCTION ACROSS ANNOUNCEMENTS

When $\chi$ is small, plans eventually imply very low levels of inflation which makes them more dificult to sustain: reputation is lost quickly when $a$ is small. This gives rise to unfavorable continuation values as the government is revealed to be rational and reverts back to the high-inflation stage Nash. For this reason, at low $\chi$ the planner prefers to make the decay rate slow by choosing $\omega$ as low as possible. This way, the plan only promises very low inflation in the far future. When $\chi$ is higher, the planner uses a decay rate that provides incentives even in the short run. These values of $\chi$ turn out to be preferred.

Finally, $\chi$ cannot grow too much either. As $\chi$ approaches Nash inflation, the plan becomes arbitrarily easy to keep, but provides very small gains.

## 4.4   Credibility

Our setup distinguishes reputation $p$, the posterior that the government is the behavioral type that was announced, from credibility $C(p, a; c)$, the expected discounted deviations from plan $c$ at reputation $p$ and current announcement $a$, as defined in (8). Figure 7 plots the credibility of different plans at vanishingly small reputation, as a function of the decay rate $\omega$ and the asymptote $\chi$, for the loss-minimizing initial inflation $a_0$ at those parameters.

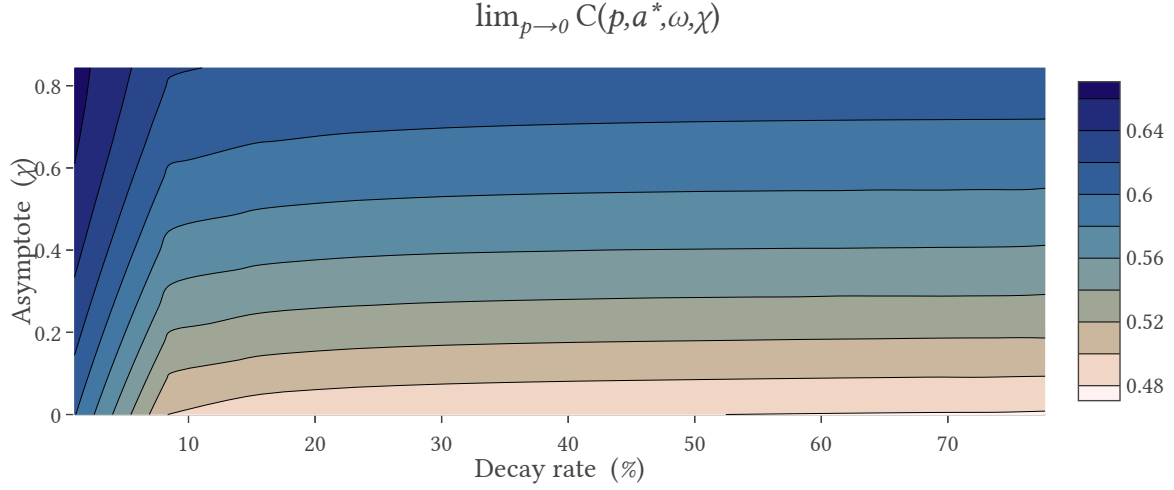$$\lim_{p \to 0} C(p, a^*, \omega, \chi)$$

FIGURE 7: CREDIBILITY

Plans with a lower asymptote are less credible, as are plans with a steeper promised descent of inflation. One should be careful about this result, as it mostly reflects the fact that plans with fast decay reach a phase in which the targets are almost constant more quickly.

## 4.5 Distribution of announcements in the reputational equilibrium

We now turn to a description of the reputational equilibrium and its distributions $\mu_z$. Figure 8 plots the average plan as a function of initial reputation $z$.
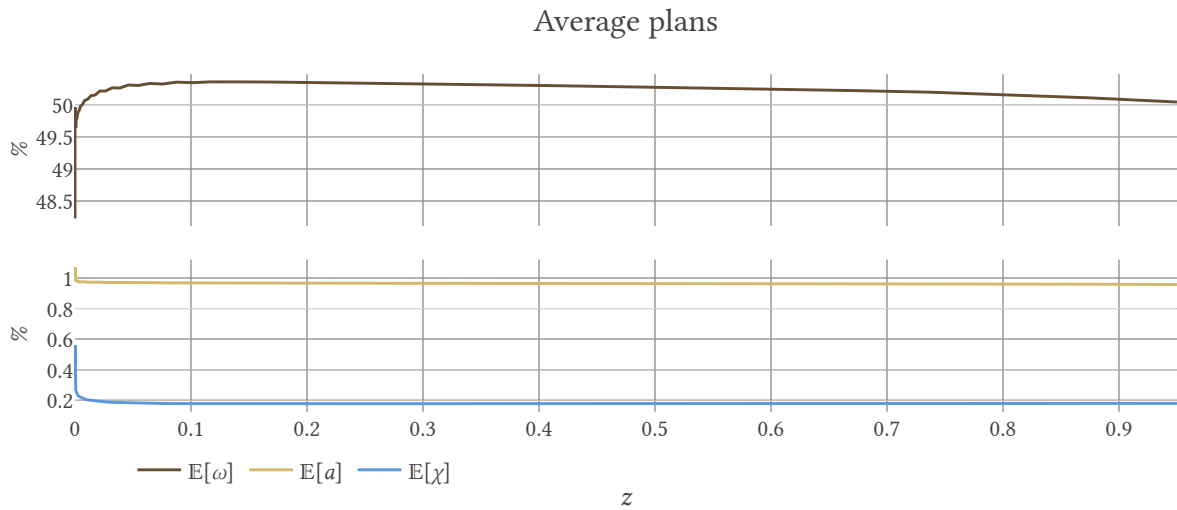


FIGURE 8: REPUTATIONAL EQUILIBRIUM ANNOUNCEMENTS

For intermediate values of initial reputation $z$, the planner chooses (on average) a disinflation path that starts from about half Nash inflation and converges towards a tenth of it, by about half the distance each period. As initial reputation becomes very small, as before, the planner starts to put more weight on plans that converge toward a higher asymptote $\chi$.

For extremely low initial reputation, Figure 9 shows the limiting distribution $\mu^{\star} = \lim_{z \to 0} \mu_z$. The left panel shows the distribution of types as a function of the asymptote $\chi$ and initial inflation $a_0$, integrating over the decay rate $\omega$, while the right panel integrates over initial inflation. Figure
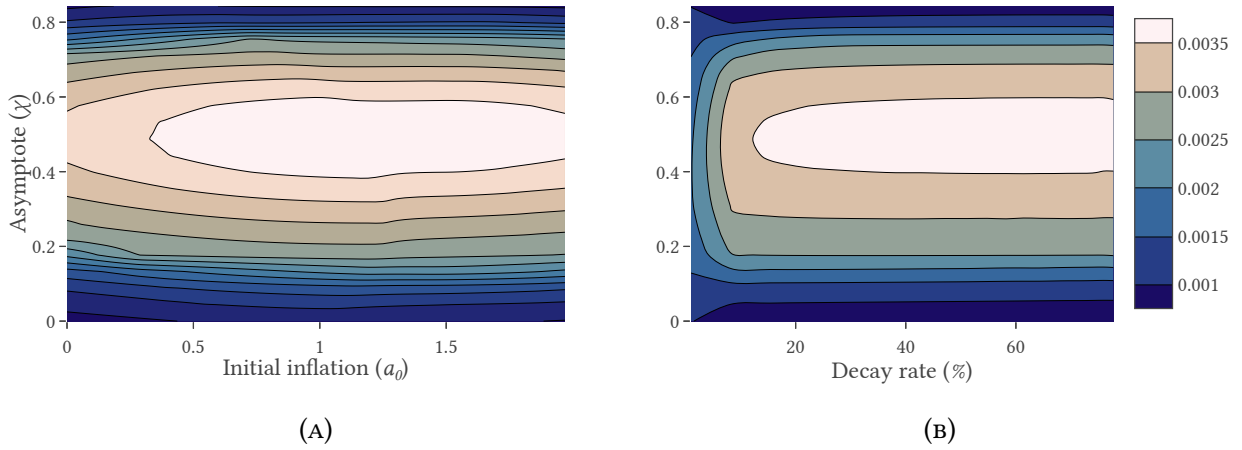


FIGURE 9: DISTRIBUTION OF TYPES

9a on the left shows that the planner tends to choose gradual plans with higher initial inflation $a_0$ than asymptote inflation $\chi$. This probability is $\mathbb{P}\left(a_0 > \chi\right) = 70.5\%$. Moreover, the planner chooses plans whose initial inflation is at least five times the asymptote quite often, $\mathbb{P}\left(a_0 > 5\chi\right) = 17.2\%$. While the level of initial inflation varies from plan to plan, the asymptote seems more precisely set: the density of $a_0$ and $\chi$ in the reputational equilibrium announcement falls sharply for $\chi$ away from its maximum, while it stays flat over many more values of initial inflation $a_0$.

On the right, Figure 9b bears a close resemblance to Figure 6 which plotted the $K$-equilibrium loss function at low $p_0$. Plans with a lower loss in the $K$-equilibrium are good for the planner, so they are announced more often. Hence, the planner starts with lower reputation in those plans, which lowers their value in the equilibrium. This initial update of reputation (from $z$ to $p_0$) makes the planner indifferent across all plans (announced in equilibrium), which ultimately justifies the

mixed strategy of announcement. There are however some differences between Figures 6 and 9b: the planner does not appear to play plans with a low decay rate, as the density $\mu^\star$ falls sharply as $\omega$ becomes small. Other than this, the density of announcement also seems flat along the decay rate dimension, as happened with the initial level of inflation.

## 5. COMPARATIVE STATICS

Figure 10 shows the average plan announced in the reputational equilibrium, as a function of the variance of the control shock $\sigma$. Broadly speaking, more noise in the control makes deviations less observable. Therefore, the level of adherence to plans decreases with the noise. This makes the planner choose less ambitious plans when the control over inflation is less tight: as $\sigma$ increases, the average plan has a higher asymptote $\chi$, a slightly higher starting point $a_0$, and a slower rate of decay $\omega$.
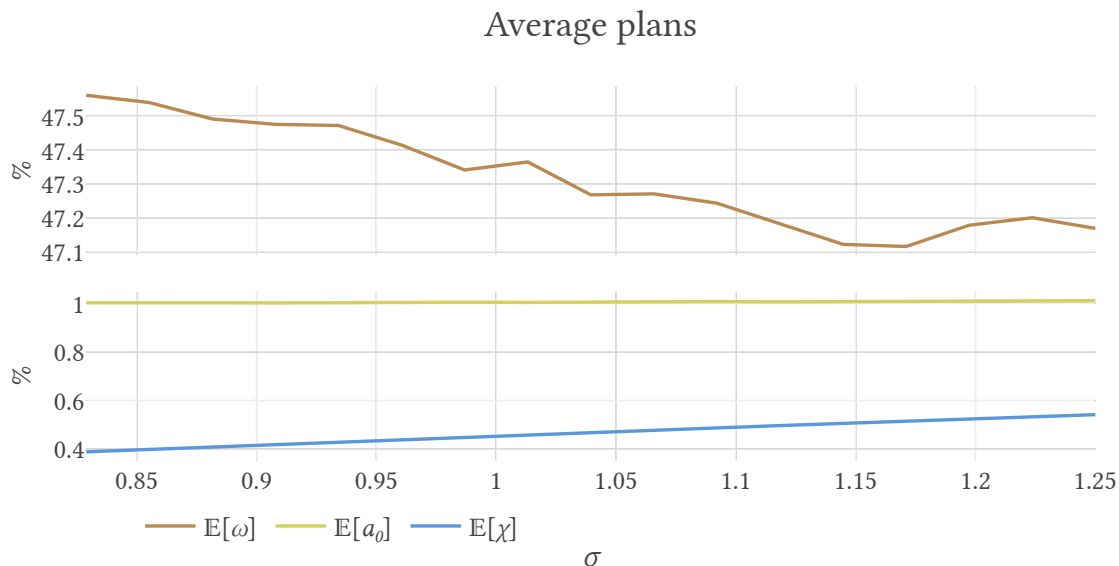


FIGURE 10: AVERAGE PLANS AND THE CONTROL SHOCK VARIANCE

Figure 11 repeats the exercise varying the discount factor $\beta$ and the slope of the Phillips curve $\kappa$. It reveals some subtleties in the manipulation of the three parameters that describe our plans. Figure 11a shows the average plan as a function of the discount rate $1/\beta - 1$ (whose benchmark value is 2% in annual terms). As the planner becomes more impatient, average plans

start higher and converge to lower inflation, with a faster decay rate. With more impatience, the public expects a larger inflation bias. For this reason, the planner tends to choose plans that are more resilient. Increasing initial inflation makes the plan easier to keep, while decreasing asymptotic inflation makes it more costly to deviate early on. Having a steeper descent of inflation contributes to both objectives.

When we vary the slope of the Phillips curve, the planner chooses to announce lower inflation throughout. Figure 11b shows that when the Phillips curve is steeper (meaning that the same increase in current inflation produces a smaller output boom), the planner chooses to lower targets for inflation. Here the logic is that with a steep Phillips curve there are weaker incentives to create surprise inflation, which allows the planner to announce less inflation throughout.
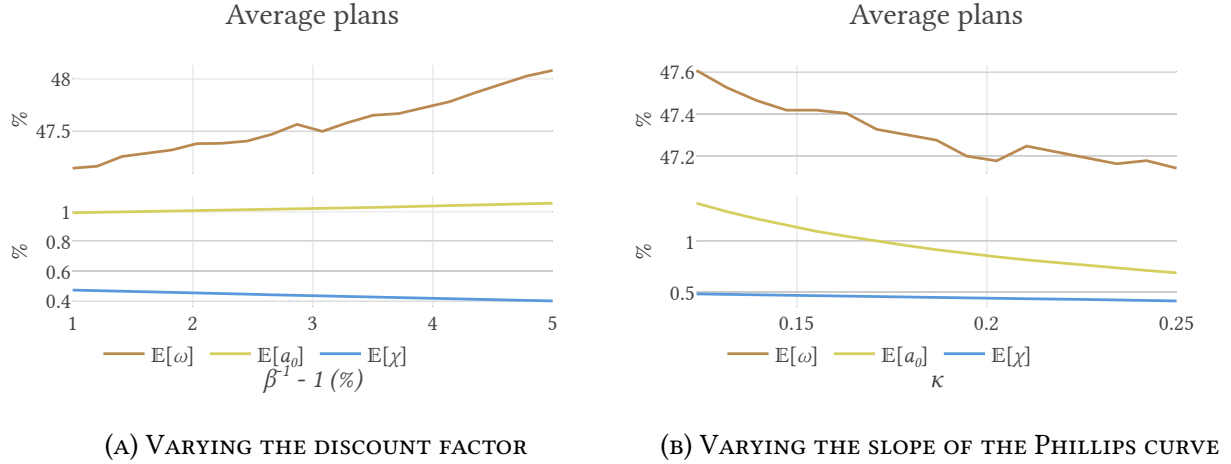


(A) Varying the discount factor

(B) Varying the slope of the Phillips curve

Figure 11: Average plans

## 6. Other Models

Our benchmark model of reputation with imperfect control yields gradual disinflation plans. We dissect this result by comparing our model to salient models in the literature on sustainable plans. We start from the Ramsey plan and slowly enrich the structure of the model to see which mathematical features create the incentive for gradualism.

## 6.1 The Ramsey plan

We refer to choosing an entire path $\{g_t\}_t$ with commitment to minimize (1) subject to (2) and (3) as the *Ramsey* plan. The linear-quadratic structure of this problem alows us to disregard the issue of imperfect control: the presence of the shocks $\epsilon_t$ only affects the planner through a variance term independent of policy.

Standard techniques allow us to use Lagrange multipliers of each time-$t$ constraint to write the problem recursively for $t > 0$ as

$$v^{FB}(\theta) = \max_{\theta'} \min_{y,\pi} (y - y^\star)^2 + \gamma \pi^2 + \theta'(\pi - \kappa y) - \theta\pi + \beta v^{FB}(\theta') \tag{9}$$

Problem (9) produces policy functions $g_\pi^{FB}(\theta), g_y^{FB}(\theta), g_\theta^{FB}(\theta)$ that describe the planner's actions for each period. At time 0, the planner does not carry any multipliers from the past and attains a value

$$\mathcal{J}^{FB} = v^{FB}(0) \tag{10}$$

To reconstruct the plan, we recursively apply the policy functions $g^{FB}$, starting from the solution $\theta^{FB}$ to (10)

$$\theta_t = \begin{cases} g_\theta^{FB}(\theta_{t-1}) & \text{if } t > 0 \\ 0 & \text{if } t = 0 \end{cases} \quad \text{and} \quad \pi_t = g_\pi^{FB}(\theta_t) \tag{11}$$

Figure 12 plots the Ramsey plan against the average announcement in the reputational equilibrium, as well as the announcement in the $K$-equilibrium. The power of commitment enables a complete disinflation: Ramsey inflation is basically zero about a year and a half after the announcement of the plan. The Ramsey plan also starts from a high level, about three quarters of the way to Nash inflation. This is because the planner understands that inflation in the first period of the plan does not affect past inflation, which is sunk at the moment of the announcement. Inflation then comes down as the planner smooths the benefits of initial inflation on output over a few of the initial periods.

In contrast, the reputational equilibrium announcements do not converge to zero (Figure 9a shows a low probability that $\chi = 0$). The $K$-equilibrium announcement, which minimizes the
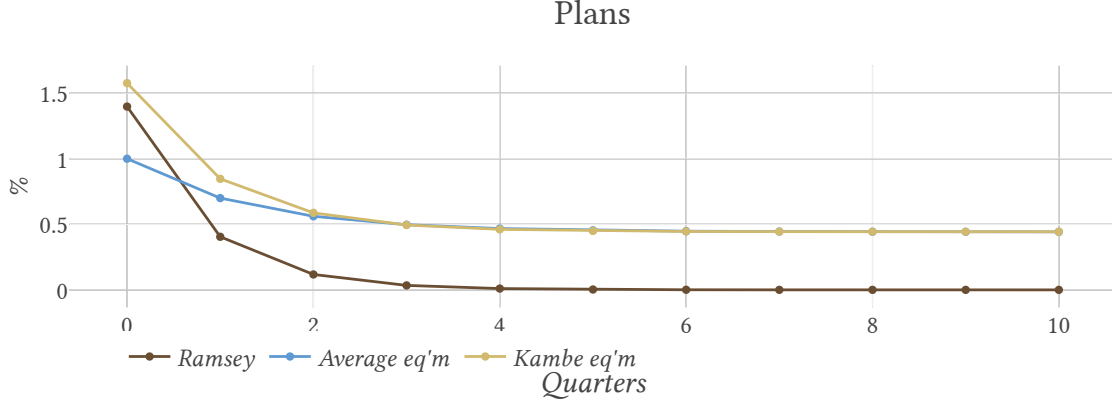
Plans

FIGURE 12: THE RAMSEY PLAN AND EQUILIBRIUM ANNOUNCEMENTS

loss conditional on starting from a very low (but constant) level of reputation, starts above the Ramsey plan. It needs high initial inflation to create the descent that fuels incentives. Turning to the average reputational equilibrium announcement, it starts below the *K*-equilibrium plan. This is because some of the plans in the support of the announcement distribution do not resort to such high initial inflation: as they are announced less often, they start with higher reputation. This makes them attractive even as their credibility would be lower at the same *p*.

## 6.2   Sustainable plans with expectations as threats

The Ramsey plan can be decentralized by choosing appropriately high inflation expectations $\xi$ in case of deviation. We start by considering a world in which control over inflation is perfect. Letting $p \in \{0, 1\}$ be the indicator of whether the planner is keeping past promises,

$$v^{\xi}(p, a) = \min_{y, \pi, a'} \ (y - y^{\star})^2 + \gamma \pi^2 + \beta v^{\xi}(p', a') \tag{12}$$

$$\text{subject to} \quad \pi = \kappa y + \beta \left( p' g_{\pi}^{\xi}(1, a') + (1 - p') \xi \right)$$

$$p' = \begin{cases} 1 & \text{if } \pi = a \text{ and } p = 1 \\ 0 & \text{otherwise} \end{cases}$$

where as our main analysis $g_{\pi}^{\xi}(a)$ is the equilibrium policy function (when the punishment is $\xi$) at state $a$, which the planner takes as given but coincides with its $v^{\xi}$-minimizing choice. In the

first period, the planner is also allowed to choose the initial $a_0$, attaining a value

$$\bar{\mathcal{J}}^{\xi} = \min_a v^{\xi}(1, a) \tag{13}$$

We let the planner start with 'full reputation' ($p = 1$) as in this interpretation $p$ stands for whether or not the planner has deviated from the path. Figure 13 plots sustainable plans for different values of $\xi$, along with the Ramsey plan. We recover a well-known result from the
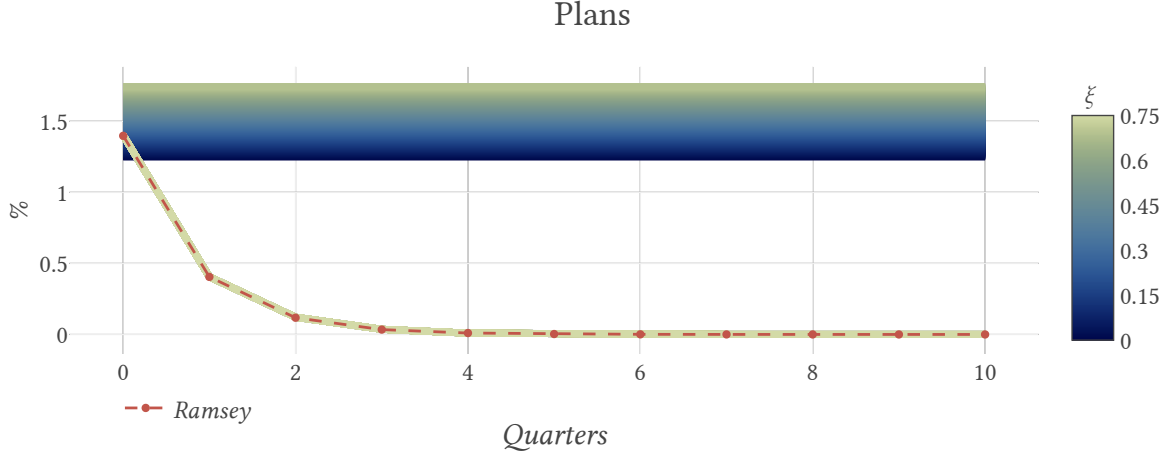


FIGURE 13: SUSTAINABLE PLANS AT DIFFERENT PUNISHMENTS

literature: when the punishment is harsh enough, (12) recovers the Ramsey plan. However, when the Ramsey plan is not sustainable, the planner deviates from any plan. $\xi$ then only affects the level of inflation expectations that the planner, who deviates immediately, is best-responding to.

## 6.3 Sustainable plans with reverting triggers

The Ramsey plan is built on the fact that all deviations are detected. In this case, the private sector can threaten to, in our language, send the reputation to zero. With imperfect control, this is no longer the case. The private sector understands that any threat might be triggered on-path without actual deviations having taken place. Assessing punishment strategies needs to weigh deterrent against the costs from false positives. This is why we consider a version in which, like in Green and Porter (1984), the private sector shifts to a punishment regime whenever realized inflation deviates from the target by more than some threshold, and reverts stochastically from it.

An equilibrium with reverting triggers is parametrized by a distance $D$ between realized and announced inflation that triggers the punishment, a probability of return $\theta$ to the normal regime, and 'punishing' expectations $\xi$. We have

$$v^G(a) = \min_{g,a'} \mathbb{E}\left[(y - y^\star)^2 + \gamma\pi^2 + \beta\left(p'v^G(a) + (1 - p')v^P\right)\right] \tag{14}$$

$$\text{subject to} \quad \pi = g + \epsilon$$

$$\pi = \kappa y + \beta\left(p'g^G(a') + (1 - p')\xi\right)$$

$$p' = \begin{cases} 1 & \text{if } \frac{|\pi - a|}{a} < D \\ 0 & \text{otherwise} \end{cases}$$

with, as the control shock only leaves a variance term like before,

$$v^P = \min_{\pi,a'} (y - y^\star)^2 + \gamma\pi^2 + \beta\left(\theta v^G(a) + (1 - \theta)v^P\right) + \sigma_\epsilon^2\left(\gamma + \frac{1}{\kappa^2}\right) \tag{15}$$

$$\text{subject to} \quad \pi = \kappa y + \beta\xi$$

where, once more, in the first period the planner can choose the very first announcement in the $G$ regime ($p = 1$) attaining a value

$$\mathcal{J}^G = \min_a v^G(a) \tag{16}$$

Figure 14 shows the path of mean inflation $g^G(a_t)$ assuming that the punishment regime is never triggered, for different levels of $\xi$.
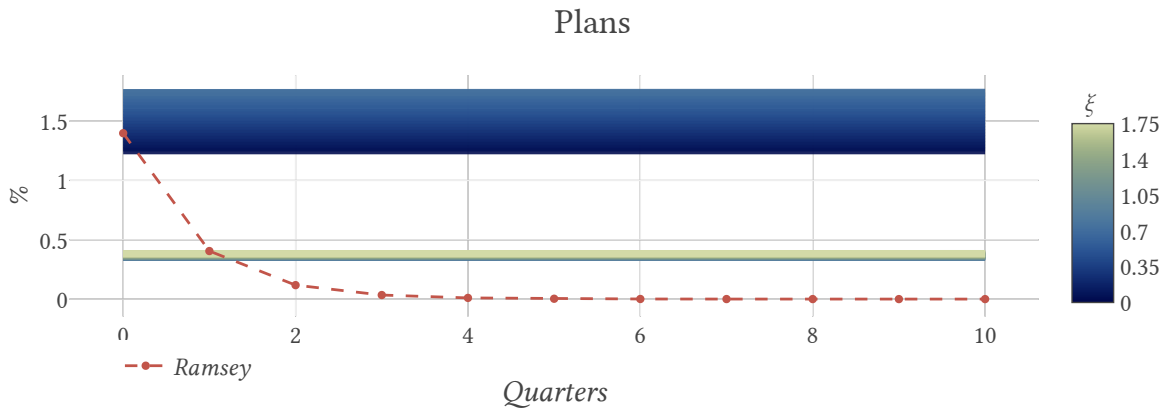


FIGURE 14: SUSTAINABLE PLANS WITH REVERTING TRIGGERS AT DIFFERENT PUNISHMENTS

As before, when $\xi$ is small the planner understands that promises will be broken and simply best responds to these expectations. When $\xi$ is larger, the planner is able to target lower levels of inflation. In this case with imperfect control, something interesting happens: while the planner is able to announce lower levels of inflation, it can promise neither zero inflation nor the Ramsey plan.

## 6.4    Recursive plans with reputation

Notice that in all these previous versions, the roles of $g(a)$ and $\xi$ are reversed in comparison to our baseline notions of reputational and $K$-equilibrium. In the Ramsey model and our version of the Green-Porter model, the private sector expects the government's strategy when reputation is high and the exogenous parameter $\xi$ (the private sector's threat) when it is low. In both reputational and $K$-equilibria, the private sector expects the behavioral government to follow the announcement and the rational government to follow its strategy. While this may appear as an innocuous relabelling of types, we will now show that this shift makes the optimal plan look very different.

We now consider a version in which, like in Dovis and Kirpalani (2019), the government is made up of two agents: a morning planner and an afternoon policy maker. In the morning of period $t$, the planner announces a policy recommendation for the afternoon of $t + 1$ (given an announcement for the afternoon of $t$ made earlier). The action in each period happens in the afternoon, when the policy maker chooses inflation. The policy maker can be either a commitment type who stubbornly follows the recommendation, or a rational type who chooses whether to follow it. The planner and the private sector do not know which type of policy maker they face but make statistical inference based on past realizations of inflation. In contrast to Dovis and Kirpalani (2019), we retain the feature of imperfect control and the new Keynesian Phillips curve that we use in our baseline. We refer to the equilibrium announcements in this game as *recursive plans (with reputation)*.

Our timing assumption is done for simplicity and to improve comparability to our benchmark. The target at $t + 1$ can depend on reputation at $t$ but not on realized inflation at $t$, or reputation at $t + 1$. Thus, when faced with a target $a$ and its current reputation is $p$, the policy maker attains

a value of

$$v^R(p, a) = \min_{g, a'} \mathbb{E}\left[(y - y^\star)^2 + \gamma\pi^2 + \beta v^R(p', a')\right] \tag{17}$$

$$\text{subject to} \quad \pi = g + \epsilon$$

$$\pi = \kappa y + \beta\left(p'a' + (1 - p')g^R(p', a')\right)$$

$$p' = p + p(1 - p)\frac{f_\epsilon(\pi - a) - f_\epsilon(\pi - g^R(p, a))}{pf_\epsilon(\pi - a) + (1 - p)f_\epsilon(\pi - g^R(p, a))}$$

Like in our benchmark analysis, we are interested in the low-reputation case. The planner then attains an initial value of

$$\mathcal{F}^R = \lim_{p \to 0} \min_a v^R(p, a)$$

Figure 15 plots the recursive plan with reputation for different levels of initial reputation. The
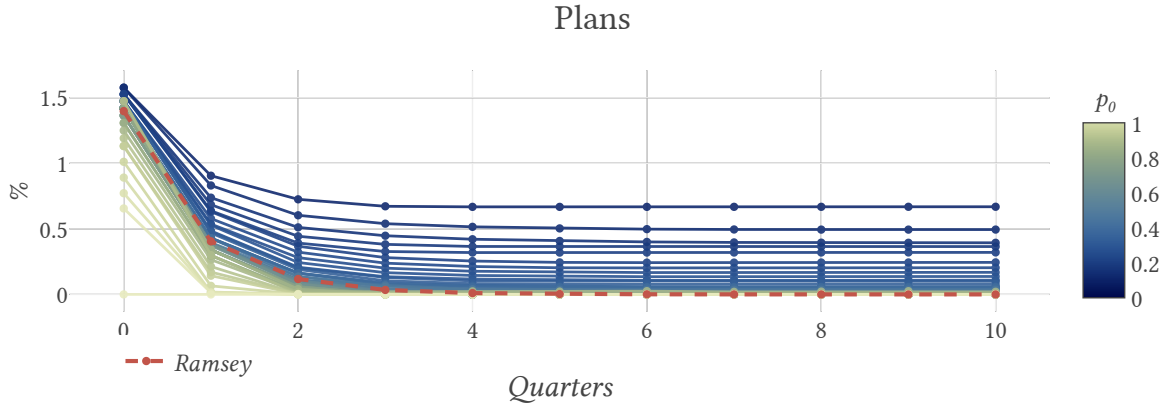


FIGURE 15: RECURSIVE PLANS WITH REPUTATION

planner with full reputation enjoys complete credibility for all plans and hence announces a plan of zero inflation throughout, which it intends to break, as this will not alter expectations in any way. With moderate initial reputation the planner announces a positive level of initial inflation, which converges to zero inflation. When initial reputation is low, the plan stops converging to zero, in a similar pattern to the one delivered by the $K$-equilibrium.

## 6.5 Discussion

In this section, we explored the role of the various assumptions that describe our model in relation to the literature. Our model differs from the Ramsey plan (and its descentralization as a

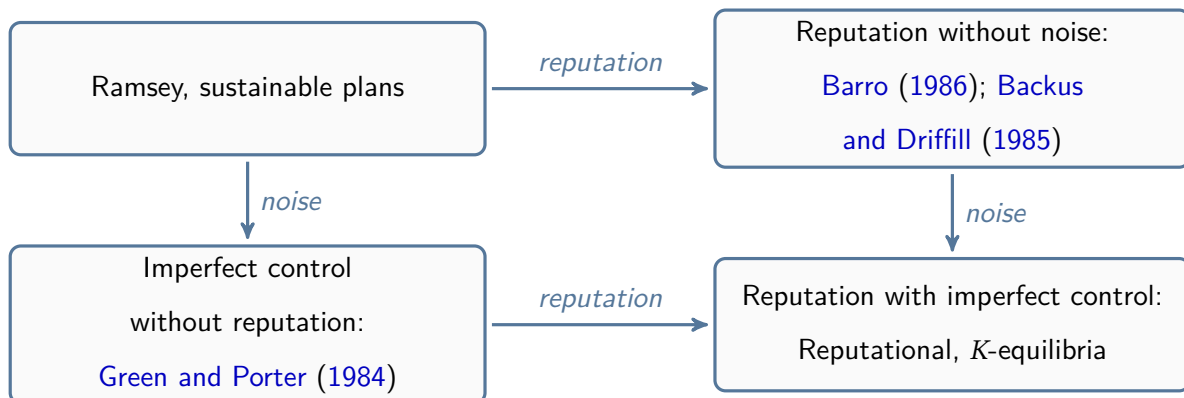sustainable plan) along two key aspects: reputation and imperfect control.



FIGURE 16: MODELS

Figure 16 illustrates this relation. Early papers like Barro (1986) and Backus and Driffill (1985) departed from the sustainable plan by introducing reputation without noise. Their results were negative in the sense that they recovered the Ramsey plan (zero inflation throughout in their context of a simultaneous Phillips curve). Our reformulation of the Green and Porter (1984) model introduces noise but leaves out reputation. This switch produced the result that, at high enough threat, the planner chooses a plan with inflation below Nash. However, the threat structure under which reputation can only jump to zero induced the planner to choose inflation targets that are constant over time.

Our model of reputational equilibria mixes both of these assumptions by combining reputation and noise. In this case, the planner is able to take advantage of the dynamics of targets as they impart dynamics to its reputation. Our reformulation in terms of recursive plans with reputation shows that the result does not depend on the planner being able to choose all targets at once.

While recursive plans with reputation are inspired on Dovis and Kirpalani (2019), the models are very different. Theirs is predicated on considering perfect control of inflation as well as an old-style Phillips curve which depends on the difference between realized and expected inflation for the current period. Both differences turn out to be important: both intermediate combinations (no noise plus forward-looking Phillips curve and noise plus old-style Phillips curve) yield a flat optimal plan.

## 6.6 Gains from preannouncement and flexibility

Figure 17 plots the recursive plan with reputation against some of the other plans we have considered so far.
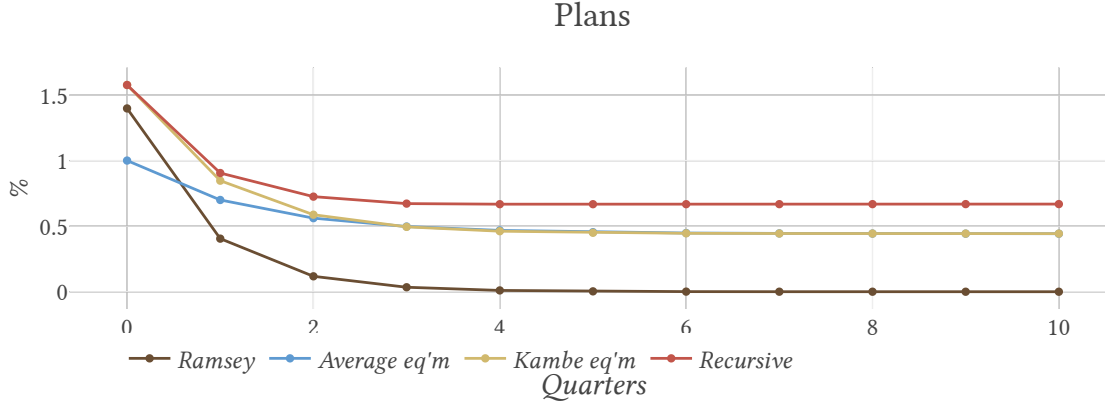


FIGURE 17: PLANS WITH REPUTATION

Inspecting problems (6) and (17) reveals that, while very similar, the recursive plan differs from optimal plans in reputational and $K$-equilibria in two important ways. In the latter, inflation targets for all periods are chosen at the beginning of time, while in the recursive plan they are chosen sequentially. Secondly, as a consequence of this, the recursive plan allows for feedback between the evolution of reputation and future targets.

Because of these differences, comparing the recursive plans to our baseline notions of equilibrium will mix two distinct effects. On the one hand, because the recursive plan can respond to the evolution of reputation, it benefits from the *flexibility* of tailoring future announcements to the current assessment of the credibility of different plans. On the other hand, reputational and $K$-equilibrium plans benefit from *pre-announcing* the targets. This allows the planner to use the partial credibility of plans in the future to induce movements in expectations which provide incentives in the present.

To disentangle both effects, we consider an average recursive plan, as follows. After solving for the recursive plan, we take the expected path of announcements which takes into account the fact that reputation will drift down over time, as the planner and the private sector understand. We then project this path onto the $(\omega, \chi, a_0)$ space of our announcements, and solve for the

continuation equilibrium after the announcement of this projected plan.

Table 2 provides a summarized comparison of our plans. In this parametrization, the gains from pre-announcing seem to be of the same magnitude as the gains from flexibility.

<p style="text-align:center">TABLE 2: INFLATION PLANS</p>

| Model | Ramsey | *K*-equilibrium | Avg. recursive plan | Recursive plan |
|---|---|---|---|---|
| Initial inflation | 1.40% | 1.63% | 1.58% | 1.58% |
| Long-run inflation | 0% | 0.44% | 0.67% | 0.67% |
| Value of loss function | 0.3879 | 0.7552 | 0.7585 | 0.7557 |

The recursive plan has a higher asymptote than reputational and *K*-equilibrium plans. This reveals a second form of time-inconsistency in the Ramsey plan. At time 0, the planner wants to promise to deliver low inflation in the future because this decreases the level of expected inflation in earlier periods. When the announcement is made sequentially this gain evaporates and the planner attains a higher long-run level for inflation.

## 7. CONCLUDING REMARKS

This paper addresses an old question: can reputation be a substitute for commitment? We find that a simple model of reputation combined with imperfect control on the part of the government creates incentives for staying close to announced targets. The optimal policy after a plan has been announced trades off the benefits of surprise inflation against the possibility that a deviation becomes known to the public. In this way, the government's reputation becomes an important state variable in the optimal policy problem under discretion.

Various characteristics of announced plans come to bear when determining the value of reputation. We find that a pervasive feature of optimal plans is gradualism. In anticipation of the continuation equilibrium, the planner finds it desirable to set itself up in situations where keeping its reputation is both easy and valuable. These are situations in which current announced inflation is higher now than in the future. In our model, gradualism is therefore an artifact of incentives and not the reflection of inflation inertia. Understanding how the presence of sources

of true inertia might interact with our results is one of our goals going forward.

The gradualist property of optimal plans holds at positive levels of reputation and also in the limit as initial reputation vanishes to zero. We interpret this limit case as a sensible refinement of the game between a rational government and the private sector.

As an important aside, we provide a comparison to models that stand between our reputational equilibria and more standard sustainable plans, loosely based on some contributions to the literature. We argue that our model of reputation effectively operates by modifying the incentive constraint in the recursive version of a planning problem. When reputation is low, large option values of sticking to the plan are created, which become even greater when the plan is backloaded.

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