Central Bank Swap Lines as Bilateral Sovereign Debt

Francisco Roldán IMF César Sosa-Padilla Notre Dame & NBER

XXVI Workshop in International Economics and Finance September 2024

The views expressed herein are those of the authors and should not be attributed to the IMF, its Executive Board, or its management.

- · Swap line: two lines of credit involving two central banks
 - ... Each makes available some of its own currency to the other, for a fixed term
 - ... Short-term arrangements (typically one year, typically renewed)
- Used to mainly involve AEs
 Fed-ECB-BoE-BoJ-SNB
 - ... to support lender-of-last-resort functions with multinational firms
- Large increase in bilateral swaps and loans involving EMs since early 2000s
 - ... for EM, swap resources are hard currency
 - ... for EM, swap can be used for financing BoP (or as borrowed reserves)
 - ... EMs borrowing from swap lines tend to use different counterparts

Question

How do swap lines interact with sovereign debt?

- Swap line: two lines of credit involving two central banks
 - ... Each makes available some of its own currency to the other, for a fixed term
 - ... Short-term arrangements (typically one year, typically renewed)
- Used to mainly involve AEs
 Fed-ECB-BoE-BoJ-SNB
 - ... to support lender-of-last-resort functions with multinational firms
- Large increase in bilateral swaps and loans involving EMs since early 2000s
 - ... for EM, swap resources are hard currency
 - ... for EM, swap can be used for financing BoP (or as borrowed reserves)
 - ... EMs borrowing from swap lines tend to use different counterparts

Question

How do swap lines interact with sovereign debt?

- · Swap line: two lines of credit involving two central banks
 - ... Each makes available some of its own currency to the other, for a fixed term
 - ... Short-term arrangements (typically one year, typically renewed)
- Used to mainly involve AEs
 Fed-ECB-BoE-BoJ-SNB
 - ... to support lender-of-last-resort functions with multinational firms
- Large increase in bilateral swaps and loans involving EMs since early 2000s
 - ... for EM, swap resources are hard currency
 - ... for EM, swap can be used for financing BoP (or as borrowed reserves)
 - ... EMs borrowing from swap lines tend to use different counterparts

- Swap line: two lines of credit involving two central banks
 - ... Each makes available some of its own currency to the other, for a fixed term
 - ... Short-term arrangements (typically one year, typically renewed)
- Used to mainly involve AEs
 Fed-ECB-BoE-BoJ-SNB
 - ... to support lender-of-last-resort functions with multinational firms
- Large increase in bilateral swaps and loans involving EMs since early 2000s
 - ... for EM, swap resources are hard currency
 - ... for EM, swap can be used for financing BoP (or as borrowed reserves)
 - ... EMs borrowing from swap lines tend to use different counterparts

Question

How do swap lines interact with sovereign debt?

How do Central Bank Swap Lines affect the Market Structure of Sovereign Debt?

We abstract from currencies, collateral, and focus on the borrowing

Tradeoff

- Borrowing with bonds
 - ... interest rate reflects default risk
- Borrowing from the swap line
 - ... interest rate and drawings negotiated
- !! Defaulting on the debt does not mean defaulting on the swap

How do Central Bank Swap Lines affect the Market Structure of Sovereign Debt?

We abstract from currencies, collateral, and focus on the borrowing

Tradeoff

- Borrowing with bonds
 - ... interest rate reflects default risk
- · Borrowing from the swap line
 - ... interest rate and drawings negotiated
- !! Defaulting on the debt does not mean defaulting on the swap

How do Central Bank Swap Lines affect the Market Structure of Sovereign Debt?

We abstract from currencies, collateral, and focus on the borrowing

Tradeoff

- Borrowing with bonds
 - ... interest rate reflects default risk
- · Borrowing from the swap line
 - ... interest rate and drawings negotiated
- !! Defaulting on the debt does not mean defaulting on the swap

A New Landscape for Sovereign Borrowing

- · Swap lines are an example of a new type of sovereign borrowing arrangement
 - · Short maturity but rolled over, with renegotiation
 - Difficult to default on Central bank ≠ Treasury
 - · Cheaper than borrowing on the market
- · Other examples: Central bank deposits, bilateral loans, IMF programs...

The Dangers of Borrowing through Swap Lines

Main findings

- Swap drawings small relative to debt, but
 - Presence of swaps affects sovereign debt markets
 - ... can provide financing when other sources dry up
 - ... can increase risk-taking
- Lending around or in default maximizes surplus in swap negotiations
 - Availability of swaps in default:
 - ... raises the value of default
 - ... which increases the default frequency
 - ... and worsens borrowing terms in bond markets
 - · Without restricting swaps in default, welfare losses for the government
- Swap lines induce relational overborrowing similar to the debt dilution problem
 - Surplus requires spreads spreads require risk

The Dangers of Borrowing through Swap Lines

Main findings

- Swap drawings small relative to debt, but
 - · Presence of swaps affects sovereign debt markets
 - ... can provide financing when other sources dry up
 - ... can increase risk-taking
- · Lending around or in default maximizes surplus in swap negotiations
 - · Availability of swaps in default:
 - ... raises the value of default
 - ... which increases the default frequency
 - ... and worsens borrowing terms in bond markets
 - · Without restricting swaps in default, welfare losses for the government
- · Swap lines induce relational overborrowing similar to the debt dilution problem
 - Surplus requires spreads spreads require risk

The Dangers of Borrowing through Swap Lines

Main findings

- Swap drawings small relative to debt, but
 - Presence of swaps affects sovereign debt markets
 - ... can provide financing when other sources dry up
 - ... can increase risk-taking
- · Lending around or in default maximizes surplus in swap negotiations
 - · Availability of swaps in default:
 - ... raises the value of default
 - ... which increases the default frequency
 - ... and worsens borrowing terms in bond markets
 - · Without restricting swaps in default, welfare losses for the government
- · Swap lines induce relational overborrowing similar to the debt dilution problem
 - Surplus requires spreads spreads require risk

Literature

- · Central Bank swaps among advanced economies
 - ... Bahaj and Reis (2021); Cesa-Bianchi, Eguren-Martin, and Ferrero (2022)
- · Data on Central Bank swaps for EMs
 - ... Perks, Rao, Shin, and Tokuoka (2021); Horn, Parks, Reinhart, and Trebesch (2023)
- · Sovereign debt/default with interactions from 'official' debt
 - ... Boz (2011), Hatchondo, Martinez, and Onder (2014), Arellano and Barreto (2023), Hatchondo, Martinez, and Sosa-Padilla (2024)



Environment

The government of a small open economy borrows from a monopolist and from markets

- · Income $y(z_t)$ follows an AR(1) process in logs
 - ... Only one good, representative risk-averse household, expected utility
- · Renegotiate the swap *m* each period
 - ... Involves a transfer x and a new loan size m'
 - ... Swap is non-defaultable \implies Repaying m is the natural threat point
- Should expect

 $x = \frac{1}{1+r}m' - n$

- ... Implicit interest rate r to vary over time
- ... Interest rate to reflect market power
- ... Interest rate to reflect outside options

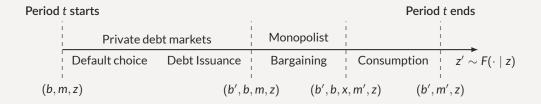
Environment

The government of a small open economy borrows from a monopolist and from markets

- · Income $y(z_t)$ follows an AR(1) process in logs
 - ... Only one good, representative risk-averse household, expected utility
- · Renegotiate the swap *m* each period
 - ... Involves a transfer x and a new loan size m'
 - ... Swap is non-defaultable \implies Repaying m is the natural threat point
- · Should expect

- $x = \frac{1}{1+r}m' m$
- ... Implicit interest rate r to vary over time
- ... Interest rate to reflect market power
- ... Interest rate to reflect outside options

Timeline of events



Borrowing from markets

Debt is a geometrically-decaying coupon

... for each unit, get q, pay
$$\kappa$$
, $(1-\rho)\kappa$, ... $(1-\rho)^{s-1}\kappa$

· Government enters first stage owing b in debt, m in swaps, income state z

$$v(b, m, z) = \max \{v_R(b, m, z) + \epsilon_R, v_D(m, z) + \epsilon_D\}$$
$$v_R(b, m, z) = \max_{b'} w_R(b', b, m, z)$$

Lenders in competitive markets need to anticipate interactions with the monopolist

$$q(b', b, m, z) = \beta_{L} \mathbb{E} \left[(1 - 1_{\mathcal{D}}(b', m', z')) \left(\kappa + (1 - \rho)q(b'', b', m', z') \right) \mid z \right]$$

$$m' = m'(b', b, m, z)$$

$$b'' = b'(b', m', z')$$

Borrowing from markets

Debt is a geometrically-decaying coupon

... for each unit, get q, pay
$$\kappa$$
, $(1-\rho)\kappa$, ... $(1-\rho)^{s-1}\kappa$

· Government enters first stage owing b in debt, m in swaps, income state z

$$v(b, m, z) = \max \{v_R(b, m, z) + \epsilon_R, v_D(m, z) + \epsilon_D\}$$
$$v_R(b, m, z) = \max_{b'} w_R(b', b, m, z)$$

· Lenders in competitive markets need to anticipate interactions with the monopolist

$$\begin{aligned} q(b',b,m,z) &= \beta_{L} \mathbb{E} \left[(1 - 1_{\mathcal{D}}(b',m',z')) \left(\kappa + (1 - \rho)q(b'',b',m',z') \right) \mid z \right] \\ m' &= m'(b',b,m,z) \\ b'' &= b'(b',m',z') \end{aligned}$$

Borrowing from markets

- Debt is a geometrically-decaying coupon
 - ... for each unit, get q, pay κ , $(1-\rho)\kappa$, ... $(1-\rho)^{s-1}\kappa$
- · Government enters first stage owing b in debt, m in swaps, income state z

$$v(b, m, z) = \max \{v_R(b, m, z) + \epsilon_R, v_D(m, z) + \epsilon_D\}$$
$$v_R(b, m, z) = \max_{b'} w_R(b', b, m, z)$$

· Lenders in competitive markets need to anticipate interactions with the monopolist

$$q(b',b,m,z) = \beta_{\rm L} \mathbb{E} \left[(1-1_{\mathcal{D}}(b',m',z')) \left(\kappa + (1-\rho)q(b'',b',m',z') \right) \mid z \right]$$

$$m' = m \qquad b,m,z \qquad \text{same sdf as monopolist}$$

$$b'' = b'(b',m',z')$$

Bargaining stage with monopolist

· At state z, owing debt b bonds and m on the swap and having issued b'

$$\max_{x,m} \mathcal{L}_R(b',x,m,m',z)^{\theta} \times \mathcal{B}_R(b',b,x,m,m',z)^{1-\theta}$$
Lender surplus

Lender's surplus

$$\mathcal{L}_{R}(b', \mathsf{x}, \mathsf{m}, \mathsf{m}', \mathsf{z}) = \underbrace{(a - \mathsf{x} + \beta_{\mathsf{L}} \mathbb{E} \left[h(b', \mathsf{m}', \mathsf{z}') \mid \mathsf{z} \right])}_{\mathsf{agreement}} - \underbrace{(a + \mathsf{m} + \beta_{\mathsf{L}} \mathbb{E} \left[h(b', \mathsf{0}, \mathsf{z}') \mid \mathsf{z} \right])}_{\mathsf{threat point}}$$

$$\mathcal{B}_{R}(b',b,x,m,m',z) = \underbrace{u\big(y(z) + B(b',b,m,z) + x\big) + \beta \mathbb{E}\left[v(b',m',z') \mid z\right]}_{\text{agreement}} - \underbrace{\big(u\big(y(z) + B(b',b,m,z) - m\big) + \beta \mathbb{E}\left[v(b',0,z') \mid z\right]\big)}_{\text{threat point}}$$

with
$$B(b', b, m, z) = q(b', b, m, z)(b' - (1 - \rho)b) - \kappa b$$

Bargaining stage with monopolist

• At state z, owing debt b bonds and m on the swap and having issued b'

$$\max_{x,m} \mathcal{L}_R(b',x,m,m',z)^{\theta} \times \mathcal{B}_R(b',b,x,m,m',z)^{1-\theta}$$

Lender's surplus

$$\mathcal{L}_{R}(b',x,m,m',z) = \underbrace{(a-x+\beta_{L}\mathbb{E}\left[h(b',m',z')\mid z\right])}_{\text{agreement}} - \underbrace{(a+m+\beta_{L}\mathbb{E}\left[h(b',0,z')\mid z\right])}_{\text{threat point}}$$

$$\mathcal{B}_{R}(b',b,x,m,m',z) = \underbrace{u\big(y(z) + B(b',b,m,z) + x\big) + \beta \mathbb{E}\left[v(b',m',z') \mid z\right]}_{\text{agreement}} - \underbrace{\big(u\big(y(z) + B(b',b,m,z) - m\big) + \beta \mathbb{E}\left[v(b',0,z') \mid z\right]\big)}_{\text{threat point}}$$

with
$$B(b', b, m, z) = q(b', b, m, z)(b' - (1 - \rho)b) - \kappa b$$

• At state z, owing debt b bonds and m on the swap and having issued b'

$$\max_{x,m} \mathcal{L}_R(b',x,m,m',z)^{\theta} \times \mathcal{B}_R(b',b,x,m,m',z)^{1-\theta}$$

Lender's surplus

$$\mathcal{L}_{R}(b',x,m,m',z) = \underbrace{(a-x+\beta_{L}\mathbb{E}\left[h(b',m',z')\mid z\right])}_{\text{agreement}} - \underbrace{(a+m+\beta_{L}\mathbb{E}\left[h(b',0,z')\mid z\right])}_{\text{threat point}}$$

$$\mathcal{B}_{R}(b',b,x,m,m',z) = \underbrace{u\big(y(z) + B(b',b,m,z) + x\big) + \beta \mathbb{E}\left[v(b',m',z') \mid z\right]}_{\text{agreement}} \\ - \underbrace{\big(u\big(y(z) + B(b',b,m,z) - m\big) + \beta \mathbb{E}\left[v(b',0,z') \mid z\right]\big)}_{\text{threat point}}$$

with
$$B(\mathbf{b'}, \mathbf{b}, m, z) = q(\mathbf{b'}, \mathbf{b}, m, z)(\mathbf{b'} - (1 - \rho)\mathbf{b}) - \kappa \mathbf{b}$$

Bargaining: intuition

Lender's surplus

$$\mathcal{L}_{R}(b', \mathbf{x}, \mathbf{m}, \mathbf{m}', \mathbf{z}) = (a - \mathbf{x} + \beta_{L} \mathbb{E} \left[h(b', \mathbf{m}', \mathbf{z}') \mid \mathbf{z} \right]) - (a + \mathbf{m} + \beta_{L} \mathbb{E} \left[h(b', \mathbf{0}, \mathbf{z}') \mid \mathbf{z} \right])$$

· When $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high: monopolist willing to lend at low rates

$$\mathcal{B}_{R}(b', b, x, m, m', z) = u(y(z) + B(b', b, m, z) + x) + \beta \mathbb{E} [v(b', m', z') \mid z] - (u(y(z) + B(b', b, m, z) - m) + \beta \mathbb{E} [v(b', 0, z') \mid z])$$

- If default risk is low, not much role for monopolist
- When m B(b', b, m, z) is large: government willing to borrow at high rates

Bargaining: intuition

Lender's surplus

$$\mathcal{L}_{R}(b', \mathbf{x}, \mathbf{m}, \mathbf{m}', \mathbf{z}) = (a - \mathbf{x} + \beta_{L} \mathbb{E} \left[h(b', \mathbf{m}', \mathbf{z}') \mid \mathbf{z} \right]) - (a + \mathbf{m} + \beta_{L} \mathbb{E} \left[h(b', \mathbf{0}, \mathbf{z}') \mid \mathbf{z} \right])$$

• When $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high: monopolist willing to lend at low rates

$$\mathcal{B}_{R}(b',b,x,m,m',z) = u(y(z) + B(b',b,m,z) + x) + \beta \mathbb{E} [v(b',m',z') \mid z] - (u(y(z) + B(b',b,m,z) - m) + \beta \mathbb{E} [v(b',0,z') \mid z])$$

- · If default risk is low, not much role for monopolist
- When m B(b', b, m, z) is large: government willing to borrow at high rates

Quantitative Effects of Swap Lines

Calibration

· Calibrate to Argentina without swaps (as in Roch & Roldán, 2023)

	Parameter	Value
Sovereign's discount factor	β	0.9504
Sovereign's risk aversion	γ	2
Preference shock scale parameter	χ	0.02
Lender's bargaining power	θ	0.5
Risk-free interest rate	r	0.01
Duration of debt	ρ	0.05
Income autocorrelation coefficient	$ ho_{z}$	0.9484
Standard deviation of y_t	σ_{z}	0.02
Reentry probability	ψ	0.0385
Default cost: linear	d_0	-0.24
Default cost: quadratic	d_1	0.3

Calibration

· Calibrate to Argentina without swaps (as in Roch & Roldán, 2023)

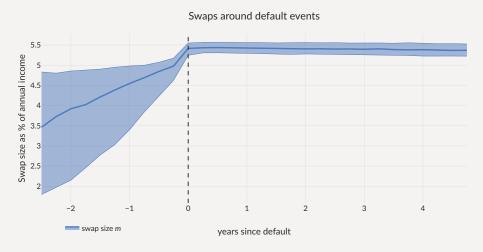
	Parameter	Value
Sovereign's discount factor	β	0.9504
Sovereign's risk aversion	γ	2
Preference shock scale parameter	χ	0.02
Lender's bargaining power	heta	0.5
Risk-free interest rate	r	0.01
Duration of debt	ho	0.05
Income autocorrelation coefficient	$ ho_{z}$	0.9484
Standard deviation of y_t	σ_{z}	0.02
Reentry probability	ψ	0.0385
Default cost: linear	d_0	-0.24
Default cost: quadratic	d_1	0.3

How do swaps affect equilibrium?

	No swap	Unrestricted, $\theta = 0.25$	Unrestricted, $\theta = 0.5$
Avg spread (bps)	804	1,841	2,396
Std spread (bps)	470	1,099	1,541
$\sigma(c)/\sigma(y)$ (%)	111	111	110
Debt to GDP (%)	21.4	20.8	20.2
Swap to GDP (%)	0	3.74	3.32
Corr. swap & spreads (%)	-	53.8	62.2
Default frequency (%)	6.53	13	14.7
Welfare gains (rep)	-	-0.082%	-0.41%

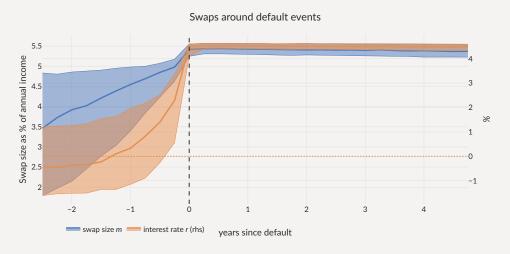


· Swaps shoot up before and during defaults



· Also consider Limited versions: $m' \leq \Gamma(m)$ while in default

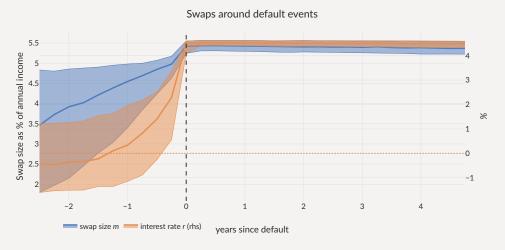
· Swaps shoot up before and during defaults



· Also consider Limited versions: $m' \leq \Gamma(m)$ while in default



· Swaps shoot up before and during defaults



· Also consider Limited versions: $m' \leq \Gamma(m)$ while in default

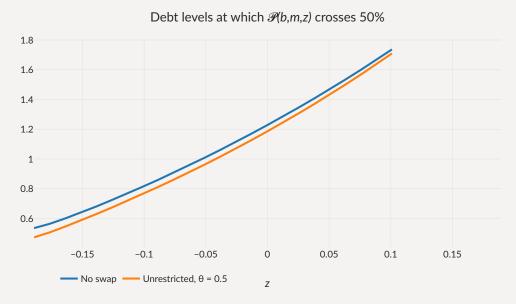
Limiting swaps in default

· Limited: entire swap must be repaid while in default $\Gamma(m) = 0$

	No swap	Unrestricted, $\theta = 0.5$	Limited, $\theta = 0.5$
Avg spread (bps)	804	2,396	1,216
Std spread (bps)	470	1,541	779
$\sigma(c)/\sigma(y)$ (%)	111	110	113
Debt to GDP (%)	21.4	20.2	21.7
Swap to GDP (%)	0	3.32	1.05
Corr. swap & spreads (%)	-	62.2	69.4
Default frequency (%)	6.53	14.7	9.34
Welfare gains (rep)	-	-0.41%	-0.084%

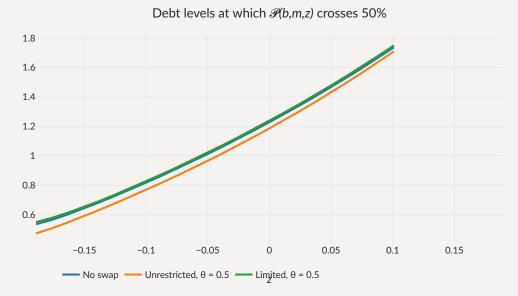
Default Barriers with Swaps

· Unrestricted: default barrier moves inward, Limited: marginal impact



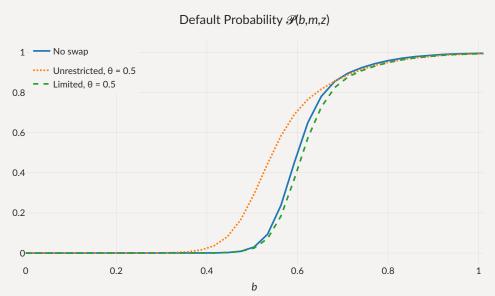
Default Barriers with Swaps

· Unrestricted: default barrier moves inward, Limited: marginal impact



Debt Tolerance with Swaps

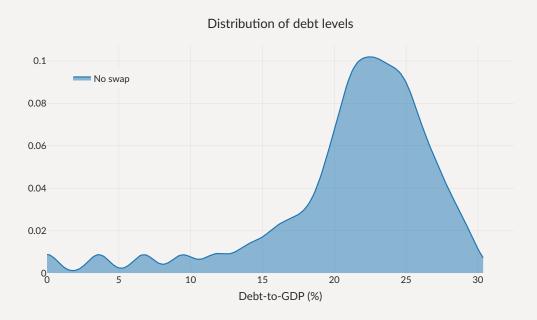
· Unrestricted: default more often, Limited: marginal impact



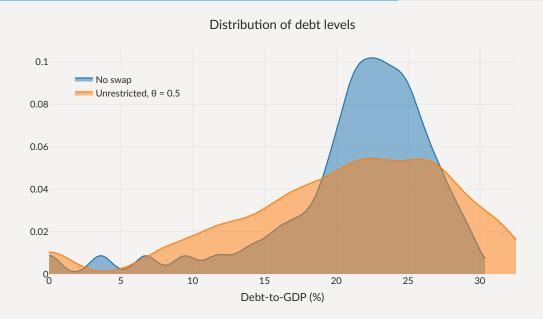
If **Limited** swaps help repay the debt,

Why are there more defaults with swaps?

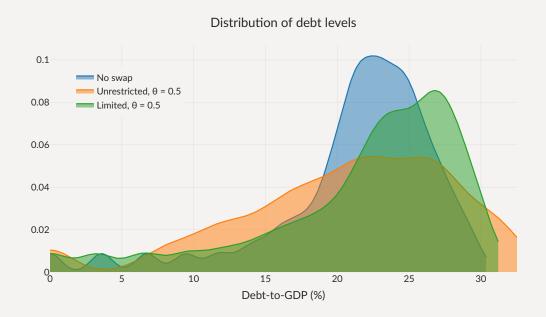
Debt Levels with Swaps



Debt Levels with Swaps



Debt Levels with Swaps



$$\mathcal{L}_{R}(b', x, m, m', z) = (a - \mathbf{x} + \beta_{L} \mathbb{E} [h(b', \mathbf{m}', z') \mid z]) - (a + \mathbf{m} + \beta_{L} \mathbb{E} [h(b', \mathbf{0}, z') \mid z])$$

$$\mathcal{B}_{R}(b', b, x, m, m', z) = u(y(z) + B(b', b, m, z) + \mathbf{x}) + \beta \mathbb{E} [v(b', \mathbf{m}', z') \mid z] - (u(y(z) + B(b', b, m, z) - \mathbf{m}) + \beta \mathbb{E} [v(b', \mathbf{0}, z') \mid z])$$

- Low rates when $\mathbb{E}\left[h(b', \mathbf{m'}, \mathbf{z'}) h(b', \mathbf{0}, \mathbf{z'})\right] \gg 0$ (e.g. when > m')
- High rates when $m B(b', b, m, z) \gg 0$
- Lender surplus today $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high (>m') when
 - high rates in the future
 - $\cdot m' \gg B(b'',b',m',z')$
 - q(b'', b', m', z') is low
 - $\cdot b' \gg 0$

$$\mathcal{L}_{R}(b', x, m, m', z) = (a - x + \beta_{L} \mathbb{E} [h(b', m', z') \mid z]) - (a + m + \beta_{L} \mathbb{E} [h(b', 0, z') \mid z])$$

$$\mathcal{B}_{R}(b', b, x, m, m', z) = u(y(z) + B(b', b, m, z) + x) + \beta \mathbb{E} [v(b', m', z') \mid z]$$

$$- (u(y(z) + B(b', b, m, z) - m) + \beta \mathbb{E} [v(b', 0, z') \mid z])$$

- Low rates when $\mathbb{E}\left[h(b', m', z') h(b', 0, z')\right] \gg 0$ (e.g. when > m')
- High rates when $m B(b', b, m, z) \gg 0$
- · Lender surplus today $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high (>m') when
 - · high rates in the future
 - $\cdot m' \gg B(b'', b', m', z')$
 - q(b'', b', m', z') is low
 - $\cdot b' \gg 0$

$$\begin{split} \mathcal{L}_{R}(b',x,m,m',z) &= (a - x + \beta_{L}\mathbb{E}\left[h(b',m',z') \mid z\right]) - (a + m + \beta_{L}\mathbb{E}\left[h(b',0,z') \mid z\right]) \\ \mathcal{B}_{R}(b',b,x,m,m',z) &= u\big(y(z) + B(b',b,m,z) + x\big) + \beta\mathbb{E}\left[v(b',m',z') \mid z\right] \\ &- \big(u\big(y(z) + B(b',b,m,z) - m\big) + \beta\mathbb{E}\left[v(b',0,z') \mid z\right]\big) \end{split}$$

- Low rates when $\mathbb{E}\left[h(b', \mathbf{m'}, \mathbf{z'}) h(b', \mathbf{0}, \mathbf{z'})\right] \gg 0$ (e.g. when > m')
- High rates when $m B(b', b, m, z) \gg 0$
- · Lender surplus today $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high (>m') when
 - high rates in the future
 - · $m' \gg B(b'', b', m', z')$
 - q(b'', b', m', z') is low
 - $\cdot b' \gg 0$

$$\mathcal{L}_{R}(b', x, m, m', z) = (a - x + \beta_{L}\mathbb{E} [h(b', m', z') \mid z]) - (a + m + \beta_{L}\mathbb{E} [h(b', 0, z') \mid z])$$

$$\mathcal{B}_{R}(b', b, x, m, m', z) = u(y(z) + B(b', b, m, z) + x) + \beta\mathbb{E} [v(b', m', z') \mid z]$$

$$- (u(y(z) + B(b', b, m, z) - m) + \beta\mathbb{E} [v(b', 0, z') \mid z])$$

- Low rates when $\mathbb{E}\left[h(b', \mathbf{m'}, \mathbf{z'}) h(b', \mathbf{0}, \mathbf{z'})\right] \gg 0$ (e.g. when > m')
- High rates when $m B(b', b, m, z) \gg 0$
- · Lender surplus today $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high (>m') when
 - high rates in the future
 - · $m' \gg B(b'', b', m', z')$
 - q(b'', b', m', z') is low
 - $\cdot b' \gg 0$

$$\mathcal{L}_{R}(b', x, m, m', z) = (a - x + \beta_{L} \mathbb{E} [h(b', m', z') \mid z]) - (a + m + \beta_{L} \mathbb{E} [h(b', 0, z') \mid z])$$

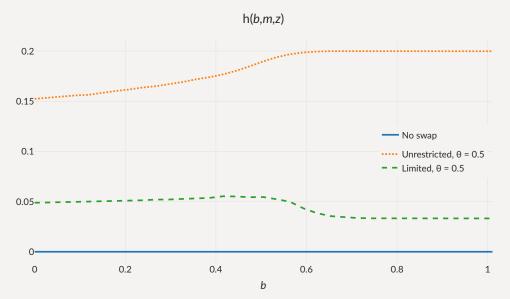
$$\mathcal{B}_{R}(b', b, x, m, m', z) = u(y(z) + B(b', b, m, z) + x) + \beta \mathbb{E} [v(b', m', z') \mid z]$$

$$- (u(y(z) + B(b', b, m, z) - m) + \beta \mathbb{E} [v(b', 0, z') \mid z])$$

- Low rates when $\mathbb{E}\left[h(b', m', z') h(b', 0, z')\right] \gg 0$ (e.g. when > m')
- High rates when $m B(b', b, m, z) \gg 0$
- · Lender surplus today $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$ is high (>m') when
 - high rates in the future
 - · $m' \gg B(b'', b', m', z')$
 - q(b'', b', m', z') is low
 - $\cdot b' \gg 0$

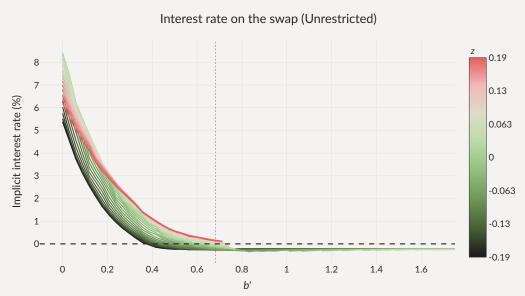
Monopolist's profits

Monopolist's profits increasing in debt (cond. on repayment) – surplus requires spreads



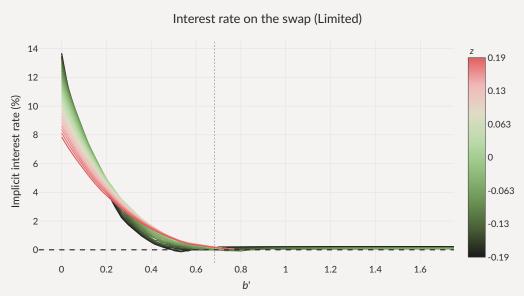
Risk-taking incentives

Surplus on swap requires spreads: relationship creates incentives for risk taking



Risk-taking incentives

Surplus on swap requires spreads: relationship creates incentives for risk taking



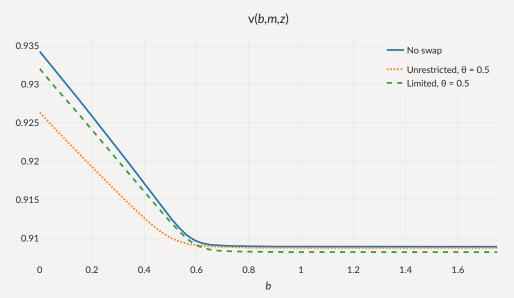
Debt Prices with Swaps

Equilibrium dynamics worsen prices: relational overborrowing similar to debt dilution



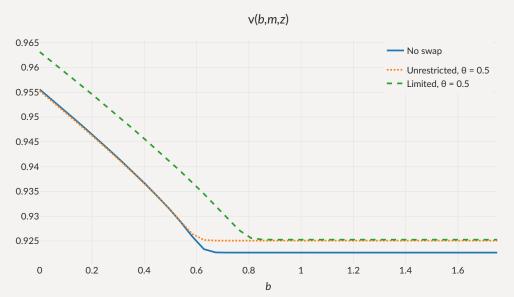
Welfare effects of swap lines

 $Limited \succcurlyeq Unrestricted, but...$



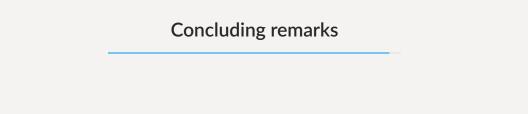
Welfare effects of swap lines — Short-term debt

Short-term debt: swaps beneficial – interest on the swap small wrt to whole debt stock



Welfare effects of swap lines — Short-term debt (cont'd)

	No swap, ST	Unrestricted, $\theta = 0.5$, ST	$\begin{array}{c} \textbf{Limited,} \\ \theta = 0.5, \textbf{ST} \end{array}$
Avg spread (bps)	80.7	377	247
Std spread (bps)	110	373	197
$\sigma(c)/\sigma(y)$ (%)	129	130	138
Debt to GDP (%)	19	18.7	23.5
Swap to GDP (%)	0	3.13	3.65
Corr. swap & spreads (%)	-	54.9	50.3
Default frequency (%)	0.574	3.14	1.97
Welfare gains (rep)	-	-0.074%	0.8%

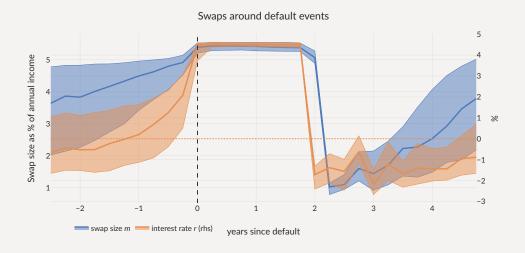


Concluding remarks

- Simple model with monopolist/fringe structure
- Strong interaction between two markets for sovereign debt
 - ... even if swaps are **not** used intensely on the equilibrium path
- · Market power crucial in model
 - ... how to discipline in model?
 - ... how to affect in reality?
- · Large welfare effects, policy challenges
 - · How to limit their use during defaults?
 - · Relational overborrowing more gains from fiscal rules, state-contingent debt?



· Further conditioning on default events lasting exactly two years





• With Limited: $\Gamma(m) = m$

