# Uncertainty Premia, Sovereign Default Risk, and State-Contingent Debt

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# Why do governments borrow noncontingent?

#### State-contingent debt instruments

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- · Reduce cyclicality of fiscal policy
- Improve risk-sharing

Why aren't they used?

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  - $\cdot$  Costa, Chamon, and Ricci (2008) compute wide spreads for Argentine GDP-warrants
    - $\sim$  300-400bps from default risk of other securities
    - 600-1200bps residual: 'novelty' premium

#### This paper proposes a framework that

- Rationalizes pricing of SCI + welfare analysis
  - With ingredients from resolutions of the equity premium puzzle
- $\cdot$  Links unfavorable prices to common 'threshold' structure
  - Example: Argentina's GDP-warrants, also Ukraine, Greece. . .

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#### A framework for pricing state-contingent debt

- Standard quantitative model of sovereign default with long-term debt
  - Aguiar and Gopinath (2006), Arellano (2008), Hatchondo and Martinez (2009), Chatterjee and Eyigungor (2012)
- International lenders with concerns about model misspecification
  - · Preference for robustness Hansen and Sargent (2001), Pouzo and Presno (2016)
- Mechanism: lenders act as if the probability of states with low repayment was higher
  - · With noncontingent debt, lenders overestimate the default probability
  - · Pouzo and Presno (2016) uses robustness to reconcile spreads with default frequencies
  - · In general, probability distortion depends on type and quantity of debt issued

### Main findings

- 1. Robust lenders dislike repayment structures with thresholds in good times
  - · Heavy discounts for these bonds  $\implies$  welfare losses
- 2. Explain most of the 'novelty premium' in Argentina's GDP warrants as ambiguity premia
  - · Calibration of robustness from noncontingent debt only
- 3. Characterize the optimal design and how it changes with robustness
  - $\cdot$  With high robustness, want to minimize ex-ante and ex-post contingency

# Roadmap

- · Stylized Model
- Probability Distortions
- · Pricing and Welfare
- · Quantitative Implementation
- · Concluding Remarks

Stylized Model

#### The model

# We consider a simple two-period model, small open economy

- Uncertain endowment y(z) in the second period
- The government has access to one asset which promises a return R(z).
- A few benchmarks

6

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| Noncontingent debt | R(z)                  |                       | 1                         |
|--------------------|-----------------------|-----------------------|---------------------------|
| Linear indexing    | $R^{\alpha}(z)$       |                       | $1 + \alpha(y(z) - 1)$    |
| Threshold debt     | $R^{\tau}(z)$         |                       | $\mathbb{1} \ (z > \tau)$ |
| Optimal design     | $R^{\star}(z;\theta)$ | chosen state-by-state |                           |

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# The government's problem

 $\cdot$  The government takes as given the price schedule q(b)

$$\max_b u(c_1^b) + \beta_b \mathbb{E}\left[u(c_2^b)\right]$$
 subject to  $c_1^b = y_1 + q(b)b$  
$$c_2^b = y_2(z) - h(z, \Delta)d(b, z) - (1 - d(b, z))R(z)b$$

where

$$h(z,\Delta)=y_2(z)^2\Delta$$

In the second period, default it

$$\underbrace{u\left(y_2(z)-h(z,\Delta)\right)}_{\text{v. default}}>\underbrace{u\left(y_2(z)-R(z)b\right)}_{\text{v. repayment}}$$

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### The lenders' problem

Foreign lenders are less standard and have multiplier preferences

$$egin{aligned} \max c_1^L - rac{eta}{ heta} \log \left( \mathbb{E}\left[ \exp(- heta v_2^L) 
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ight) \ & ext{subject to} \ v_2^L = c_2^L \ & c_2^L = w_2 + (1 - d(b,z)) R(z) b \ & c_1^L = w_1 - q_1 b \end{aligned}$$

Lenders provide us with an Euler equation to price the debt

$$q(b; \mathsf{R}) = \beta \mathbb{E} \left[ rac{\exp(- heta c_2^\mathsf{L})}{\mathbb{E} \left[ \exp(- heta c_2^\mathsf{L}) 
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$$q(b;R) = \beta \mathbb{E} \left[ \frac{\exp(-\theta c_2^L)}{\mathbb{E} \left[ \exp(-\theta c_2^L) \right]} (1 - d(b,z)) R(z) \right]$$

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- The lenders' Euler equation explains the sources of the spreads they charge
- · Call  $M = \beta \frac{\exp(-\theta c_2^l)}{\mathbb{E}[\exp(-\theta c_2^l)]}$  the stochastic discount factor

$$q(b;R) = \beta \mathbb{E} \left[ \frac{\exp(-\theta c_2^L)}{\mathbb{E} \left[ \exp(-\theta c_2^L) \right]} (1 - d(b,z)) R(z) \right]$$

$$= \underbrace{\beta \mathbb{E} \left[ (1 - d)R \right]}_{=q_{RE}} + \underbrace{(1 - \mathbb{P}(d)) \operatorname{cov}(M,R)}_{=q_{\theta}^{\text{cont}}} - \underbrace{\mathbb{E} \left[ R \right] \operatorname{cov}(M,d)}_{=-q_{\theta}^{\text{def}}}$$

• The debt price is a rational-expectations price and two sources of ambiguity premia

# Distorted probabilities

#### Interpret lenders' stochastic discount factor as probability distortions

For a random variable X

$$\tilde{\mathbb{E}}\left[X\right] = \mathbb{E}\left[\frac{\exp(-\theta v_2^L)}{\mathbb{E}\left[\exp(-\theta v_2^L)\right]}X\right]$$

-  $\tilde{\mathbb{E}}$  tilts probabilities towards less-favorable states for lenders

Obs The tilting is endogenous to the lenders' outcomes

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**Probability Distortions** 

#### **Parametrization**

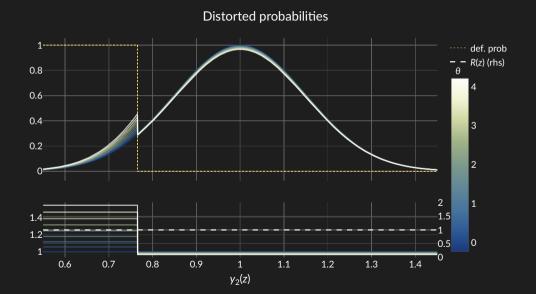


#### Costa, Chamon, and Ricci (2008) study the GDP-warrants issued by Argentina

- The warrant paid if
  - · Output growth above pre-set level (4.3% initially, later 3%)
  - · Output level above the compounded cutoff growth
  - · There is also a cap on total payments

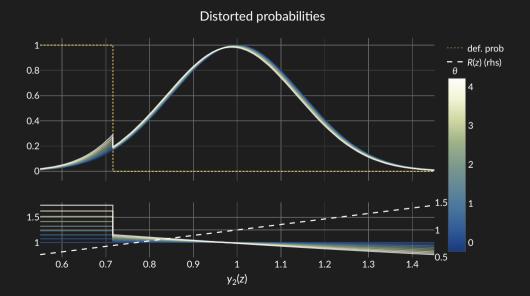
# Distorted probabilities - noncontingent debt



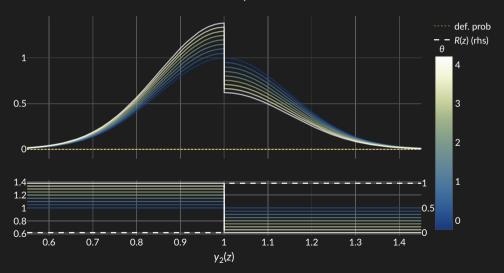


# Distorted probabilities - linearly indexed debt





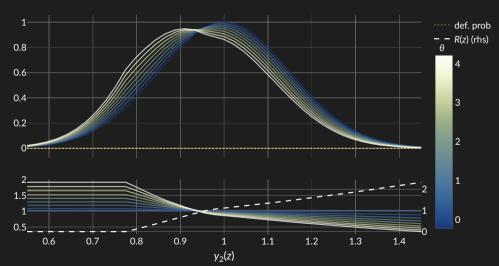
#### Distorted probabilities



# Distorted probabilities - debt for RE lenders

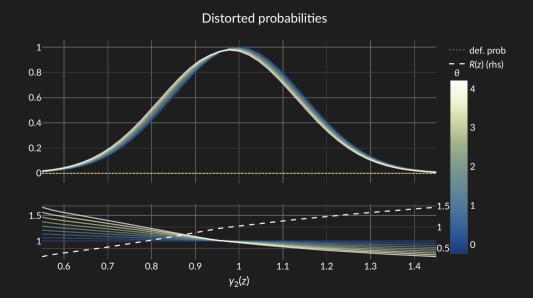




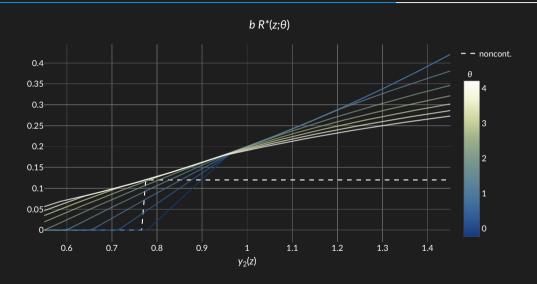


# Distorted probabilities - debt for robust lenders



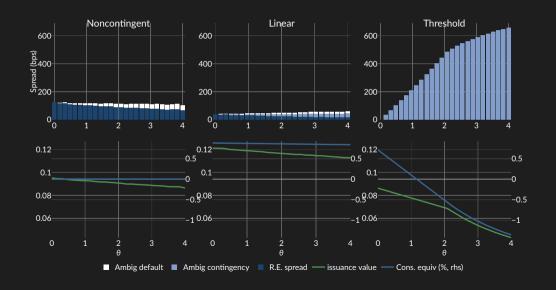


# Design of debt



Pricing and Welfare

# Parametric debt types



## Optimal debt designs



Quantitative Implementation

#### **Quantitative Model**

- · Infinite horizon, small-open economy
- Robust lenders as before
- Long-term debt, debt issued at t pays coupon at t + s

$$\max\left\{0,(1-\delta)^{s-1}(1+\alpha(y_s-1))\mathbb{1}(y_s>\tau)\right\}$$

- · Noncontingent debt:  $\alpha = 0, \tau = -\infty$
- $\cdot$  Default triggers exclusion + output costs for a random amount of periods  $\sim$  Geo $(\psi)$

### Calibration

|                | Data  | Benchmark | Rational<br>Expectations |
|----------------|-------|-----------|--------------------------|
| Spread         | 8.15  | 8.15      | 8.1                      |
| Std Spread     | 4.58  | 4.6       | 4.5                      |
| Debt           | 46    | 44        | 48.7                     |
| Std(c)/Std(y)  | 0.87  | 1.25      | 1.24                     |
| Corr(y,c)      | 0.97  | 0.98      | 0.98                     |
| Corr(y,tb/y)   | -0.77 | -0.68     | -0.71                    |
| Corr(y,spread) | -0.72 | -0.76     | -0.77                    |
| Default Prob   | 3.0   | 3.0       | 5.5                      |
| DEP            | -     | 31%       | -                        |

Note: Statistics computed in the model with noncontingent debt



|               | Rational Expectations |           |              | heta= 1.6155 (benchmark) |           |              |
|---------------|-----------------------|-----------|--------------|--------------------------|-----------|--------------|
| Statistic     | Noncontingent         | Threshold | $\alpha = 1$ | Noncontingent            | Threshold | $\alpha = 1$ |
| Spread        | 8.1                   | 0.36      | 7.2          | 8.15                     | 11.1      | 7.1          |
| Std Spread    | 4.5                   | 0.23      | 3.7          | 4.6                      | 1.58      | 3.6          |
| Debt          | 48.7                  | 116.5     | 50.8         | 44.0                     | 67.6      | 46.1         |
| Std(c)/Std(y) | 1.24                  | 0.82      | 1.22         | 1.25                     | 0.84      | 1.23         |
| Default Prob  | 5.5                   | 0.3       | 5.3          | 3.0                      | 0.0       | 2.6          |
| Welfare Gains |                       | 1.19      | 0.09         |                          | -0.37     | 0.07         |
| DEP           | -                     | -         | -            | 31%                      | 20%       | 30%          |

Table 1: Statistics from calibrated model simulations



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| Statistic     | Rational Expectations $\tau$ = 0.875, $\alpha$ = 7 | Robustness $\tau$ = 0.875, $\alpha$ = 5 |
|---------------|--|---|
| Spread        | 0.1  | 2.8                                     |
| Std Spread    | 0.04   | 0.13                                    |
| Debt          | 79.3   | 65.9                                    |
| Std(c)/Std(y) | 0.76   | 0.96                                    |
| Default Prob  | 0.1  | 0.23                                    |
| Welfare Gains | 1.79   | 0.79                                    |

Table 2: Statistics under the optimal state-contingent bond for different types of lenders

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Concluding Remarks

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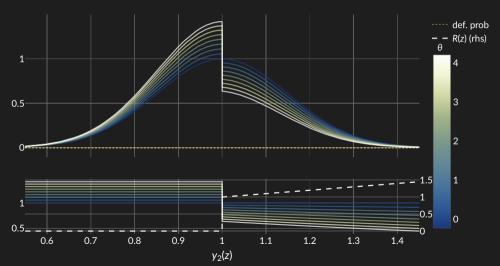
- Standard sovereign debt model augmented with robust lenders
  - 1. accounts for spreads on typical threshold SCDIs
  - 2. rationalizes part of the 'novelty' premium as a premium for ambiguity
  - 3. links unfavorable prices to common threshold structure
  - 4. Welfare gains of SCDI decreasing in robustness
    - · Both for given instrument and for optimally-designed debt
- Optimal design
  - · With realistic robustness, lower thresholds and flatter indexation than RE
  - · With extreme robustness, eliminate contingency ex-ante (stipulated) and ex-post (default)
  - · In general, tradeoff between contingency and risk-sharing



# Distorted probabilities - threshold+linear debt







### Quantitative model



|                | Rational Expectations (benchmark) |           | heta= 1.6155 |               |           |              |
|----------------|-----------------------------------|-----------|--------------|---------------|-----------|--------------|
| Statistic      | Noncontingent                     | Threshold | $\alpha = 1$ | Noncontingent | Threshold | $\alpha = 1$ |
| Spread         | 8.5                               | 0.6       | 6.8          | 8.4           | 15.5      | 7.1          |
| Std Spread     | 4.3                               | 0.4       | 3.0          | 4.4           | 2.3       | 3.1          |
| Debt           | 69.9                              | 159.6     | 74.4         | 62.6          | 87.7      | 67.2         |
| Std(c)/Std(y)  | 1.24                              | 0.83      | 1.21         | 1.25          | 0.82      | 1.22         |
| Corr(y,c)      | 0.98                              | 0.53      | 0.98         | 0.98          | 0.94      | 0.98         |
| Corr(y,tb/y)   | -0.7                              | 0.52      | -0.62        | -0.67         | 0.58      | -0.6         |
| Corr(y,spread) | -0.77                             | -0.87     | -0.78        | -0.75         | -0.61     | -0.77        |
| Default Prob   | 5.8                               | 0.56      | 5.3          | 2.3           | 0.12      | 1.8          |
| Welfare Gains  | -                                 | 1.86      | 0.27         | -             | -0.87     | 0.2          |

Table 3: Statistics based on Chatterjee and Eyigungor (2012)

#### CARA



Euler equations of a rational-expectations agent with CARA preferences and access to a risk-free bond

$$q = \beta \mathbb{E}\left[\frac{u'(c_2)}{u'(c_1)}R\right] = \beta \mathbb{E}\left[\frac{\exp(-\gamma c_2)}{\exp(-\gamma c_1)}R\right]$$
$$\frac{1}{1+r} = \beta \mathbb{E}\left[\frac{u'(c_2)}{u'(c_1)}\right]$$

hence

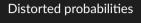
$$q = \beta \mathbb{E}\left[\frac{\exp(-\gamma c_2)}{\beta(1+r)\mathbb{E}\left[\exp(-\gamma c_2)\right]}R\right]$$

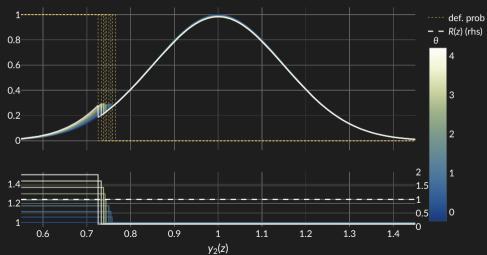
Same as robustness in two periods, in general the robust sdf is

$$q = eta \mathbb{E}\left[rac{\exp(- heta \mathbf{v}')}{\mathbb{E}\left[\exp(- heta \mathbf{v}')
ight]}R
ight]$$

## Distorted probabilities - noncontingent debt

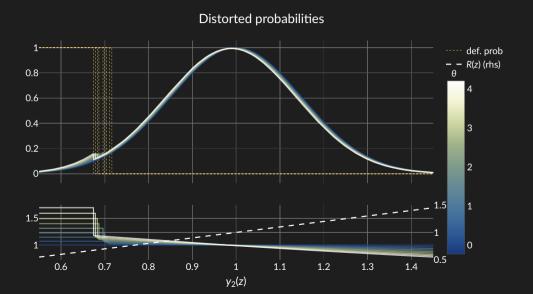






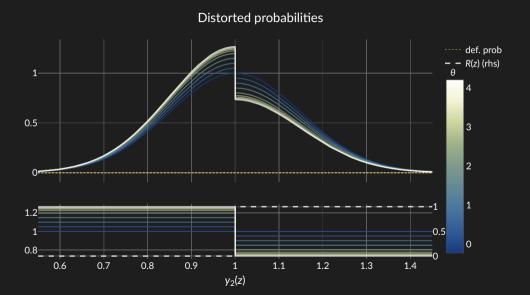
## Distorted probabilities - linearly indexed debt





## Distorted probabilities - threshold debt

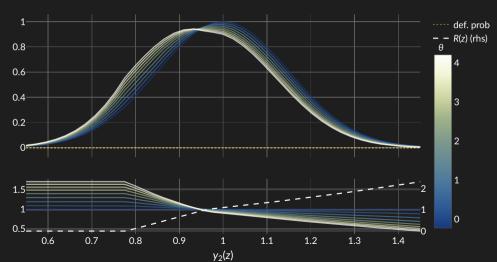




## Distorted probabilities - debt for RE lenders

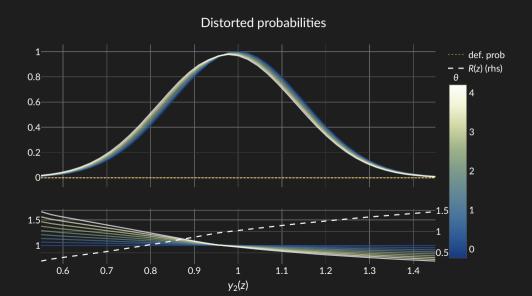






# Distorted probabilities - debt for robust lenders





#### **Parametrization**



We represent this bond with threshold debt, one period = five years, and

| Parameter              | Target                   | Value   |
|------------------------|--------------------------|---------|
| $\overline{eta_{f b}}$ | Borrower's discount rate | 6% ann. |
| $\beta$                | Risk-free rate           | 3% ann. |
| $\gamma$               | Borrower's risk aversion | 2       |
| Δ                      | Output cost of default   | 20%     |
| g                      | Expected growth rate     | 8% ann. |
| k                      | Threshold for repayment  | 50%     |

## **Decomposition of spreads**



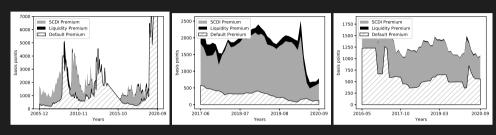


Figure 1: GDP-linked security premia.

The figure shows the estimated spread decomposition in Igan and Kim (2021) for the GDP-warrants issued by Argentina (left), Greece (middle) and Ukraine (right).