# Central Bank Swap Lines as Bilateral Sovereign Debt

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St. Louis Fed brown bag seminar
March 2025

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- · Swap line: two lines of credit involving two central banks
  - ... Each makes available some of its own currency to the other, for a fixed term
  - ... Short-term arrangements (typically one year, typically renewed)
- Used to mainly involve AEs
   Fed-ECB-BoE-BoJ-SNB
  - ... to support lender-of-last-resort functions with multinational firms
- · Large increase in bilateral swaps and loans involving EMs since early 2000s
  - ... for EM, swap resources are hard currency
  - ... for EM, swap can be used for financing BoP (or as borrowed reserves)
  - ... EMs borrowing from swap lines tend to use different counterparts

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## How do Central Bank Swap Lines Affect the Market Structure of Sovereign Debt?

#### We abstract from currencies, collateral, and focus on the borrowing

#### Tradeoff

- Borrowing with bonds
  - ... interest rate reflects default risk
- Borrowing from the swap line
  - ... interest rate and drawings negotiated

!! Defaulting on the debt does not mean defaulting on the swap

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## A New Landscape for Sovereign Borrowing

- · Swap lines are an example of a new type of sovereign borrowing arrangement
  - · Short maturity but rolled over, with renegotiation
  - Difficult to default on Central bank  $\neq$  Treasury
  - · Cheaper than borrowing on the market
- · Other examples: Central bank deposits, bilateral loans, IMF programs...

## Risk-taking Incentives and Relational Overborrowing

#### Main findings

- · Swap drawings small relative to debt, but
  - · Presence of swaps affects sovereign debt markets
    - ... can provide financing when other sources dry up
    - ... can increase risk-taking
- Lending around or in default maximizes surplus in swap negotiations
  - Availability of swaps in default:
    - ... raises the value of default
    - ... which increases the default frequency
    - ... and worsens borrowing terms in bond markets
  - Without restricting swaps in default, welfare losses for the government
- Swap lines induce relational overborrowing similar to the debt dilution problem
  - Surplus requires spreads spreads require risk

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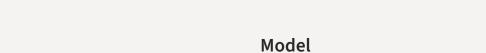
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#### Literature

- · Central Bank swaps among advanced economies
  - ... Bahaj and Reis (2021); Cesa-Bianchi, Eguren-Martin, and Ferrero (2022)
- · Data on Central Bank swaps for EMs
  - ... Perks, Rao, Shin, and Tokuoka (2021); Horn, Parks, Reinhart, and Trebesch (2023)
- Sovereign debt/default with interactions from 'official' debt
  - ... Boz (2011), Hatchondo, Martinez, and Onder (2014), Arellano and Barreto (2024), Liu, Liu, and Yue (2025)



#### **Environment**

## The government of a small open economy borrows from a monopolist and from markets

- Income  $y(z_t)$  follows an AR(1) process in logs
  - ... Only one good, representative risk-averse household, expected utility
- · Renegotiate the swap *m* each period
  - ... Involves a transfer x and a new loan size m'
  - $\dots$  Swap is non-defaultable  $\implies$  Repaying m is the natural threat point
- · Should expect
  - ... Implicit interest rate r to vary over time
  - ... Interest rate to reflect market power
  - ... Interest rate to reflect outside options

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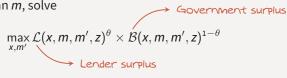
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- $x = \frac{1}{1+r}m' m$
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· At income state z and loan m, solve



Government (borrower) surplus

$$\mathcal{B}(x,m,m',z) = \underbrace{u(y(z)+x) + \beta \mathbb{E}\left[v(m',z')\mid z\right]}_{\text{agreement: receive } x, \text{ owe } m'} - \underbrace{\left(u(y(z)-m) + \beta \mathbb{E}\left[v(0,z')\mid z\right]\right)}_{\text{threat point: repay } m, \text{ clean slate}}$$

Lender surplus

$$\mathcal{L}(x, m, m', z) = \underbrace{a - x + \beta_L \mathbb{E}\left[h(m', z') \mid z\right]}_{ ext{agreement}} - \underbrace{\left(a + m + \beta_L \mathbb{E}\left[h(0, z') \mid z\right]\right)}_{ ext{threat point}}$$

· Value functions v(m, z) and h(m, z) encode expected outcomes of future rounds

· At income state z and loan m, solve

$$\max_{x,m'} \mathcal{L}(x,m,m',z)^{\theta} \times \mathcal{B}(x,m,m',z)^{1-\theta}$$

· Government (borrower) surplus

$$\mathcal{B}(x,m,m',z) = \underbrace{u(y(z) + x) + \beta \mathbb{E}\left[v(m',z') \mid z\right]}_{\text{agreement: receive } x, \text{ owe } m'} - \underbrace{\left(u(y(z) - m) + \beta \mathbb{E}\left[v(0,z') \mid z\right]\right)}_{\text{threat point: repay } m, \text{ clean slate}}$$

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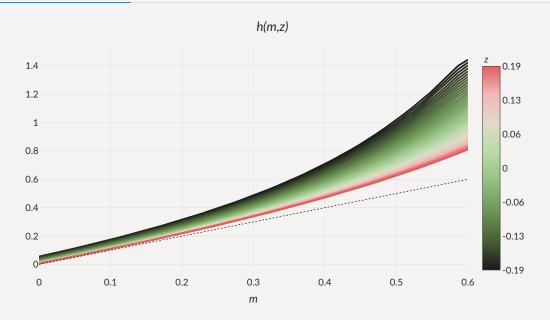
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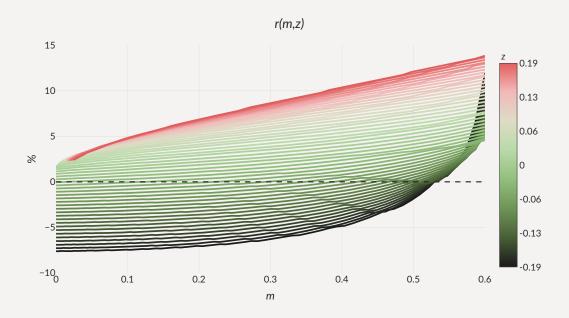
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## Monopolist Terms: Lender's Value Function



## Monopolist Terms: Implicit Interest Rate



#### **Monopolist Terms: Takeaways**

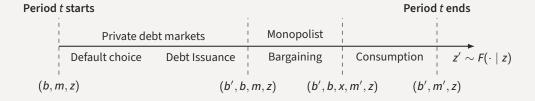
key requirement:

threat point value decreasing in m

## The threat point is less 'credible' when m is large

- · This creates convexity in the lender's value function
  - ... making the lender act 'as if' risk-loving
- · The lender initially subsidizes the loan to induce indebtedness and high profits
  - Gamble for debt overhang
- Initial subsidy and high rates consistent with B's risk aversion 'Participation constraint'

#### **Timeline of Events**



#### **Borrowing from Markets**

Debt is a geometrically-decaying coupon

... for each unit, get 
$$q$$
, pay  $\kappa$ ,  $(1-\rho)\kappa$ , ...  $(1-\rho)^{s-1}\kappa$ 

· Government enters first stage owing b in debt, m in swaps, income state z

$$v(b, m, z) = \max \{v_R(b, m, z) + \epsilon_R, v_D(m, z) + \epsilon_D\}$$
$$v_R(b, m, z) = \max_{b'} w_R(b', b, m, z)$$

· Lenders in competitive markets need to anticipate interactions with the monopolist

$$q(b', b, m, z) = \beta_L \mathbb{E} \left[ (1 - 1_D(b', m', z')) \left( \kappa + (1 - \rho) q(b'', b', m', z') \right) \mid z \right]$$
 $m' = m'(b', b, m, z)$ 
 $b'' = b'(b', m', z')$ 

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$$m' = m \quad b,m,z \quad \text{same sdf as monopolist}$$

$$b'' = b'(b',m',z')$$

## **Bargaining Stage with Monopolist**

· At state z, owing debt b bonds and m on the swap and having issued b'

$$\max_{x,m} \mathcal{L}_R(b',x,m,m',z)^{\theta} \times \mathcal{B}_R(b',b,x,m,m',z)^{1-\theta}$$
Lender surplus

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$$\mathcal{L}_{R}(b',x,m,m',z) = \underbrace{(a-x+\beta_{L}\mathbb{E}\left[h(b',m',z')\mid z\right])}_{\text{agreement}} - \underbrace{(a+m+\beta_{L}\mathbb{E}\left[h(b',0,z')\mid z\right])}_{\text{threat point}}$$

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#### Lender's surplus

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· Low rates when value of relationship  $\mathbb{E}\left[h(b',m',z')-h(b',0,z')\right]$  is high

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Quantitative Effects of Swap Lines

## Calibration

· Calibrate to Argentina without swaps (as in Roch & Roldán, 2023)

	Parameter	Value
Sovereign's discount factor	β	0.9504
Sovereign's risk aversion	$\gamma$	2
Preference shock scale parameter	$\chi$	0.02
Lender's bargaining power	$\theta$	0.5
Risk-free interest rate	r	0.01
Duration of debt	ho	0.05
Income autocorrelation coefficient	$ ho_{z}$	0.9484
Standard deviation of $y_t$	$\sigma_{z}$	0.02
Reentry probability	$\psi$	0.0385
Default cost: linear	$d_0$	-0.24
Default cost: quadratic	$d_1$	0.3

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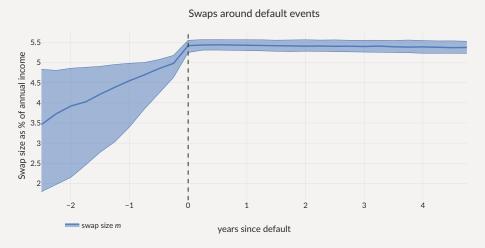
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# How Do Swaps Affect Equilibrium?

	No swap	Unrestricted, $\theta = 0.25$	Unrestricted, $\theta = 0.5$
Avg spread (bps)	804	1841	2396
Std spread (bps)	470	1099	1541
$\sigma(c)/\sigma(y)$ (%)	111	111	110
Debt to GDP (%)	21.4	20.8	20.2
Swap to GDP (%)	0	3.74	3.32
Corr. swap & spreads (%)	-	53.8	62.2
Default frequency (%)	6.53	13.0	14.7
Welfare gains (rep)	_	-0.082%	-0.41%



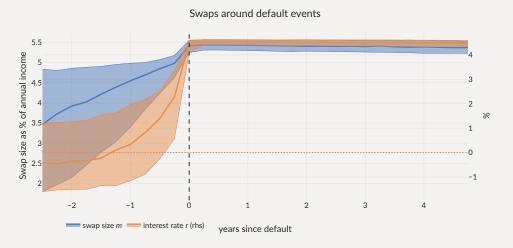
· Swaps shoot up before and during defaults



· Also consider Limited versions:  $m' \leq \Gamma(m)$  while in default



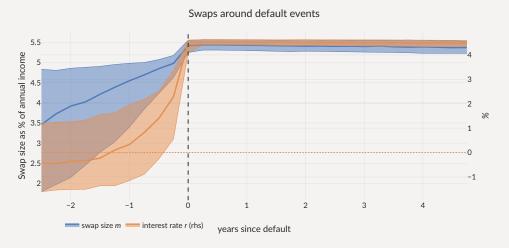
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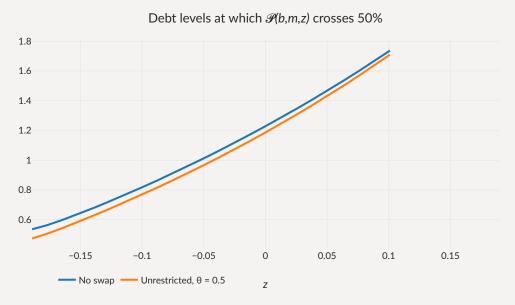
### **Limiting Swaps in Default**

· Limited: entire swap must be repaid while in default  $\Gamma(m) = 0$ 

	No swap	Unrestricted, $ heta=$ 0.5	Limited, $\theta = 0.5$
Avg spread (bps)	804	2,396	1,216
Std spread (bps)	470	1,541	779
$\sigma(c)/\sigma(y)$ (%)	111	110	113
Debt to GDP (%)	21.4	20.2	21.7
Swap to GDP (%)	0	3.32	1.05
Corr. swap & spreads (%)	-	62.2	69.4
Default frequency (%)	6.53	14.7	9.34
Welfare gains (rep)	-	-0.41%	-0.084%

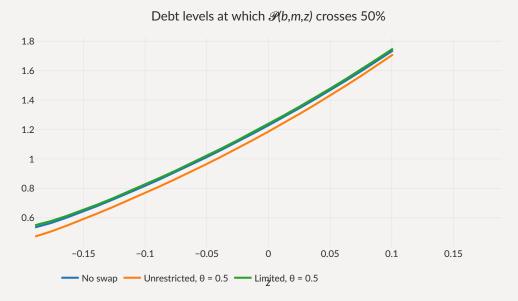
# **Default Barriers with Swaps**

· Unrestricted: default barrier moves inward, Limited: marginal impact



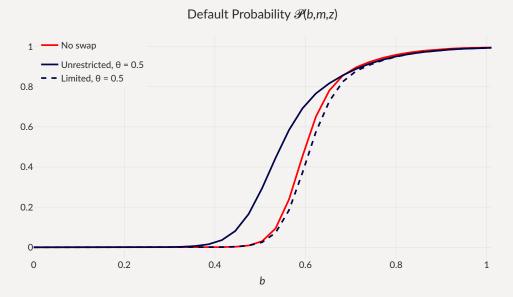
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### **Debt Tolerance with Swaps**

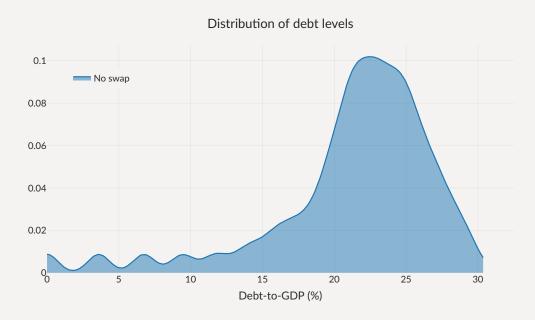
· Unrestricted: default more often, Limited: marginal impact



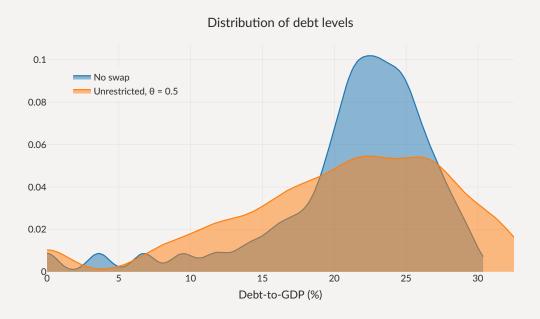
If **Limited** swaps help repay the debt,

Why are there more defaults with swaps?

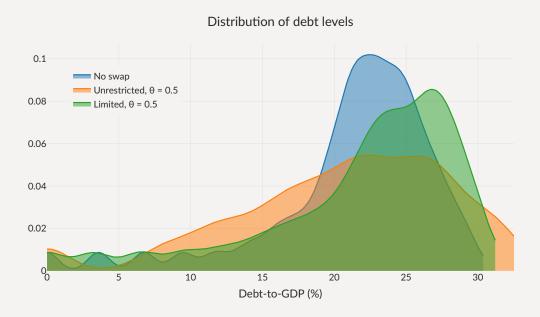
# **Debt Levels with Swaps**



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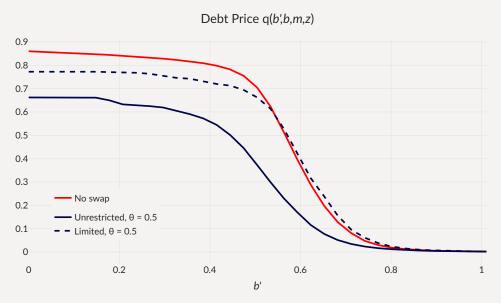


# **Debt Levels with Swaps**



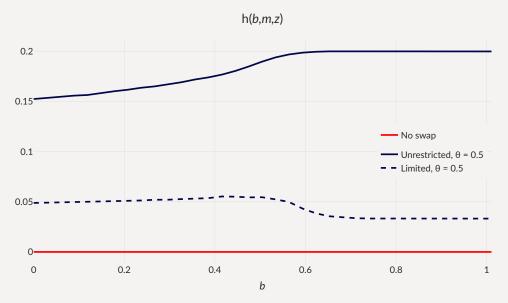
## **Debt Prices with Swaps**

Lower prices with same default rates: relational overborrowing similar to debt dilution



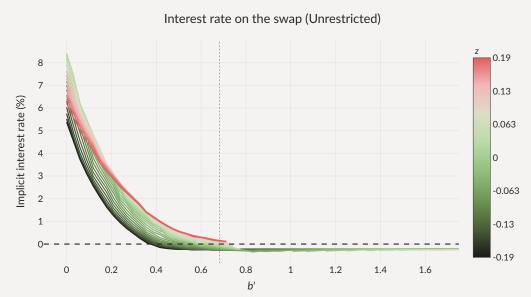
#### **Monopolist's Profits**

Monopolist's profits increasing in debt (cond. on repayment) – surplus requires spreads > 0



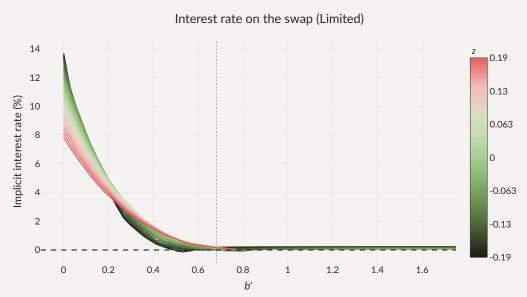
### **Risk-taking Incentives**

Surplus on swap requires spreads > 0: monopolist provides incentives for risk taking



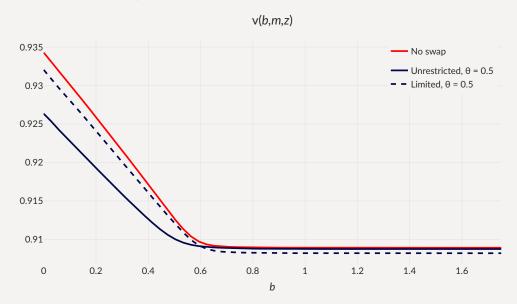
### **Risk-taking Incentives**

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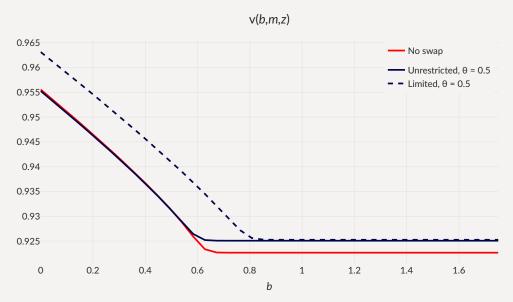
### **Welfare Effects of Swap Lines**

Limited ≽ Unrestricted, but...



#### Welfare Effects of Swap Lines — Short-term Debt

Short-term debt: swaps beneficial – interest on the swap small wrt to whole debt stock



Exogenous Terms for Bilateral Loan

#### Possible rules

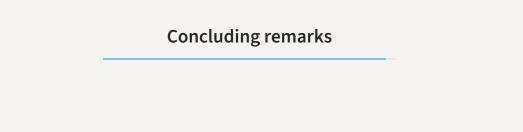
- · Bargaining over bilateral terms endogenously leads to punishment for deleveraging
- · Explore interest rate rules of the form

$$r(b', m') = \max\{r, \alpha_0 + \alpha_b b' + \alpha_m m'\}$$

- · Two versions
  - Risk-inducing rule:  $\alpha_0 > 0, \alpha_b < 0, \alpha_m = 0$
  - · Size-dependent (similar to surcharges):  $\alpha_{\rm 0}>$  0,  $\alpha_{\it b}=$  0,  $\alpha_{\it m}>$  0

# **Equilibrium with Exogenous Rules**

	No swap	Size dependent <i>r</i>	Risk inducing r	$\begin{array}{l} \textbf{Limited,} \\ \theta = \textbf{0.5} \end{array}$
Avg spread (bps)	802	635	1,118	1,211
Std spread (bps)	454	241	1,051	753
$\sigma(c)/\sigma(y)$ (%)	112	120	118	113
Debt to GDP (%)	21.5	25.8	21.9	21.8
Swap to GDP (%)	0	2.32	1.37	1.05
Swap spread (bps)	-	836	2,267	408
Corr. swap & spreads (%)	-	50.2	43.6	70.1
Default frequency (%)	6.27	5.13	7.56	9.17
Welfare gains (rep)	-	0.61%	-0.094%	-0.084%

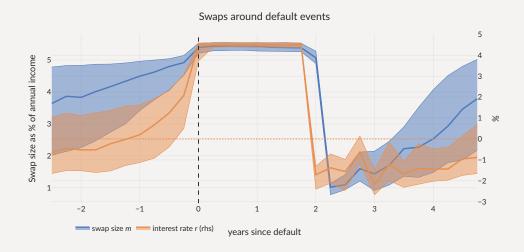


#### The Perils of Bilateral Sovereign Debt

- Simple model with monopolist/fringe structure
- · Strong interaction between two markets for sovereign debt
  - ... even if swaps are **not** used intensely on the equilibrium path
- Market power crucial in model
  - ... how to discipline in model?
  - ... how to **affect** in reality?
- · Large welfare effects, policy challenges
  - How to limit their use during defaults?
  - Relational overborrowing more gains from fiscal rules, state-contingent debt?
- · Simple test to determine welfare gains of a new instrument



· Further conditioning on default events lasting exactly two years





• With Limited:  $\Gamma(m) = m$ 

