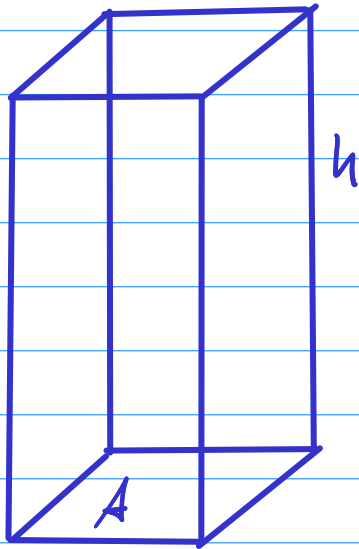


Chap. 2. p. 12

Force and pressure at bottom of a liquid column (incompressible: density = const.)



liquid density ρ

liquid volume

$$V = A \cdot h$$

$$F_G = \rho g V = \rho g A h$$

$$\Rightarrow P = \frac{F_G}{A} = \rho g h$$

Exercise 2.2:

absolute pressure:

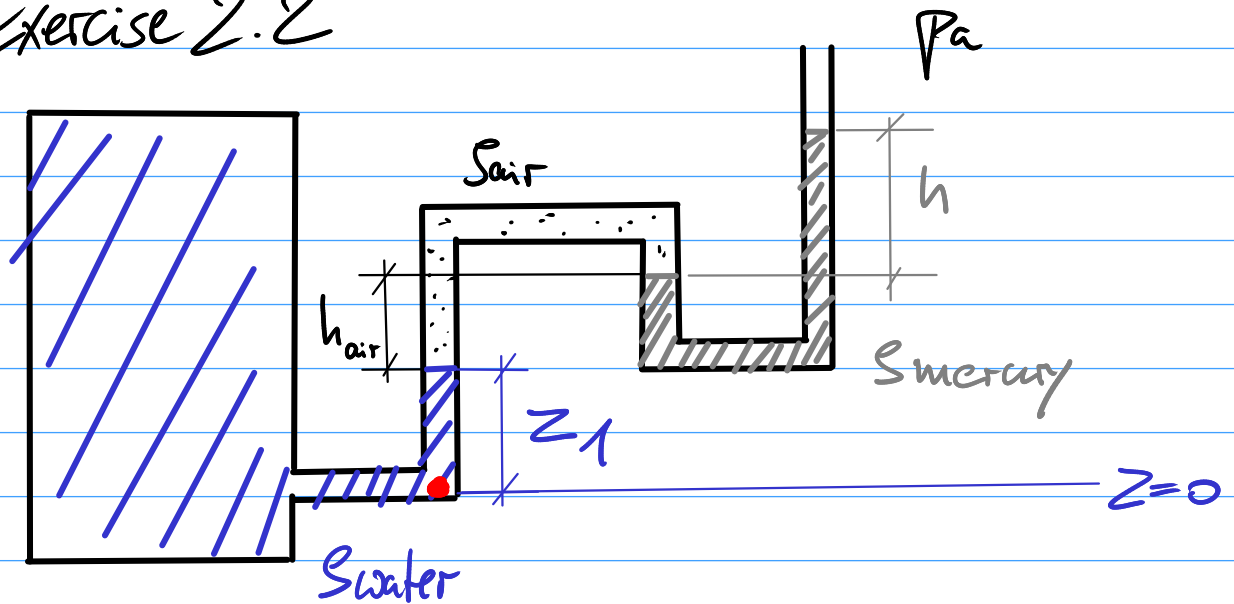
ambient pressure plus
pressure inside fluid

gauge pressure:

pressure inside fluid

$$\text{absolute pressure} = P(z) = P_0 + \underbrace{\rho g (h-z)}_{\text{gauge pressure}}$$

Exercise 2.2



a)

$$\begin{aligned}
 P(z=0) &= P_{\text{water column}} + P_{\text{air column}} + P_{\text{mercury column}} \\
 &= \rho_{\text{water}} z_1 + \rho_{\text{air}} h_{\text{air}} + \rho_{\text{mercury}} h
 \end{aligned}$$

negligible for $h_{\text{air}} \lesssim 1000 \text{ m}$

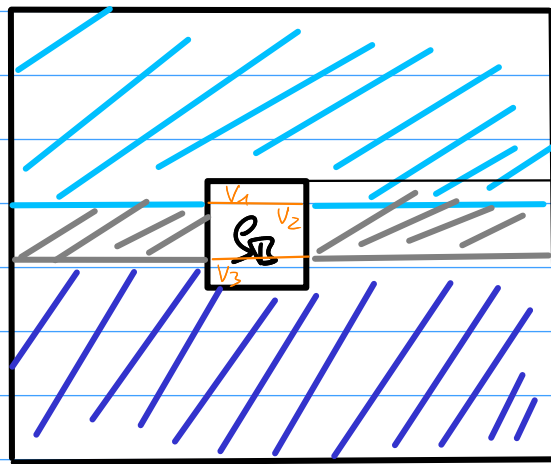
$$\begin{aligned}
 \rho_{\text{air}} &= 1 \frac{\text{kg}}{\text{m}^3} \ll \rho_{\text{water}} < \rho_{\text{mercury}} \\
 \rho_{\text{water}} &= 1000 \frac{\text{kg}}{\text{m}^3} \\
 \rho_{\text{mercury}} &= 13600 \frac{\text{kg}}{\text{m}^3}
 \end{aligned}$$

$$\begin{aligned}
 &\approx \rho_{\text{water}} z_1 + \rho_{\text{mercury}} h \\
 &= \dots \text{ numbers } \dots = P_{\text{gauge}}
 \end{aligned}$$

b)

$$P_{\text{abs}} = P_a + P_{\text{gauge}} = \dots$$

Exercise 2.3



Cube with edges a
 $\Rightarrow A = a^2$ is horizontal area

$l_1 = ?$
 l_2

Buoyancy effects from all 3 liquids:

$$F_{B1} = g \rho_1 V_1 = g \rho_1 A l_1$$

$$F_{B2} = g \rho_2 V_2 = g \rho_2 A l_2$$

$$F_{B3} = g \rho_3 V_3 = g \rho_3 A (a - l_1 - l_2)$$

l_3 is what remains from a

$$F_G = F_B = F_{B1} + F_{B2} + F_{B3}$$

$$\cancel{g} \cancel{A} \cdot a \rho_B = \cancel{g} \rho_1 \cancel{A} l_1 + \cancel{g} \rho_2 \cancel{A} l_2 + \cancel{g} \rho_3 \cancel{A} (a - l_1 - l_2)$$

$$a \rho_B = \rho_1 l_1 + \rho_2 l_2 + \rho_3 a - \rho_3 l_1 - \rho_3 l_2$$

$$a \rho_B - \rho_2 l_2 - \rho_3 a + \rho_3 l_2 = (\rho_1 - \rho_3) l_1$$

$$\frac{a(\rho_B - \rho_3) + l_2(\rho_3 - \rho_2)}{(\rho_1 - \rho_3)} = l_1 = \dots \text{numbers}$$