Architetture dei Sistemi Di Elaborazione

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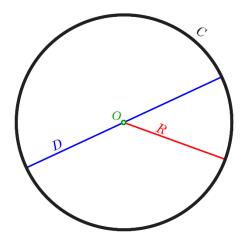
Laboratory 8

Expected delivery of lab_08.zip must include:

- zipped project folder
- this lab track completed and converted to pdf format.

Download the template project for Keil µVision "ABI_C+ASM" from the course material. NB: Deliver a single Keil project including Exercise 1 and Exercise 2.

Exercise 1) – Compute the value of π using the circle method.



Pythagoreans called a set of points equally spaced from a given origin Monad (from Ancient Greek $\mu ov\acute{\alpha}\varsigma$ (monas) 'unity', and $\mu\acute{o}vo\varsigma$ (monos) 'alone'). As originally conceived by the Pythagoreans, the Monad is the Supreme Being, divinity, the totality of all things, or the unreachable perfection by human beings (but we can at least try \mathfrak{G}). The Monad (aka circle) in geometry is strongly intertwined with π (a mathematical transcendental irrational constant), commonly defined as the ratio between a circle's circumference and diameter.

$$\pi = \frac{C}{D}$$

An irrational number <u>cannot</u> be expressed <u>exactly</u> as a ratio of two integers. Consequently, its decimal representation never ends!

3.14159265358979323846264338327950288419716939937510...

However, mathematical operations in computers are finite! In the literature, some interesting methods and algorithms to compute an approximated value of π have been developed.

One of the most intuitive methods is the circle method (not the best in terms of performance). It is based on the following observations.

- The area of the circle is:

$$A=\pi r^2 \, (Eq. \, 1)$$

- Where π can be computed as:

$$\pi = A/_{r^2}(Eq.2)$$

- The assumption is to have a circle of radius **r centered in the origin (0,0).**

Therefore, the Pythagoras theorem states that the distance from the origin is:

$$d^2 = x^2 + y^2(Eq.3)$$

The cartesian plane can be built thinking of unitary squares centered in every (x, y) point, where x and y are the integers between -x and x.

Squares whose center belongs within or on the circumference contribute to the final area. They must satisfy the following:

$$x^2 + y^2 \le r^2(Eq.4)$$

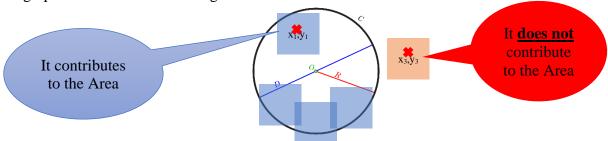
The number of points that satisfy the above condition (Eq. 4) approximates the area of the circle.

Therefore, the final formula is (where the double sums are the Area):

$$\pi \approx \frac{1}{r^2} \sum_{x=-r}^{r} \sum_{y=-r}^{r} check_square(x, y, r) \ (Eq. 5)$$

where
$$check_square(x, y, r) = \begin{cases} 1, & x^2 + y^2 \le r^2 \\ 0, & x^2 + y^2 > r^2 \end{cases}$$

The graphical idea is the following:



Declare the coordinates as couples of (x, y) (<u>signed integer</u>) into a read-only memory region 2-byte aligned (<u>into an assembly file</u>) as follows:

The parsing of Matrix_Coordinates must be done in C. Remember that the extern keyword must be used for referencing assembly data structures:

```
extern <datatype> _ Matrix_Coordinates;
extern <datatype> _ ROWS;
extern <datatype> _ COLUMNS;
```

In the loop body of Eq. 4, check_square (x, y, r) is called using an assembly function with the following prototype:

which implements:

check_square(x, y, r) =
$$\begin{cases} 1, & x^2 + y^2 \le r^2 \\ 0, & x^2 + y^2 > r^2 \end{cases}$$

1.1) Moreover, the Arm Cortex-M3 <u>does not provide hardware floating point support.</u> Therefore, we can resort to software emulated floating-point algorithms, including the type float. As an example, Arm FPlib has the following EABI-compliant function for float division:

```
float aeabi fdiv (float a ,float b) /* return a/b */
```

https://developer.arm.com/documentation/dui0475/m/floating-point-support/the-software-floating-point-library--fplib/calling-fplib-routines?lang=en

You are required to compute the division with r^2 in (Eq. 5) by calling a second assembly function with the following prototype:

```
float my division(float* a, float* b)
```

The function body to implement is:

```
my_division:
    /*save R4,R5,R6,R7,LR,PC*/
    /*obtain value of a and b and prepare for next function call*/
    /*call __eabi_fdiv*/
    /*results has to be returned!*/
    /*restore R4,R5,R6,R7,LR,PC*/
```

1.2) Compute the value of π using a radius of 2,3,5 and store it into a variable.

Radius (r)	Area	Approximated value of π	Clock Cycle
		(3 decimal units)	(xtal=18 MHz)
2	13	3,250	27415
3	29	3,222	27505
5	81	3,240	27781

Converter from hex to FP (and viceversa): https://gregstoll.com/~gregstoll/floattohex/

Exercise 2) – SuperVisorCall (SVC)

Enhance the program developed in Exercise 1 by using the **SVC** instruction after the computation of π . Copy part of the template project for Keil μ Vision "SVC".

You must set the control to user mode (unprivileged) and use the Process Stack Pointer.

2.1) Starting from Exercise 1, write a code to compute a **signature** by calling the SVC with *0xCA*.

In safety-critical domains, such as the automotive one, functional test programs based on CPU instructions are developed to verify the correct in-field behavior of microprocessor-based systems. This safety process is also known as online testing. A possible way to assess if a functional test program has executed its computations correctly is to introduce a signature computation to be checked at the end of the test program.

A signature typically accumulates into one register the others' values by means of an arithmetic operation. For example, suppose you have R0, R1, R2, R3, R4, R5, and you want to compute the signature into R0.

```
XOR R0, R0, R1
XOR R0, R0, R2
XOR R0, R0, R3
XOR R0, R0, R4
XOR R0, R0, R5
```

Implement an SVC call to compute the signature between Registers from 0 to 12, the LR and XPSR with the XOR instruction.

```
This must be done by calling the SVC at the end of Exercise 1. 
 asm ("svc 0xca");
```

The computed signature value must be accumulated into R0 and returned from the SVC through the PSP stack (as shown in the figure below).

	Stack		
	result_here		
+28	xPSR		
+24	PC		
+20	LR		
+16	R12		
+12	R3		
+8	R2		
+4	R1		
SP >	R0		

2.2) Starting from Exercise 1, write a code for **memory compaction** by calling the SVC with *0xFE*.

Compute the memory footprint of *Matrix Coordinates* in bytes in Exercise 1.

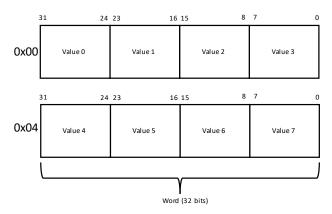
Data	Size [bytes]
Matrix_Coordinates	968

In this case, it can be safely assumed that points are <u>always in the range [-128,127].</u> Therefore, data can be <u>compacted</u> (4 values for each word).

Implement a SVC call to compact *Matrix_Coordinates* and store its compacted version into an empty optimized data structure called *Opt_M_Coordinates* (declared into an assembly file as Read/Write region), you have to calculate the required size!

This must be done by calling the SVC at the end of Exercise 1.

The idea is:



Then compute the memory footprint.

Data	Size [bytes]	Memory saved [bytes]	
Matrix_Coordinates	968	0	
Opt_M_Coordinates	242	724	