Feature Importance in Decision Trees:

Impurity-based Importance Calculations & Explainable AI

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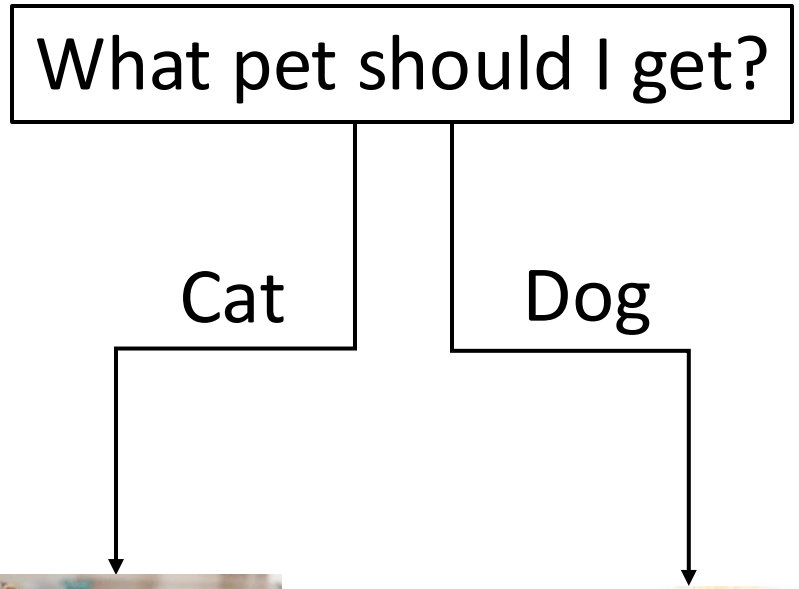
SprintML

You already interact(ed) with decision trees!



May 11, 2023 2m read

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… or listening to music.

Outline for Today

- Intuition on classification with decision tree
- Impurity-based feature importance metrics
- Building decision trees based on impurity reduction
- Feature importance and explainable AI

Datasets and Tree-based Classification

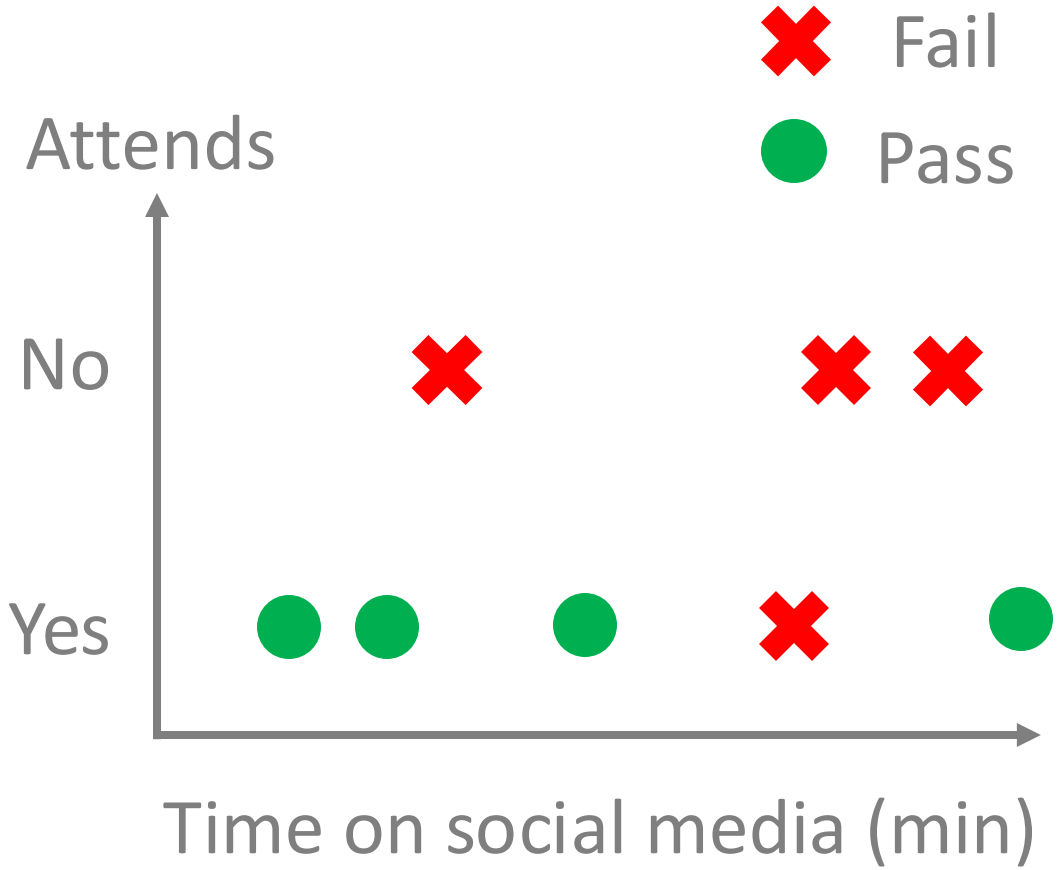
Dataset from my Lecture

Social Media Time (min)	Attends Class	Passed the Midterm
30	Yes	Pass
80	Yes	Pass
140	Yes	Pass
50	Yes	Pass
110	No	Fail
60	No	Fail
100	Yes	Fail
120	No	Fail

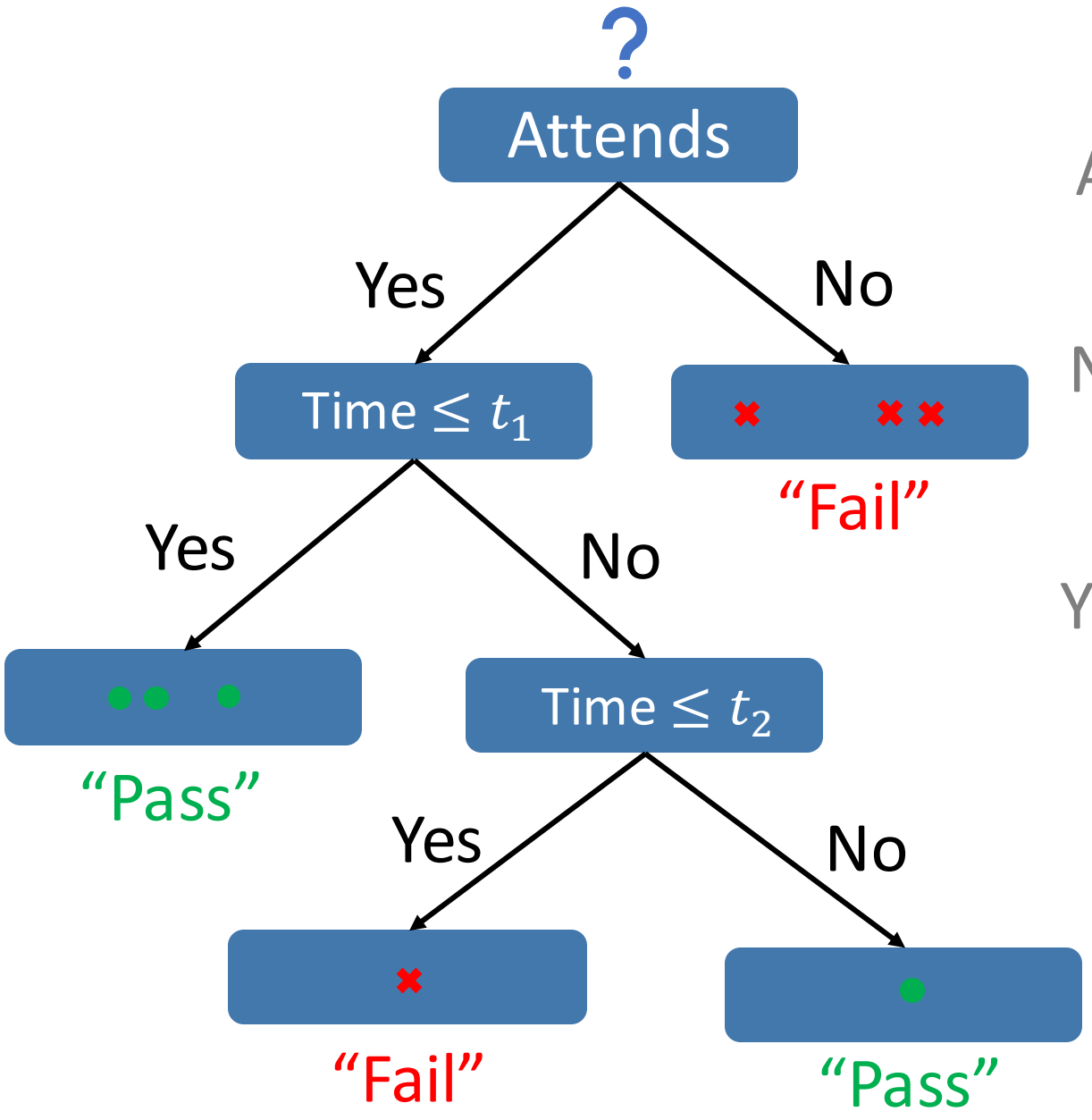
Continuous Categorical

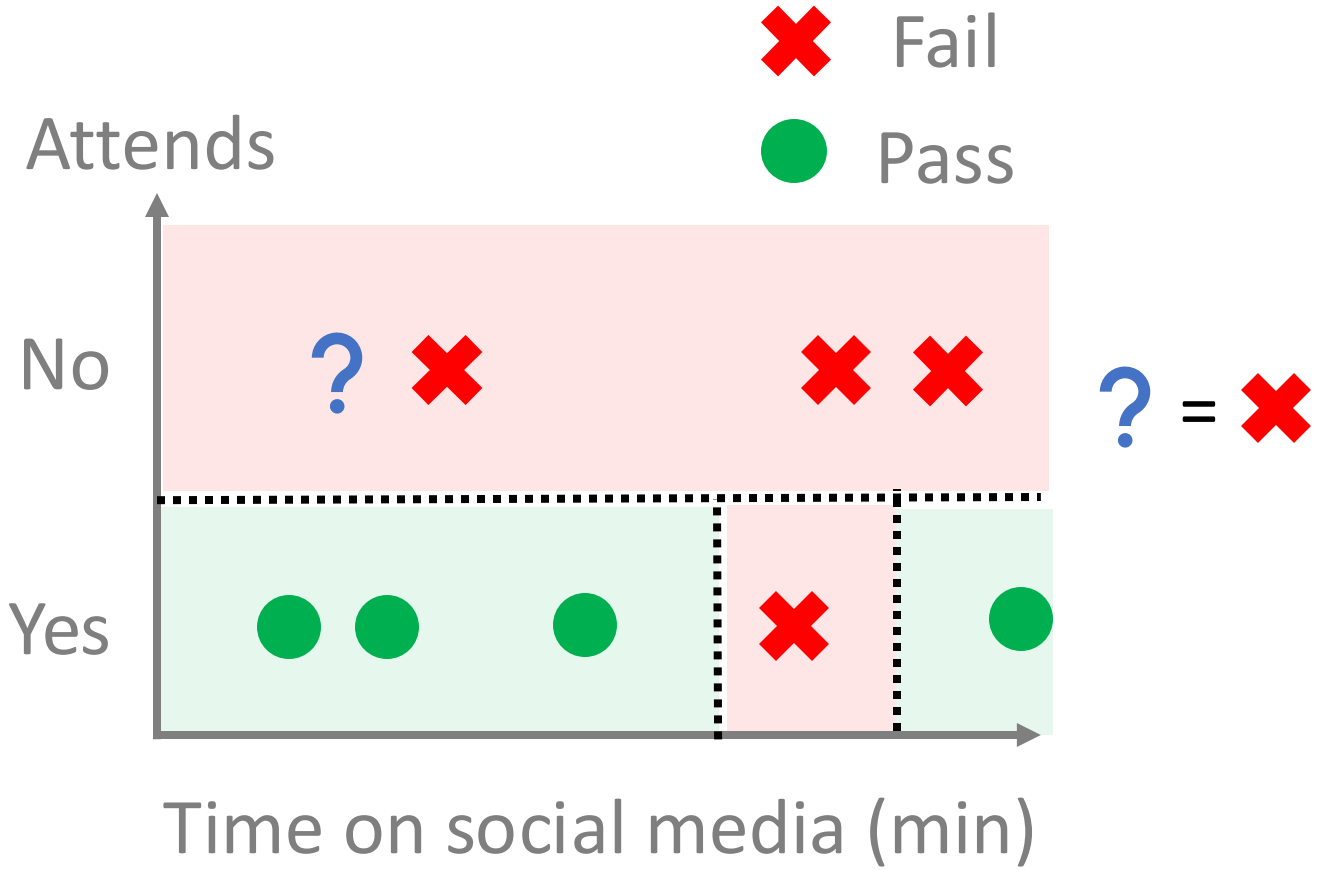
Features

Label



Datasets and Tree-based Classification





Successively find splits of the data to create decision regions

Greedy, recursive partitioning

Finding the Best Split Criterion

Social Media Time (min)	Attends Class	Passed the Midterm
30	Yes	Pass
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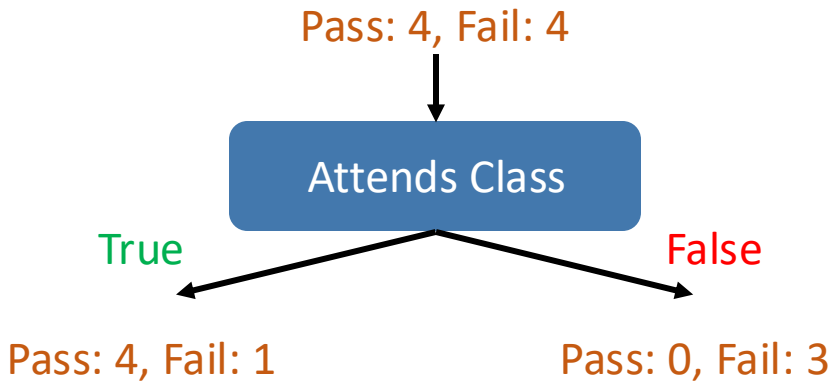


Impure split

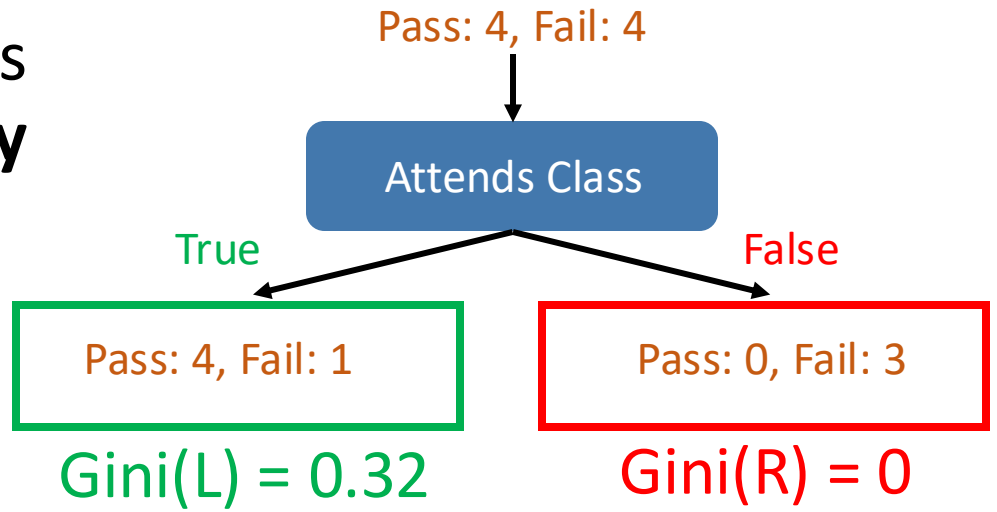
Pure split

Is attendance our best spilt?

Gini Impurity: Definition

Given a node with K classes and class probabilities $p_1, \ldots, p_k$. The **Gini Impurity** is defined as

$$Gini(Node) = 1 - \sum_{k=1}^{K} p_k^2 .$$



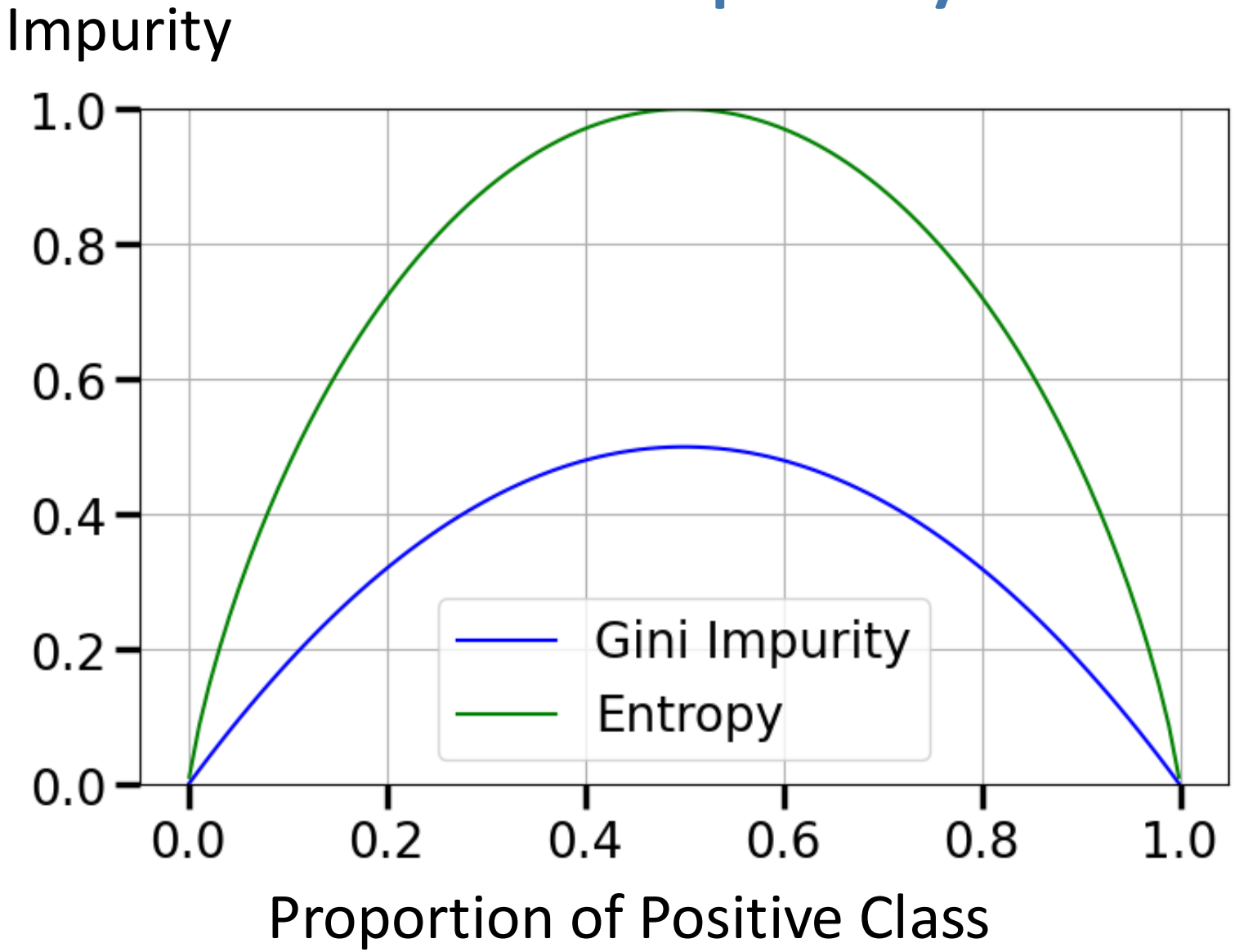
Here: $1 - \left(p_{pass}^2 + p_{\text{fail}}^2\right)$ $\quad p_{pass} = \frac{4}{5}, p_{fail} = \frac{1}{5}$ $\quad p_{pass} = \frac{0}{3}, p_{fail} = \frac{3}{3}$

In our example:

- True branch: Gini(L) = $1 - \left(\frac{4}{5}\right)^2 - \left(\frac{1}{5}\right)^2 = 0.32$
- False branch: Gini(R) = $1 - (0)^2 - (1)^2 = 0$

Gini of a pure split is zero

Gini Impurity and Entropy



Alternative to Gini:

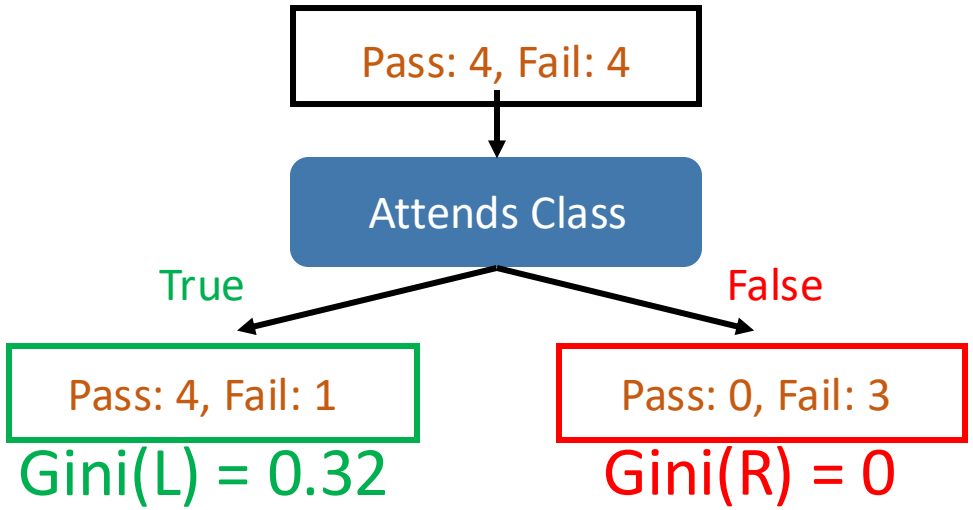
Entropy $= -\sum_k p_k \log_2 p_k$,

with p_k : proportion of data from class k in the node.

Gini Impurity of the Entire Split

When evaluating a split, we compute the **weighted Gini of the children**:

$$Gini_{split} = \frac{n_L}{n} Gini(L) + \frac{n_R}{n} Gini(R)$$



→ 8

→ 5

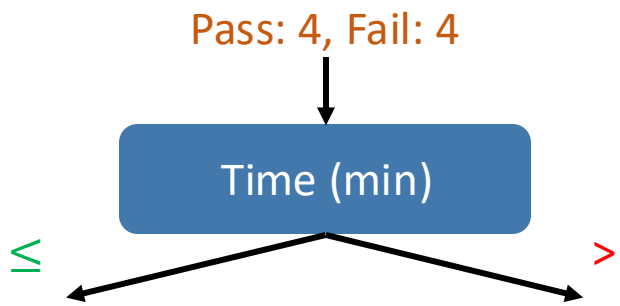
→ 3

$Gini_{split} = 0.2$

$$Gini_{split} = \frac{5}{8} * 0.32 + \frac{3}{8} * 0 = 0.2$$

Gini Impurity on Continuous Values

Goal: Identify the best splitting threshold



Social Media Time (min)	Passed the Midterm
30	Pass
50	Pass
60	Fail
80	Pass
100	Fail
110	Fail
120	Fail
140	Pass

1. Sort ascending

2. Identify where class changes

3. Take average as threshold

≤ 55

≤ 70

≤ 90

≤ 130

Gini Impurity on Continuous Values

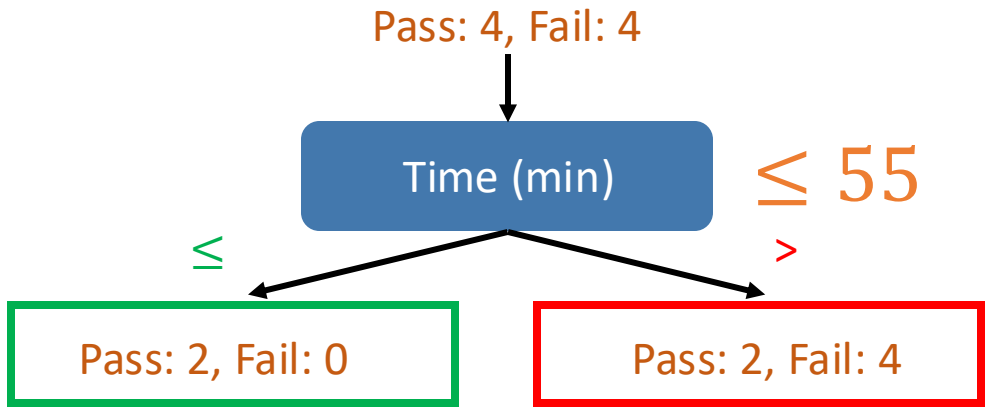
Social Media Time (min)	Passed the Midterm
30	Pass
50	Pass
60	Fail
80	Pass
100	Fail
110	Fail
120	Fail
140	Pass

0.33

0.48

0.38

0.44



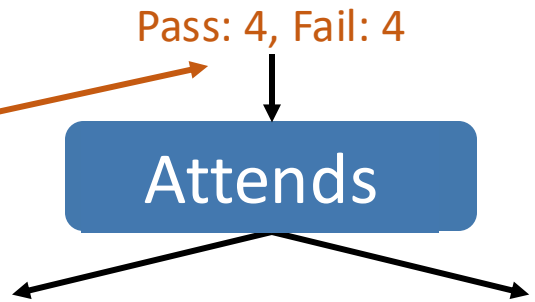
$Gini(L) = 0$ $Gini(R) \approx 0.44$

$$Gini_{split} \approx 0.33$$

Impurity Reduction to Choose the Best Split

Choose the split that causes the maximum **impurity reduction** $\Delta i(\text{split})$:

$$\Delta i\,(split) = \max(Gini_{parent} - Gini_{split})$$



$$Gini_{parent} = 1 - \left(\frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^2 = 0.5$$

is fixed → find lowest $Gini_{split}$

$$\Delta i\,(Attends) = 0.5 - 0.2 = 0.3$$

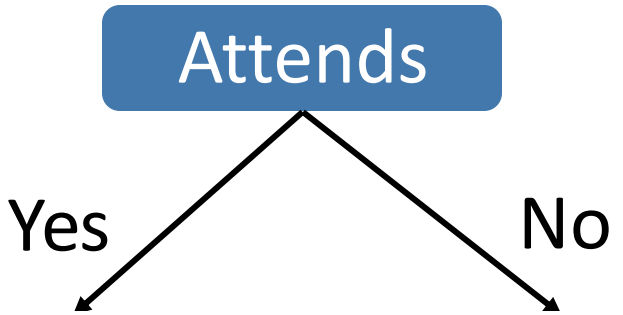
Gini impurity over all possible splits:

$$Gini_{Attends} = 0.2$$
$$Gini_{Time \leq 55} = 0.33$$
$$Gini_{Time \leq 70} = 0.48$$
$$Gini_{Time \leq 90} = 0.38$$
$$Gini_{Time \leq 130} = 0.44$$

From Trees to Explainable AI

Decisions in the tree are:

- Human-interpretable
- Verifiable
- We can ask “What if?” (Counterfactuals)



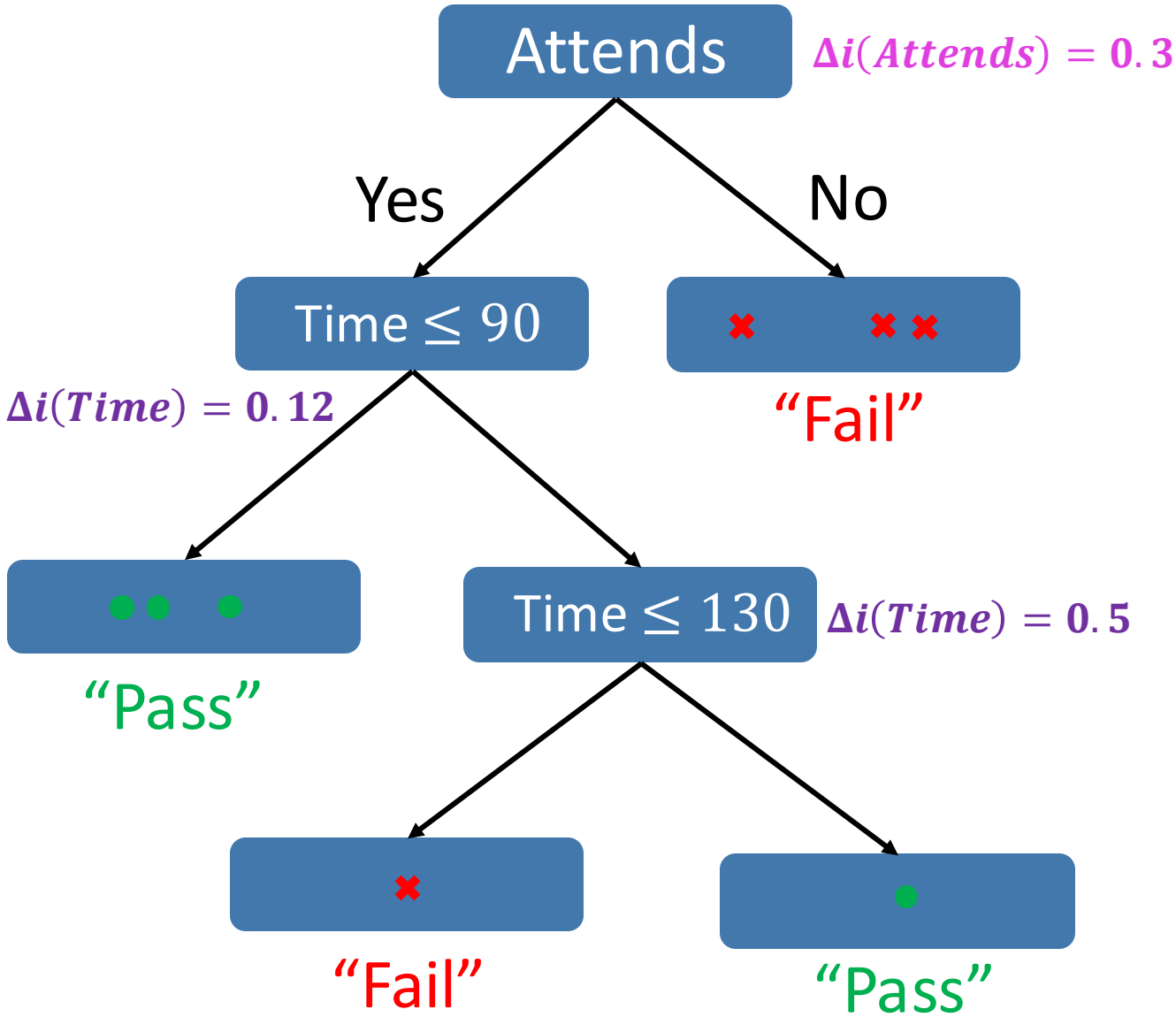
Impurity-based Feature importance

We calculate the **importance** of a feature f in a tree as:

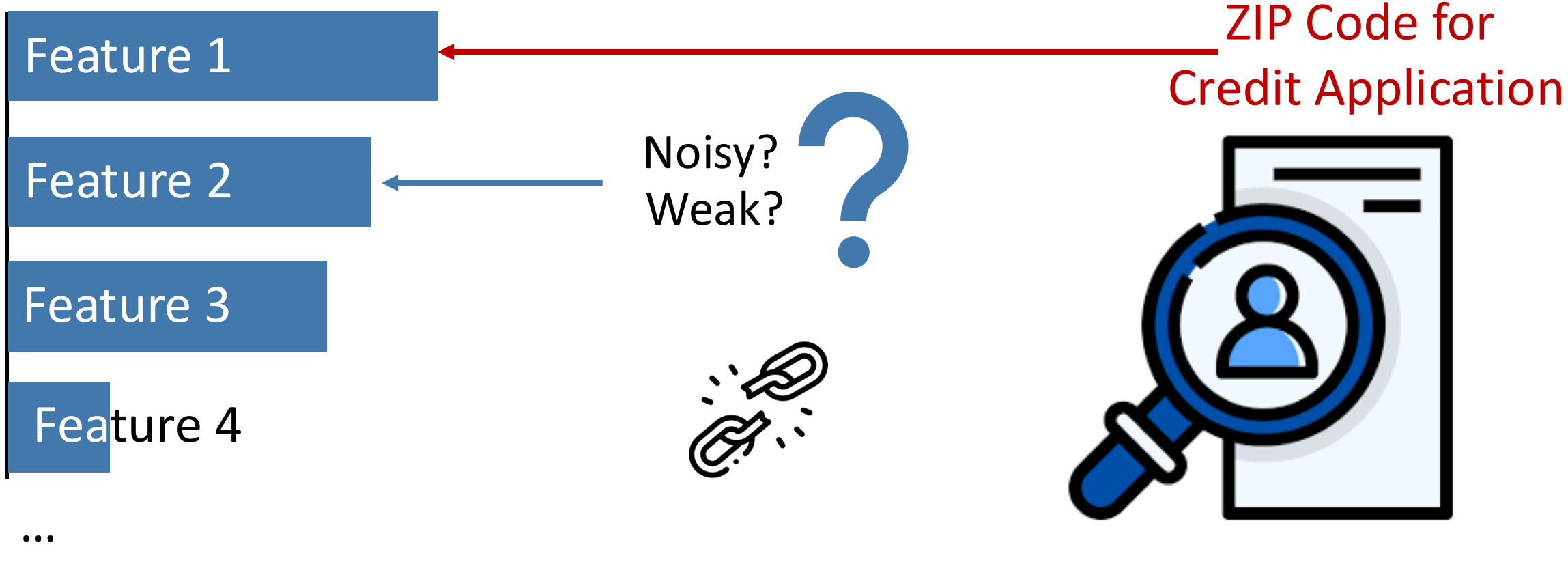
$$Importance(f) = \frac{\sum_{t \in Splits\ on\ f} \Delta i(t)}{\sum_{s \in All\ splits} \Delta i(s)}.$$

$$Importance(Attends) = \frac{0.3}{0.3 + 0.12 + 0.5} \approx 32.6\%$$

$$Importance(Time) = \frac{0.12 + 0.5}{0.3 + 0.12 + 0.5} \approx 67.4\%$$



Feature Importance for Explainability

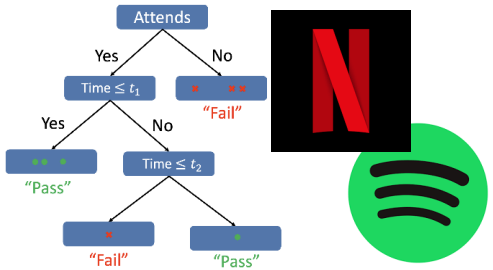


Understanding predictions

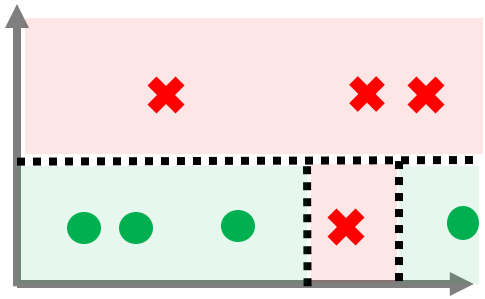
Model debugging

Identifying biases

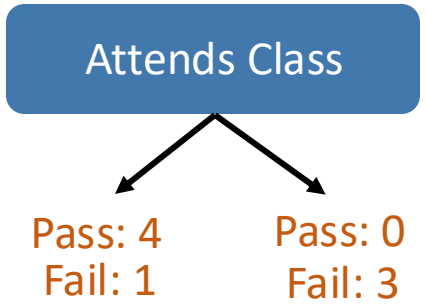
Summary & Lecture Materials



Decision Trees: Omnipresent



Divide Data in Regions



Impurity-based Feature Splits

Serve Explainable AI

Lecture Materials:

SCAN ME