

Homework 6

Christopher Achenbach

Problems from 2.10

1. $(x \leq 0) \vee (y \geq 0)$
2. $(x \in \mathbb{P}) \wedge (\sqrt{x} \in \mathbb{Q})$
3. $\exists p \in \mathbb{P}, \forall q \in \mathbb{P}, q \leq p$
4. $\exists \epsilon \in \mathbb{R}^+, \forall \delta \in \mathbb{R}^+, (|x - a| < \delta) \wedge (|f(x) - f(a)| \geq \epsilon)$
5. $\exists \epsilon \in \mathbb{R}^+, \forall M \in \mathbb{R}^+, (x > M) \wedge (|f(x) - b| \leq \epsilon)$
6. $\forall a \in \mathbb{R}, \exists x \in \mathbb{R}, a + x \neq x$
7. I eat a thing with a face.
 $\exists x \in \{\text{Things that I eat}\}, x \in \{\text{Things with faces}\}.$

Problems from 4.1

1. Suppose $\neg((\neg P) \wedge (\neg Q))$ is true.
Suppose $\neg Q$ is true.

$$\begin{aligned}\neg(\neg P \wedge \neg Q) &= \neg(\neg P \wedge \text{true}) \\ &= P \vee \text{false} \\ &= P\end{aligned}$$

Since $\neg(\neg P \wedge \neg Q)$ is true, P is also true.
Therefore P .

2. Suppose the statements $\neg R$, $P \rightarrow R$, and $P \vee Q$ are all true.
Since $\neg R$ is false, R must be true.

$$\begin{aligned}P \rightarrow R &= \neg P \vee R \\ &= \neg P \vee \text{true} \\ &= \text{true}\end{aligned}$$

Since $\neg R$ is false, R must be true.

$$\begin{aligned}P \vee Q &= \text{true} \vee Q \\ &= \text{true}\end{aligned}$$

Since $P \vee Q$ is true, Q is also true.
Therefore Q .