



CentraleSupélec

Machine Learning

M.Sc. in DSBA & M.Sc. in AI

Lecture 1

Part I: Introduction; Part II: Model selection and evaluation

Fragkiskos Malliaros

Wednesday, October 9, 2019

About Me

- Undergrad at the University of Patras, Greece
- Ph.D. in CS at Ecole Polytechnique, Paris
- Postdoc researcher at UC San Diego
- Assistant Professor at CentraleSupélec (since Oct. 2017)

Research interests: Data science, ML, graph mining, text mining and NLP

The Team



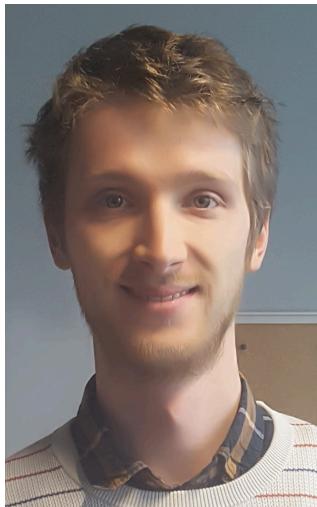
Instructor: **Fragkiskos Malliaros**

Office: Bâtiment Bouygues, CVN Lab, Room SC.217

Office hours: I will be available right after the lecture

Or, send me an email and we will find a good time to meet

Email: fragkiskos.me@gmail.com



TA: **Sylvain Lannuzel** (Ph.D. student)

Email: sylvain.s.lannuzel@gmail.com

Acknowledgements

- The lecture is partially based on material by
 - Richard Zemel, Raquel Urtasun and Sanja Fidler (University of Toronto)
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 - Julian McAuley (UC San Diego)
 - Dimitris Papailiopoulos (UW-Madison)
 - Jure Leskovec, Anand Rajaraman, Jeff Ullman (Stanford Univ.)
 - <http://www.mmds.org>
 - Panagiotis Tsaparas (UOI)
 - Evinaria Terzi (Boston University)

Thank you!

Slides of Today's Lecture

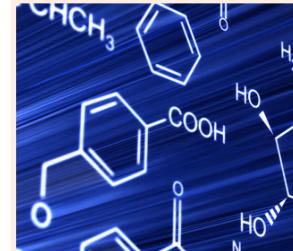
<http://fragkiskos.me/introduction.pdf>

Why Machine Learning?

Automation and Robotics



Drug Discovery and Healthcare



Intelligent Personal Assistants



Recommender Systems

Recommendations for You, Dimt



Automation and Robotics



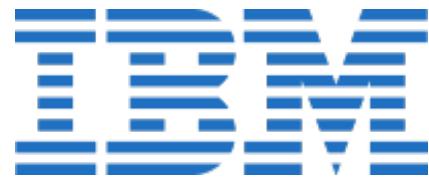
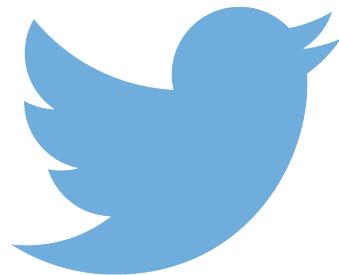
Real and important problems



Recommender Systems

Recommendations for You, Dimitris





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8,184 Machine Learning jobs in United States

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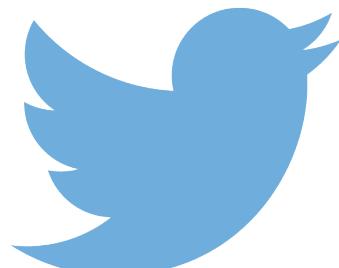
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30,669 Data Scientist jobs in United States

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become available



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Job market

8,184 Machine Learning jobs in United States

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Data Scientist



United States



Find jobs

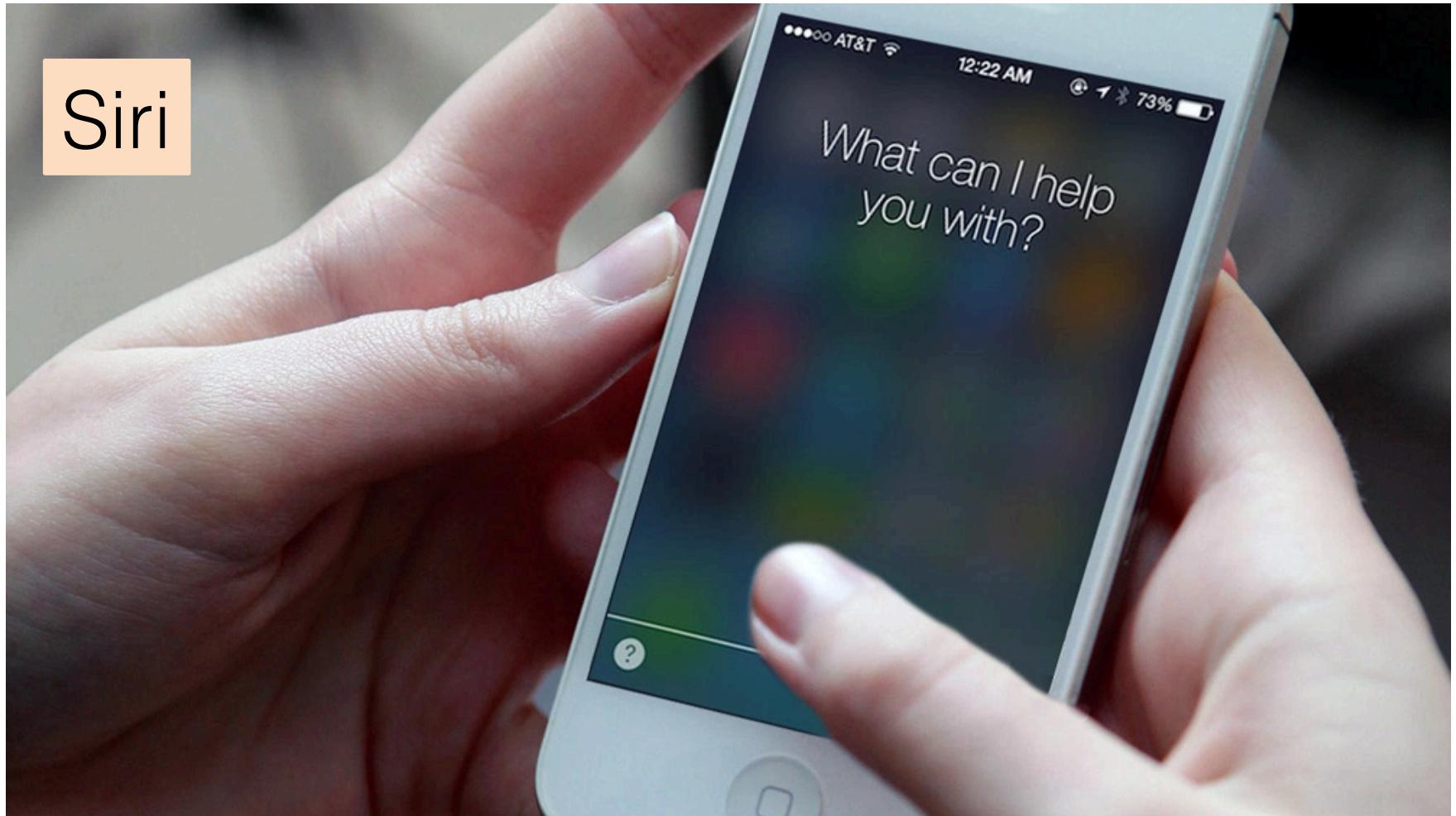
30,669 Data Scientist jobs in United States

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We'll email you new jobs as they
become available

Machine Learning is Almost Everywhere

- Recognizing patterns: Speech Recognition, facial identity, etc

Speech Recognition



Source: <http://bgr.com/2017/01/24/iphone-8-enhanced-siri-upgrade/>

Machine Learning is Almost Everywhere

- Recognizing patterns: Speech Recognition, facial identity, etc
- Recommender Systems: Noisy data, commercial pay-off
(e.g., Amazon, Netflix)

Example of a Recommendation System

NETFLIX | Your Account & Help

Movies, TV shows, actors, directors, genres

Watch Instantly | Browse DVDs | Your Queue | **Movies You'll ❤**

Congratulations! Movies we think **You** will ❤

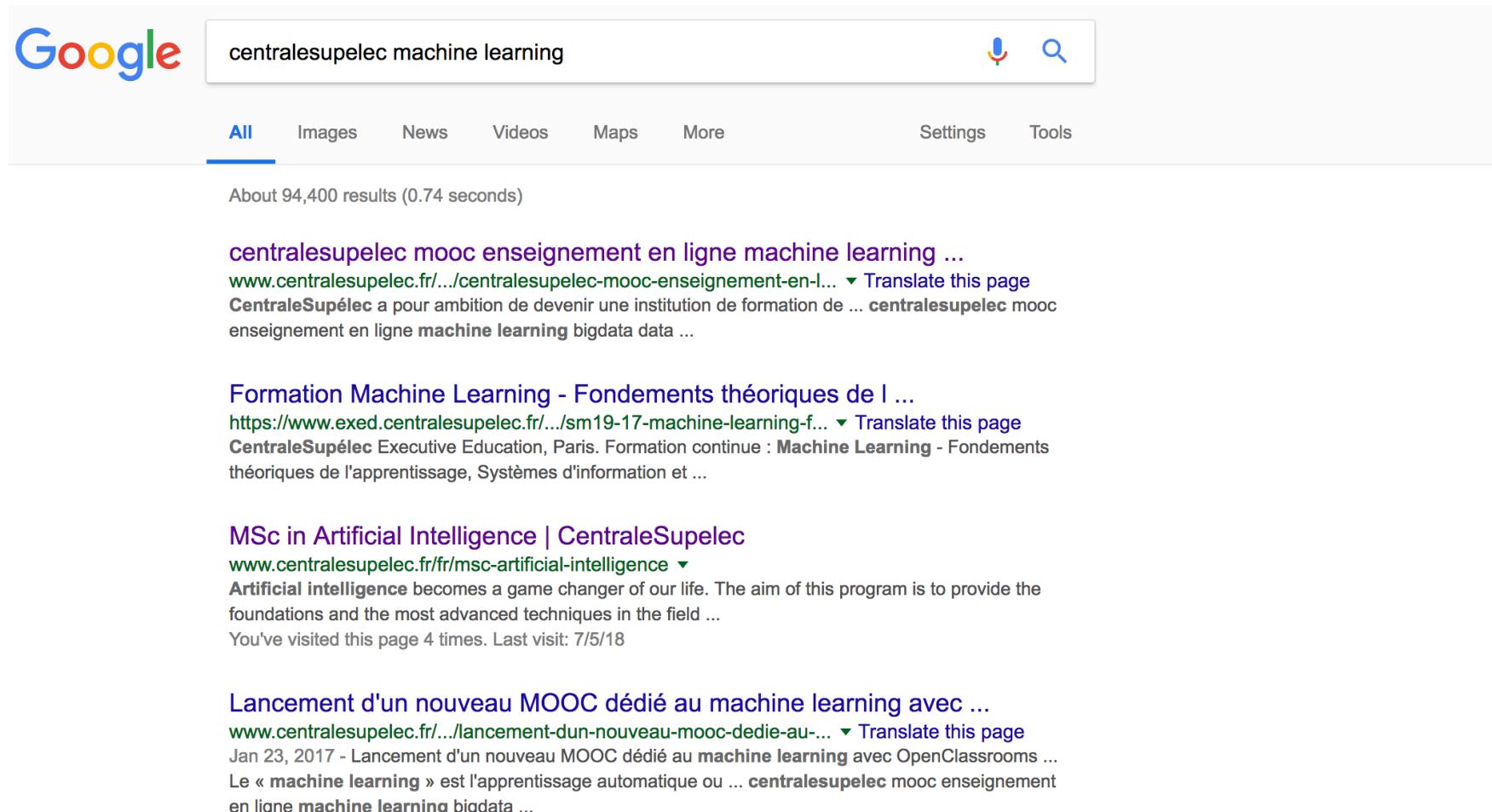
Add movies to your Queue, or Rate ones you've seen for even better suggestions.

Spider-Man 3 <input type="button" value="Add"/> 	300 <input type="button" value="Add"/> 	The Rundown <input type="button" value="Add"/> 	Bad Boys II <input type="button" value="Add"/>
Las Vegas: Season 2 (6-Disc Series) 	The Last Samurai 	Star Wars: Episode III 	Robot Chicken: Season 3 (2-Disc Series)

Machine Learning is Almost Everywhere

- Recognizing patterns: Speech Recognition, facial identity, etc
- Recommender Systems: Noisy data, commercial pay-off
(e.g., Amazon, Netflix)
- Information retrieval: Find documents or images with similar content

Information Retrieval (1/2)



A screenshot of a Google search results page. The search query is "centralesupelec machine learning". The results are filtered by "All" and show approximately 94,400 results in 0.74 seconds. The first result is a link to a Mooc page titled "centralesupelec mooc enseignement en ligne machine learning ...". The second result is a link to a formation page titled "Formation Machine Learning - Fondements théoriques de l ...". The third result is a link to an MSc program page titled "MSc in Artificial Intelligence | CentraleSupélec". The fourth result is a news article titled "Lancement d'un nouveau MOOC dédié au machine learning avec ...".

Google

centralesupelec machine learning

All Images News Videos Maps More Settings Tools

About 94,400 results (0.74 seconds)

centralesupelec mooc enseignement en ligne machine learning ...
www.centralesupelec.fr/.../centralesupelec-mooc-enseignement-en-l... ▾ Translate this page
CentraleSupélec a pour ambition de devenir une institution de formation de ... centralesupelec mooc enseignement en ligne machine learning bigdata data ...

Formation Machine Learning - Fondements théoriques de l ...
<https://www.exed.centralesupelec.fr/.../sm19-17-machine-learning-f...> ▾ Translate this page
CentraleSupélec Executive Education, Paris. Formation continue : Machine Learning - Fondements théoriques de l'apprentissage, Systèmes d'information et ...

MSc in Artificial Intelligence | CentraleSupélec
www.centralesupelec.fr/fr/msc-artificial-intelligence ▾
Artificial intelligence becomes a game changer of our life. The aim of this program is to provide the foundations and the most advanced techniques in the field ...
You've visited this page 4 times. Last visit: 7/5/18

Lancement d'un nouveau MOOC dédié au machine learning avec ...
www.centralesupelec.fr/.../lancement-dun-nouveau-mooc-dedie-au-... ▾ Translate this page
Jan 23, 2017 - Lancement d'un nouveau MOOC dédié au machine learning avec OpenClassrooms ...
Le « machine learning » est l'apprentissage automatique ou ... centralesupelec mooc enseignement en ligne machine learning bigdata ...

Information Retrieval (2/2)

Google Machine Learning

All News Videos **Images** Books More Settings Tools View saved SafeSearch ▾

data science artificial intelligence big data iot analytic scalable cloud self training statistical deep learning supervised neural bayes

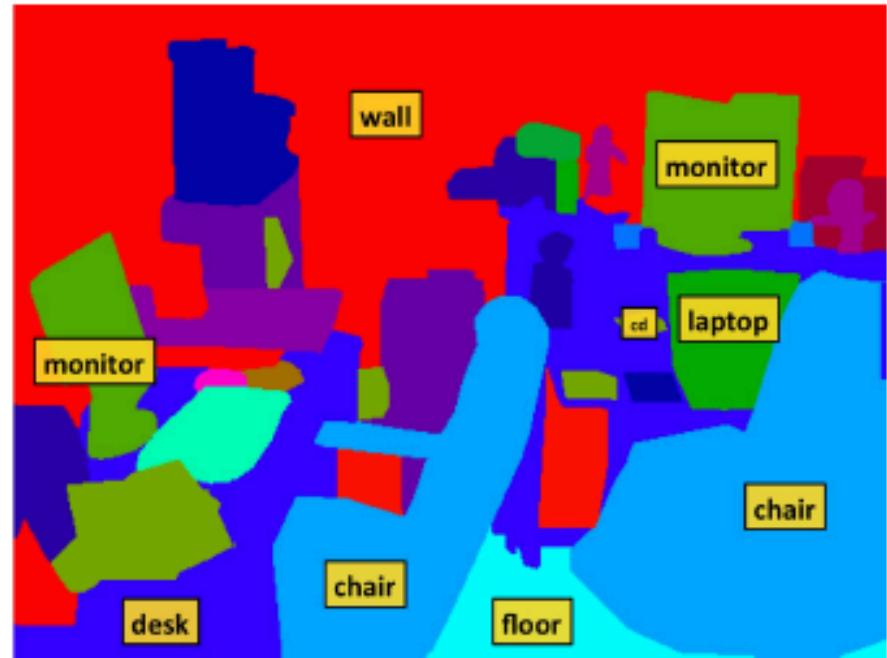
MACHINE LEARNING

The search results show eight images arranged in two rows of four. The first row includes: a brain composed of nodes and connections; a complex network diagram with various icons like clouds, databases, and code snippets; a white humanoid robot holding a tablet with a green background; and a hand interacting with a glowing blue neural network. The second row includes: a circular diagram showing the machine learning process (Preprocess data, Train model, Apply model, Capture feedback); a network graph with nodes labeled 'MACHINE LEARNING'; a glowing blue brain circuit board against a black background; and a profile view of a head containing various icons representing different fields of knowledge.

Machine Learning is Almost Everywhere

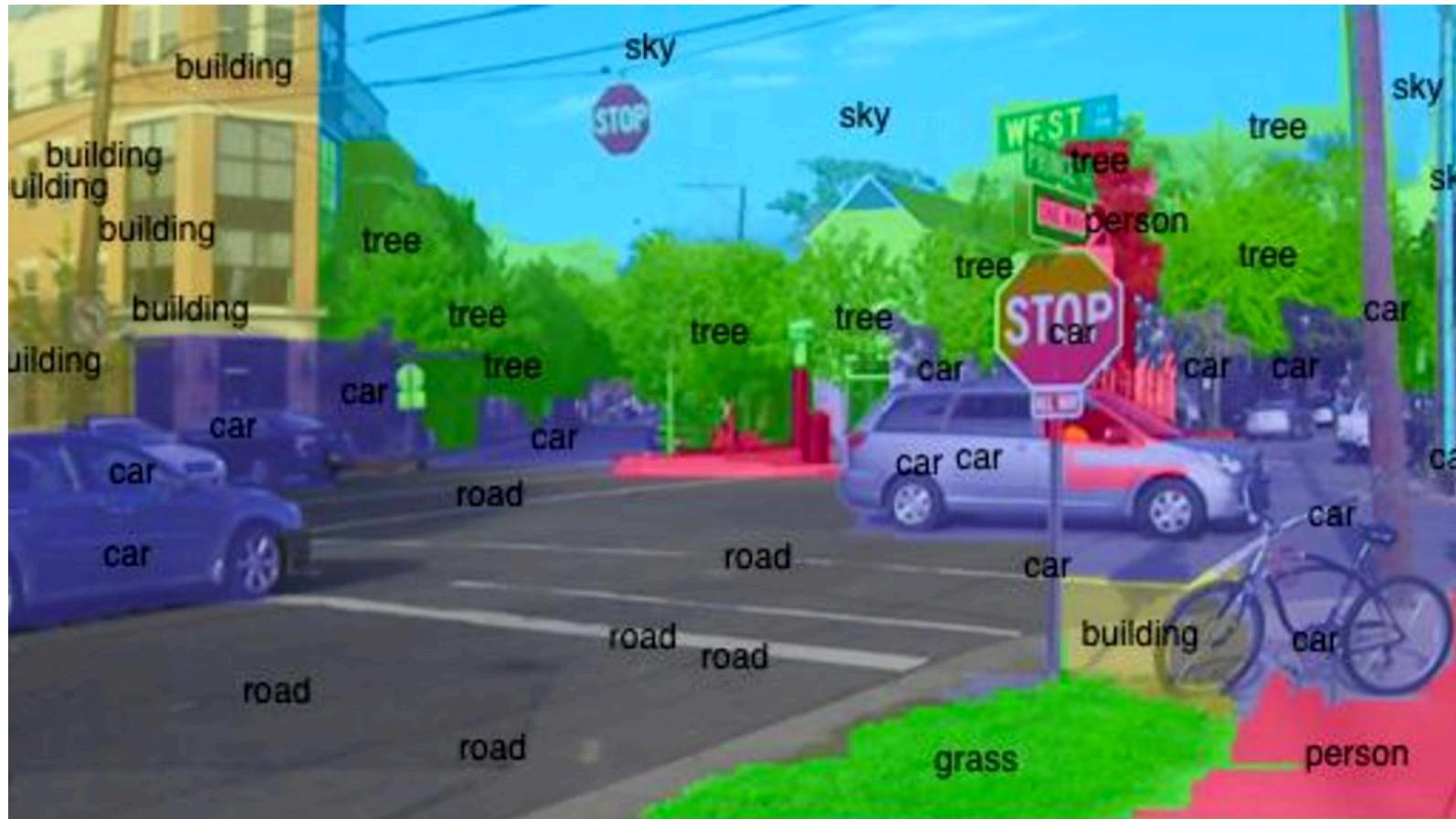
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(e.g., Amazon, Netflix)
- Information retrieval: Find documents or images with similar content
- Computer vision: detection, segmentation, depth estimation, optical flow, etc.

Computer Vision (1/3)



Source: R. Urtusan, U. of Toronto

Computer Vision (2/3)



Source: <https://techcrunch.com/2016/11/13/wtf-is-computer-vision/>

Computer Vision (3/3)



[Gatys, Ecker, Bethge. A Neural Algorithm of Artistic Style. Arxiv'15.]

Machine Learning is Almost Everywhere

- Recognizing patterns: Speech Recognition, facial identity, etc
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- Computer vision: detection, segmentation, depth estimation, optical flow, etc.
- **Robotics:** perception, planning, autonomous driving, etc.

Autonomous Driving



Source: <https://www.tesla.com/videos/autopilot-self-driving-hardware-neighborhood-long>
<https://www.youtube.com/watch?v=hLaEV72elj0>

Machine Learning is Almost Everywhere

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- Computer vision: detection, segmentation, depth estimation, optical flow, etc.
- Robotics: perception, planning, autonomous driving etc
- **Learning to play games**

AlphaGo



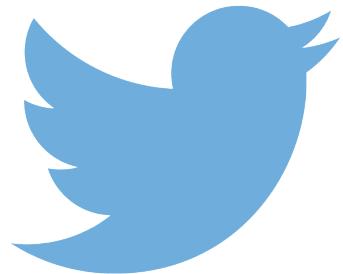
Source: <https://www.newscientist.com>

Also, large-scale. Why?

Content Generation



More than 700 photos uploaded / second



More than 7k tweets / second



More than 55K google searches / second

More than 2.5 million emails sent / second



Content Generation



More than 700 photos uploaded / second



We have to handle large data sets

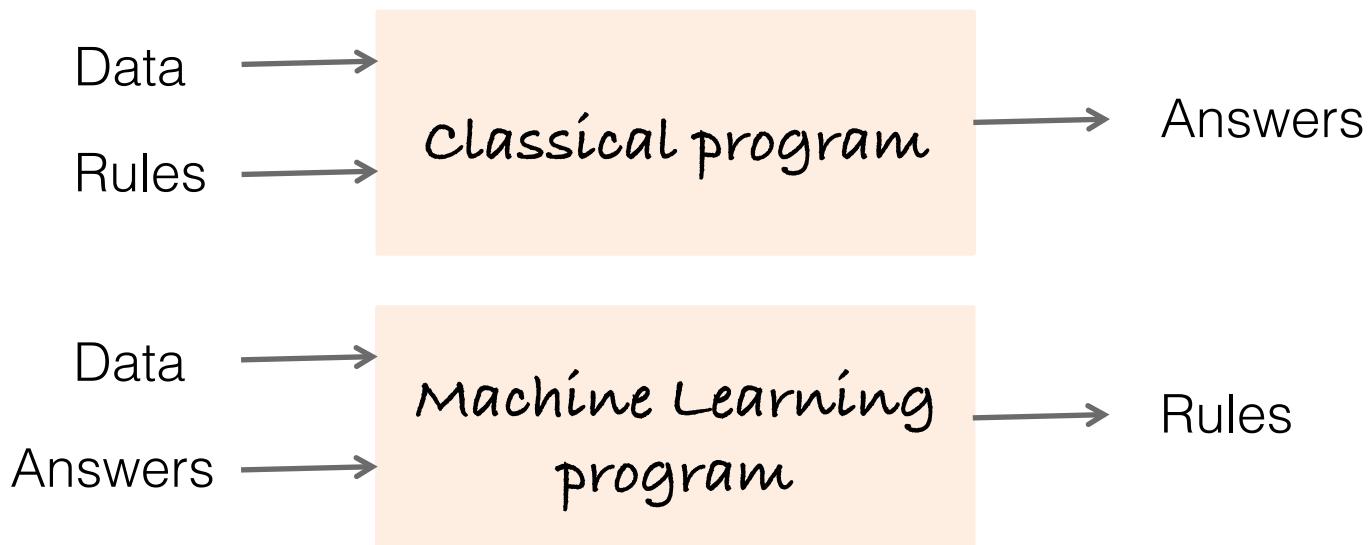


More than 2.5 million emails sent / second



Why Learning?

- There is no need to “learn” to calculate our taxes
- Learning is used when
 - Human expertise does not exist (e.g., bioinformatics)
 - Humans are unable to explain their expertise (speech recognition, computer vision)
 - Complex solutions change in time (routing computer networks)



What is Machine Learning?

- Learning systems are not directly programmed to solve a problem, instead **develop their own program** based on:
 - **Examples** of how they should behave
 - From **trial-and-error** experience trying to solve the problem
- Different than standard CS programs
 - Want to implement unknown function, only having access to sample input-output pairs (**training examples**)
- Learning simply means incorporating information from the training examples into the system

Task that Requires ML

What makes a '2'?

0 0 0 1 1 (1 1 1, 2

2 2 2 2 2 2 2 3 > 3

3 4 4 4 4 5 5 5 5

6 6 7 7 7 7 7 8 8 8

8 8 9 7 9 4 9 9 7

Why Use Learning?

- It is very hard to write programs that solve problems like recognizing a handwritten digit
 - What distinguishes a ‘2’ from a ‘7’?
 - How does our brain do it?
- Instead of writing a program by hand, we **collect examples** that specify the correct output for a given input
- A machine learning algorithm then takes these examples and produces a program that does the job
 - The program produced by the learning algorithm may look very different from a typical hand-written program
 - If we do it right, the program works for **new cases** as well as for the ones we trained it on

Learning Objectives of Today's Class

- Given a problem
 - Decide weather it can be solved with machine learning
 - Decide as what type of machine learning problem you can formalize it (unsupervised – clustering, dimensionality reduction, supervised – classification, regression?)
 - Describe it formally in terms of design matrix (observations x features), features, samples
- Define a loss function
- Model selection and evaluation in ML

More on that will follow soon

Example of ML Pipeline

- Running example: image classification
- Goal: “train a computer to recognize a cat from a dog”
- How?

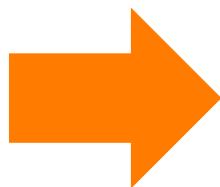


Example of ML Pipeline

- Running example: image classification
- Goal: “train a computer to recognize a cat from a dog”
- How?

Simple idea, inspired by inductive human learning

Show it a lot of
labeled examples



“predicts” the right
label on unseen data

From This

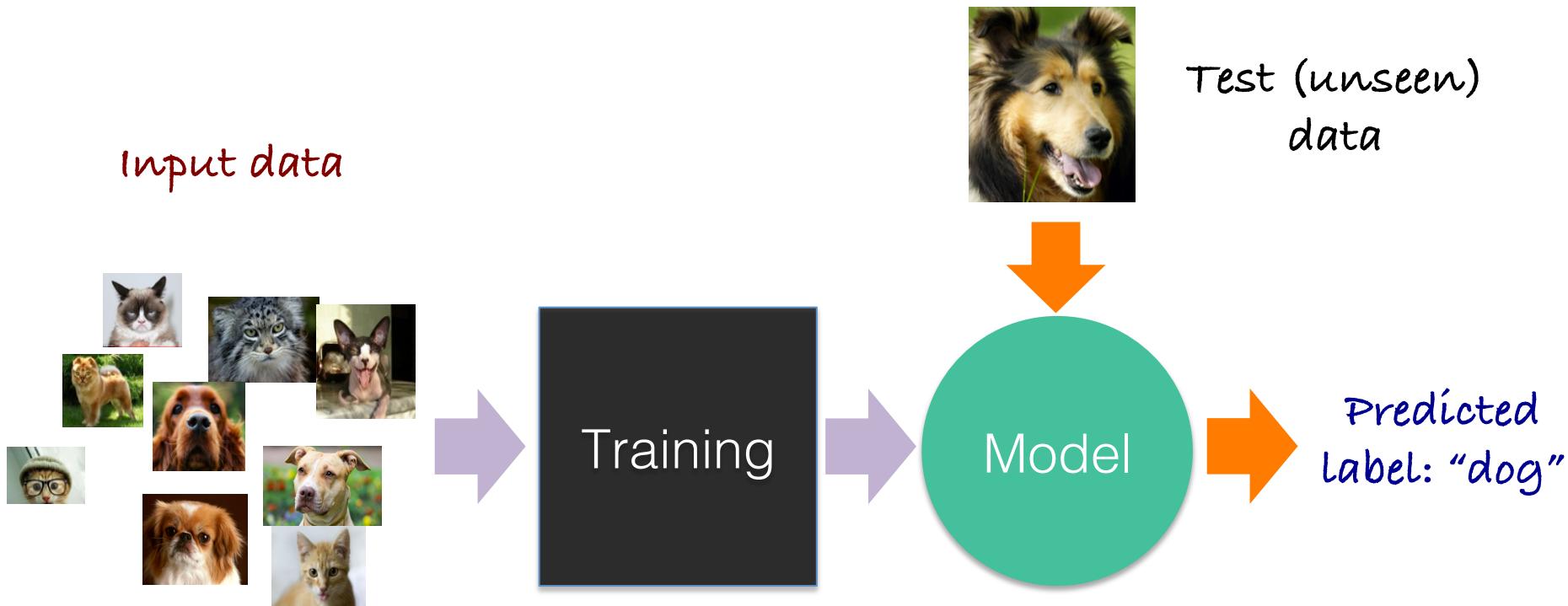


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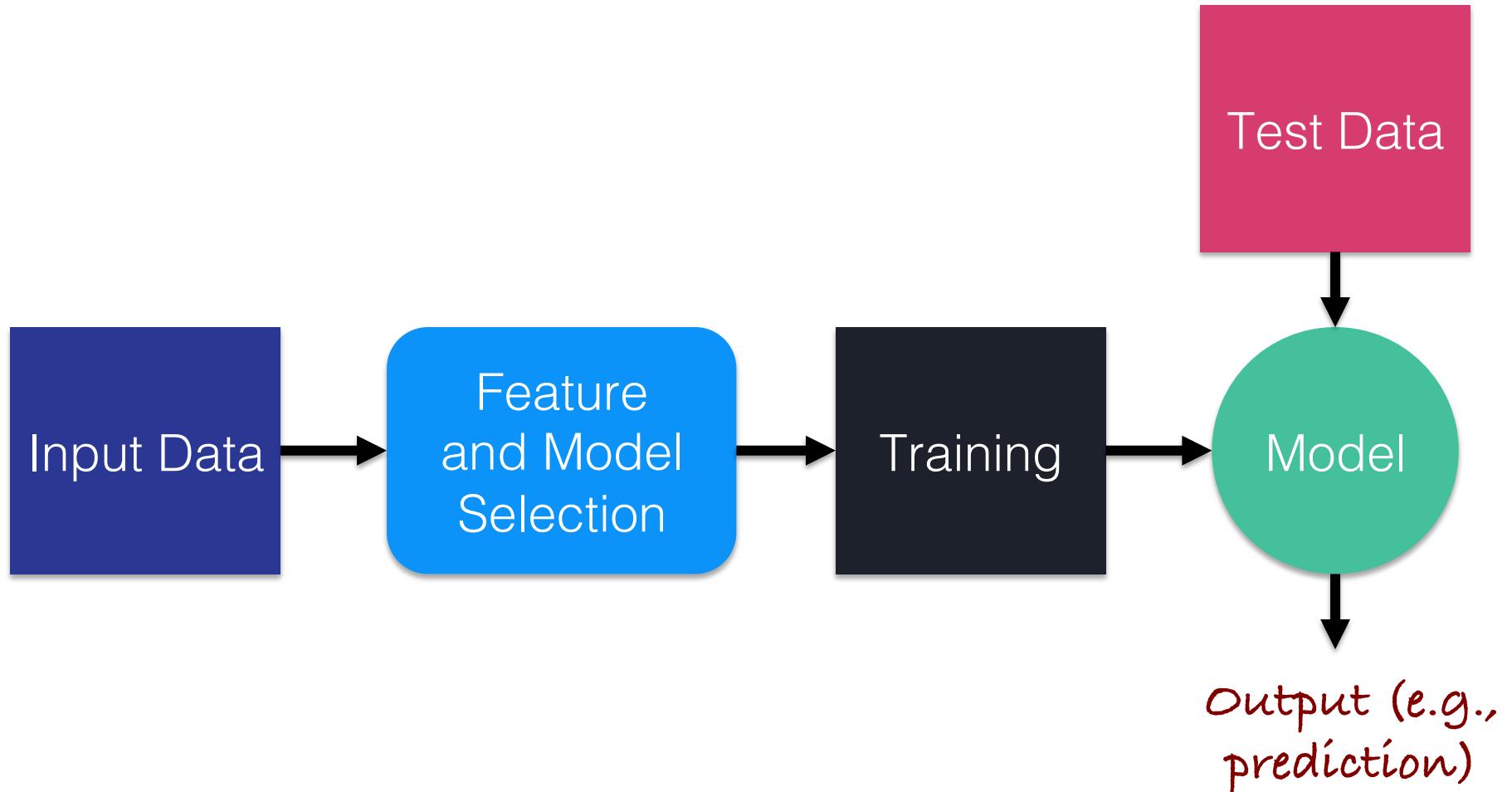


Example of ML Pipeline

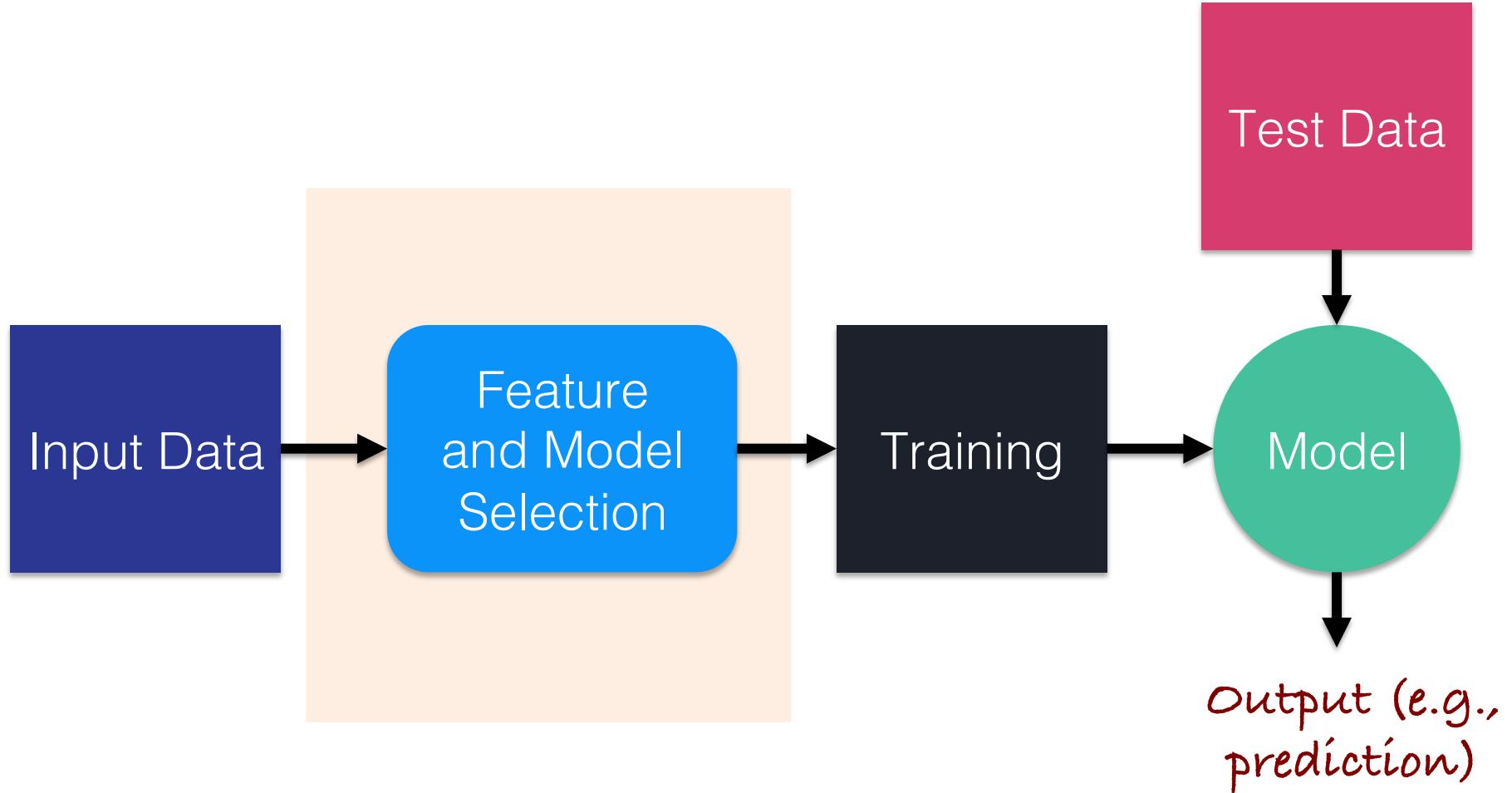
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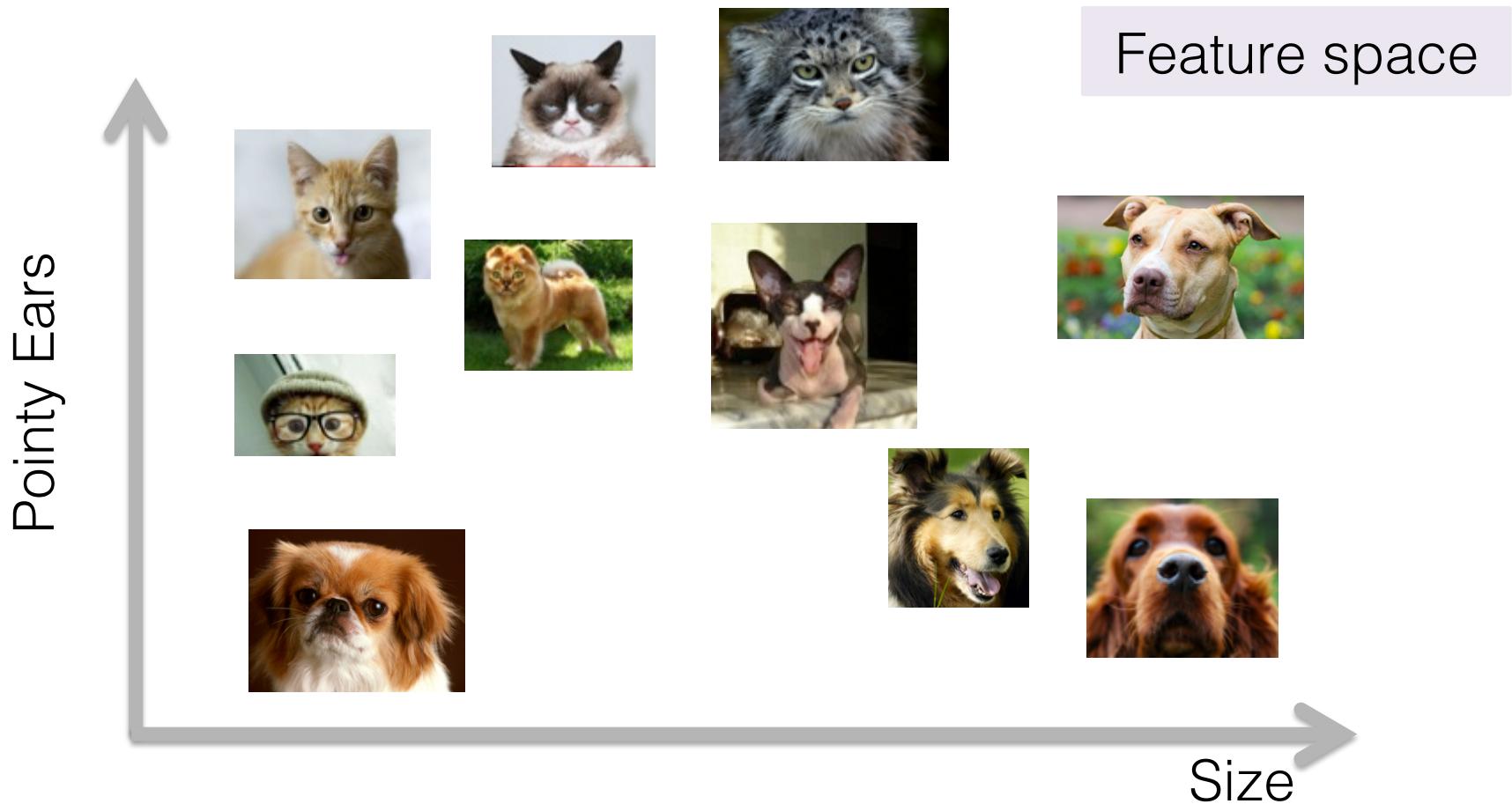
ML Pipeline



ML Pipeline

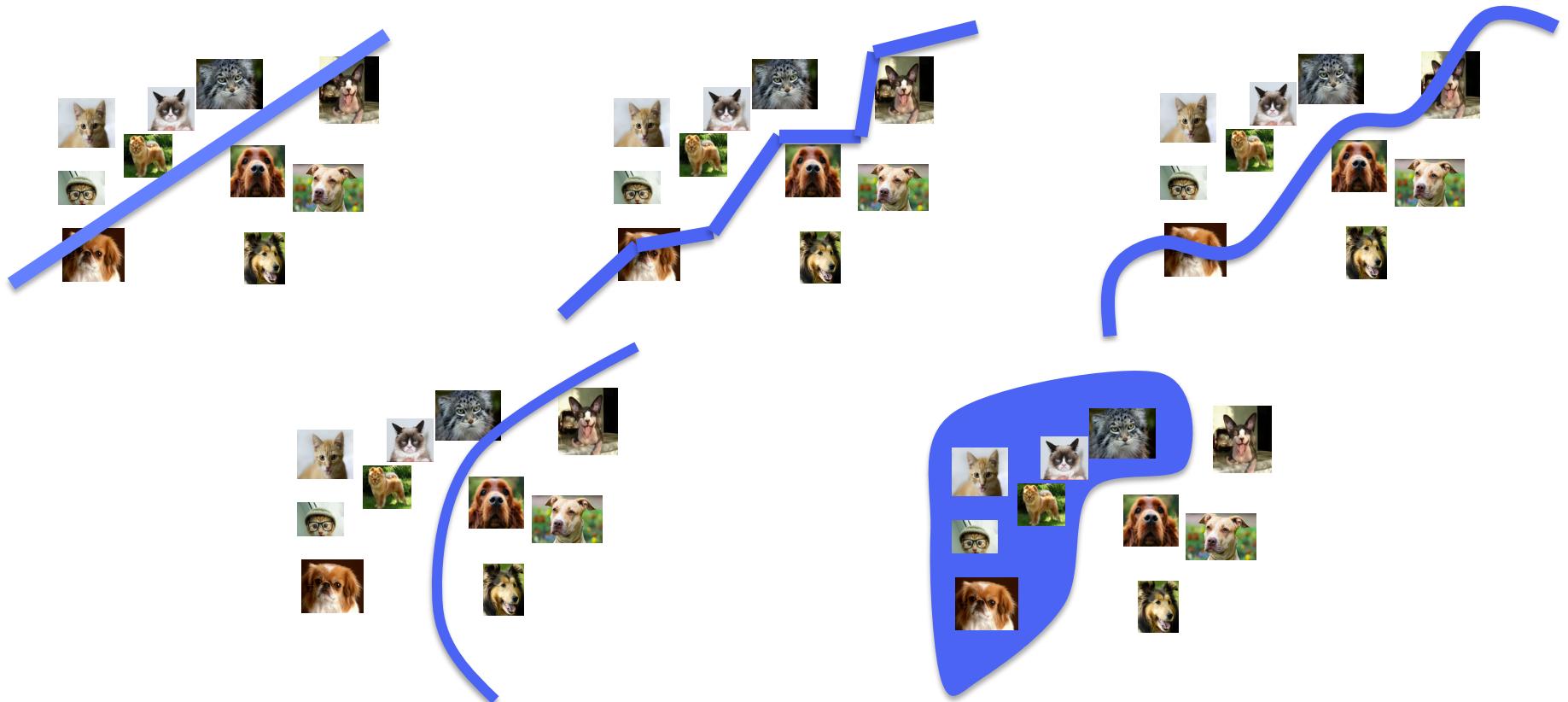


Feature Selection



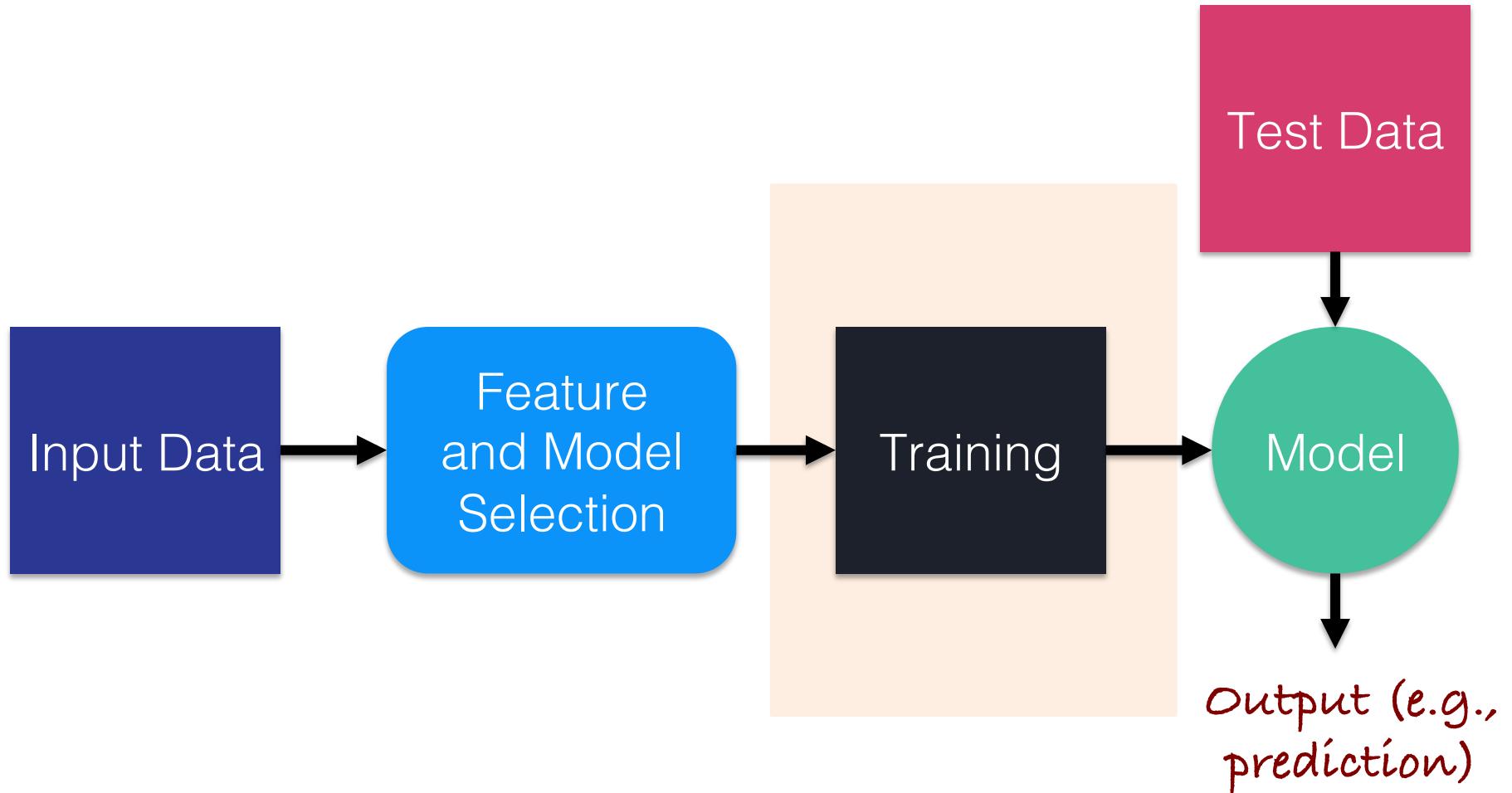
Goal: Use “informative” features

Choose your Predictor (Hypothesis Class)



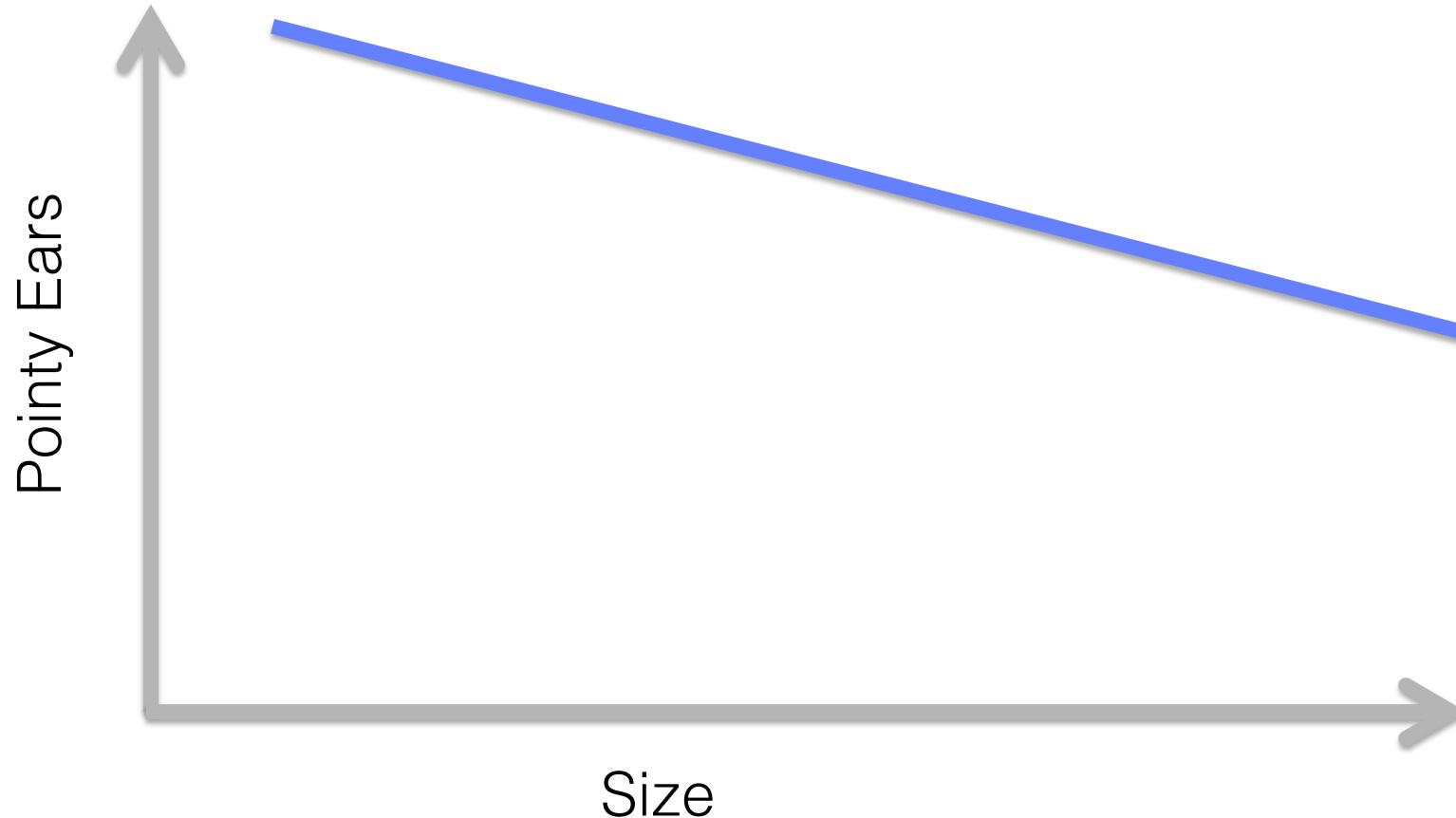
Goal: Pick a predictor that is
1) expressive 2) easy to train 3) doesn't overfit

ML Pipeline



Then, Train the Model

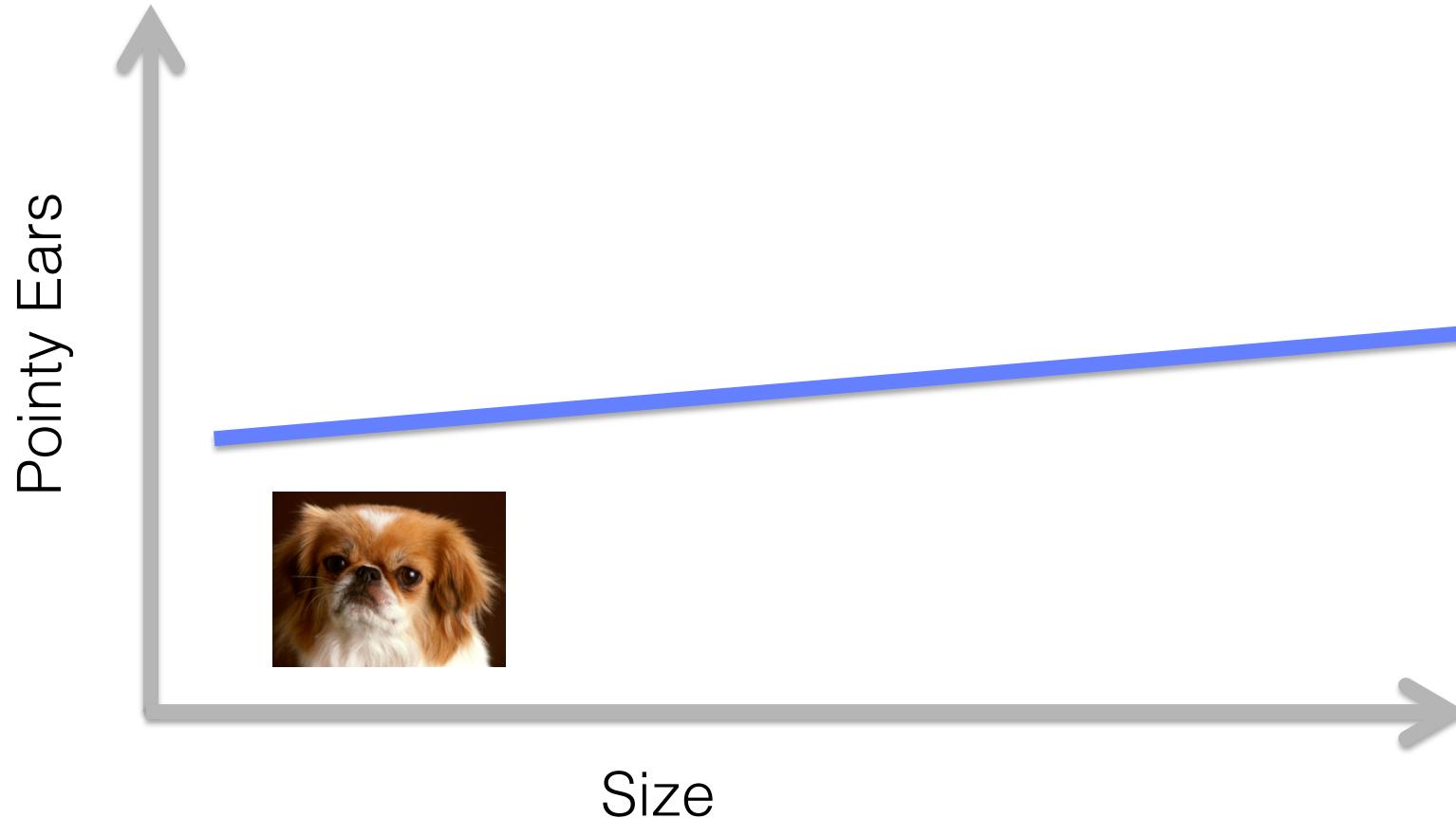
Feature space



Goal: Train a model to minimize training error

Then, Train the Model

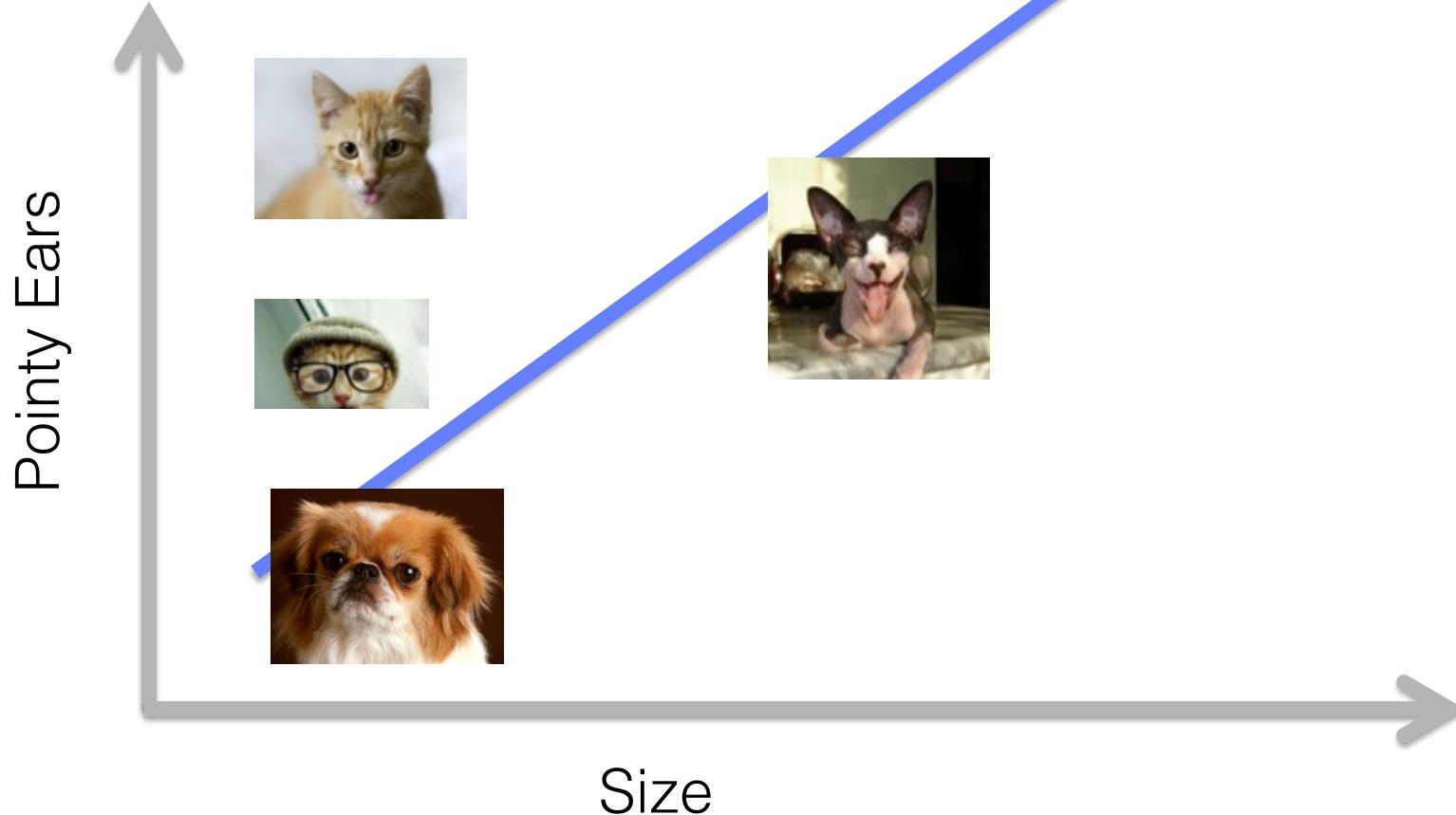
Feature space



Goal: Train a model to minimize training error

Then, Train the Model

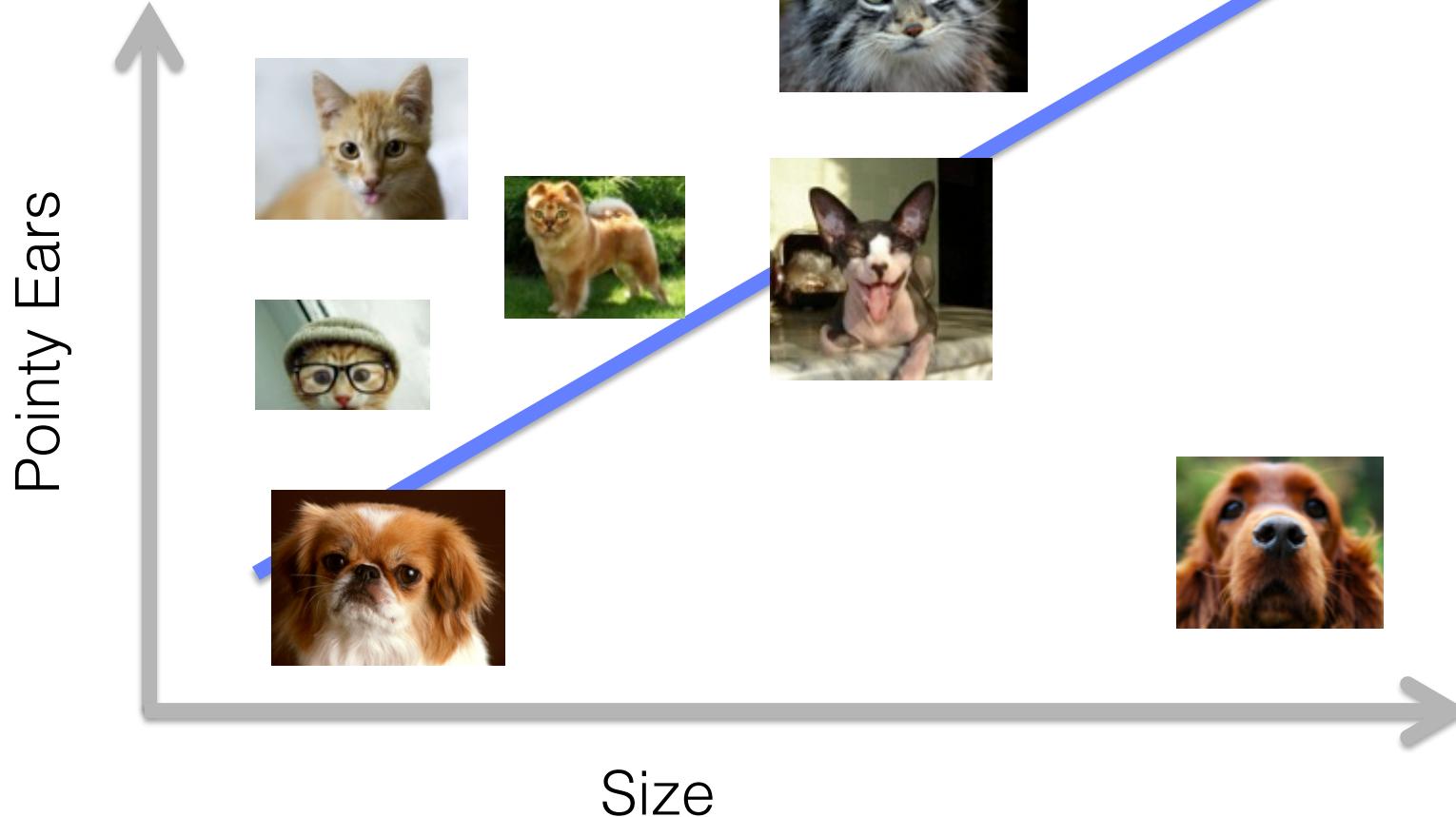
Feature space



Goal: Train a model to minimize training error

Then, Train the Model

Feature space

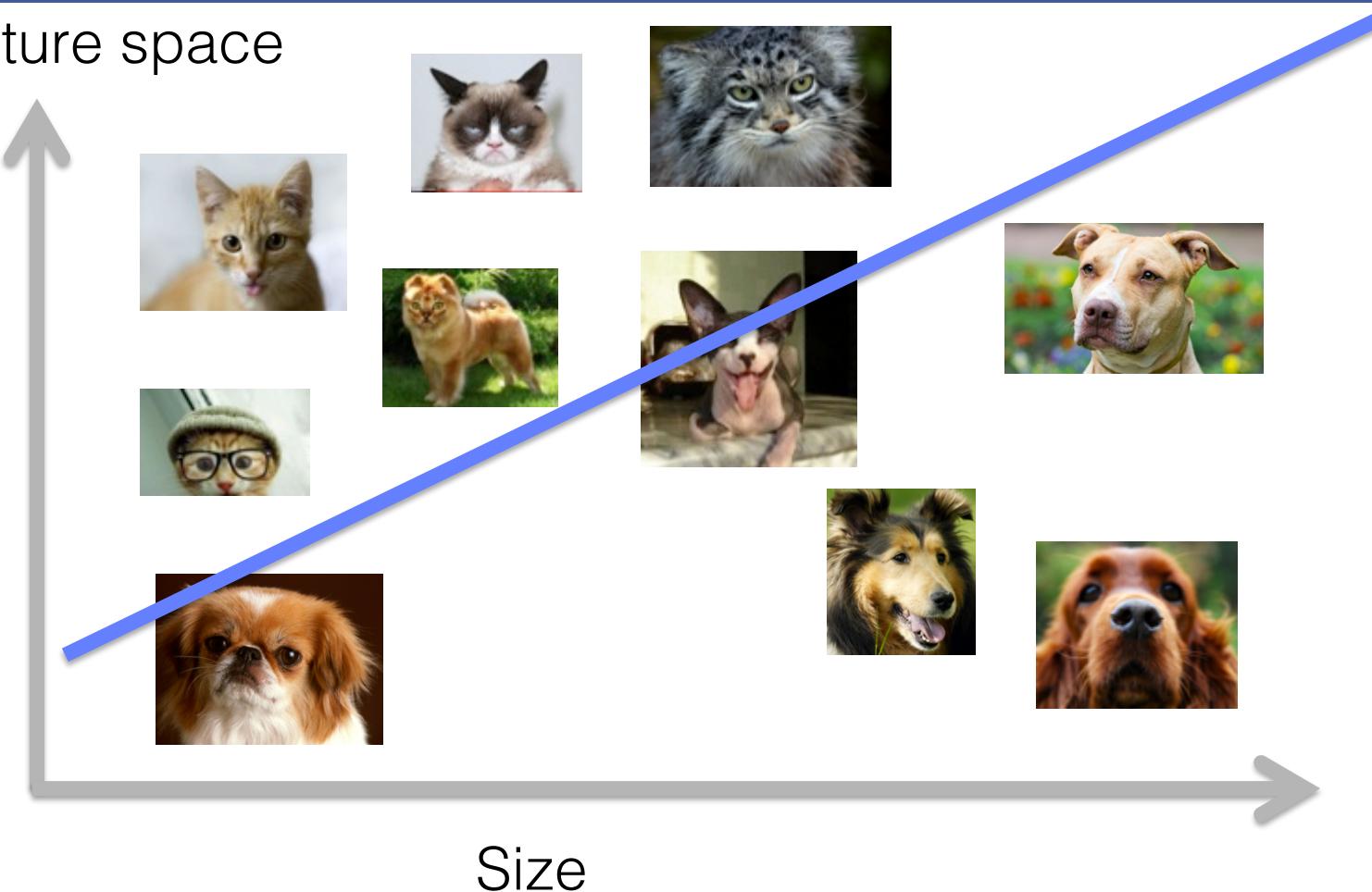


Goal: Train a model to minimize training error

Then, Train the Model

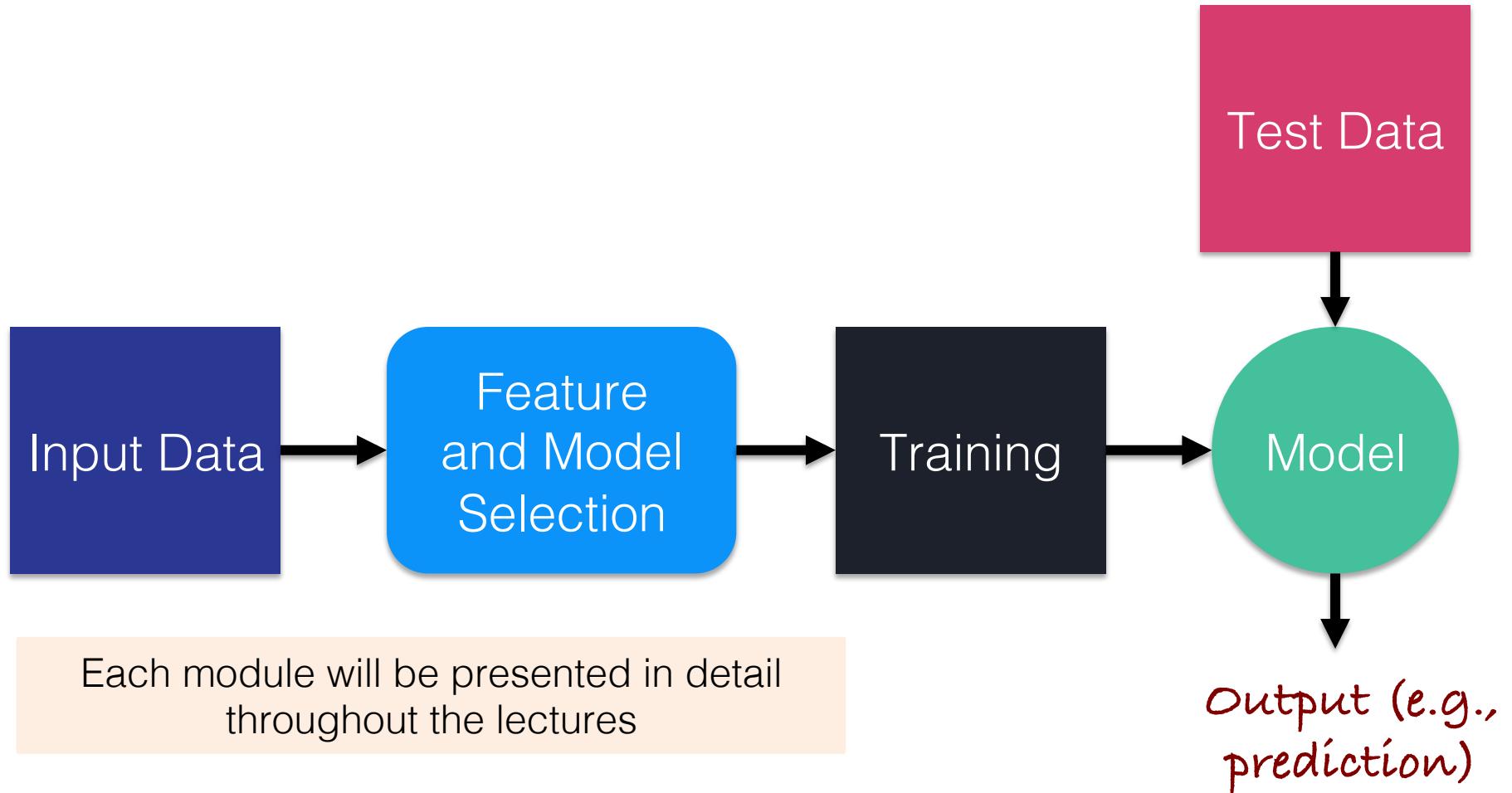
Feature space

Pointy Ears



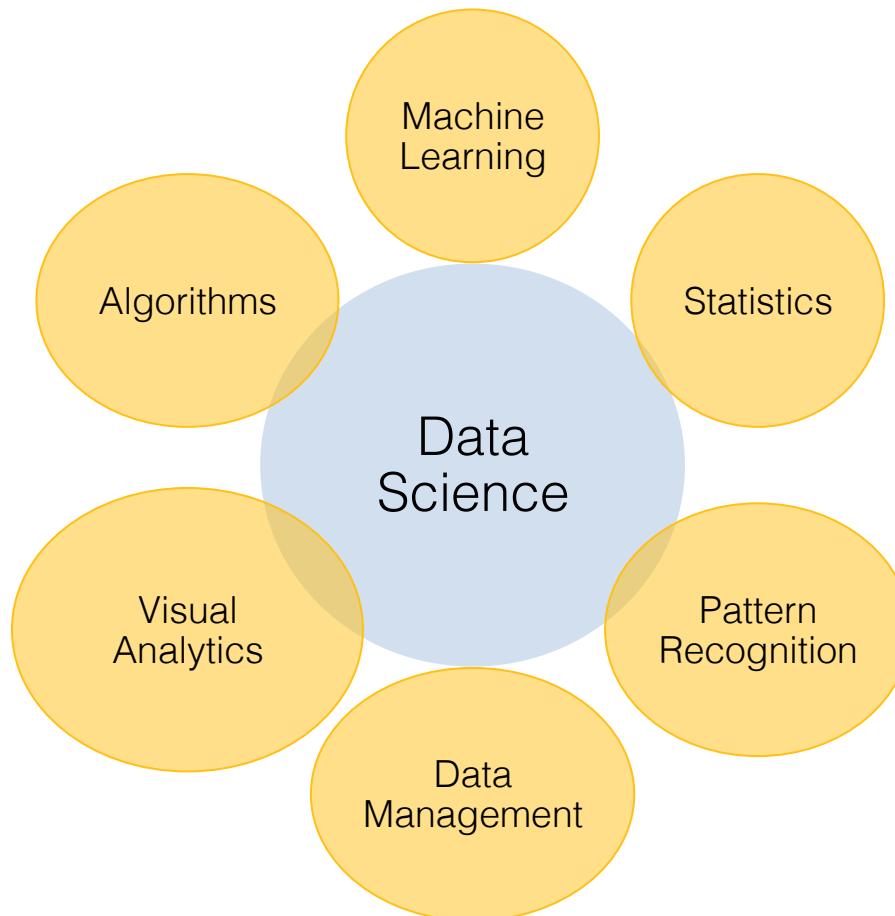
Goal: Train a model to minimize training error

ML Pipeline



Questions?

Data Science: The Big Picture



About this course

Learning Objectives

- By the end of the course, you will be able to
 - Identify problems that can be solved by machine learning
 - Formulate your problem in machine learning terms
 - Given such a problem, identify and apply the most appropriate classical algorithm(s)
 - Implement some of those algorithms by yourself
 - Evaluate and compare machine learning algorithms for a particular task
 - Deal with real-world data challenges

Prerequisites

- Basic knowledge of
 - Probability theory and statistics
 - Linear algebra
 - Algorithms
- We will review the main background concepts
- Programming is necessary
 - Python (or any other language of your preference)
 - We will deal with real-world ML tasks

Structure of the Course

Three components:

1. Lectures
 - First half of each session
2. Lab sessions
 - Hands-on experience on ML algorithms
 - Some of the algorithms will be implemented from scratch
 - Need to install software and to experiment in class
 - Labs will not be graded, but will help you to further understand the material presented in the lectures
3. Assignments and project

Coursework and Grading

	Weight	Details
Assignment 1 (individual)	15%	<ul style="list-style-type: none">• Theoretical questions• Some of them may also require some programming in order to perform some tasks• <i>Lecture 2 (out) – Lecture 4 (due)</i>
Assignment 2 (teams of 3-4 students)	35%	<ul style="list-style-type: none">• Deal with a real machine learning task• Kaggle competition• Deliver short report and code• <i>Lecture 4 (out) – Lecture 7 (due)</i>
Project (teams of 3-4 students)	50%	<ul style="list-style-type: none">• Project proposal (2-pages, mandatory)• Final report and code• Presentation in class• <i>Proposal due: Lecture 3; Final report due: Lecture 9</i>

- Small adjustments may be done in the weights of the coursework
- A detailed description of the project will be provided soon
- The exact dates will be posted on the website of the course (subject to change)

Goals of the Different Course Components

- Understand the basics behind ML algorithms and get comfortable working with data and tools [Lab sessions]
- Comprehend the foundational material and the motivation behind different techniques [Assignment 1]
- Build something that actually works [Assignment 2]
- Apply your knowledge creatively [Project]

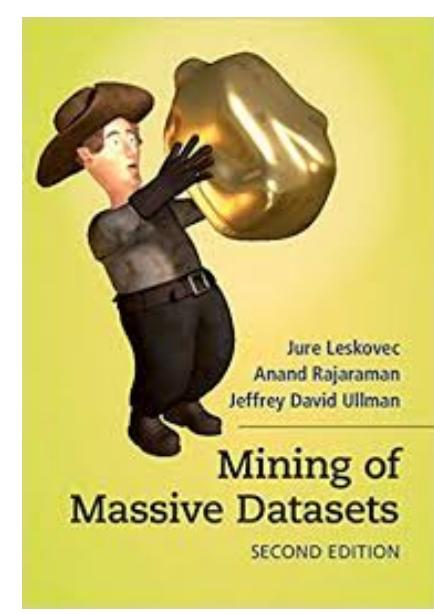
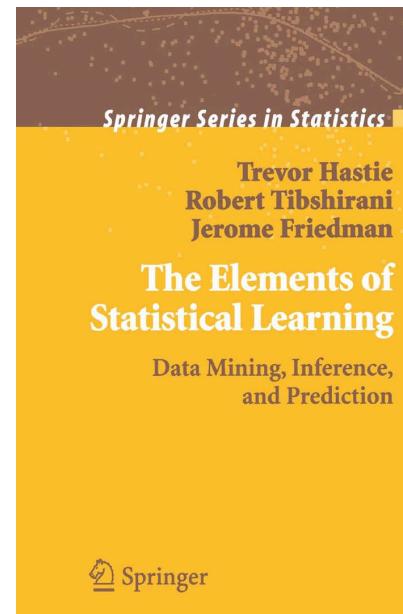
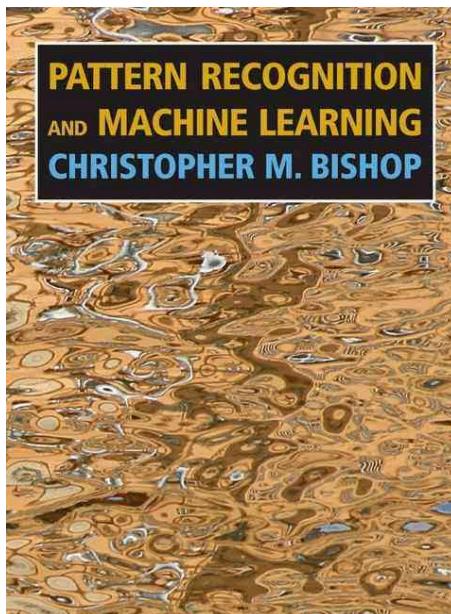
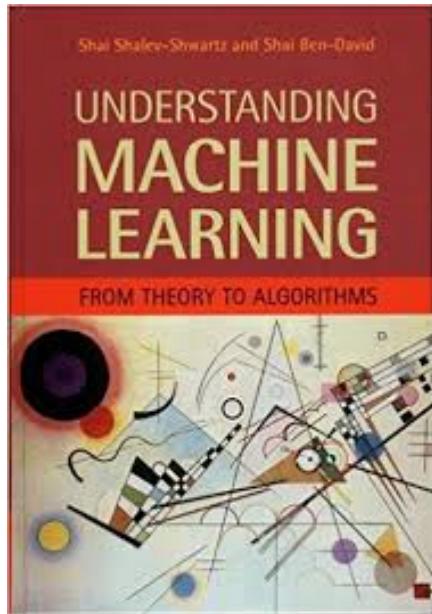
Software Tools

- We strongly advise to use **Python**
 - numpy
 - scipy
 - scikit-learn
 - pandas
 - ...
 - **anaconda** includes almost all packages that will be needed
- Python will be used in the lab sessions
- See the **Resources** section of the website

Course Logistics

- Website
 - <http://fragkiskos.me/teaching/ML-F19/>
 - Information about the course, schedule, reading material
 - Resources (helpful for the assignment and project)
- Piazza for Q&A and material
 - <https://piazza.com/centralesupelec/fall2019/mlsbaai/>
 - Please, participate and help each other!
 - All announcements will be posted there
 - Also, lecture slides and assignments
 - Use key to enroll: **ml-2019**

Reading Material



- The books are publicly available in electronic form
 - Pointers to chapters for every lecture (see the website)
- Additional resources for every lecture will be given in the website of the course

Some Personal Notes 😊

- Please ask questions, participate in discussions on piazza
- Check out the additional suggested material on the website
 - Search the web, google is your friend!
 - For every topic covered in the class, you can find material in textbooks or even in the web
 - Typically, the suggested reading material is overlapping – read selectively
- Play with software tools. Apply what you've learnt in theory
 - This is the actual goal of the lab sessions, assignments and the project
- Give us your feedback!

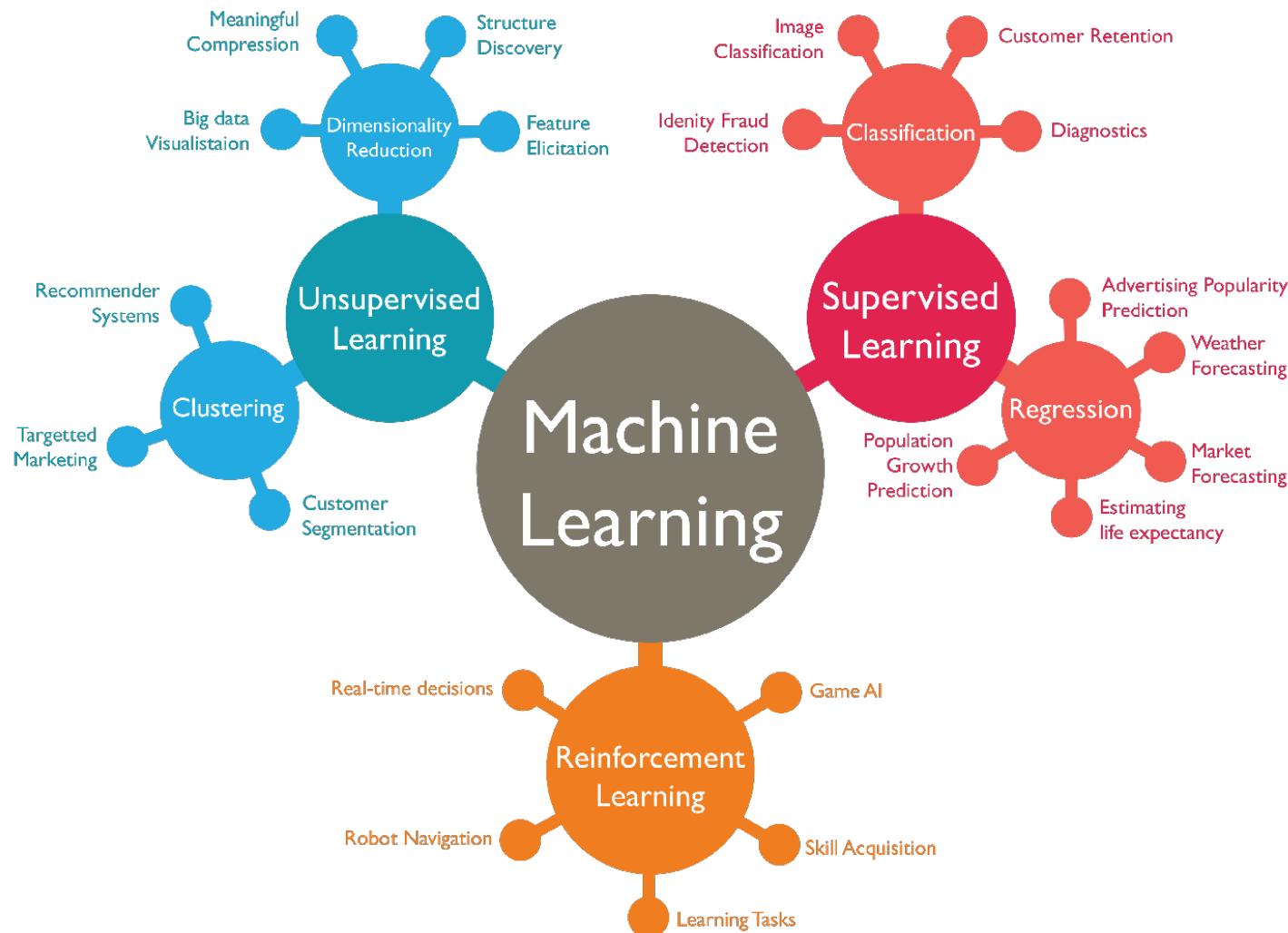
Topics that will be covered

Schedule (Subject to Change)

<http://fragkiskos.me/teaching/ML-F19/>

Date	Topic	Material	Assignments/Project
1	October 9	Introduction; Model selection and evaluation	Lecture 1
2	October 16	Dimensionality reduction	Assignment 1 out
4	October 23	Linear and logistic regression	Project proposal due on October 27
5	October 30	Probabilistic classifiers and linear discriminant analysis	Assignment 1 due on November 3 Assignment 2 out
6	November 6	Non-parametric learning and nearest neighbor methods	
7	November 14	Tree-based methods and ensemble learning	
8	November 21	Support Vector Machines	Assignment 2 due on November 24
9	November 28	Unsupervised learning: clustering	
10	December 5	Project presentations	Project final report due

ML Models and Applications



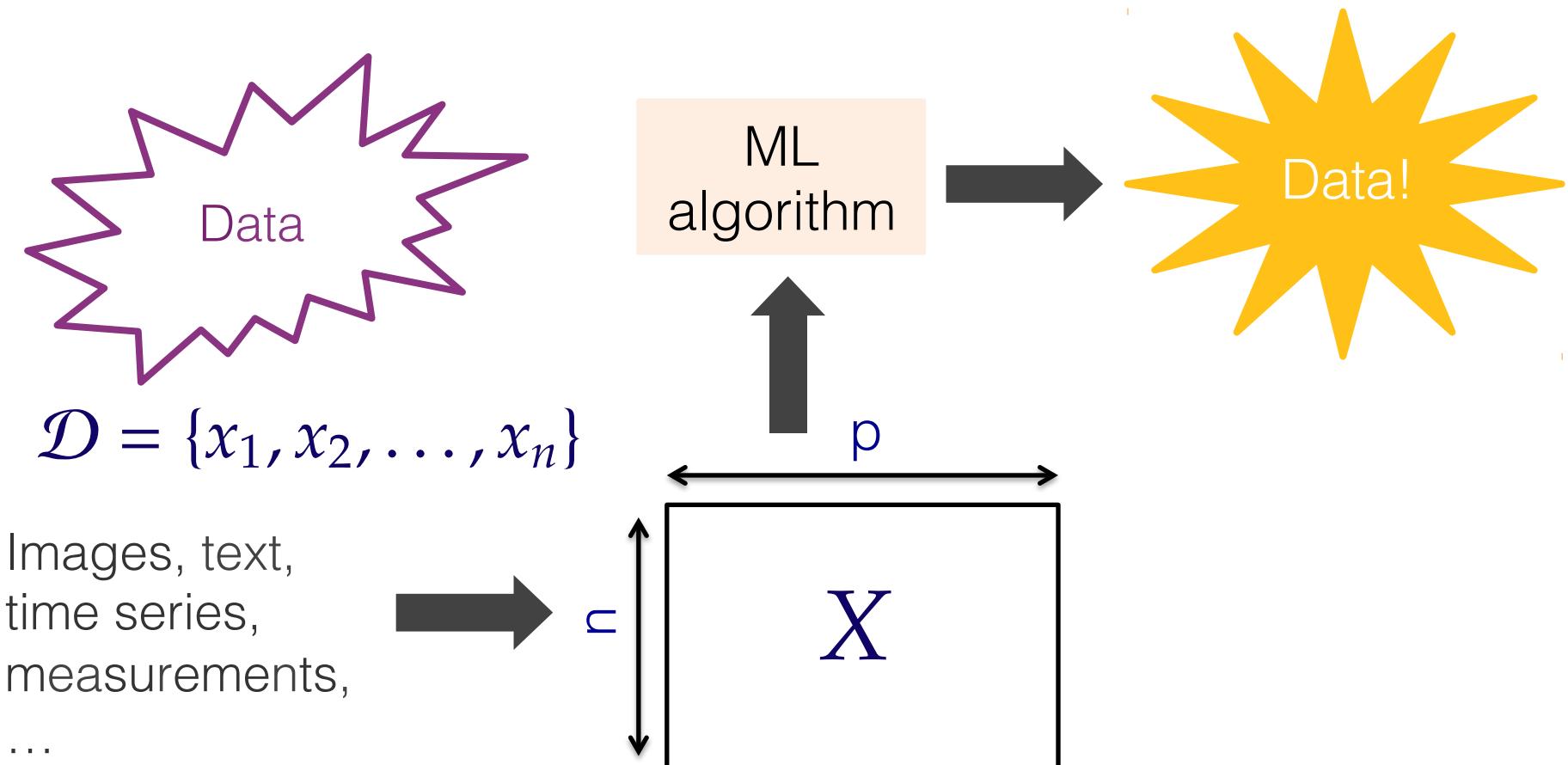
Schedule (Subject to Change)

1. Introduction. Overview of ML problems. Model evaluation and selection. Overfitting and regularization
2. Dimensionality reduction. Feature selection. Principal Component Analysis (PCA).
3. Linear and logistic regression
4. Probabilistic classifiers. Linear Discriminant Analysis (LDA)
5. Non-parametric learning. K-Nearest Neighbors
6. Tree-based methods. Ensemble methods. Boosting. Random forests
7. Support Vector Machines (SVMs)
8. Unsupervised learning. Data Clustering

Over 8 lectures

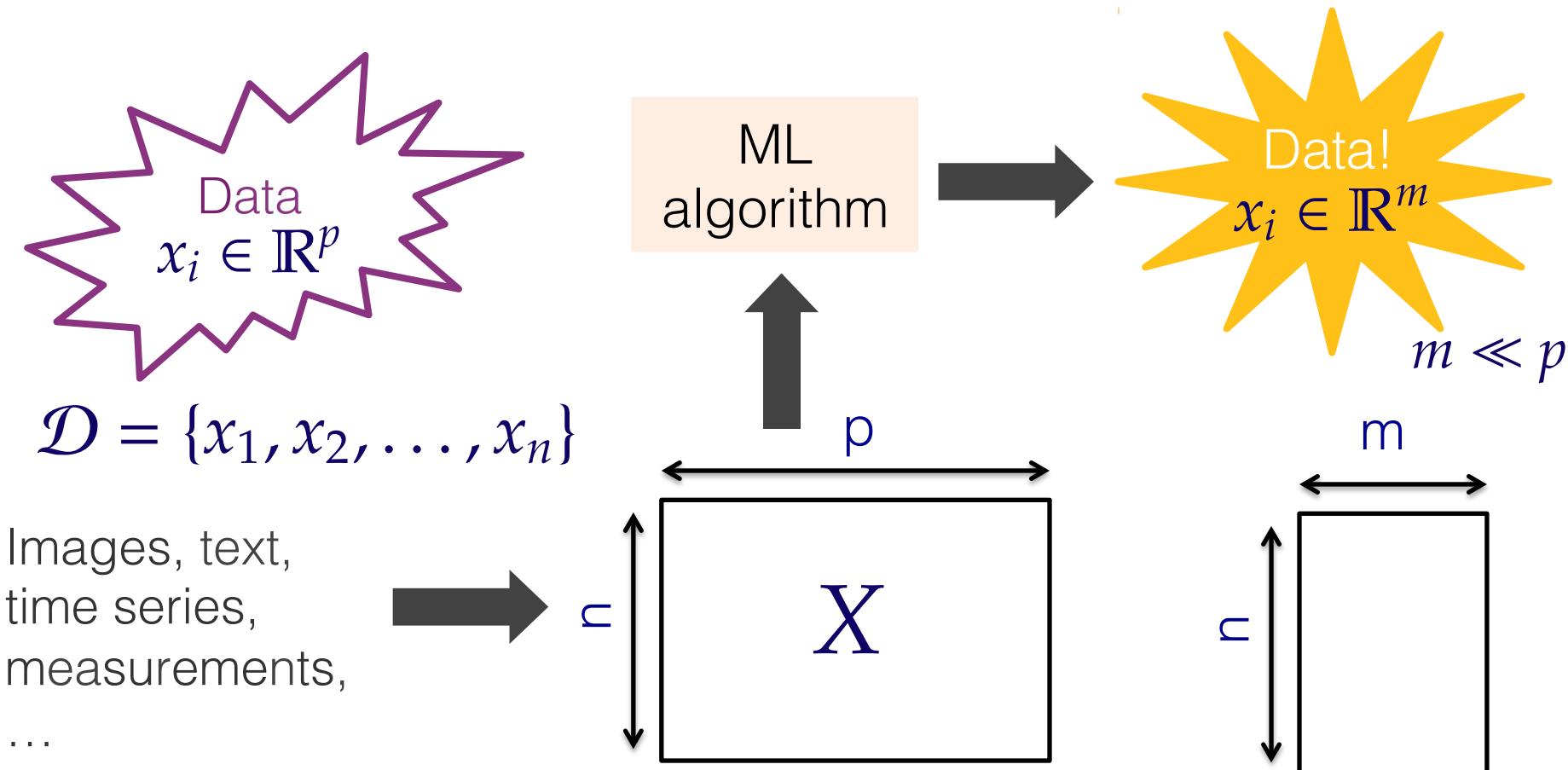
Unsupervised Learning

Learn a new representation of the data



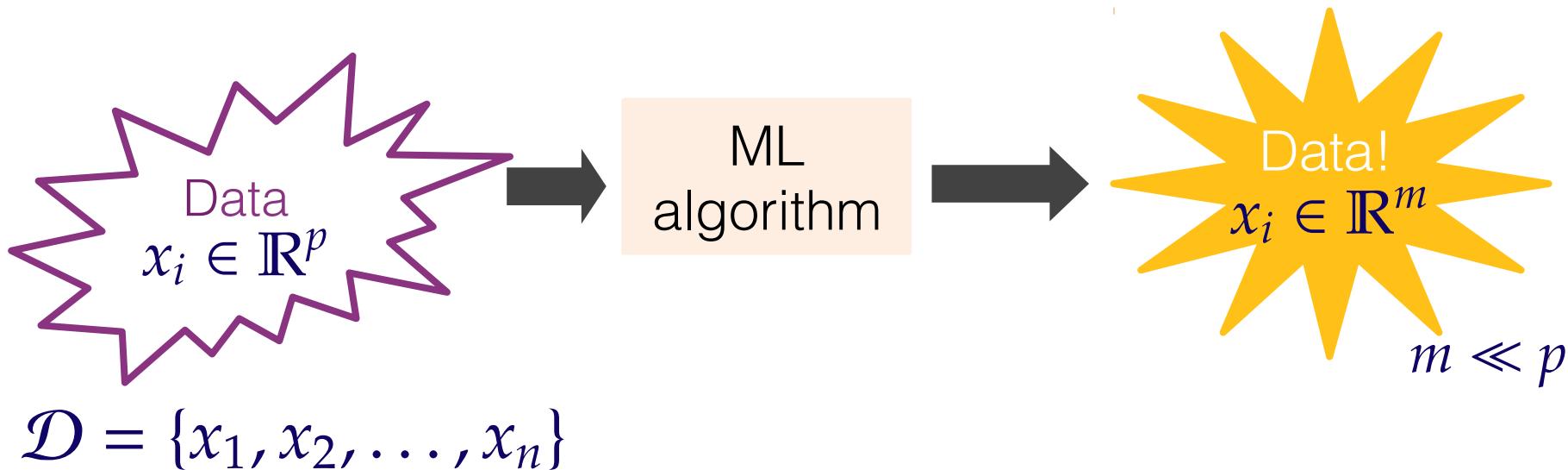
Dimensionality Reduction (1/2)

Find a lower-dimensional representation



Dimensionality Reduction (2/2)

Find a lower-dimensional representation

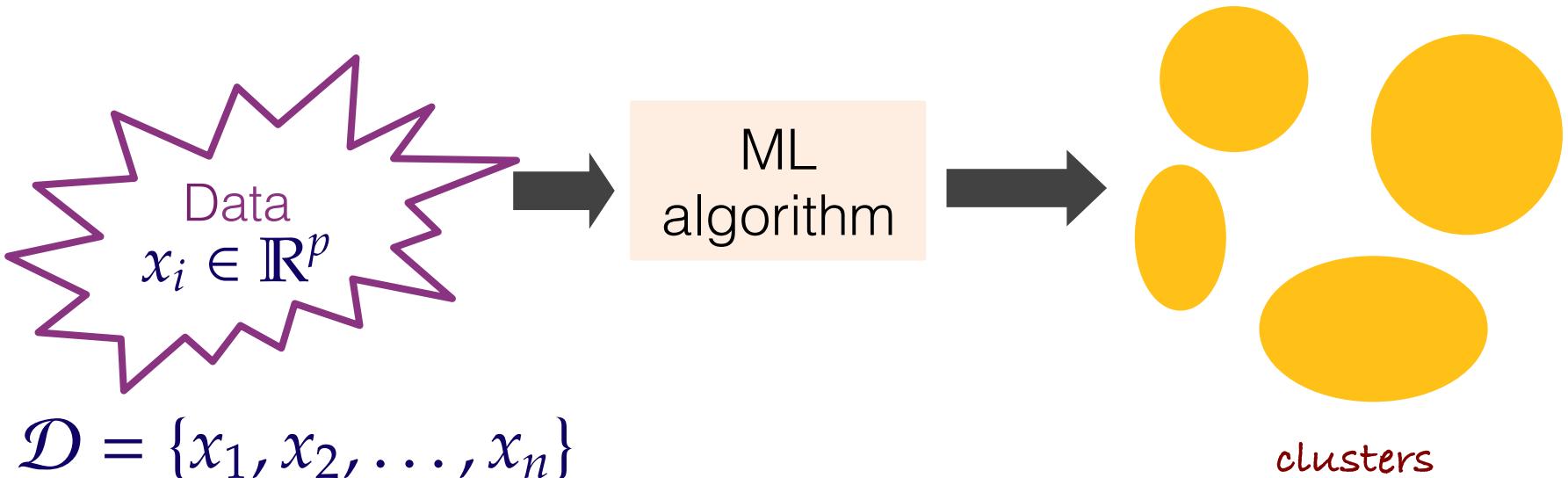


why dimensionality reduction is useful?

- Reduce storage space and computational time
- Remove redundancies
- Curse of dimensionality
- Visualization (in 2 or 3 dimensions) and interpretability

Data Clustering

Group **similar** data points together



- Understand **general characteristics** of the data
- Infer some properties of an object based on how it relates to other objects
- Problems that can be solved by clustering?

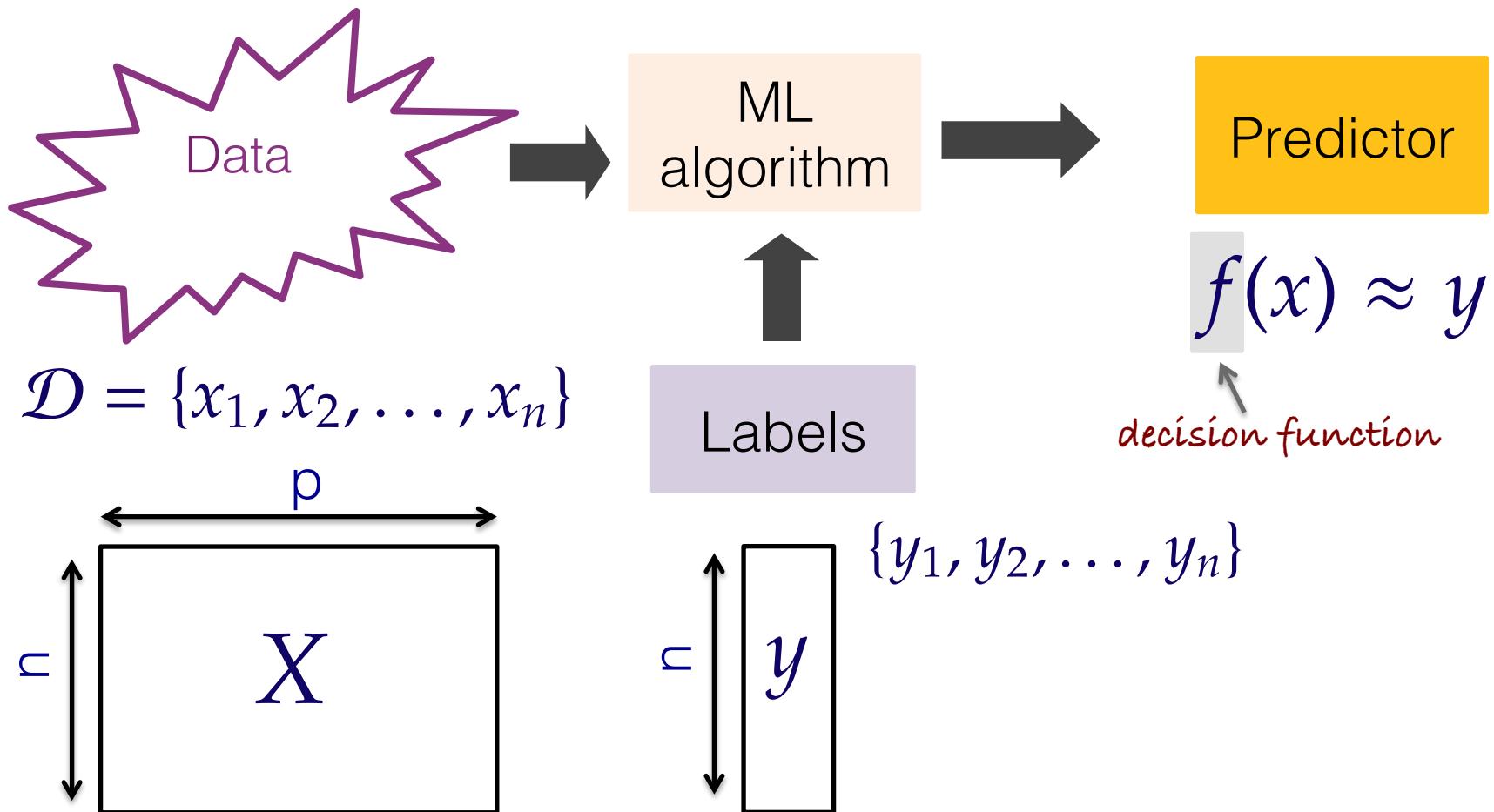
Data Clustering – Applications

- Customer segmentation
 - Find groups of customers with similar buying behavior
- Topic modeling
 - Group documents based on the words they contain to identify common topics
- Image compression and segmentation
 - Find groups of similar pixels that can easily be summarized
- Disease subtyping (e.g., cancer, mental health)
 - Find groups of patients with similar pathologies (at the molecular or symptoms level)
- Community detection in networks
 - Communities of similar users in social networks
- ...

Can you think any inherent difficulty in the clustering task?

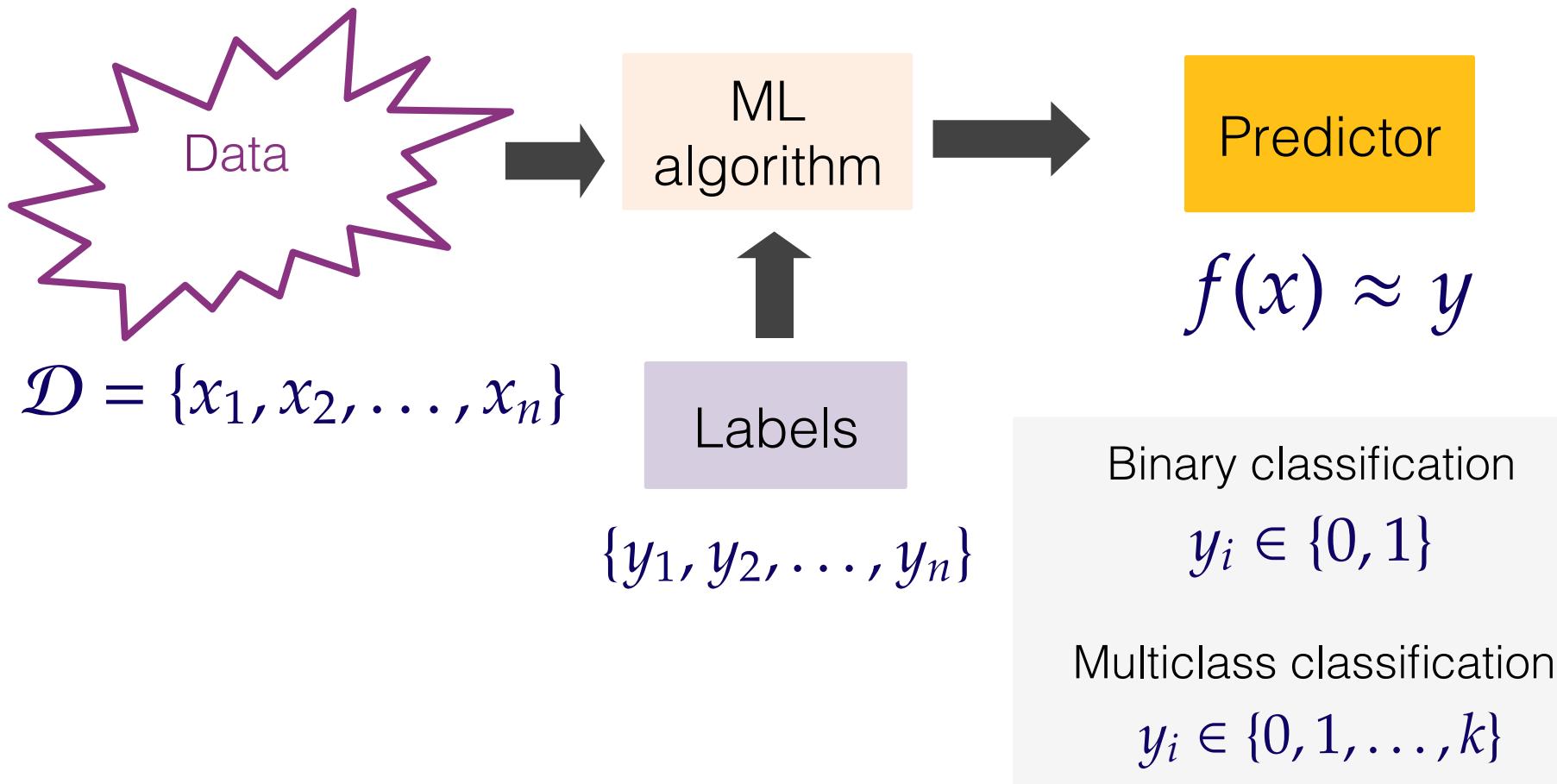
Supervised Learning

Make predictions

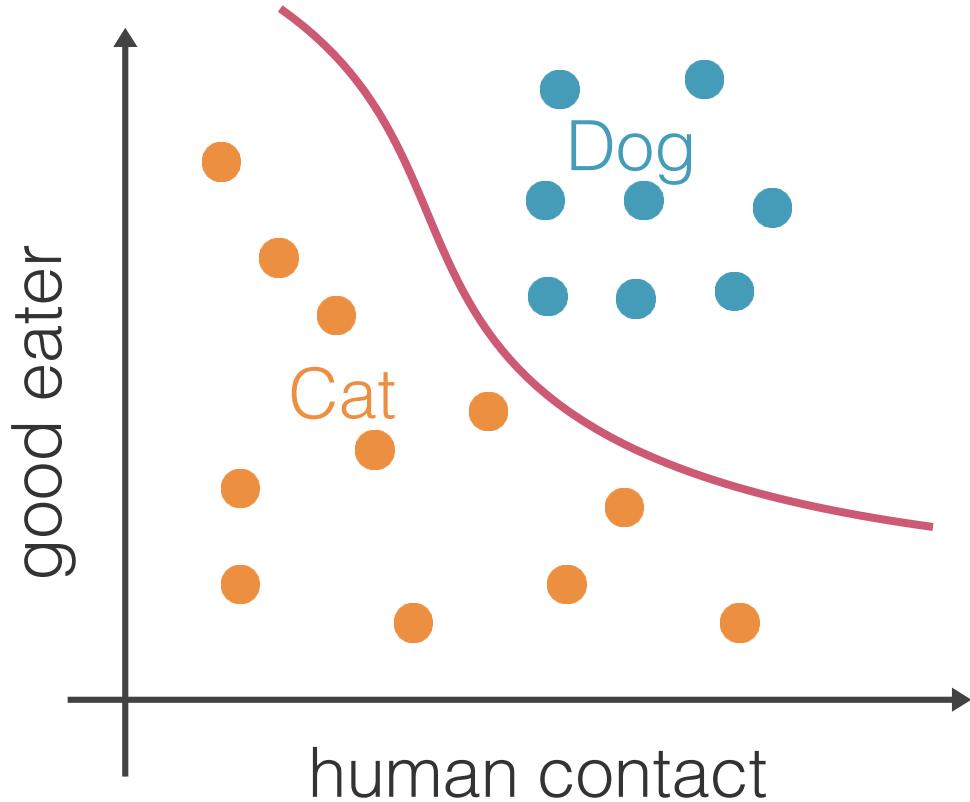


Classification (1/2)

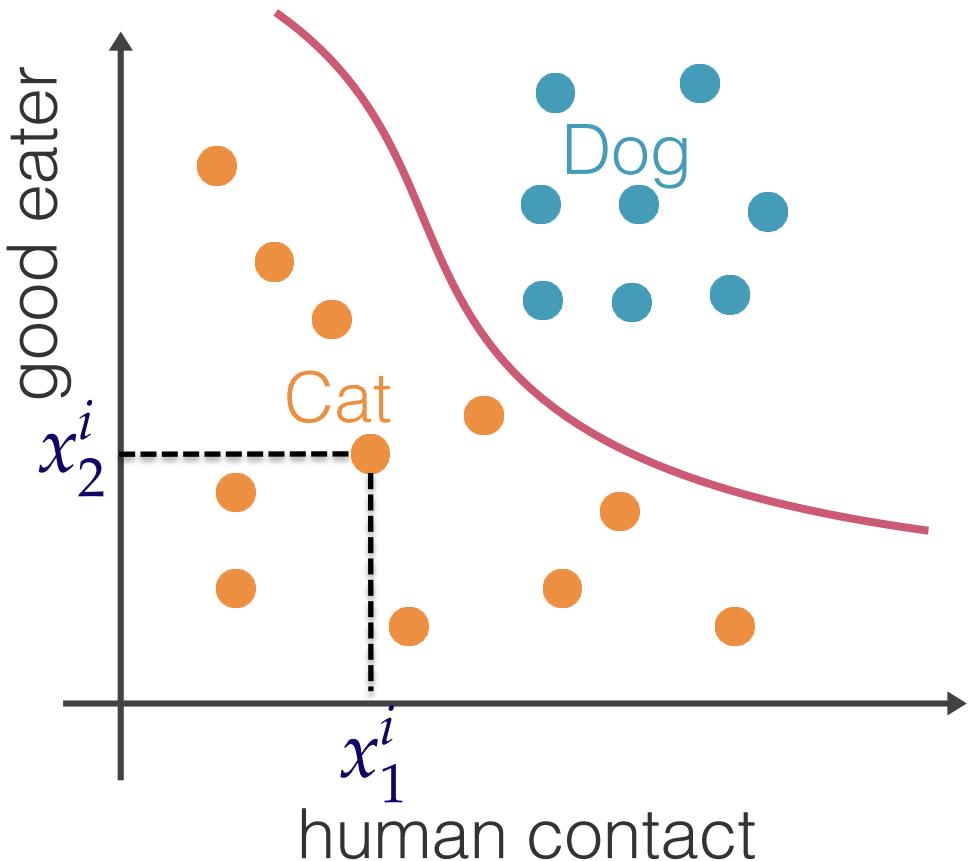
Make discrete predictions



Classification (2/2)



Training Set \mathcal{D}



$$\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$$

$$y_i = \begin{cases} 1 & \text{if } x^i \in \mathcal{P} \\ -1 & \text{if } x^i \in \mathcal{N} \end{cases}$$

$$x^i = \begin{pmatrix} x_1^i \\ x_2^i \end{pmatrix}$$

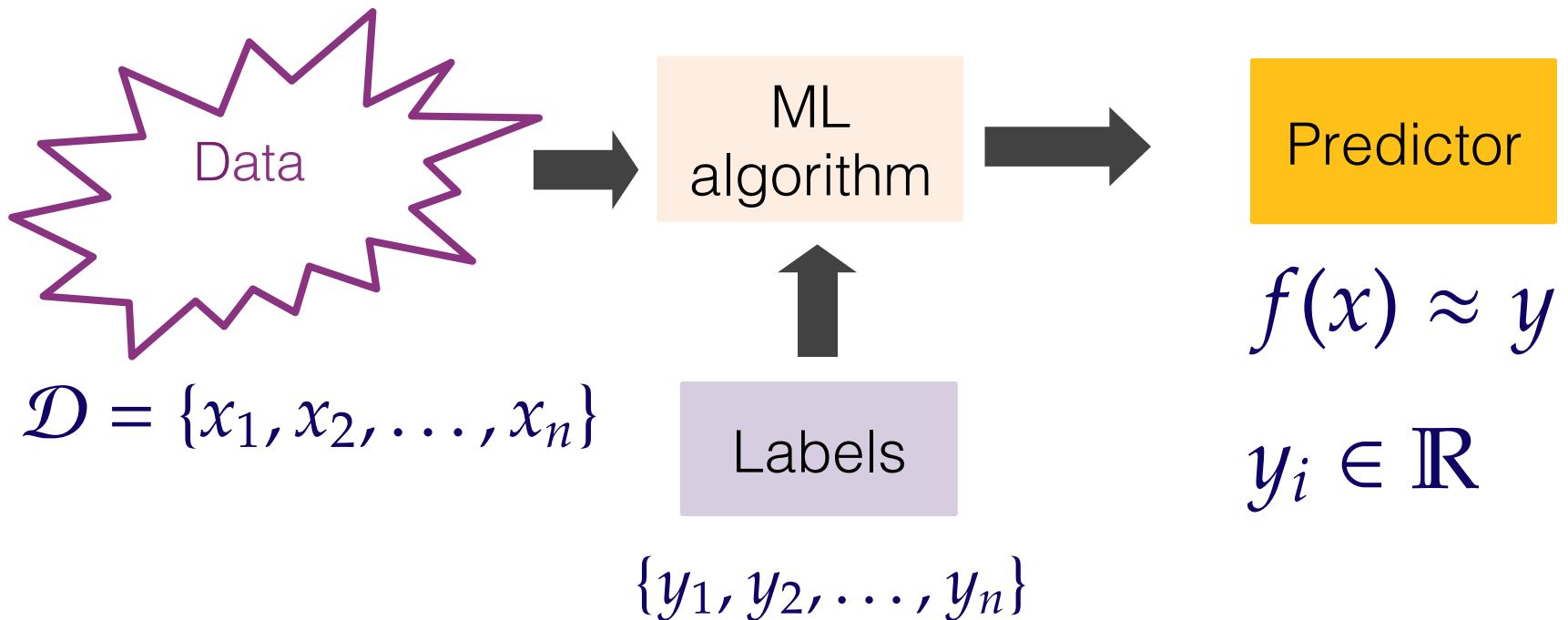
Given $\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$ find \mathbf{f} such that $f(x) \approx y$

Classification – Applications

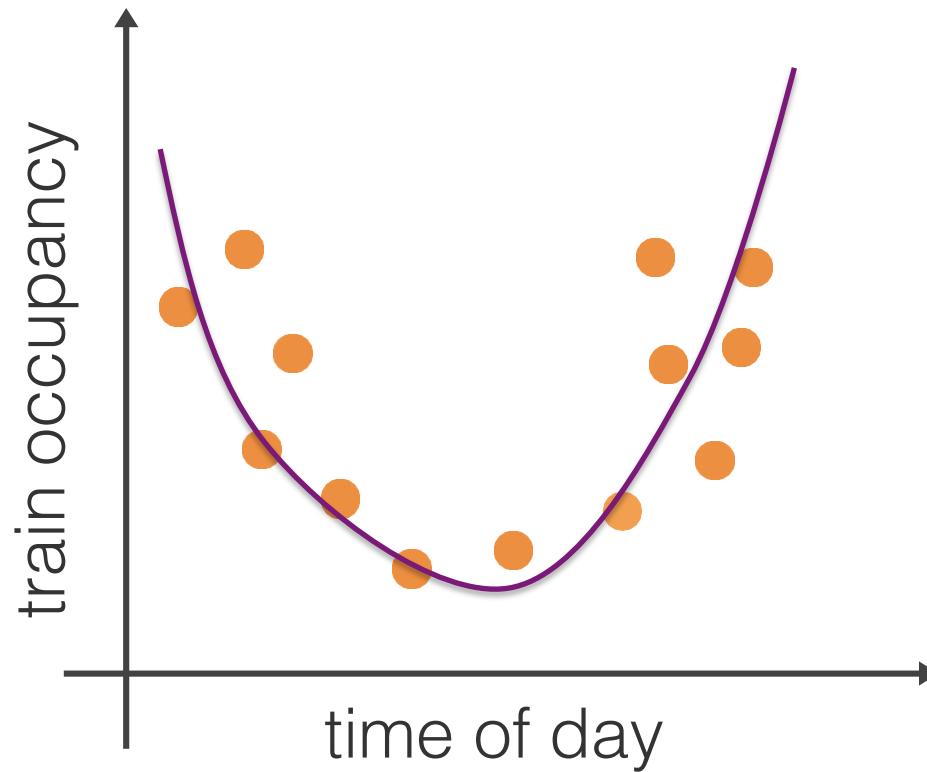
- Face recognition
 - Identify faces independently of pose, lighting, occlusion (glasses, beard), make-up, hair style
- Self-driving cars. How?
- Character recognition
 - Read letters or digits independently of different handwriting styles
- Sound recognition
 - Which language is spoken? Who wrote this music? What type of bird is this?
- Spam detection. Any spam application that you may know?
- Precision medicine
 - Does this sample come from a sick or healthy person? Will this drug work on this patient?

Regression (1/3)

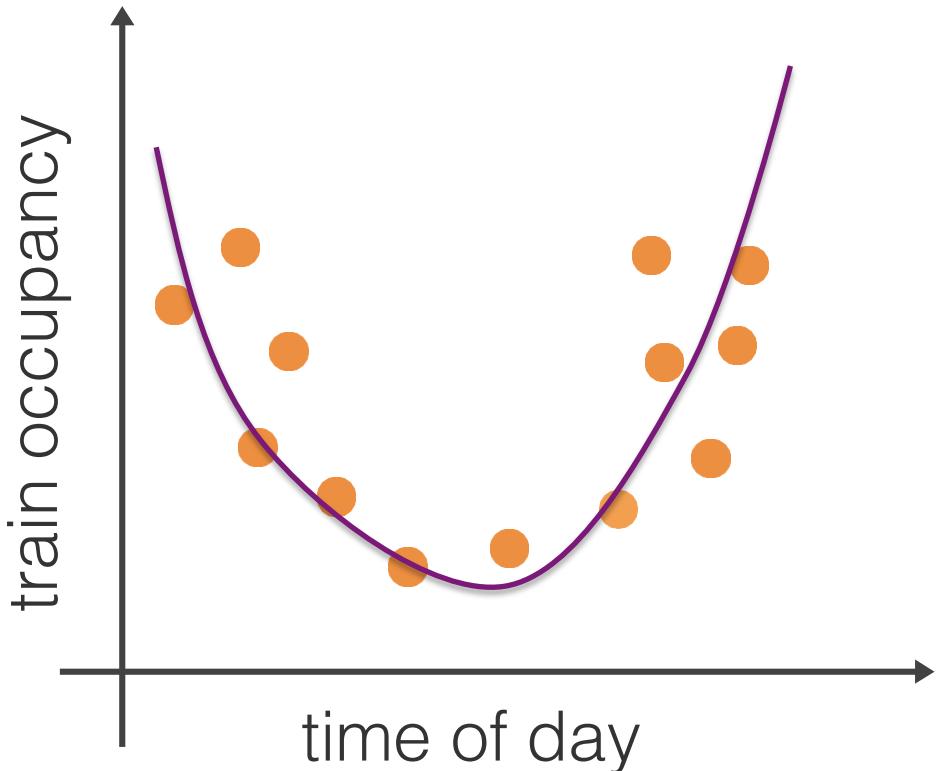
Make continuous predictions



Regression (2/3)



Regression (3/3)



$$\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$$
$$y^i \in \mathbb{R}$$

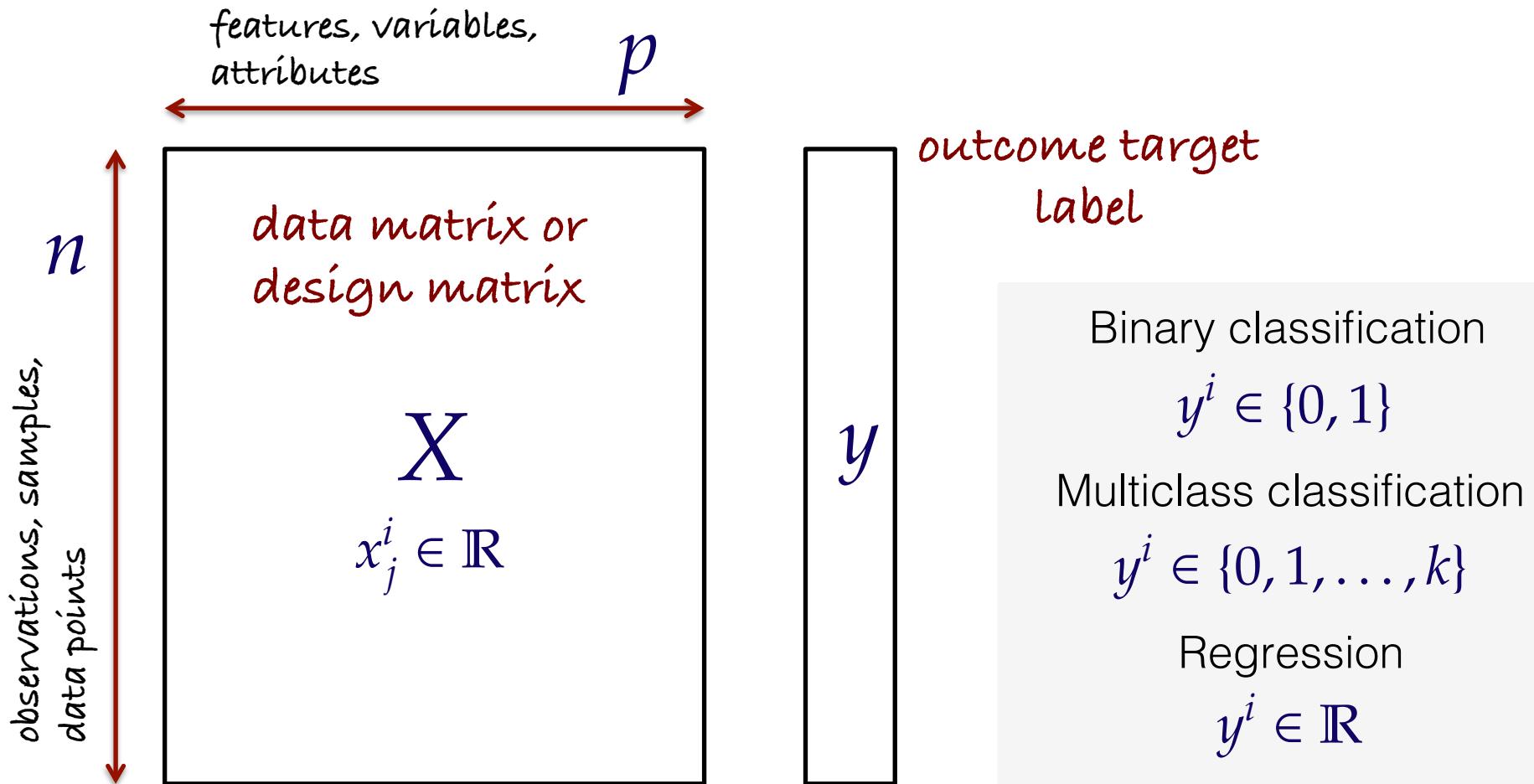
Given $\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$ find \mathbf{f} such that $f(x) \approx y$

Regression – Applications

- Click prediction
 - How many people will click on this ad? ... comment on this post? ... share this article on social media?
- Load prediction
 - How many users will my service have at a given time?
- Algorithmic trading
 - What will the price of this share be?

Supervised Learning Setting – Summary

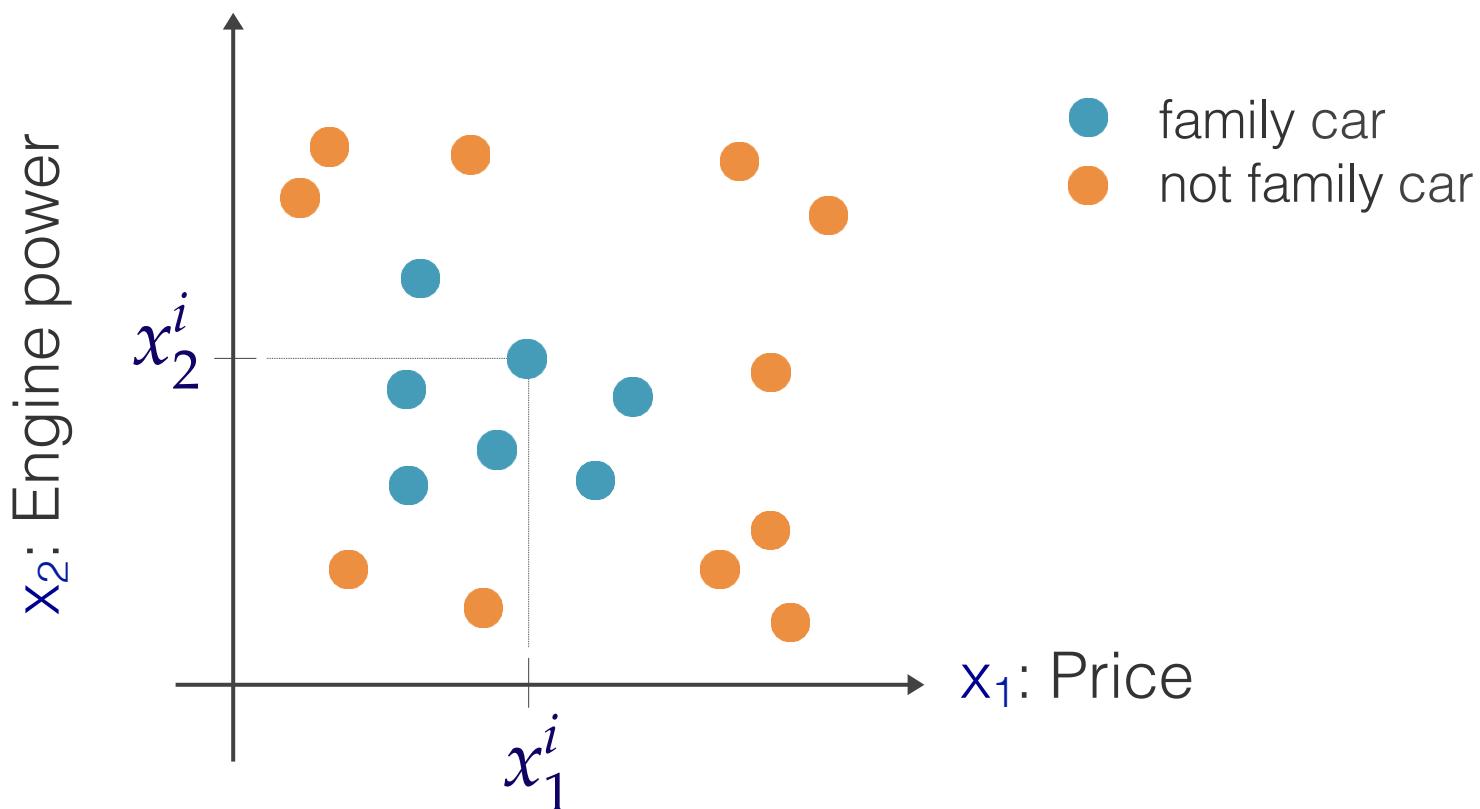
Given $\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$ find f such that $f(x) \approx y$



Hypothesis class, loss function, and risk minimization

Hypothesis Class

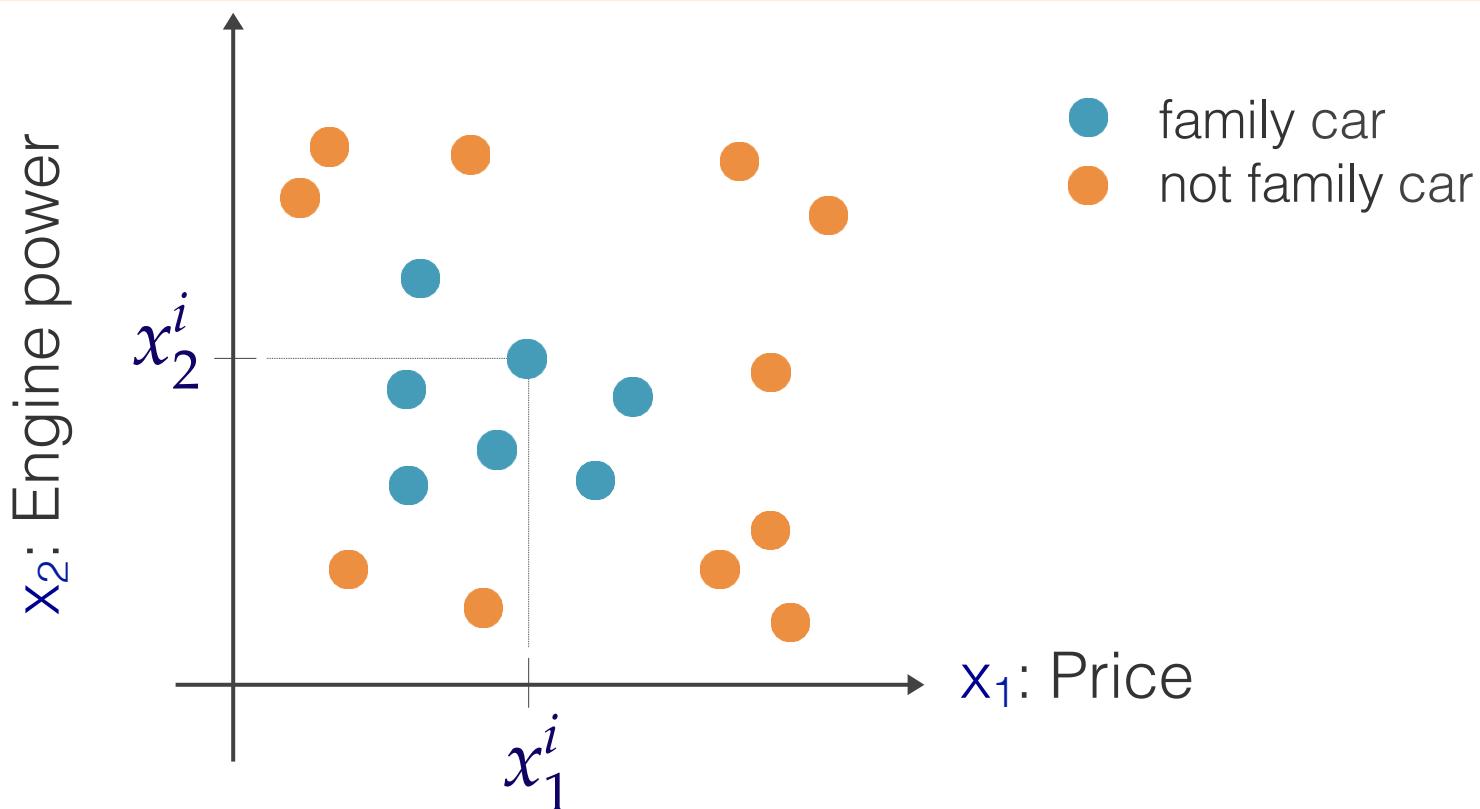
- Hypothesis class \mathcal{F}
 - The **space of possible decision functions** we are considering
 - Chosen based on our **beliefs** about the problem



Hypothesis Class

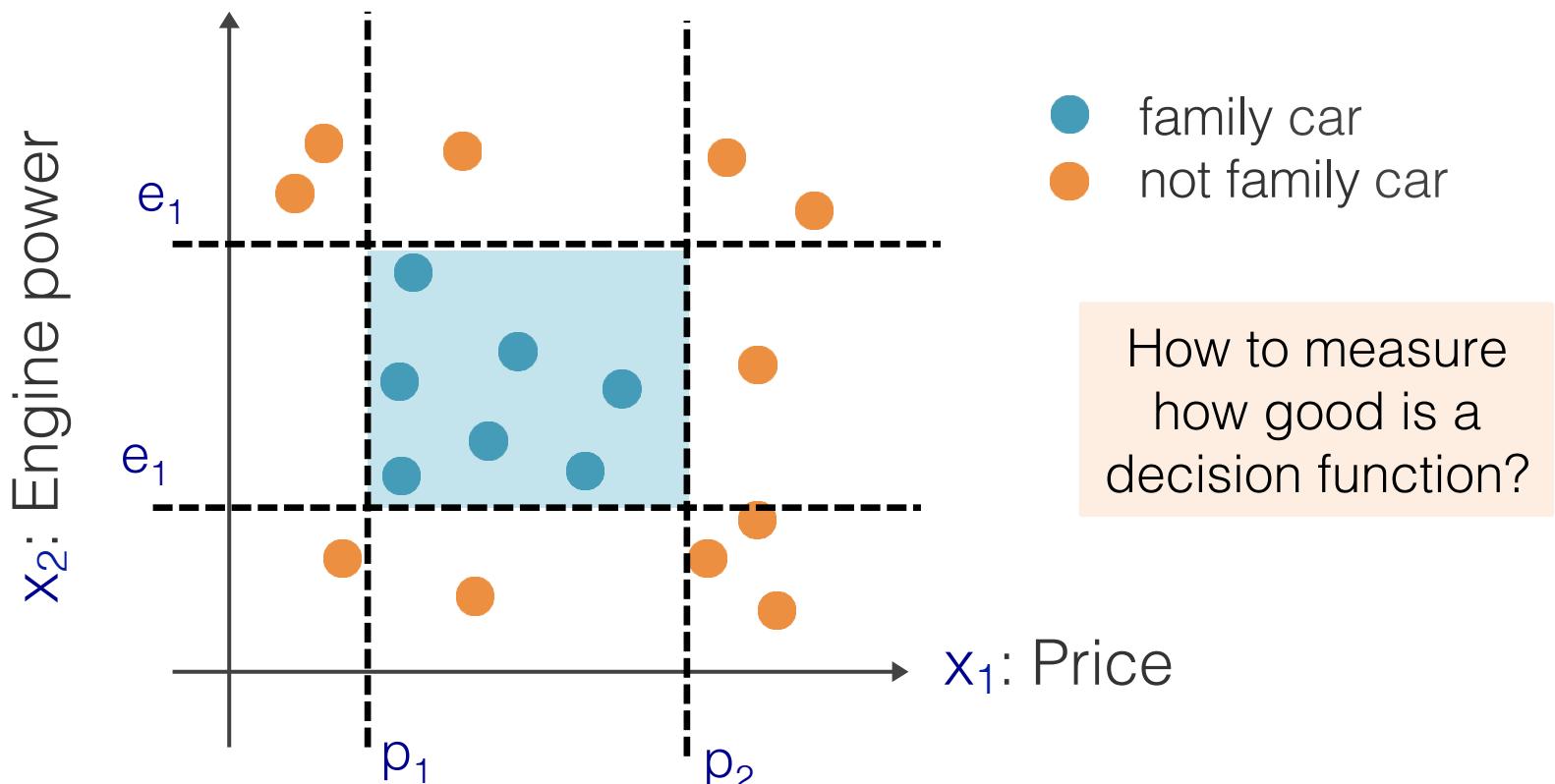
- Hypothesis class \mathcal{F}

What shape do you think the discriminant should take?



Hypothesis Class

- Hypothesis class \mathcal{F}
 - Belief: the decision function is a rectangle
$$(p_1 \leq x_1 \leq p_2) \text{ AND } (e_1 \leq x_2 \leq e_2)$$



Loss Function

- Loss function (or cost function, or risk):

$$\mathcal{L} : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}$$

$$y, f(x) \rightarrow \mathcal{L}(y, f(x))$$

Quantifies how far
the decision function
is from the truth

Example of loss
functions:

$$\mathcal{Y} = \{0, 1\} \quad \mathcal{L}(y, f(x)) = \begin{cases} 0 & \text{if } y = f(x) \\ 1 & \text{otherwise} \end{cases}$$

$$\mathcal{Y} = \mathbb{R} \quad \mathcal{L}(y, f(x)) = \|y - f(x)\|^2$$

Training via optimization: find that f among the hypothesis class \mathcal{F} that minimizes the total loss

The Goal of Training (1/4)

- What we have: labeled examples presented as (observations, label)

$$\mathbf{d}_i = (\mathbf{x}^i, y^i)$$

- E.g., observation = image, label = “cat” (-1), or “dog” (+1)

$$\left(\begin{img alt="A fluffy dog's face" data-bbox="361 475 448 600}, \quad + | \quad \right)$$

- **Assumption:** all labeled (train/test) examples come from unknown distribution, say \mathbf{D}

The Goal of Training (2/4)

- What we have: n labeled examples drawn *i.i.d.* from D

$$(\mathbf{x}^i, y^i), \dots, (\mathbf{x}^n, y^n)$$

- What we want: train a model (a predictor function f)

f : feature vector \rightarrow label

That performs well on **unseen data**

- For example:

$$f\left(\begin{array}{c} \text{[Image of a dog]} \end{array}\right) = +1$$

The Goal of Training (3/4)

- What we have: n labeled examples drawn *i.i.d.* from D

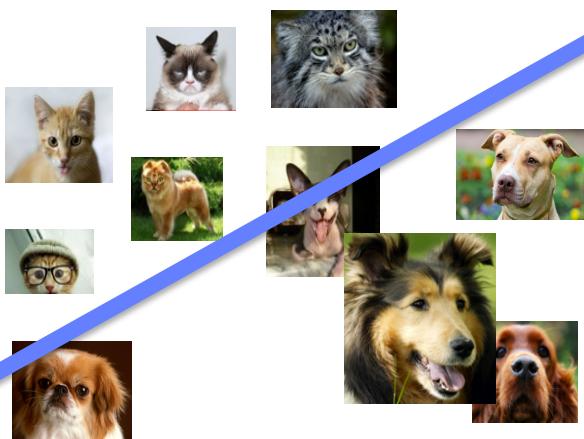
$$(\mathbf{x}^i, y^i), \dots, (\mathbf{x}^n, y^n)$$

- What we want: train a model (a predictor function f)

f : feature vector \rightarrow label

That performs well on unseen data

- For example:



Our trained predictor f

The Goal of Training (4/4)

- How to measure performance? As we said before, we need to define the **loss**:

$$\mathcal{L}(y, f(\mathbf{x}))$$

Measures disagreement
between
predicted and true label

- **Goal:** we want a predictor f with small loss on **unseen data** (e.g., on a test set)

$$\sum_{(\mathbf{x}, y) \text{ is an unseen example}} \mathcal{L}(y, f(\mathbf{x}))$$

But, we haven't seen unseen examples
(the test set is not known to the learning algorithm)

Empirical Risk

- The loss on the “unseen” examples converges to the expected loss

$$\sum_{(\mathbf{x}, y) \text{ is an unseen example}} \mathcal{L}(y, f(\mathbf{x})) \rightarrow \mathbb{E}_{\mathbf{x}, y} \{ \mathcal{L}(y, f(\mathbf{x})) \}$$

Expected/True risk

- What else converges to the expected loss?

$$\frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

Empirical risk

By averaging the loss function on
the training set

Empirical Risk Minimization (ERM)

- Training via optimization: we want to solve:

$$\arg \min_{f \in \mathcal{F}} \mathbb{E}\{\mathcal{L}(y, f(x))\}$$

f can be:

- separating hyperplanes
- NN's of depth-t
- ...

- We instead solve the ERM:

$$\arg \min_{f \in \mathcal{F}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

Supervised Learning: 3 Ingredients

Given $\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$ find \mathbf{f} such that $f(x) \approx y$

- Chose a hypothesis class \mathcal{F}
 - Parametric methods – e.g., $f(x) = \sum_{j=1}^p \beta_j x_j$
 - Non-parametric methods – e.g., $\mathbf{f}(x)$ is the label of the point closest to \mathbf{x} (Nearest Neighbors is such a method)
- Chose a loss function \mathcal{L}
 - Empirical error: $\frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$
- Chose an optimization procedure

$$f^* = \arg \min_{f \in \mathcal{F}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

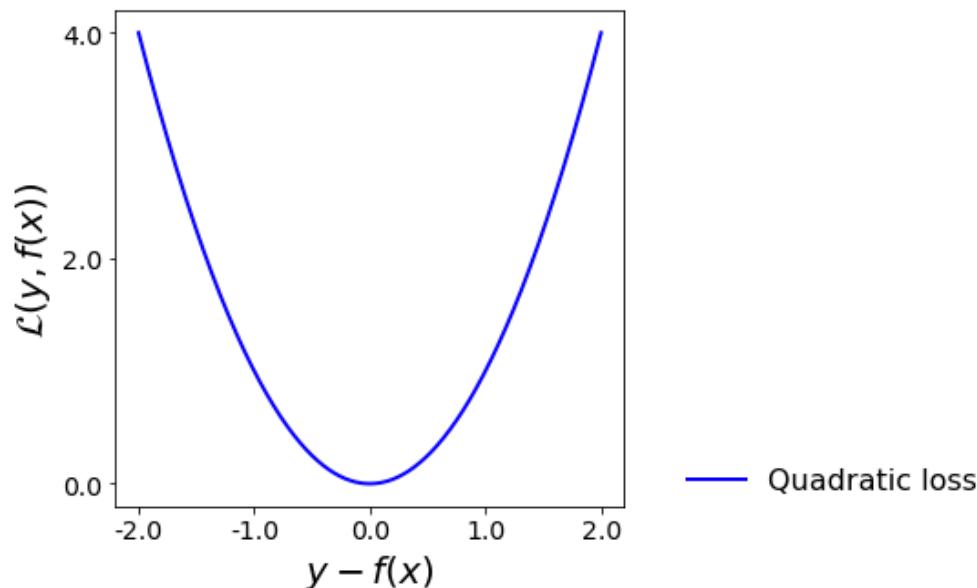
Why Optimization? (1/4)

- Empirical risk minimization:

$$f^* = \arg \min_{f \in \mathcal{F}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

Which loss functions
are mainly used?

- Quadratic loss: $\mathcal{L}(y, f(\mathbf{x})) = (y - f(\mathbf{x}))^2$



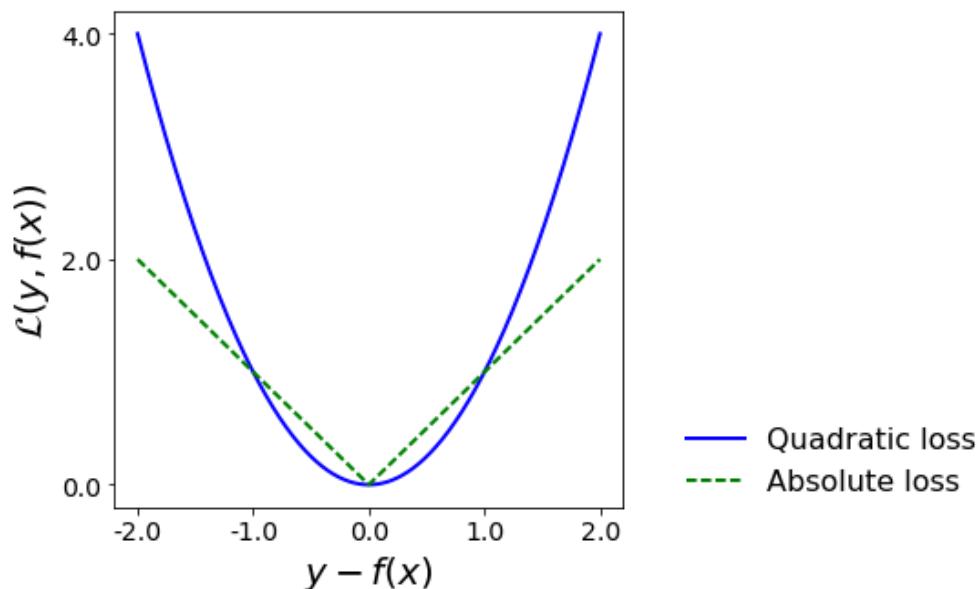
Why Optimization? (2/4)

- Empirical risk minimization:

$$f^* = \arg \min_{f \in \mathcal{F}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

Which loss functions
are mainly used?

- Absolute loss: $\mathcal{L}(y, f(\mathbf{x})) = |y - f(\mathbf{x})|$



Why Optimization? (3/4)

- Empirical risk minimization:

$$f^* = \arg \min_{f \in \mathcal{F}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

Which loss functions
are mainly used?

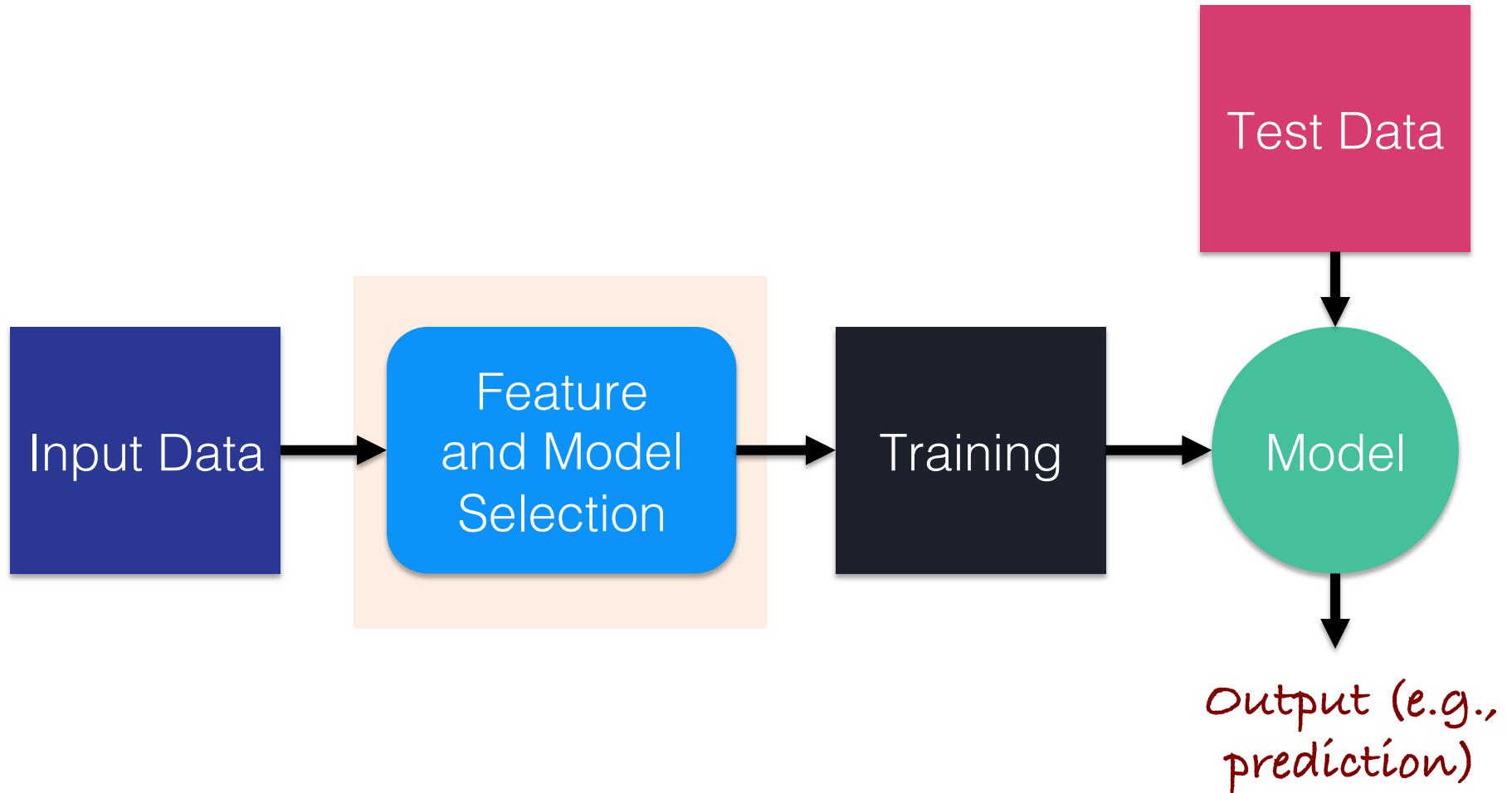
- 0/1 loss:

$$\mathcal{L}(y, f(\mathbf{x})) = \begin{cases} 0 & \text{if } y = f(\mathbf{x}) \\ 1 & \text{otherwise} \end{cases}$$

This part will be covered in the
classes about optimization

Model selection and evaluation

ML Pipeline



Generalization

- It's easy to build a model that performs well on the training data
 - But how well will it perform on new (unseen) data?
-
- Learn models that generalize well
 - Evaluate whether models generalized well

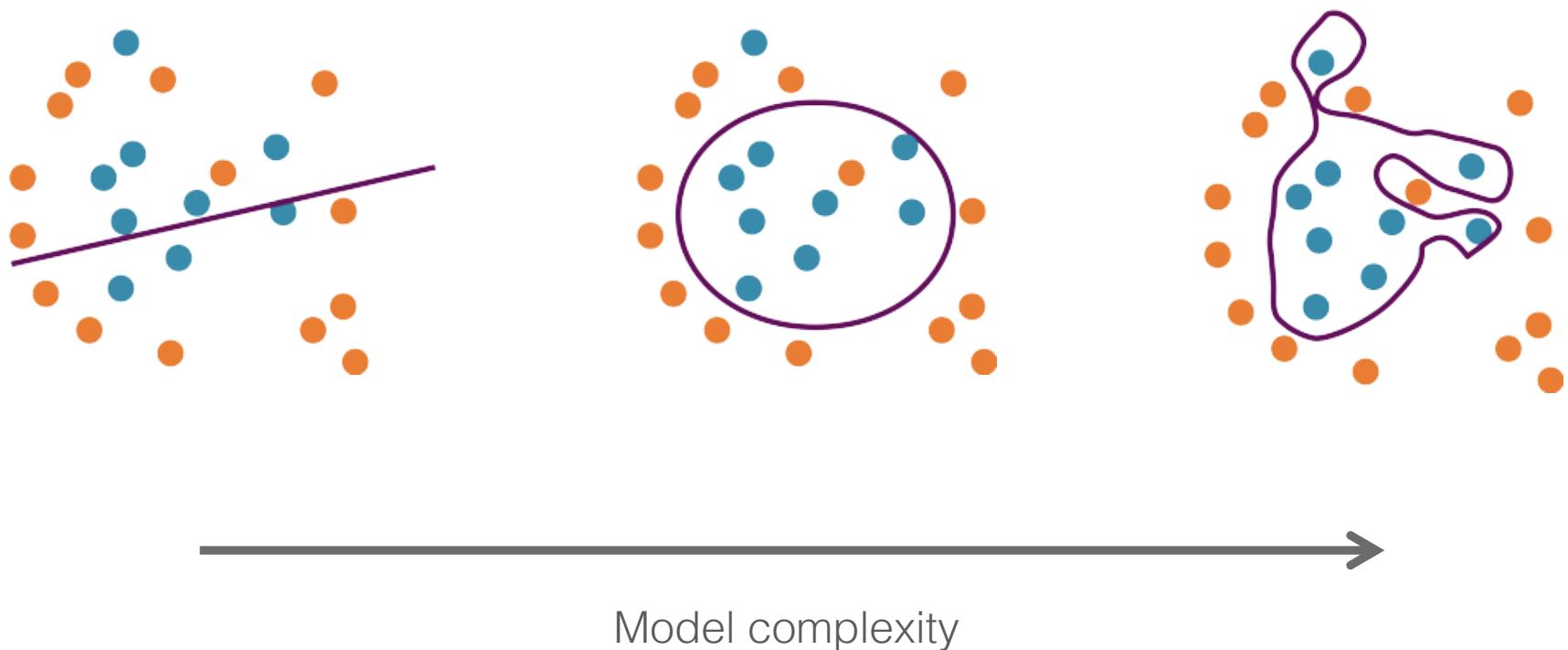
Given $\mathcal{D} = \{x^i, y^i\}_{i=1, \dots, n}$ find \mathbf{f} such that $f(x) \approx y$

Additional Factor: Noise in the Data

- Imprecision in recording the features
- Errors in labeling the data points
- Missing features (hidden or latent)

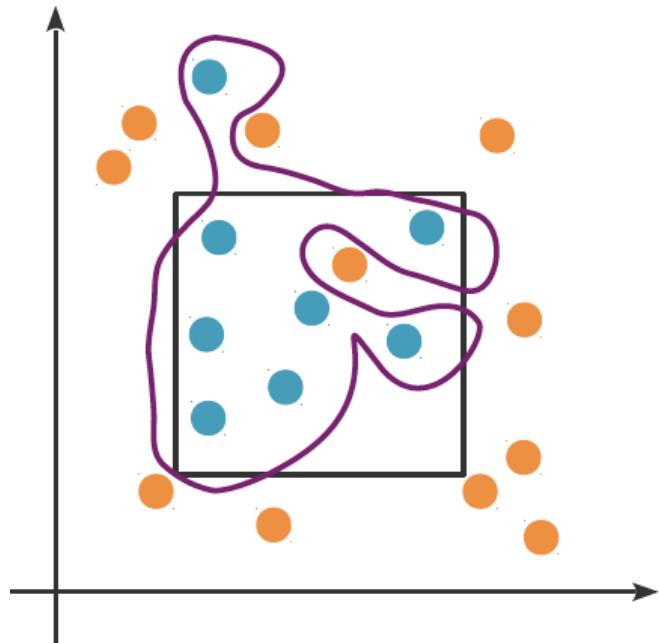
Making no errors on the training set might not be possible

Models of Increasing Complexity

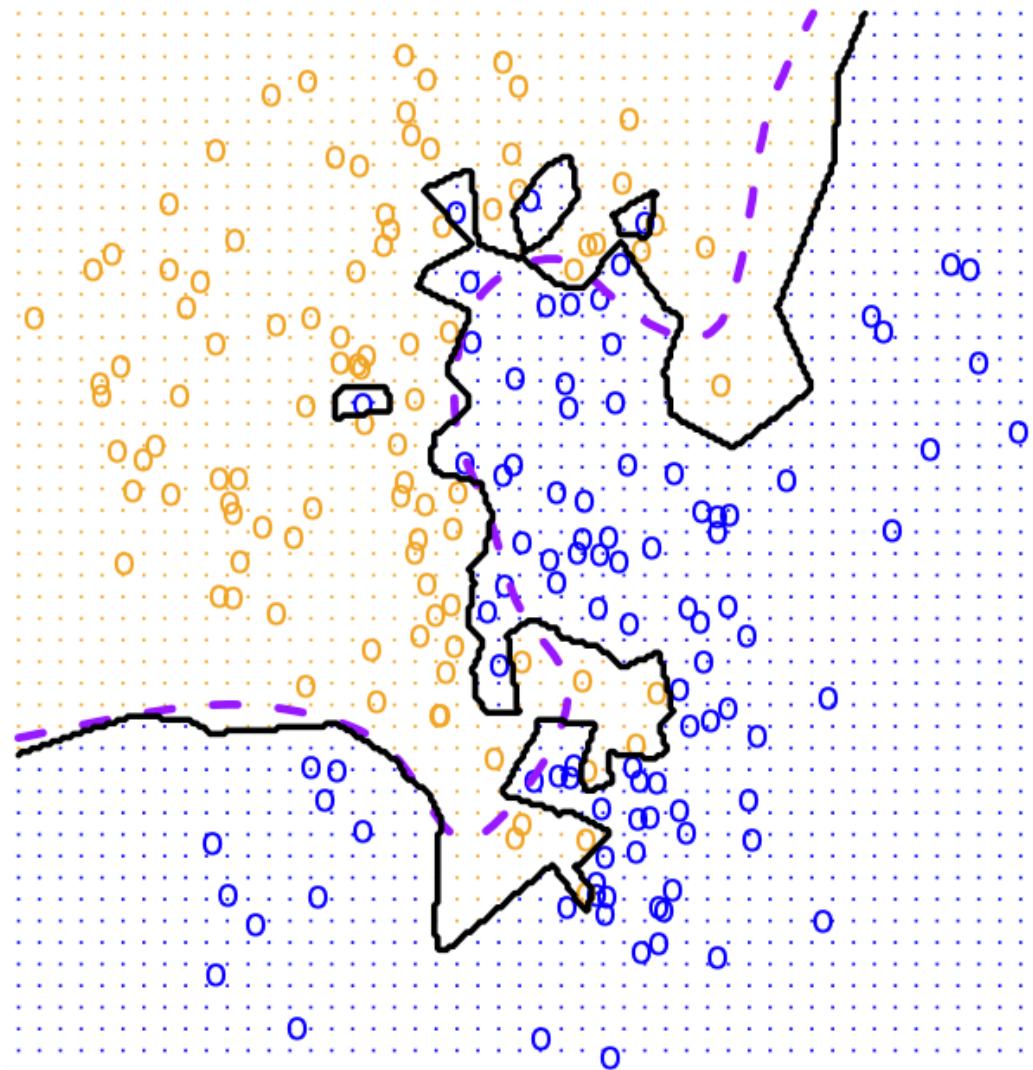


Noise and Model Complexity

- Use simple models!
 - Easier to *use*
 - Lower computational complexity
 - Easier to *train*
 - Lower space complexity
 - Easier to *explain*
 - More interpretable
 - Generalize better
 - Occam's razor: simpler explanations are more plausible



Overfitting

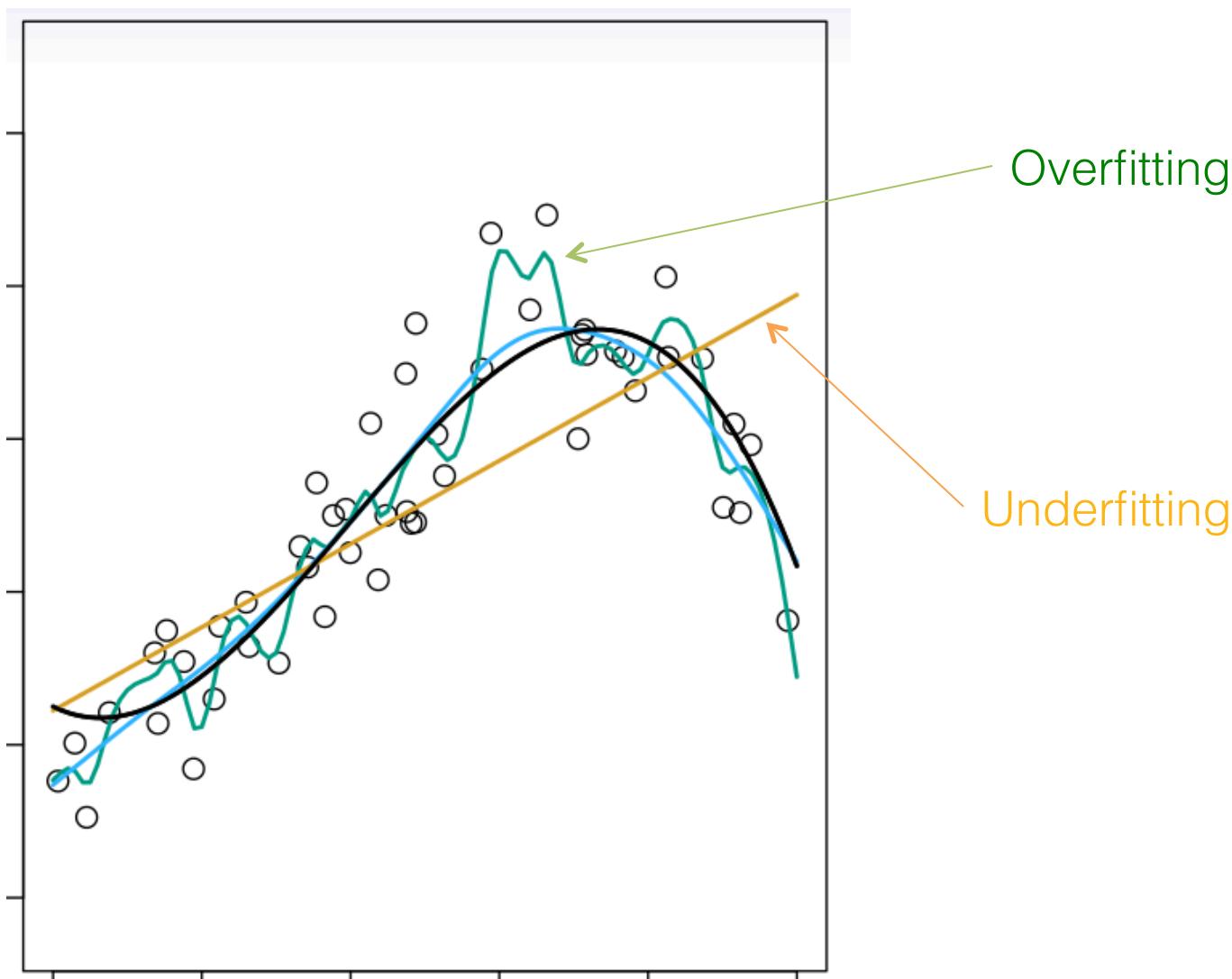


- What is the empirical error of the black and purple classifiers?

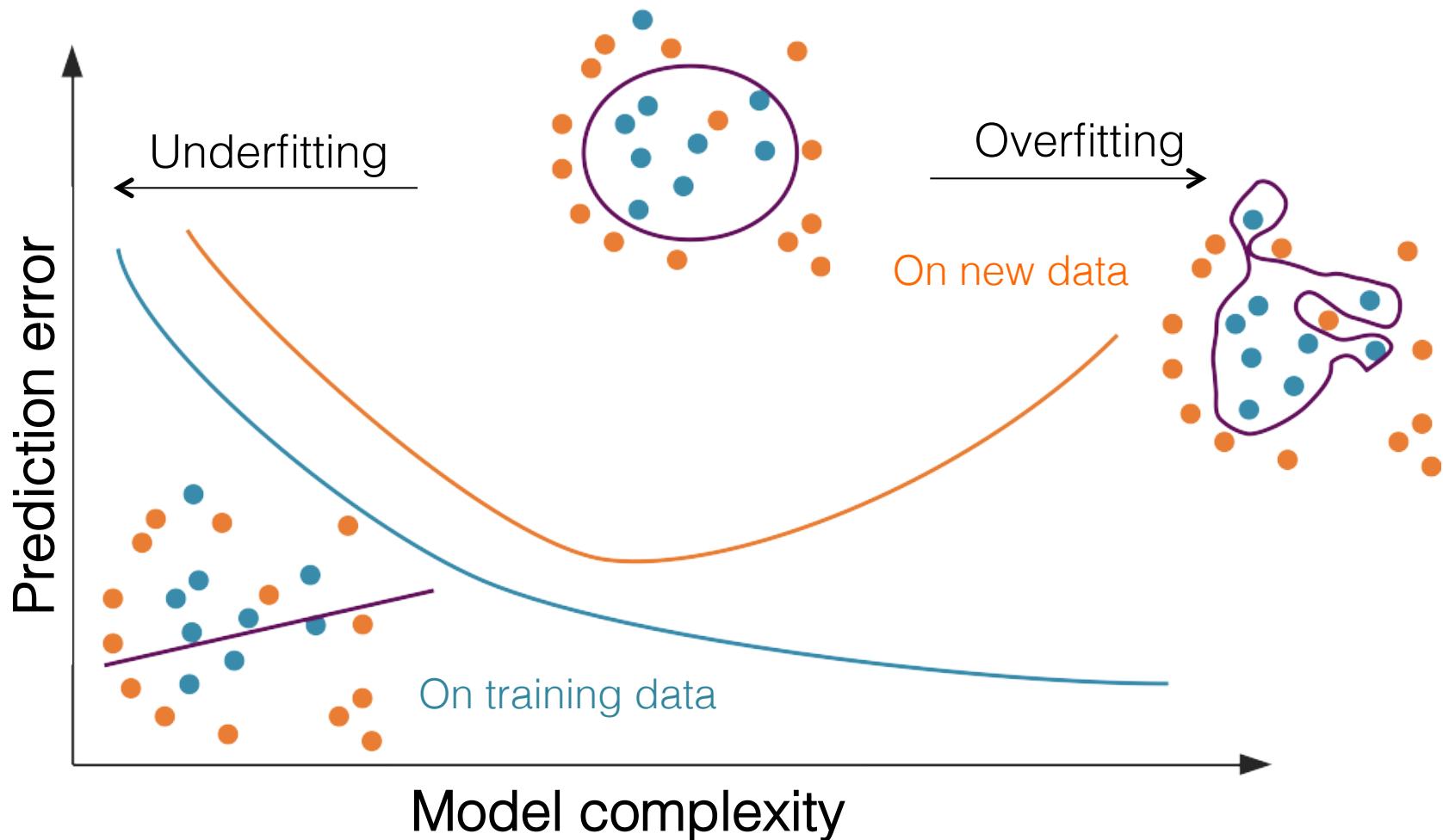
$$\frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i)) \quad \text{For some loss function } \mathcal{L}$$

- Which model seems more likely to be correct?

Overfitting and Underfitting in Regression



Generalization Error vs. Model Complexity



Fixed dataset size; varying model complexity

Bias-Variance Tradeoff (1/5)

- **Bias:** difference between the expected value of the estimator (model) and the true value being estimated

$$\text{Bias}(f(\mathbf{x})) = \mathbb{E}[f(\mathbf{x}) - y]$$

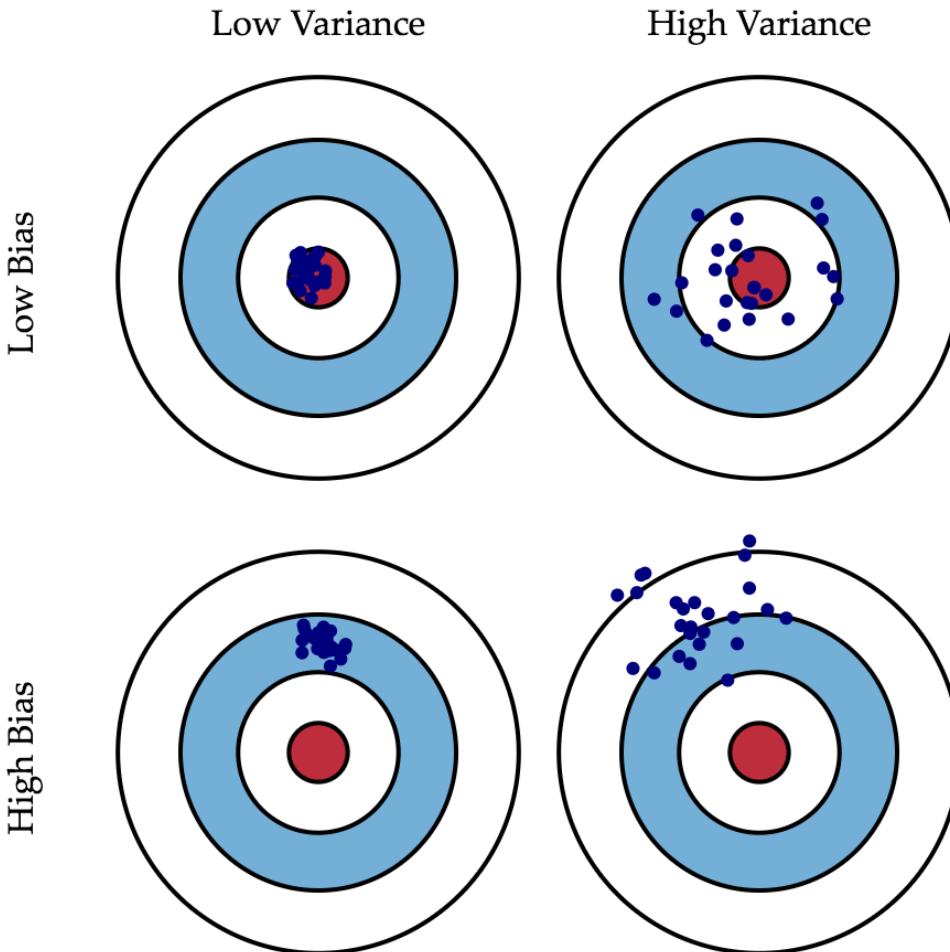
- A simpler model has a higher bias (naturally a simple model will do some errors)
- High bias can cause underfitting
- **Variance:** deviation from the expected value of the estimates

$$\text{Var}(f(\mathbf{x})) = \mathbb{E}[(f(\mathbf{x}) - \mathbb{E}(f(\mathbf{x})))^2]$$

- A more complex model has a higher variance
- High variance can cause overfitting

Ideally, we want to optimize both

Bias-Variance Tradeoff (2/5)

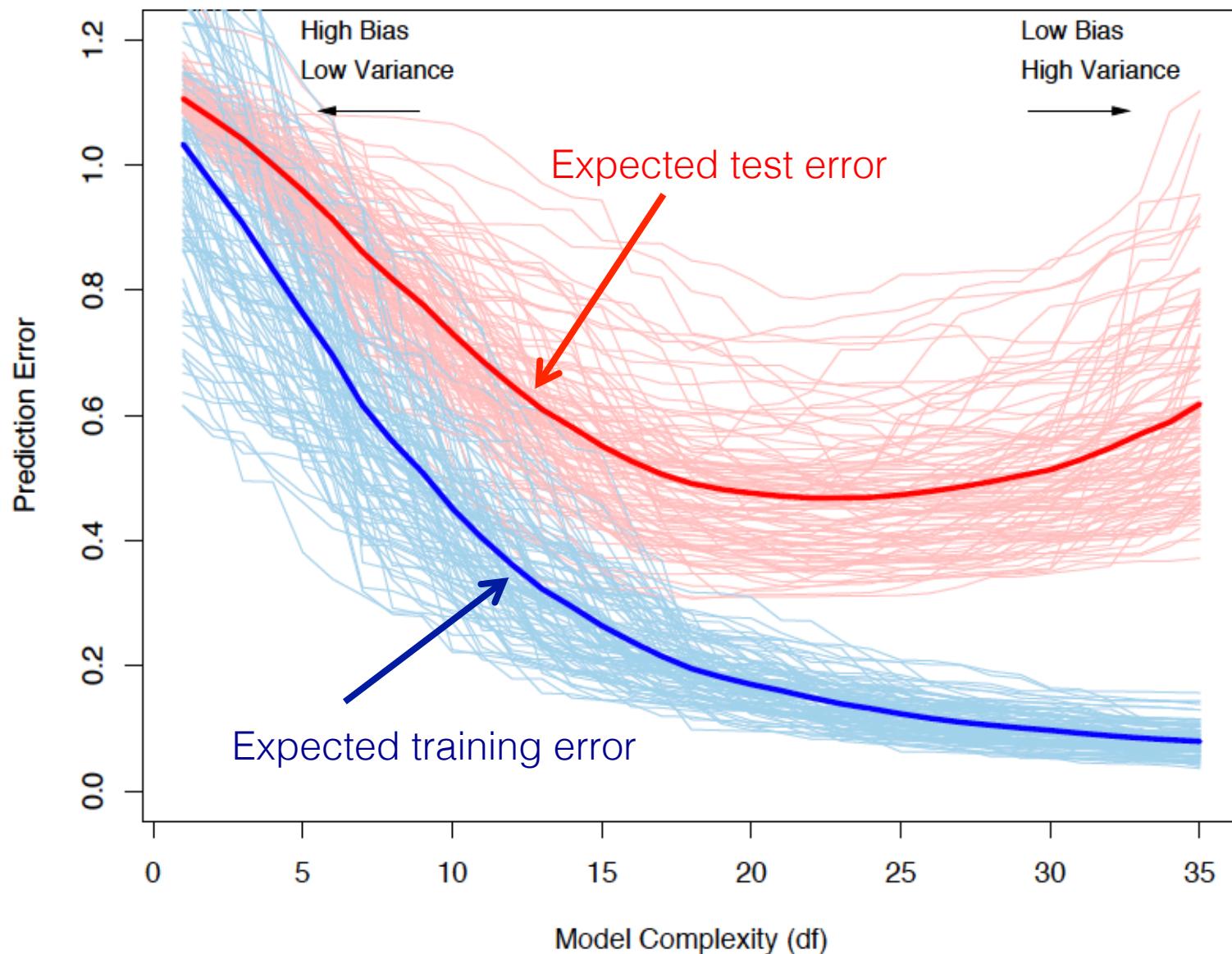


- The center of the target is a **model** that **perfectly predicts** the correct values
- We can repeat our entire model building process to get a number of separate hits on the target
 - Each hit represents an individual realization of the model
- **Bias** measures how far are in general these models' predictions are from the correct value
- **Variance** is how much the predictions for a given point vary between different realizations of the model

Bias-Variance Tradeoff (3/5)

- When do we have **high bias**?
 - We have high bias when the model (function) cannot model the true data distribution well
 - This doesn't depend on the training data size
 - Underfitting
- When do we have **high variance**?
 - We have high variance when there is a small amount of training data and a very complex model
 - Overfitting
 - Variance decreases with larger training data, and increases with more complicated classifiers

Bias-Variance Tradeoff (4/5)



Bias-Variance Tradeoff (5/5)

- High bias → high training and test errors
- High variance → low training error, high test errors

Bias-variance tradeoff

If we make the model more complicated, then, for the same training set size, the bias decreases but the variance increases

Bias-Variance Decomposition

- $\text{Bias}(f(\mathbf{x})) = \mathbb{E}[f(\mathbf{x}) - y]$
- $\text{Var}(f(\mathbf{x})) = \mathbb{E}[(f(\mathbf{x}) - \mathbb{E}(f(\mathbf{x})))^2]$
- Use the **mean squared error**: we want $(f(\mathbf{x}) - y)^2$ to be minimized, both for $\mathbf{x}_1, \dots, \mathbf{x}_m$ and for points outside the sample
 - f should generalize to samples outside the training set
- We can decompose the expected error on an unseen example \mathbf{x} as follows:

$$\begin{aligned}\text{MSE}(f(\mathbf{x})) &= \mathbb{E}[(f(\mathbf{x}) - y)^2] \\ &= \text{Var}(f(\mathbf{x})) + \text{Bias}^2(f(\mathbf{x}))\end{aligned}$$

How much your model changes if you train on a different training set

What is the inherent error that you obtain from your model even with infinite training data

Model Selection and Evaluation

- **Model selection:** estimating the performance of different models in order to choose the best
- **Model evaluation (assessment):** having chosen a final model, estimating its prediction error (generalization error) on new data

**How to estimate if a
model is good in practice**

or

**How do we estimate the
prediction error**

Learning Objectives

- After this part of the lecture you will be able to design experiments to select and evaluate supervised machine learning models
- Concepts:
 - Training and testing sets
 - Cross-validation
 - Measures of performance for classification and regression
 - Measures of model complexity

Reminder – Supervised Learning Setting

Given $\mathcal{D} = \{x^i, y^i\}_{i=1,\dots,n}$ find f such that $f(x) \approx y$

- Empirical error of f on the training set, given a loss function

$$\frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f(\mathbf{x}^i))$$

Binary classification

$$y^i \in \{0, 1\}$$

Multiclass classification

$$y^i \in \{0, 1, \dots, k\}$$

Regression

$$y^i \in \mathbb{R}$$

Generalization Error

- The empirical error on the training set is a poor estimate of the **generalization error** (expected error on new data)
 - If the model is **overfitting**, the generalization error can be arbitrarily **large**
- We would like to estimate the generalization error on **new data**, which we do not have

Any (simple) idea?

Validation Sets

- Choose the model that performs best on a validation set separate from the training set



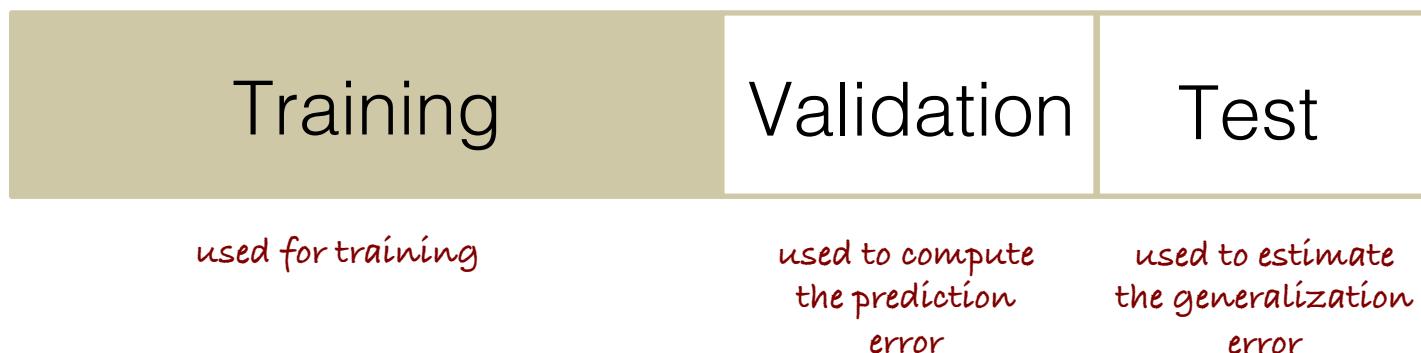
- Because we have not used the validation data at any point during training, the validation set can be considered “new data” and the error on the validation set is an estimation of the generalization error

Model Selection

- What if we want to choose among k models?
 - Train each model on the train set
 - Compute the prediction error of each model on the validation set
 - Pick the model with the smallest prediction error on the validation set
- What is the generalization error?
 - We don't know!
 - Validation data was used to select the model
 - We have “cheated” and looked at the validation data: it is not a good proxy for new, unseen data any more

Validation Sets (1/2)

- Hence we need to set aside part of the data, the **test set**, that remains untouched during the entire procedure and on which we'll estimate the generalization error
- Model selection: pick the best model
- Model assessment: estimate its prediction error on new data

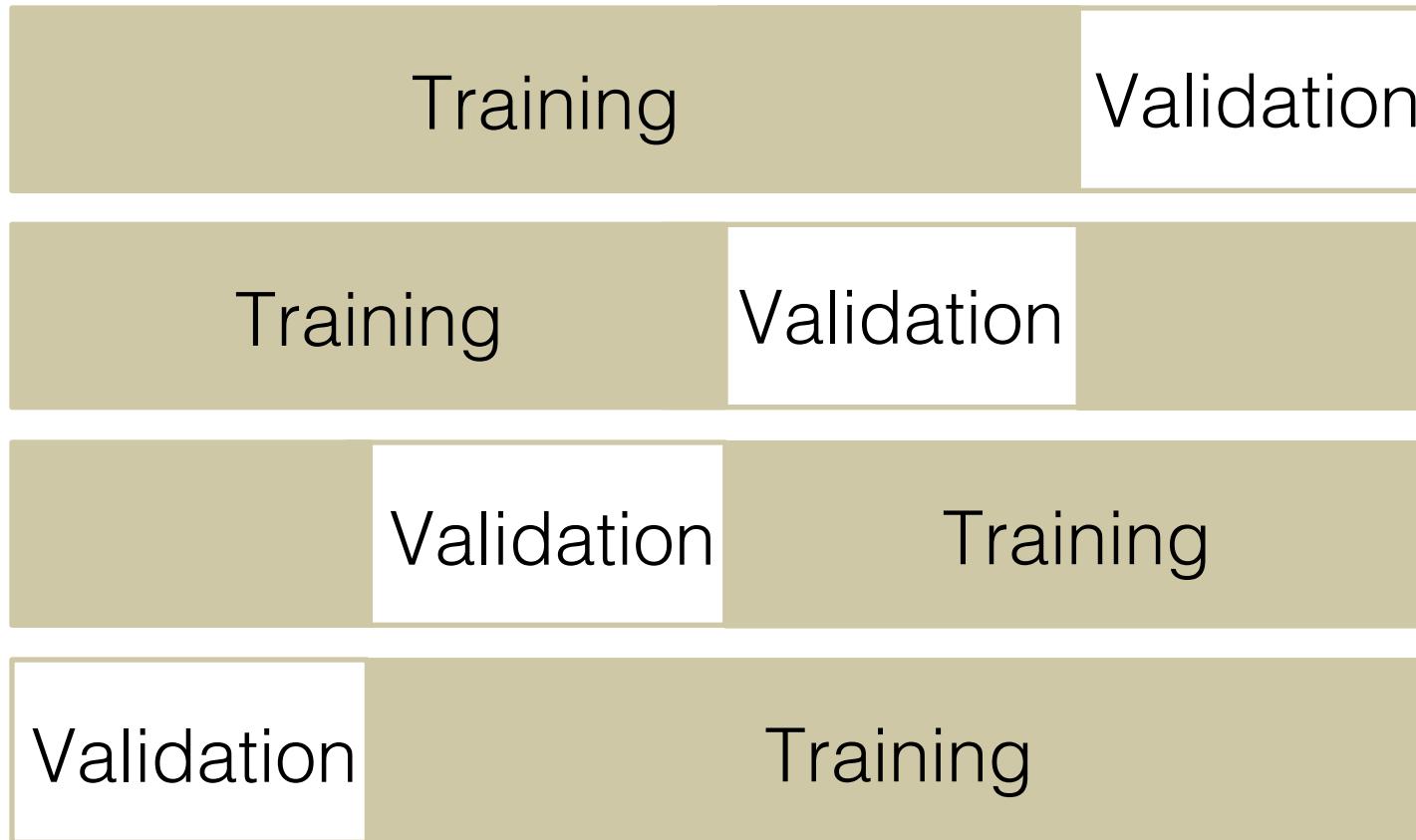


Validation Sets (2/2)

- How much data should go in each of the training, validation and test sets?
- How do we know that we have enough data to evaluate the prediction and generalization errors?
- Empirical evaluation with sample re-use
 - Cross-validation
 - Bootstrap (random sampling with replacement)

Cross-validation

- Cut the training set in k separate folds
- For each fold, **train** on the $(k-1)$ remaining folds



Cross-validated Performance

- Cross-validation estimate of the prediction error

$$CV(f) = \frac{1}{n} \sum_{i=1}^n \mathcal{L}(y^i, f_{k(i)}(\mathbf{x}^i))$$

Computed with the $k(i)$ -th part of the data removed.
 $k(i)$ = fold in which i belongs to

Issues with Cross-validation

- The training set can become very small (depending on k)
 - Small training set → biased estimator of the error
- Leave-one-out cross-validation: $k = n$
 - Approximately unbiased estimator of the expected prediction error
 - Potential high variance (the training sets are very similar to each other)
 - Computationally-intense approach (n repeats)
- In practice: set $k=5$ or $k=10$

Cross-validation in scikit-learn



http://scikit-learn.org/stable/modules/cross_validation.html

Evaluating model performance

Classification Model Evaluation

- Confusion matrix

		True class	
		-1	+1
Predicted class	-1	True Negatives	False Negatives
	+1	False Positives	True Positives

- False positives (false alarms) are also called type I errors
- False negatives (misses) are also called type II errors

Evaluation Measures (1/2)

- Sensitivity = Recall = True positive rate (TPR)

$$TPR = \frac{TP}{TP + FN}$$

of positives

- Specificity = True negative rate (TNR)

$$TNR = \frac{TN}{FP + TN}$$

- Precision = Positive predictive value (PPV)

$$PPV = \frac{TP}{TP + FP}$$

of predicted positives

- False discovery rate (FDR)

$$FDR = \frac{FP}{FP + TP}$$

Evaluation Measures (2/2)

- Accuracy

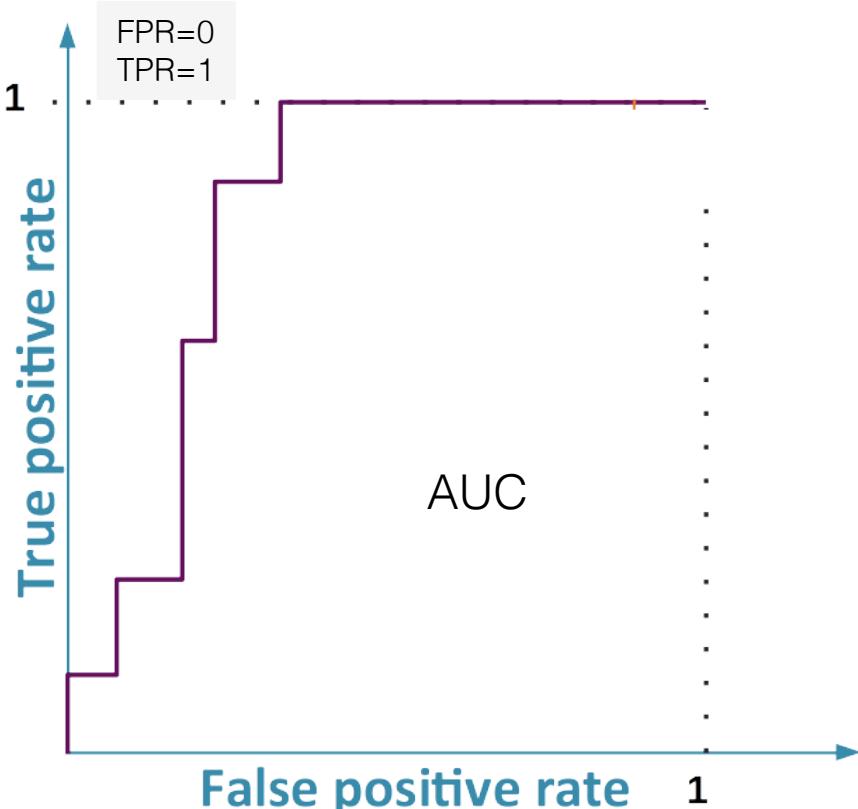
$$Acc = \frac{TP + TN}{TP + FN + FP + TN}$$

- F1-score: harmonic mean of precision and recall (sensitivity)

$$F1 = \frac{2TP}{2TP + FP + FN}$$

ROC Curve (1/2)

- ROC = Receiver-Operator Characteristic
- Summarized by the area under the curve (AUROC or AUC)

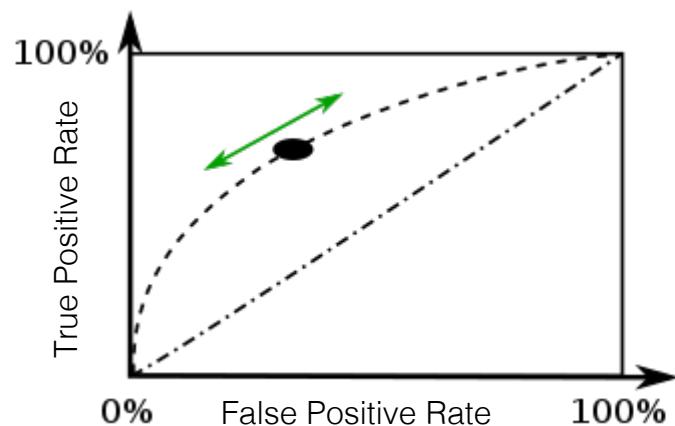
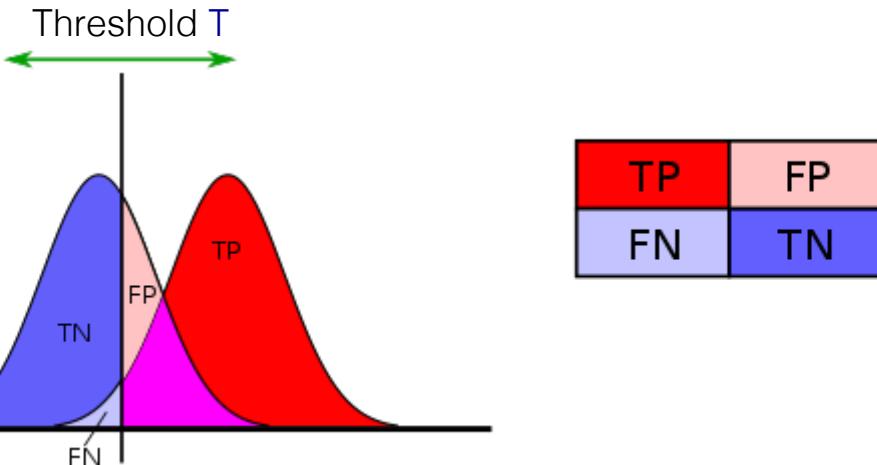


- Plot TPR vs. FPR for all possible thresholds (typically generated by the classifier)
$$TPR = \frac{TP}{TP + FN} \quad FPR = \frac{FP}{FP + TN}$$
- Shows the trade off in sensitivity (TPR) and (1 – specificity) (FPR) for all possible thresholds (cutoff values between positive and negative class)
- The larger the AUC, the better is overall performance

Source: https://en.wikipedia.org/wiki/Receiver_operating_characteristic

Visual description of ROC curve: <https://www.youtube.com/watch?v=OAI6eAyP-yo>

ROC Curve (2/2)



$$TPR = \frac{TP}{TP + FN}$$

$$FPR = \frac{FP}{FP + TN}$$

- In binary classification, the class prediction is often made based on a cont. random variable X
 - Given by the classifier
- Given a threshold parameter T , the instance is classified as positive if $X > T$
- X follows a PDF
 - $f_1(x)$, if it actually belongs to the **positive** class
 - $f_0(x)$, for the **negative** class

Evaluation Measures in scikit-learn



http://scikit-learn.org/stable/modules/model_evaluation.html

About the project

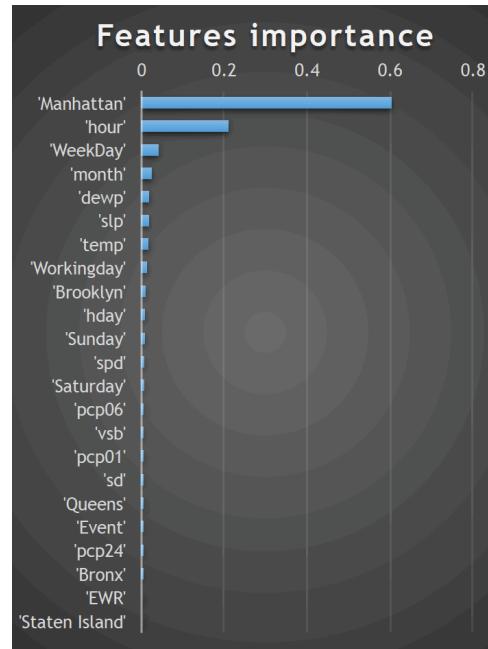
Examples of Previous Projects (1/5)

How can Uber predict the demand for pickups?

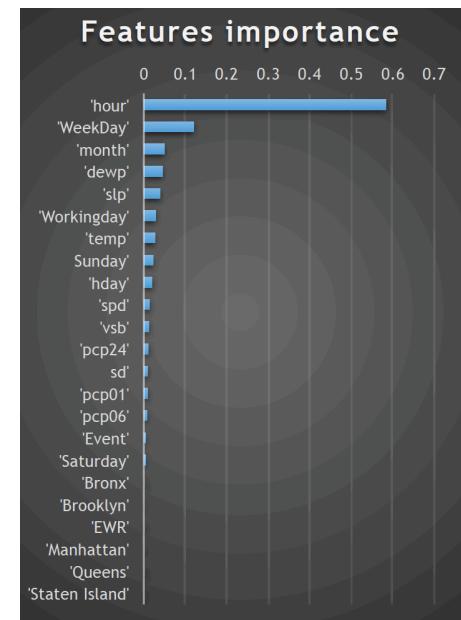
- Dataset: 34,000 rides per day in NYC
- Prediction problem

WEATHER	EVENTS	DAYS	BOROUGHS
TEMPERATURE	CONCERTS	TIME	BRONX
WIND SPEED	MUSIC FESTIVALS	DAY / MONTH	BROOKLYN
VISIBILITY		HOLIDAYS	EWR
PRECIPITATION			MANHATTAN
SEA LEVEL			QUEENS
DEW POINT			STATEN ISLAND
SNOW DEPTH			

Dataset description



For the whole dataset

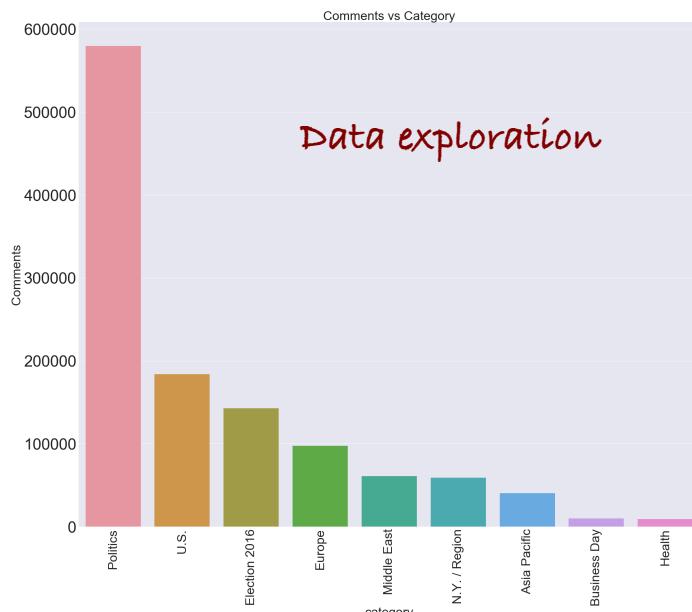


For a particular district
in NYC (Borough)

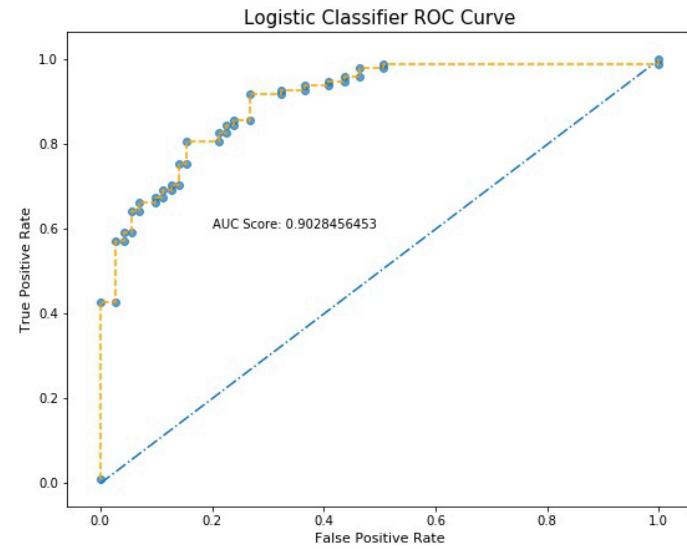
Examples of Previous Projects (2/5)

Analyzing New York Times' readers engagement

- Problem: predict if an article will be commented or not
- Data: 1,280 articles and 280 authors' data
- Features: article length, images, videos, content, authors' information, etc.



Top-10 most commented articles

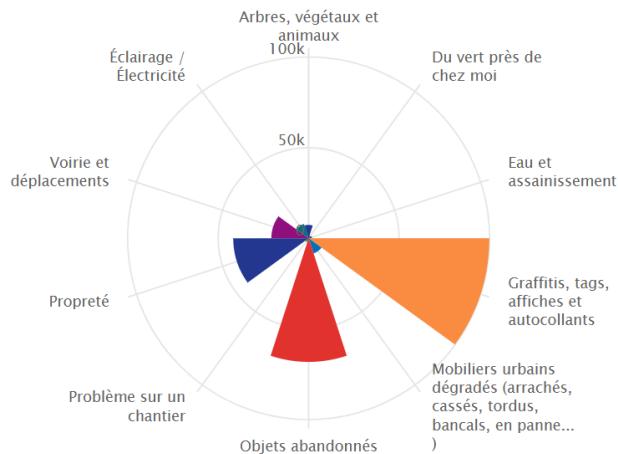
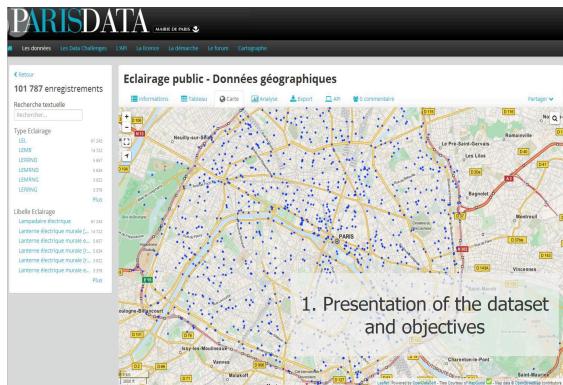


Prediction results (logistic regression)

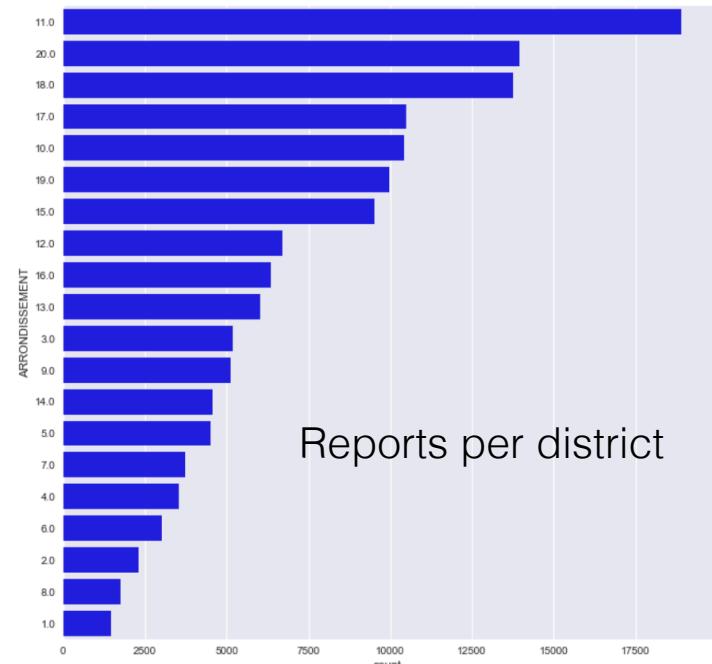
Examples of Previous Projects (3/5)

Predict reports made by citizens in Paris

- Data: open Paris data



Distribution of reports by type



Reports per district

	precision	recall	f1-score	support
Arbres, végétaux et animaux	0.48	0.02	0.03	634
Du vert près de chez moi	0.47	0.15	0.23	277
Eau et assainissement	1.00	0.01	0.02	124
Graffitis, tags, affiches et autocollants	0.54	0.86	0.66	11314
Mobiliers urbains dégradés	0.52	0.05	0.10	1067
Objets abandonnés	0.57	0.58	0.58	7286
Problème sur un chantier	0.00	0.00	0.00	229
Propreté	0.42	0.20	0.27	4120
Voirie et déplacements	0.40	0.08	0.13	2301
Éclairage / Électricité	0.42	0.04	0.07	909
avg / total	0.51	0.54	0.47	28261

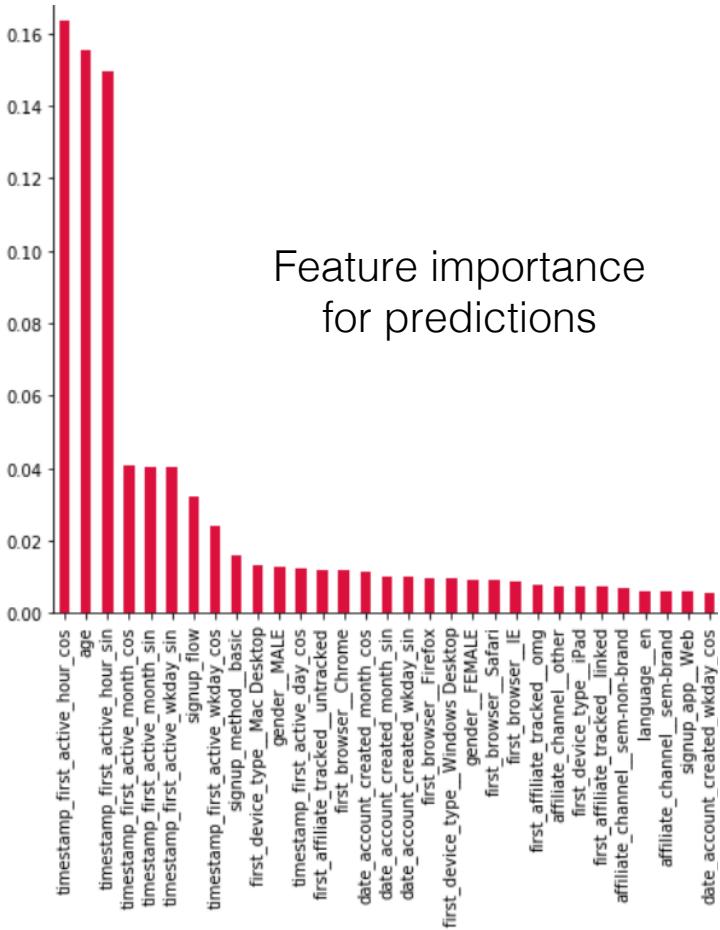
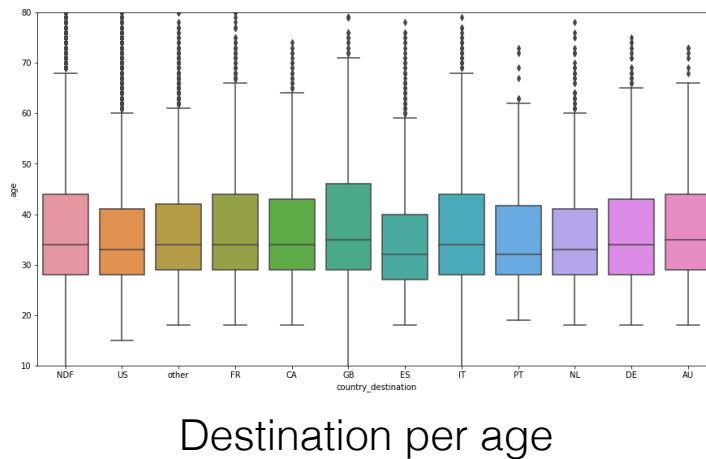
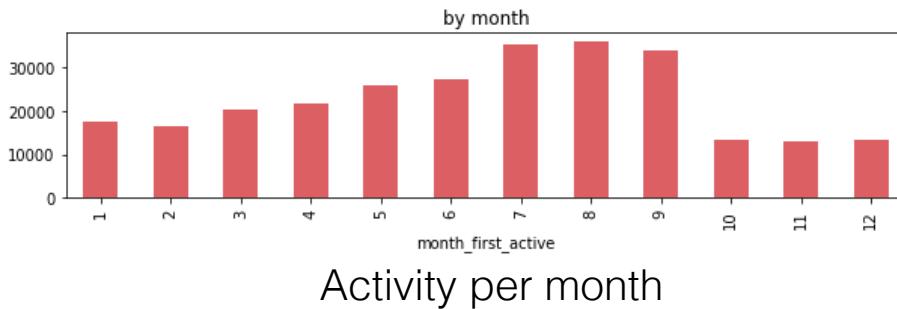
Prediction results
(random forest)

132

Examples of Previous Projects (4/5)

Airbnb destination prediction

- Data: 214,000 users (USA), 11 countries
- Features: age, gender, language, important dates



Examples of Previous Projects (5/5)

Pokemon battle prediction

- Problem: predict the outcome of a pokemon fight

	First_pokemon	Second_pokemon	Winner
0	266	298	298
1	702	701	701
2	191	668	668
3	237	683	683
4	151	231	151

- Data:

#	Name	Type 1	Type 2	HP	Attack	Defense	Sp. Atk	Sp. Def	Speed	Generation	Legendary
1	Bulbasaur	Grass	Poison	45	49	49	65	65	45	1	False
2	Ivysaur	Grass	Poison	60	62	63	80	80	60	1	False
3	Venusaur	Grass	Poison	80	82	83	100	100	80	1	False
4	Mega Venusaur	Grass	Poison	80	100	123	122	120	80	1	False
5	Charmander	Fire	NaN	39	52	43	60	50	65	1	False

	Normal	Fire	Water	Electric	Grass	Ice	Fighting	Poison	Ground	Flying	Psychic	Bug	Rock	Ghost	Dragon	Dark	Steel	Fairy
Normal	1	1	1	1	1	1	2	1	1	1	1	1	1	1	0	1	1	1
Fire	1	0.5	2	1	0.5	0.5	1	1	2	1	1	0.5	2	1	1	1	0.5	0.5
Water	1	0.5	0.5	2	2	0.5	1	1	1	1	1	1	1	1	1	1	0.5	1
Electric	1	1	1	0.5	1	1	1	1	2	0.5	1	1	1	1	1	1	0.5	1
Grass	1	2	0.5	0.5	0.5	2	1	2	0.5	2	1	2	1	1	1	1	1	1
Ice	1	2	1	1	1	0.5	2	1	1	1	1	1	2	1	1	1	2	1
Fighting	1	1	1	1	1	1	1	1	1	2	2	0.5	0.5	1	1	0.5	1	2
Poison	1	1	1	1	0.5	1	0.5	0.5	2	1	2	0.5	1	1	1	1	1	0.5
Ground	1	1	2	0	2	2	1	0.5	1	1	1	1	0.5	1	1	1	1	1
Flying	1	1	1	2	0.5	2	0.5	1	0	1	1	0.5	2	1	1	1	1	1
Psychic	1	1	1	1	1	1	0.5	1	1	1	0.5	2	1	2	1	2	1	1
Bug	1	2	1	1	0.5	1	0.5	1	0.5	2	1	1	2	1	1	1	1	1
Rock	0.5	0.5	2	1	2	1	2	0.5	2	0.5	1	1	1	1	1	1	2	1
Ghost	0	1	1	1	1	1	0	0.5	1	1	1	0.5	1	2	1	2	1	1
Dragon	1	0.5	0.5	0.5	0.5	2	1	1	1	1	1	1	1	2	1	1	2	1
Dark	1	1	1	1	1	1	2	1	1	1	0	2	1	0.5	1	0.5	1	0.5
Steel	0.5	2	1	1	0.5	0.5	2	0	2	0.5	0.5	0.5	0.5	1	0.5	1	0.5	0.5
Fairy	1	1	1	1	1	1	0.5	2	1	1	1	0.5	1	1	0	0.5	2	1

Feature engineering
(generate features for 2 opponents)



Summary and next lecture

Next Lecture

- **Lecture:** dimensionality reduction
- **Lab:** implementation of dimensionality reduction techniques in Python
 - The description/data will be posted on piazza
- **About the lab:**
 - Bring your laptops
 - Please install Python 3
 - Main libraries: numpy, scipy, matplotlib, scikit-learn
 - Strongly recommended to use **anaconda**
 - <https://www.anaconda.com/download/>

Thank You!

