

Slotted Random-Access Wireless Network

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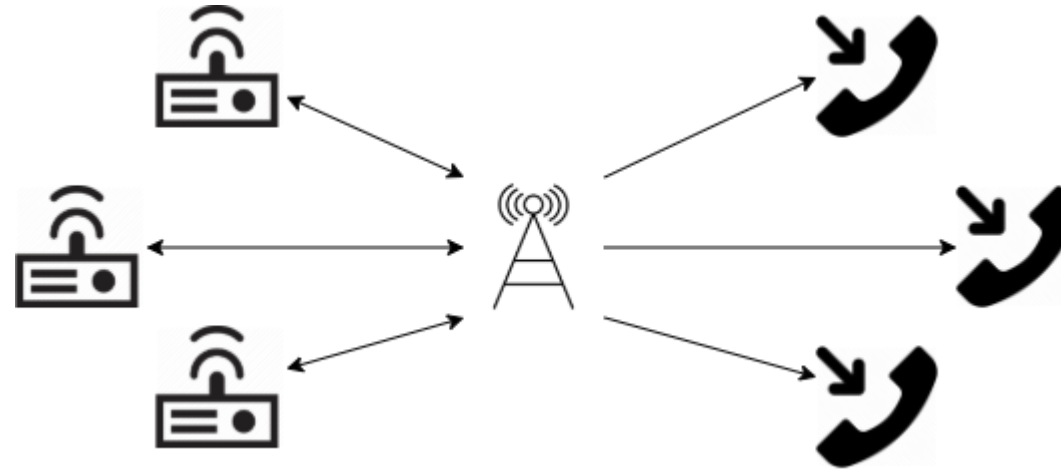


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Modelling

General Assumptions

- Transmission at the beginning
- Constant Packet Size
- No Propagation Error
- Unbounded Queues
- Tx/Rx Synchronization
- Collisions and Channel Choice



Factors

- N: Transmitter/Receiver Couples
- C: Number of Channels
- p: Sending Probability
- $1/\lambda$: Mean Inter-Arrival Time
- T_{slot} : Time Slot Duration

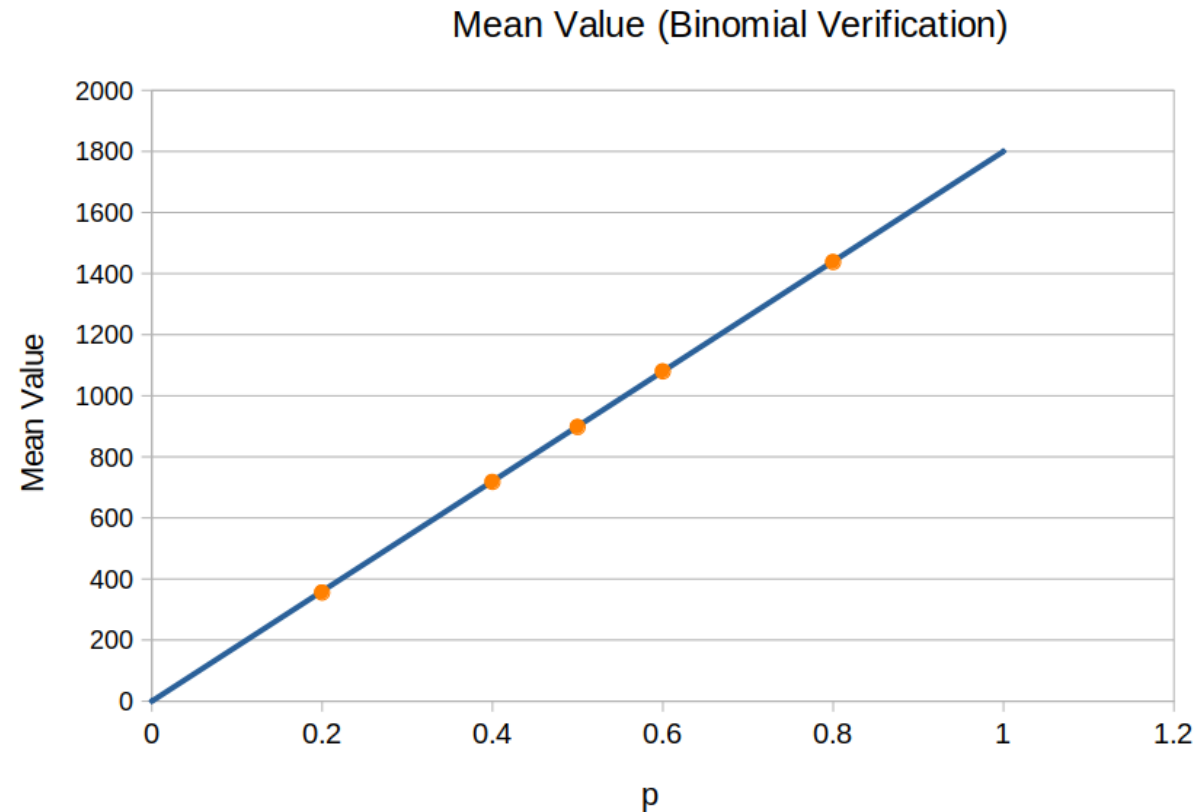
Verification (1)

Tests Performed

- Continuity Test
- Consistency Test
- Degeneracy Test
- Binomial Model
- Collision Model

Binomial Model

$N=1$; $C=1$; $1/\lambda = 1s$; $p = \{0.05, 0.1, 0.15, 0.2, 0.4, 0.5, 0.6, 0.8\}$



$$E[X] = np$$

● Simulation
—◆— Theoretical

Verification (2)

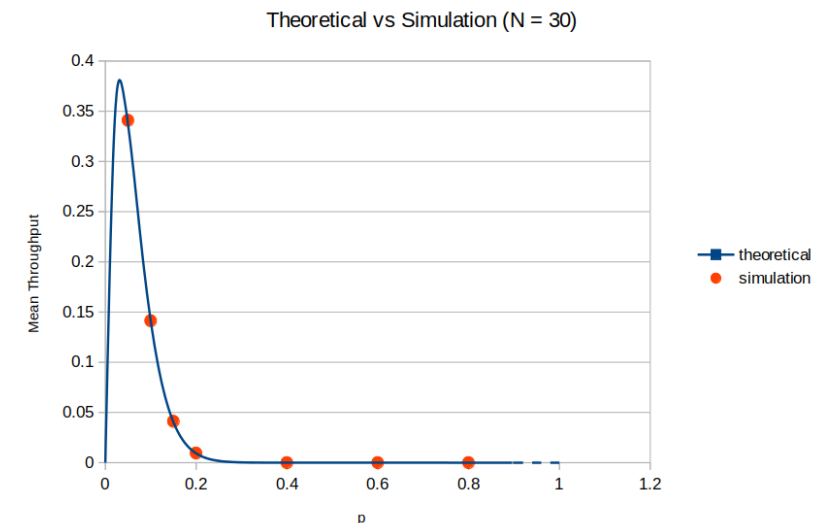
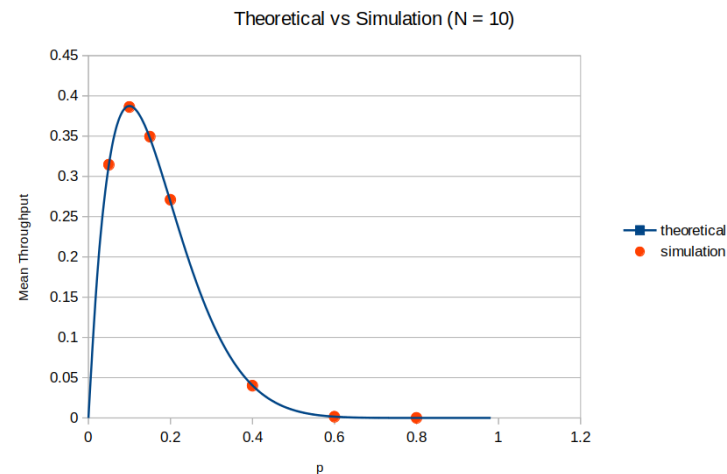
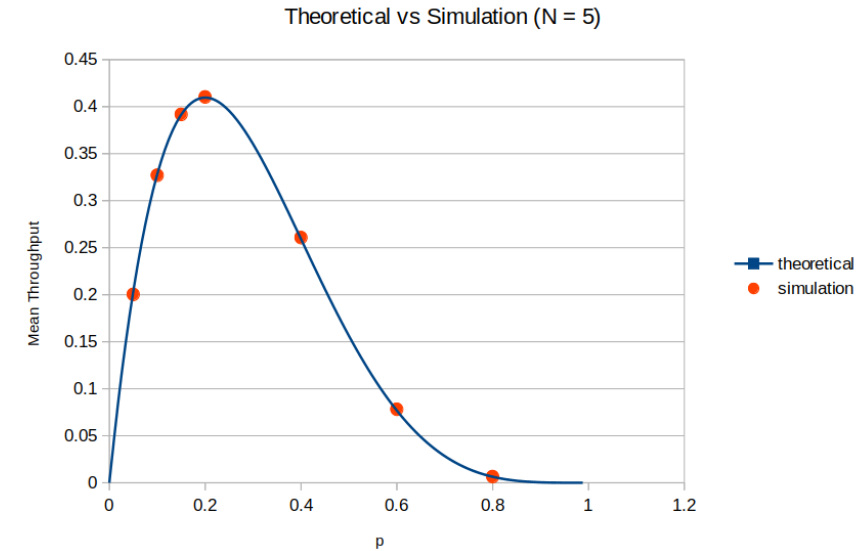
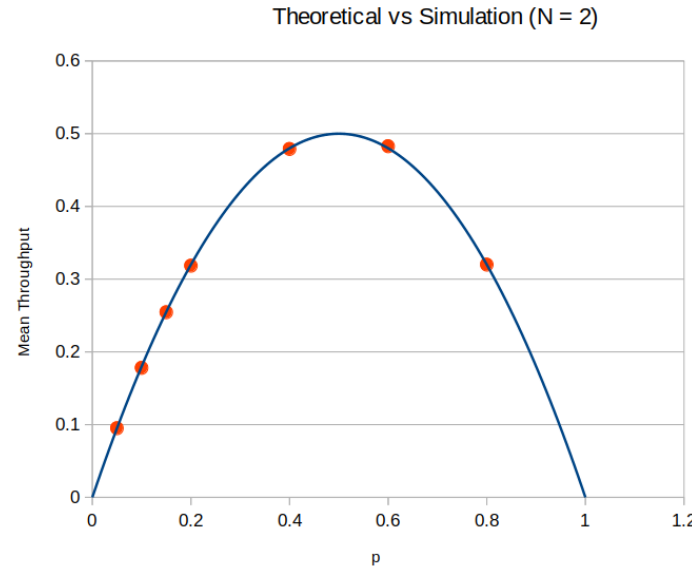
Collision Model

The probability of a successful transmission is equal to the probability that only one tx transmit, i.e.:

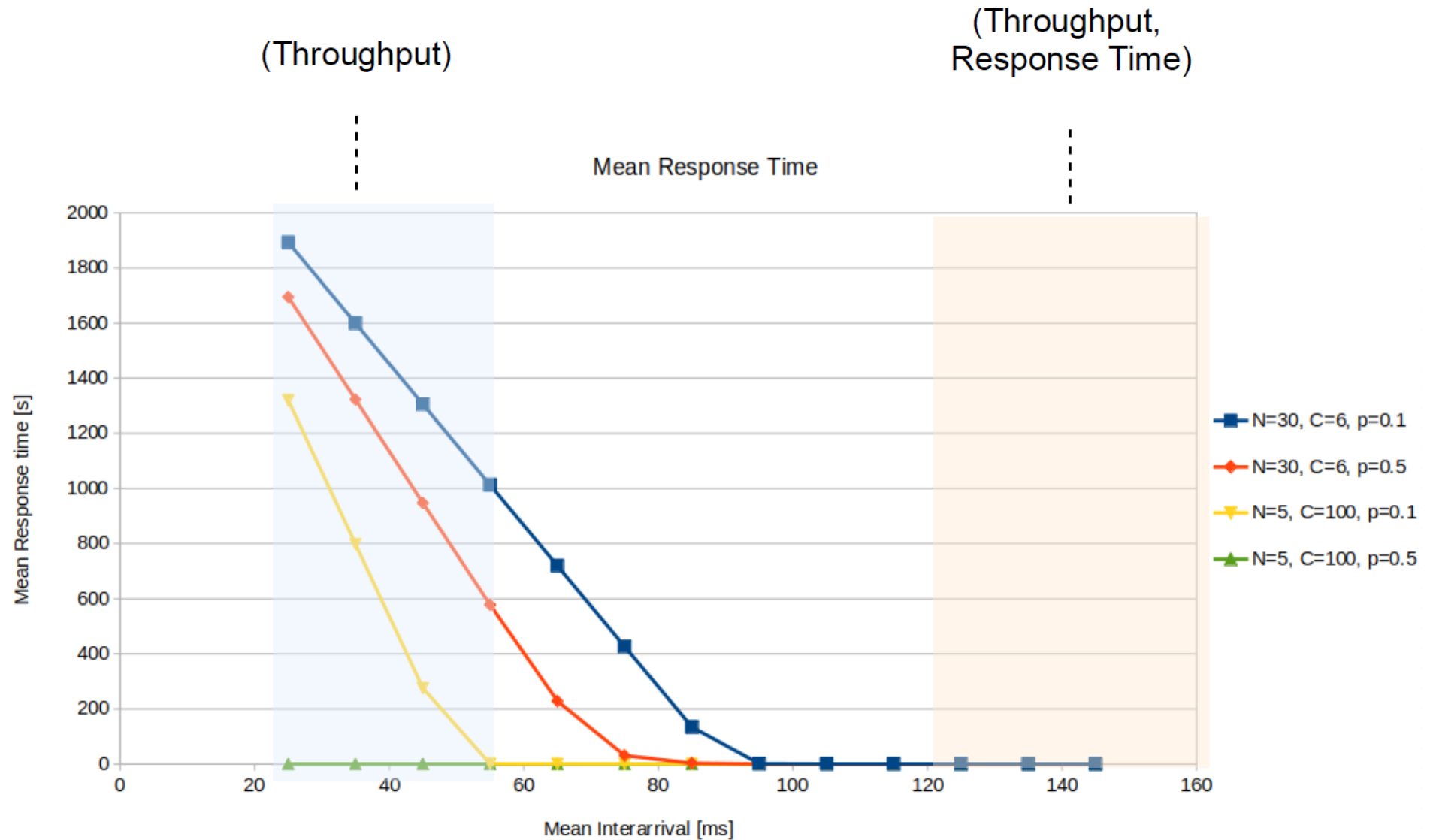
$$P\{\text{"only one tx transmit"}\} = N \cdot p \cdot (1 - p)^{N-1}$$

The latter can be seen as the mean throughput of the system in the single channel case:

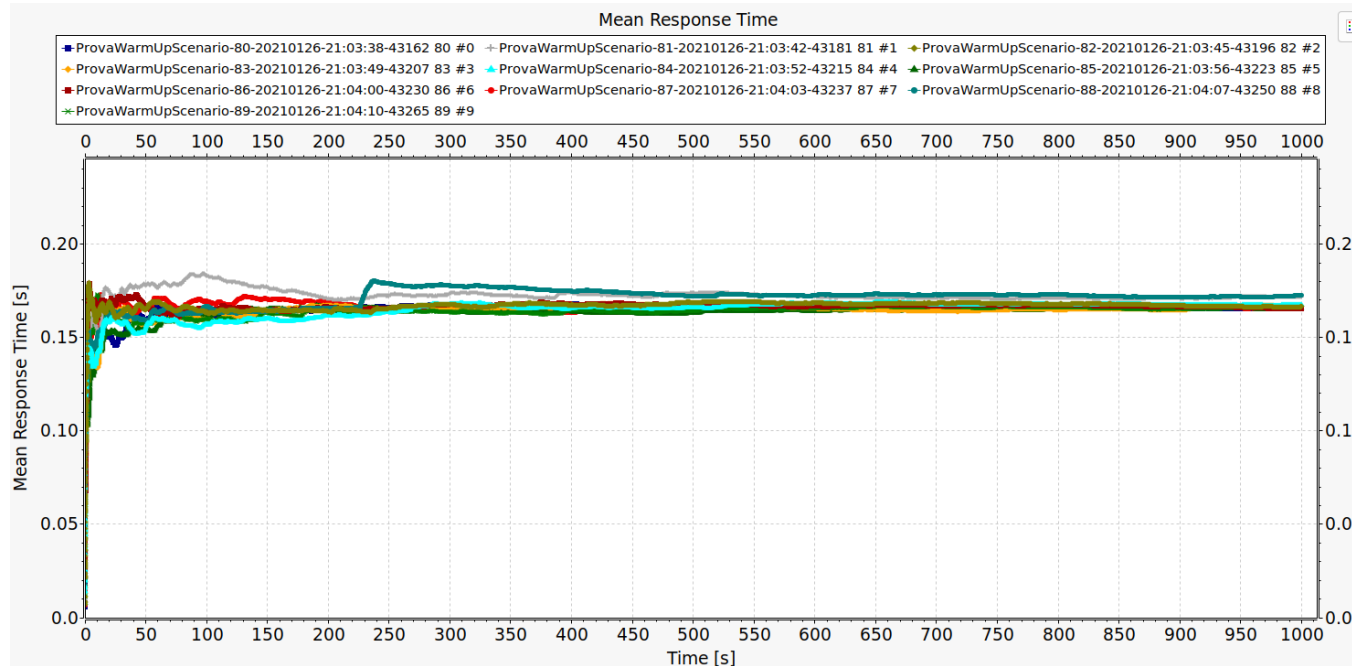
$$Tp(slot) = \frac{N_p}{N_t} = \frac{N_t \cdot P\{\text{"successful transmission"}\}}{N_t}$$



Response Time Limits



Scenario Calibration



WARMUP:

250s

SIMULATION DURATION:

5000s

Standard Scenario:

$N = [5, 30]; \quad C = [6, 100]; \quad 1/\lambda = [125\text{ms}, 500\text{ms}]; \quad p = [0.1, 0.5]; \quad T_{slot} = 5\text{ms};$

Response Time Explosion Scenario:

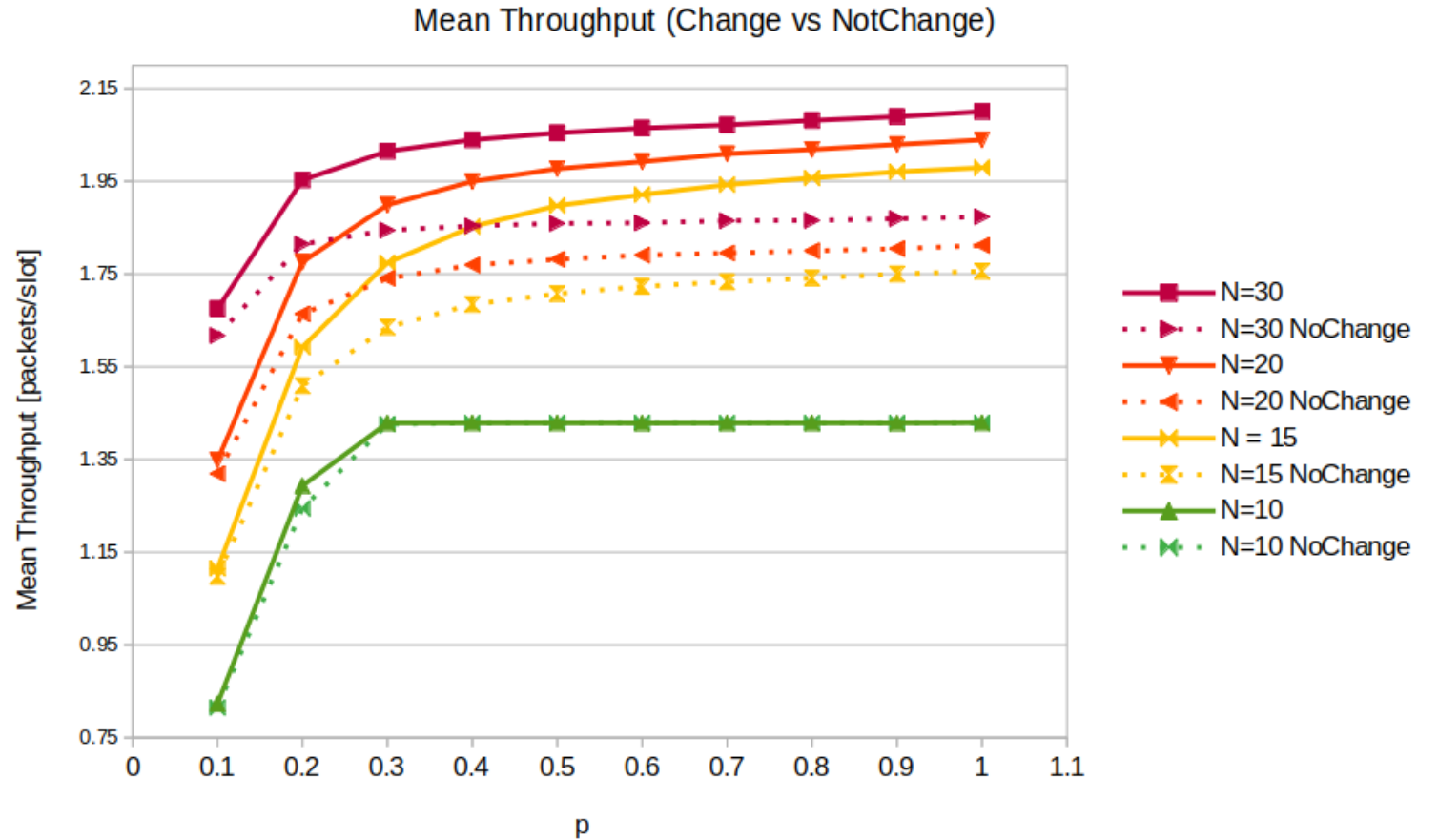
$N = [5, 30]; \quad C = [6, 100]; \quad 1/\lambda = [25\text{ms}, 55\text{ms}]; \quad p = [0.1, 1]; \quad T_{slot} = 5\text{ms};$

Response Time Explosion Scenario

Most Relevant Factors for Throughput

(Change vs NoChange)

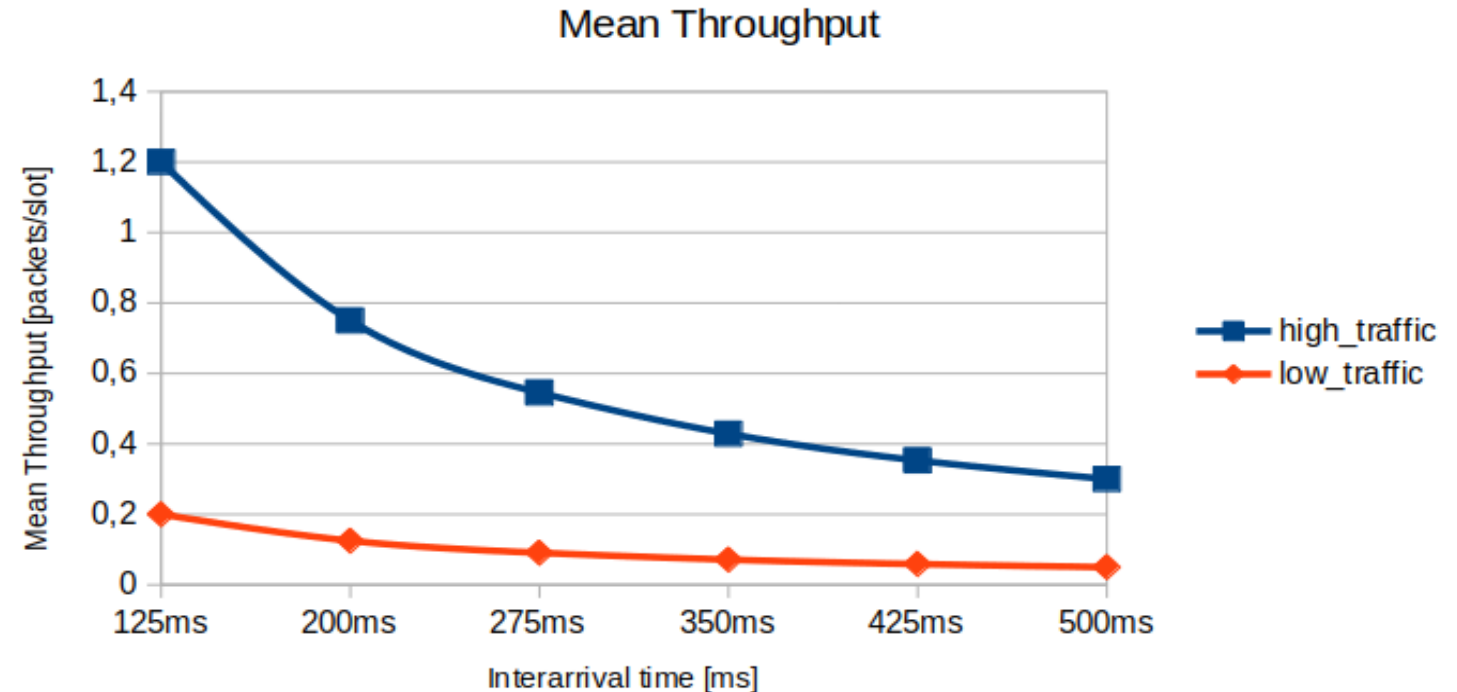
- Number Of Couples
 - 55.93% vs 53%
 - $q_A = 1.064$ vs $q_A = 1.032$
- Number of Channels
 - 9.218% vs 10.71%
 - $q_B = 0.432$ vs $q_B = 0.464$
- Jointly effect of Tx and Channels
 - 9.004% vs 10.47%
 - $q_{AB} = 0.427$ vs $q_{AB} = 0.458$



Standard Scenario - Throughput

Most Relevant Factors for Throughput

- Number of Couples
 - 48.44% of variability
 - $q_A = 0.3125$
- Mean Inter-Arrival Time
 - 34.15% of variability
 - $q_D = -0.2624$
- Jointly effect of Couples and $\frac{1}{\lambda}$
 - 17.39% of variability
 - $q_{AD} = -0.1872$



High Traffic Scenario

$N = 30$; $C = 6$; $p = 0.1$

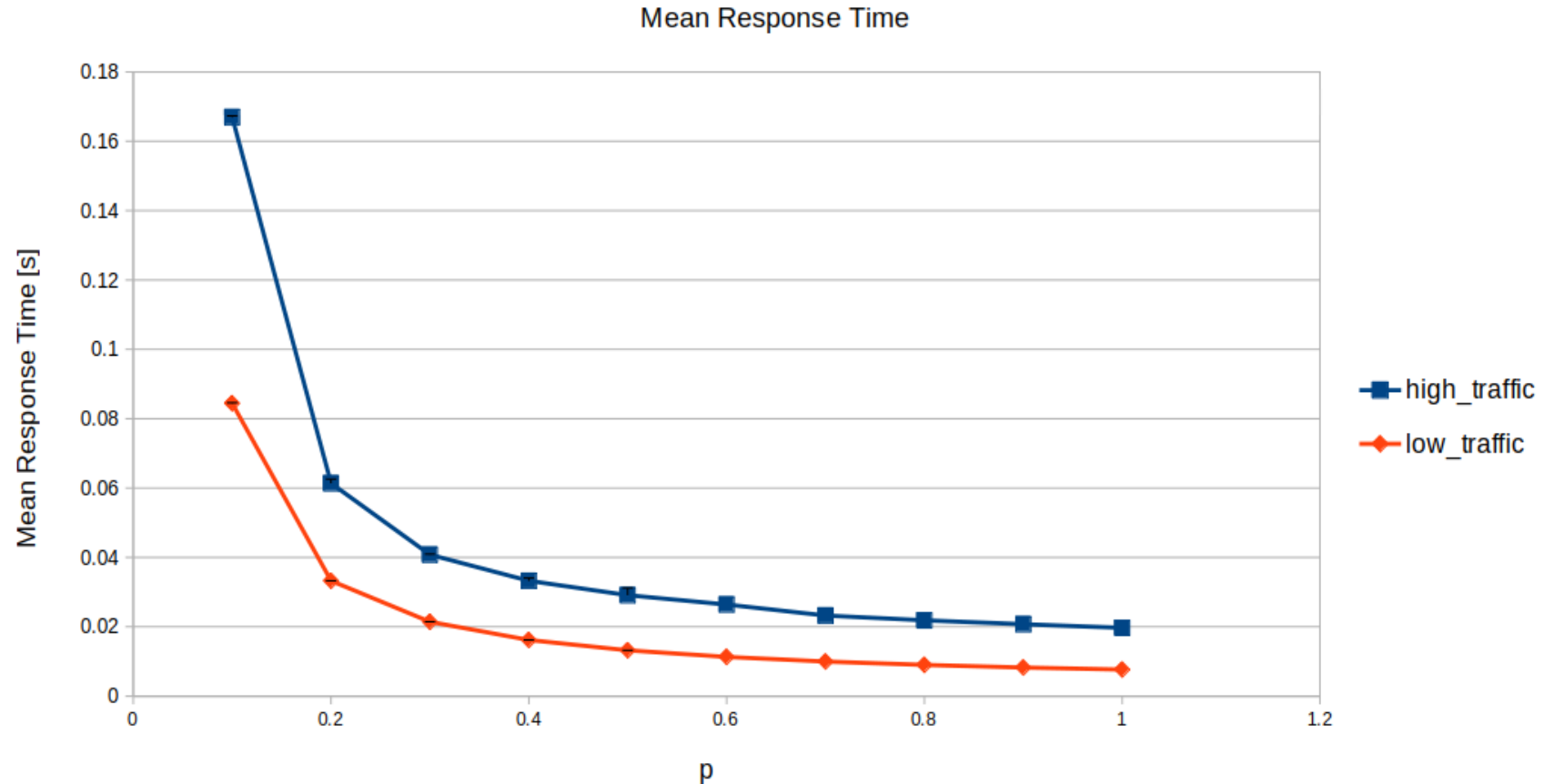
Low Traffic Scenario

$N = 5$; $C = 100$; $p = 0.1$

Standard Scenario – Response Time

Most Relevant Factors for Response Time

- Send Probability
 - 65.67% of variability
 - $q_C = -0.0339$
- Mean Inter-Arrival Time
 - 9.57% of variability
 - $q_D = -0.0129$



High Traffic Scenario: $N = 30$; $C = 6$; $1/\lambda = 125\text{ms}$

Low Traffic Scenario: $N = 5$; $C = 100$; $1/\lambda = 125\text{ms}$

Conclusions

1. General: an high **Send Probability** is better in both scenarios
2. Response Time Explosion Scenario: **No-Change of Channel** has **worst throughput**
3. Limited Response Time Scenario: the **Throughput** increases with the increasing of **N** and the decreasing of $\frac{1}{\lambda}$
4. Limited Response Time Scenario: the **Response Time** decreases with the decreasing of **N**

