

$$Q2 \quad T(n) = 3T\left(\frac{n}{\sqrt{3}}\right) + n^3 \lg n$$

$$\begin{matrix} a=3 \\ b=\sqrt{3} \end{matrix} \quad f(n) = n^3 \lg n$$

$$\therefore n^3 \lg n = \Omega(n^{1.09\sqrt{3}^3 + \epsilon}), \quad \epsilon > 0$$

$$af\left(\frac{n}{b}\right) = 3 \cdot \frac{n^3}{\sqrt{3}} \cdot \lg\left(\frac{n}{\sqrt{3}}\right) \leq c n^3 \lg n$$

$(c < 1)$

$c$  代  $0.9$  即可成立

$\therefore$  master theorem case 3

$$\Rightarrow T(n) = \Theta(f(n)) = \Theta(n^3 \lg n)$$