

# 2022 MIT Science Bowl High School Invitational

## Round 3

### TOSS UP

1) EARTH AND SPACE *Short Answer* By name or number, order the following three eons from most ancient to most recent:

- 1) Archean
- 2) Proterozoic
- 3) Hadean

ANSWER: 3, 1, 2

### BONUS

1) EARTH AND SPACE *Multiple Choice* Phytoplankton in the open ocean release sulfate aerosols which can act as condensation nuclei. Which of the following changes would you expect to occur if a large algal bloom were to occur in the open ocean?

- W) Decrease in cloud cover
- X) Increase in the Earth's albedo
- Y) Increased rain pH
- Z) Increased upwelling in the ocean

ANSWER: X) Increase in the Earth's albedo

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### TOSS UP

2) PHYSICS *Short Answer* By name or number, identify all of the following three changes that would increase the resistance of a metallic resistor:

- 1) Stretching to increase the length while keeping the volume constant
- 2) Increasing the temperature of the resistor, assuming the thermal coefficient of expansion is negligible compared to that of resistivity
- 3) Increasing all physical dimensions of the resistor by the same factor

ANSWER: 1 and 2 (ACCEPT: All but 3)

### BONUS

2) PHYSICS *Short Answer* A square loop of wire in the  $xy$ -plane has a side length of 2 centimeters and a resistance of  $10^{-4}$  ohms. A uniform magnetic field starts at 0 teslas and increases uniformly over 2 seconds until it reaches a value of 3 teslas in the positive  $z$  direction. While the magnetic field is turning on, what is the magnitude of the induced current in the wire in amperes?

ANSWER: 6

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### TOSS UP

3) ENERGY *Short Answer* The Davis Lab at MIT is working on coupling pulse-labeling with quantitative mass spectrometry, which can detect the synthesis and degradation rates of proteins. Protein degradation is known to be promoted by E3 ligases through the attachment of what molecule?

ANSWER: Ubiquitin

### BONUS

3) ENERGY *Multiple Choice* Researchers in the Davis Lab at MIT also develop analytical methods for investigating macromolecular machines, such as with single particle cryo-EM data. Though still a relatively recent tool, cryo-EM has already surpassed X-ray crystallography in determining the structure of which of the following classes of proteins?

- W) Nuclear
- X) Cytoplasmic
- Y) Membrane
- Z) Extracellular

ANSWER: Y) Membrane

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### TOSS UP

4) CHEMISTRY *Multiple Choice* Because elemental chlorine gas is highly corrosive, it is often generated in small amounts in the laboratory rather than being bought and used directly. Which of the following methods could be used to generate chlorine gas?

- W) Addition of concentrated sulfuric acid to a solution of sodium hypochlorite
- X) Addition of concentrated hydrochloric acid to a solution of sodium hypochlorite
- Y) Addition of concentrated sulfuric acid to a solution of sodium chloride
- Z) Addition of concentrated hydrochloric acid to a solution of sodium chloride

ANSWER: X) Addition of concentrated hydrochloric acid to a solution of sodium hypochlorite

### BONUS

4) CHEMISTRY *Short Answer* When gaseous nitrogen dioxide is stored in a closed container, it establishes an equilibrium with its dimer, dinitrogen tetroxide. This exothermic reaction can be represented by the equation  $2\text{NO}_2(\text{g}) \rightleftharpoons \text{N}_2\text{O}_4(\text{g})$  (read: *two N-O-2 g in equilibrium with N-2-O-4 g*). By name or number, identify all of the following three statements that are true regarding this reaction:

- 1) As temperature increases, the forward reaction becomes more favorable
- 2) As temperature increases, the equilibrium constant increases
- 3) For this reaction at 100 kelvin,  $K_p > K_c$

ANSWER: None

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### TOSS UP

5) MATH *Short Answer* Let  $x$  be the repeating decimal  $0.\overline{900}$  (read: *zero point nine zero zero repeating*). What is the value of  $x$  as a fraction in lowest terms?

ANSWER:  $100/111$

### BONUS

5) MATH *Short Answer* Let  $z$  be the product of  $(3 + 4i)$  and  $(10 - 5i)$ . What is the product of  $z$  and its conjugate?

ANSWER: 3125

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### TOSS UP

6) BIOLOGY *Multiple Choice* Which of the following amino acids does NOT contain nitrogen in its side chain?

- W) Glutamine
- X) Tryptophan (*TRIP-tuh-fan*)
- Y) Arginine (*AAR-juh-neen*)
- Z) Methionine (*muh-THY-uh-neen*)

ANSWER: Z) Methionine

### BONUS

6) BIOLOGY *Short Answer* In bacteria, the start codon codes for what modified amino acid?

ANSWER: *N*-Formylmethionine (ACCEPT: Formylmethionine, fMet, HCO-Met, For-Met)

### TOSS UP

7) EARTH AND SPACE *Short Answer* What is the name for a chain of extinct volcanoes that gets progressively older as one travels away from a hotspot?

ANSWER: Nematath (ACCEPT: Hotspot track)

### BONUS

7) EARTH AND SPACE *Short Answer* Magma intrudes into a karstic (*KAR-stick*) region and many dikes form in the limestone bedrock. What rock would the limestone bedrock metamorphose (*meh-tuh-MORE-phose*) into in the aureole (*ore-ee-OLE*) of the magma?

ANSWER: Marble

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### TOSS UP

8) MATH *Short Answer* What is the floor of the square root of 420?

ANSWER: 20

### BONUS

8) MATH *Short Answer* Three of the vertices of a cube of side length 7 form an equilateral triangle. What is the area of this triangle?

ANSWER:  $49\sqrt{3}/2$

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### TOSS UP

9) PHYSICS *Short Answer* An airplane flies forward at constant velocity. Its engines apply a total forward thrust of 50 kilonewtons, and expend a power of 10 megawatts. What is the speed of the airplane, in meters per second?

ANSWER: 200

### BONUS

9) PHYSICS *Short Answer* Two objects of masses 1 kilogram and 3 kilograms are connected by a spring with a spring constant of 3 newtons per meter. What is the period of oscillation of this system, expressed in terms of  $\pi$  and in seconds?

ANSWER:  $\pi$

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### TOSS UP

10) BIOLOGY *Short Answer* A desmotubule surrounded by a cytoplasmic sleeve forms what structure that connects the cytoplasm of adjacent plant cells?

ANSWER: Plasmodesma (ACCEPT: Plasmodesmata)

### BONUS

10) BIOLOGY *Short Answer* While most introns contain "useless" information that holds no value, in some genes specific removal of different introns can cause multiple proteins to be generated from a single transcript. What is this process called?

ANSWER: Alternative splicing

### TOSS UP

11) CHEMISTRY *Short Answer* By name or number, rank the following three elements by increasing first ionization energy:

- 1) Nitrogen
- 2) Oxygen
- 3) Fluorine

ANSWER: 2, 1, 3

### BONUS

11) CHEMISTRY *Short Answer* What is the oxidation state of the central nitrogen atom in the most representative resonance structure of  $\text{N}_2\text{O}$ ?

ANSWER: +2

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### TOSS UP

12) ENERGY *Short Answer* Researchers at MIT are studying methods of using lasers to cool clouds of atoms down to temperatures less than 1 microkelvin. What is the name for the ultracold state of matter produced in this manner?

ANSWER: Bose-Einstein condensate

### BONUS

12) ENERGY *Short Answer* Researchers from MIT's Plasma Science and Fusion Center used an optimization methodology developed for machine learning to drastically reduce the CPU time required to predict the temperature of density profiles of a magnetically confined plasma. Plasmas are often described as "ionized gas", which can be misleading. Unlike plasma, what velocity distribution do gas particles usually follow?

ANSWER: Maxwell-Boltzmann distribution



### TOSS UP

13) PHYSICS *Short Answer* A 6 kilogram bowling ball is slipping without rolling on a flat frictionless surface at a speed of 4 meters per second. Its trajectory will take it 1 meter from a bowling pin at closest approach. When the bowling ball is 10 meters from the pin, what is the magnitude of its angular momentum about the pin, in kilogram meters squared per second?

ANSWER: 24

### BONUS

13) PHYSICS *Multiple Choice* Which of the following is closest to the frequency in hertz of a pendulum with length 2.0 meters, if it were in a rocket ship on Earth accelerating at 3  $g$ 's upwards?

W) 0.06

X) 0.7

Y) 1.8

Z) 10.9

ANSWER: X) 0.7

### TOSS UP

14) MATH *Multiple Choice* Let  $f(x)$  denote the sum of the largest prime strictly less than  $x$  and the smallest prime strictly greater than  $x$ . What is the smallest value of  $x$  such that  $f(x)$  exceeds 200?

- W) 100
- X) 101
- Y) 102
- Z) 103

ANSWER: Y) 102

### BONUS

14) MATH *Short Answer* 4 fair six-sided dice are rolled. What is the probability that exactly three of them result in the same number?

ANSWER: 5/54

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### TOSS UP

15) EARTH AND SPACE *Multiple Choice* Stars that readily undergo the CNO cycle would have which of the following interiors?

- W) Radiative core and radiative envelope
- X) Radiative core and convective envelope
- Y) Convective core and radiative envelope
- Z) Convective core and convective envelope

ANSWER: Y) Convective core and radiative envelope

### BONUS

15) EARTH AND SPACE *Multiple Choice* Which of the following asteroid classes is most common in the outer asteroid belt?

- W) M-type
- X) S-type
- Y) C-type
- Z) L-type

ANSWER: Y) C-type

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### TOSS UP

16) CHEMISTRY *Short Answer* By name or number, rank the following four elements by increasing melting point of their standard state:

- 1) Carbon
- 2) Argon
- 3) Iron
- 4) Bromine

ANSWER: 2, 4, 3, 1

### BONUS

16) CHEMISTRY *Short Answer* Consider the reactions  $A \rightleftharpoons 2B$  (read: *A in equilibrium with two B*) and  $B \rightleftharpoons C$  (read: *B in equilibrium with C*). If the equilibrium constants for these reactions are 0.4 and 0.5, respectively, what is the equilibrium constant for the reaction  $4C \rightleftharpoons 2A$  (read: *four C in equilibrium with two A*)?

ANSWER: 100

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### TOSS UP

17) ENERGY *Short Answer* Researchers in the Solomon group at MIT are studying the healing of the Antarctic ozone hole, which was caused mainly by chlorofluorocarbons and other ozone-depleting substances. In the structure of the ozone molecule, what is the hybridization of the central oxygen atom?

ANSWER:  $sp^2$

### BONUS

17) ENERGY *Short Answer* Researchers in the Swager group at MIT have developed a chemiresistive sensor that exhibits selectivity for methane over heavier hydrocarbons like benzene and toluene (*TALL-you-een*). To two significant figures and in kelvin, at what temperature is the effusion rate of toluene equal to the effusion rate of methane at 400 kelvin?

ANSWER: 2300 (ACCEPT:  $2.3 \times 10^3$ )

### TOSS UP

18) BIOLOGY *Multiple Choice* How many sister chromatids are in a single human cell during the G2 phase of mitosis?

- W) 23
- X) 46
- Y) 92
- Z) 184

ANSWER: Y) 92

### BONUS

18) BIOLOGY *Short Answer* What is the term for the proteins on chromosomes that connect to the spindle fibers during mitosis?

ANSWER: Kinetochores

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### TOSS UP

19) EARTH AND SPACE *Multiple Choice* Which of the following types of resonance do quasi-satellites of a planet exhibit with the planet?

- W) 1 to 1
- X) 2 to 1
- Y) 4 to 5
- Z) 2 to 3

ANSWER: W) 1 to 1

### BONUS

19) EARTH AND SPACE *Short Answer* What effect, caused by inverse Compton scattering, allows the cosmic microwave background to map out regions of high and low density?

ANSWER: Sunyaev-Zeldovich effect (ACCEPT: SZ effect)

### TOSS UP

20) PHYSICS *Multiple Choice* An object moving through a fluid at a velocity  $v$  experiences a drag force. Which of the following best describes the dependence of this drag force on the velocity?

- W) Proportional to  $v$  at all velocities
- X) Proportional to  $v^2$  at all velocities
- Y) Proportional to  $v$  at low velocities and proportional to  $v^2$  at high velocities
- Z) Proportional to  $v$  at low velocities and inversely proportional to  $v$  at high velocities

ANSWER: Y) Proportional to  $v$  at low velocities and proportional to  $v^2$  at high velocities

### BONUS

20) PHYSICS *Multiple Choice* On the  $x$ -axis, a negative 2 coulomb charge is placed at  $x = 2$  meters, and a positive 1 coulomb charge is placed at the origin. At how many points on the  $x$ -axis can a positive 1 coulomb charge be placed, such that it experiences no net force?

- W) 0
- X) 1
- Y) 2
- Z) 3

ANSWER: X) 1

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### TOSS UP

21) MATH *Short Answer* If it takes 10 builders 10 days to build 10 boats, how long does it take 5 builders to build 20 boats?

ANSWER: 40

### BONUS

21) MATH *Short Answer* An arithmetic sequence has first term 1, and the sum of its first 100 terms is 2000. What is the value of the common difference between adjacent terms?

ANSWER: 38/99

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### TOSS UP

22) CHEMISTRY *Multiple Choice* Which of the following pairs of compounds could be used to set up an effective buffer?

- W) HF and NaF
- X) HCl and NaCl
- Y) HBr and NaBr
- Z) HI and NaI

ANSWER: W) HF and NaF

### BONUS

22) CHEMISTRY *Short Answer* The  $pK_a$  of HF is 3.14. To two significant figures and in grams, how much NaF must be added to a 500 milliliter sample of 1 molar hydrofluoric acid to produce a solution buffered at a pH of 4.14?

ANSWER: 210

### TOSS UP

23) BIOLOGY *Short Answer* Paracoumaryl (*pair-uh-COO-muh-ril*) alcohol is the monomer of what compound in the secondary cell wall of plants that provides compressive strength and stiffness?

ANSWER: Lignin

### BONUS

23) BIOLOGY *Short Answer* During late telophase in plant cell mitosis, the microtubules (*mai-krow-TOO-byoolz*) of the daughter cells form what structure that guides Golgi vesicles that eventually form the cell plate?

ANSWER: Phragmoplast

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