Cálculo I A - Professora: Luciana Prado Mouta Pena (UFF)

Exercícios da apostila da Profa Valéria Zuma

1ª LISTA DE EXERCÍCIOS

Resolva, se possível, os seguintes limites:

1)
$$\lim_{x \to 1} (5x^3 - 2x - 4) = -1$$

2)
$$\lim_{x \to -1} (3x^4 - 2x^3 - 4x^2 + 2x + 1) = 0$$

3)
$$\lim_{x \to -2} (2x^5 - x^3 + 10) = -46$$

4)
$$\lim_{x \to 2} \sqrt[3]{\frac{2x^3 + 2x^2 + 8}{x^2 + 2x - 4}} = 2$$

5)
$$\lim_{x \to 5} \frac{x-5}{\sqrt{3+x}} = 0$$

6)
$$\lim_{x \to 4} \frac{x^2 - 16}{x^2 - 5x + 4} = \frac{8}{3}$$

7)
$$\lim_{x \to 1} \frac{x^4 - 1}{x^2 - 1} = 2$$

8)
$$\lim_{x \to 2} \frac{x^2 - 7x + 10}{x^2 - x - 2} = -1$$

9)
$$\lim_{x \to 2} \frac{x^3 - 8}{x - 2} = 12$$

10)
$$\lim_{x \to -1} \frac{x^4 - 6x^2 + 5}{x^2 - 1} = -4$$

11)
$$\lim_{x\to 0} \frac{3x^4 - x^2 + x}{4x^3 - 2x} = -\frac{1}{2}$$

12)
$$\lim_{x \to 1} \frac{2x^3 - 2x}{x^2 - 3x + 2} = -4$$

13)
$$\lim_{t \to 0} \frac{(x+t)^4 - x^4}{t} = 4x^3$$

14)
$$\lim_{x \to 0} \frac{\sqrt{1+x} - 1}{x} = \frac{1}{2}$$

15)
$$\lim_{x \to 1} \frac{3x^4 - 2x^3 + 2x^2 - x - 2}{x^3 - x^2 + 2x - 2} = 3$$
16)
$$\lim_{x \to -2} \frac{x^3 - 2x + 4}{x^4 + 3x - 10} = -\frac{10}{29}$$

16)
$$\lim_{x \to -2} \frac{x^3 - 2x + 4}{x^4 + 3x - 10} = -\frac{10}{29}$$

17)
$$\lim_{x \to 6} \frac{\sqrt{3+x} - 3}{x - 6} = \frac{1}{6}$$

18)
$$\lim_{x \to 0} \frac{\sqrt{2 + x} - \sqrt{2 - x}}{x} = \frac{\sqrt{2}}{2}$$

19)
$$\lim_{x \to 2} \frac{2 - \sqrt{x + 2}}{x^2 - 4} = -\frac{1}{16}$$

20)
$$\lim_{x \to 3} \frac{\sqrt{4x - 3} - 3}{\sqrt{2x - 2} - 2} = \frac{4}{3}$$

21)
$$\lim_{x \to 4} \frac{3 - \sqrt{5 + x}}{1 - \sqrt{5 - x}} = -\frac{1}{3}$$

22)
$$\lim_{x \to 0} \frac{\sqrt{x^2 + m^2} - m}{\sqrt{x^2 + q^2} - q} = \frac{q}{m}$$

23)
$$\lim_{x \to 9} \frac{\sqrt{x} - 3}{x - 9} = \frac{1}{6}$$

24)
$$\lim_{x \to 8} \frac{x-8}{\sqrt[3]{x}-2} = 12$$

25)
$$\lim_{x \to 1} \frac{\sqrt{x} - 1}{\sqrt[3]{x} - 1} = \frac{3}{2}$$

Cálculo I A - Professora: Luciana Prado Mouta Pena (UFF)

Exercícios da apostila da Profª Valéria Zuma

2º parte: Limite Finito de uma função quando x tende a um valor Infinito

8)
$$\lim_{x \to +\infty} \frac{3x+2}{5x-1} = \frac{3}{5}$$

9)
$$\lim_{x \to -\infty} \frac{4x-1}{3x^2+5x-2} = 0$$

10)
$$\lim_{x \to +\infty} \frac{3 - 2x}{5x + 1} = -\frac{2}{5}$$

11)
$$\lim_{x \to +\infty} \frac{x^2 - 3x + 4}{3x^3 + 5x^2 - 6x + 2} = 0$$

12)
$$\lim_{x \to -\infty} \frac{x^2 + x + 1}{(x+1)^3 - x^3} = \frac{1}{3}$$

13)
$$\lim_{x \to -\infty} \frac{(3x+2)^{30}}{2x^{10}(3x+1)^{15}(4x-1)^5} = \frac{3^{15}}{2^{11}}$$

14)
$$\lim_{x \to +\infty} \frac{\sqrt{x^2 - 2x + 1}}{x + 1} = 1$$

15)
$$\lim_{x \to -\infty} \frac{\sqrt{x^2 - 2x + 1}}{x + 1} = -1$$

16)
$$\lim_{x \to +\infty} \frac{\sqrt{x^2 + x + 1}}{x + 1} = 1$$

17)
$$\lim_{x \to -\infty} \frac{\sqrt{x^2 + x + 1}}{x + 1} = -1$$

18)
$$\lim_{x \to -\infty} \frac{x + \sqrt[3]{x}}{x^2 + 1} = 0$$

19)
$$\lim_{x \to +\infty} \frac{\sqrt[3]{x^2 + 1}}{x + 1} = 0$$

20)
$$\lim_{x \to +\infty} (\sqrt{x+4} - \sqrt{x+2}) = 0$$

21)
$$\lim_{x \to +\infty} \left(\sqrt{x \cdot (x+4)} - x \right) = 2$$

22)
$$\lim_{x \to -\infty} \frac{3x^5 + 2x^3 + 5}{5x^5 + 4x^3 + 2x + 1} = \frac{3}{5}$$

23)
$$\lim_{x \to +\infty} x \cdot \left(\sqrt{x^2 + 2} - x\right) = 1$$

24)
$$\lim_{x \to -\infty} \frac{4x - 3}{3x + 2} = \frac{4}{3}$$

25)
$$\lim_{x \to +\infty} \frac{\sqrt{x^2 - 3}}{\sqrt[3]{x^3 + 1}} = 1$$

26)
$$\lim_{x \to -\infty} \frac{x^2 + 4}{8x^3 - 1} = 0$$

27)
$$\lim_{x \to +\infty} \frac{(2x-3)^{45}}{x^{15}(x+1)^{20}(x+2)^{10}} = 2^{45}$$

28)
$$\lim_{x \to +\infty} \frac{(2x-3)^3 \cdot (3x-2)^2}{x^5} = 72$$

29)
$$\lim_{x \to +\infty} \frac{2x^2 - 3x - 5}{\sqrt{x^4 + 1}} = 2$$

30)
$$\lim_{x \to -\infty} \frac{2x^2 - 3x - 5}{\sqrt{x^4 + 1}} = 2$$

31)
$$\lim_{x \to -\infty} \frac{x}{\sqrt[3]{x^3 - 1000}} = 1$$

32)
$$\lim_{x \to +\infty} \left(\sqrt{x^2 + 3x + 2} - x \right) = \frac{3}{2}$$

33)
$$\lim_{x \to +\infty} \left(\sqrt{x^2 + 1} - \sqrt{x^2 - 1} \right) = 0$$

34)
$$\lim_{x \to +\infty} \left(\sqrt{x^2 + ax + b} - x \right) = \frac{a}{2}$$

35)
$$\lim_{x \to +\infty} \frac{x + \sqrt[3]{x^3 - 5x^2 - 2}}{\sqrt[3]{x^3 + 1}} = 2$$

36)
$$\lim_{x \to +\infty} \frac{\sqrt{x} - \sqrt{x+1}}{\sqrt{x+2} - \sqrt{x+3}} = 1$$

37)
$$\lim_{x \to +\infty} \frac{\sqrt{x^2 + 2x + 4} - x}{x - \sqrt{x^2 - x + 1}} = 2$$

38)
$$\lim_{x \to +\infty} \left(\sqrt{x + \sqrt{x + \sqrt{x}}} - \sqrt{x} \right) = \frac{1}{2}$$

39)
$$\lim_{x \to +\infty} \frac{\sqrt{x} + \sqrt[4]{x} + \sqrt[4]{x}}{\sqrt{4x + 1}} = \frac{1}{2}$$

40)
$$\lim_{x \to +\infty} \frac{2x+3}{x+\sqrt[3]{x}} = 2$$