

# The Innovation Long-Run Risk Component

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## Abstract

This paper provides robust empirical evidence that shocks to aggregate Research and Development (R&D) have persistent effects on macroeconomic dynamics and represent a significant risk for investors, as predicted by the ‘long-run risk’ literature. The analysis focuses on a single variable, ‘effective R&D’, which captures the entire contribution of R&D to productivity growth, flexibly accounting for knowledge spillovers and product proliferation effects. Deviations of effective R&D from its equilibrium level can be empirically identified leveraging the error correction term in the cointegration relationship among R&D, total factor productivity, and the labor force. In US data, structural effective R&D shocks affect productivity and consumption growth rates beyond business cycle horizons and are associated with a significant risk premium in a cross section of stock and bond portfolios (around 2% annually), with cash-flow sensitivities proving a key determinant.

**Keywords:** Asset Pricing, Long-run risk, Innovation, Cointegration

**JEL Codes:** E32, E44, G12, O30

## 1 Introduction

Investments in Research and Development (R&D) have a profound and well-documented impact on the economy. At the aggregate level, R&D has been linked to slow-moving fluctuations in macroeconomic quantities such as productivity and consumption (Comin and Gertler 2006; Evans et al. 1998), and theory has shown that this nexus carries substantial implications for asset prices (Kung and Schmid 2015). The underlying mechanism is that of the ‘Long-Run Risk’ (LRR) framework from Bansal and Yaron (2004), who first demonstrated how persistence in consumption growth enables macroeconomic models to account for the large equity risk premium observed in financial markets, a premium that far exceeds predictions based on observed consumption growth volatility alone (Mehra and Prescott 1985). This

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framework has since become a central reference in macro-finance research,<sup>1</sup> but has also faced sustained criticism,<sup>2</sup> making rigorous empirical validation of models built on it essential.

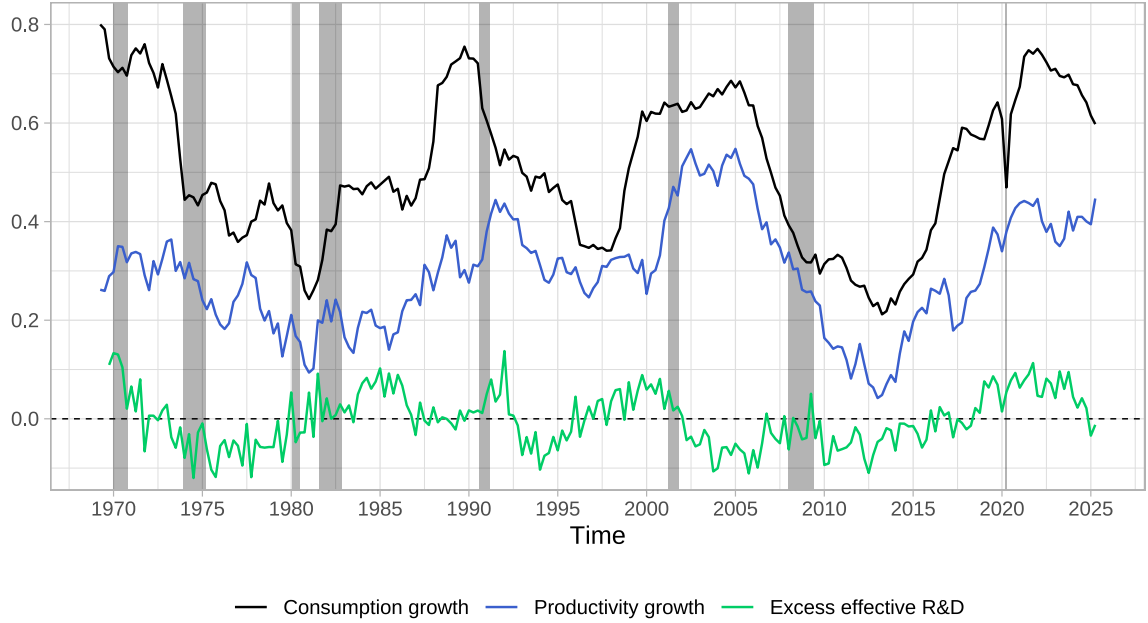
This paper provides robust empirical evidence that shocks to US aggregate R&D have persistent effects on productivity and consumption growth, and carry substantial implications for asset prices. Specifically, I focus on a theoretical measure of aggregate R&D – ‘effective R&D’ – that uniquely summarizes the total impact of R&D on productivity growth, accounting for virtually any degree of spillover and product proliferation effects. I then propose an empirical framework to recover its time series and the associated structural shocks, illustrating their persistent effects on the economy. Finally, I show that structural shocks to effective R&D, derived from a theoretically identified system, serve as a risk factor with significant power in pricing the cross-section of financial assets. This represents a dual novelty: both in using aggregate R&D as the basis for a risk factor and in employing structural shocks from a theoretically identified system.

In the long-run risk framework, agents have recursive preferences as in Epstein and Zin (1989), which are characterized by an aversion to swings in forecasts of distant future consumption growth. Persistent shocks can induce such fluctuations with very small variance, making them a powerful theoretical feature by allowing models to account for sizable risk premia with little added complexity, but also an elusive one to validate empirically, since low-frequency processes are challenging to identify in finite samples. A growing literature has tackled the empirical challenge directly, either by devising refined empirical strategies (Dew-Becker and Giglio 2016; Gourieroux and Jasiak 2024; Ortu et al. 2013; Schorfheide et al. 2018) or by exploiting new data (Liu and Matthies 2022). Another strand has derived the LRR pivotal conditions as reduced forms of richer structural models, yielding additional testable implications (e.g. Kaltenbrunner and Lochstoer 2010). Within this framework, Croce (2014) showed that the predictable component of productivity growth is persistent and does transmit to consumption growth. He termed this component the ‘productivity long-run risk component’, which Kung and Schmid (2015) later rationalized as originating from persistent fluctuations in R&D investment. This paper provides direct empirical evidence on the macroeconomic mechanism and financial predictions developed in this theoretical framework, while contributing a novel econometric procedure, grounded in macroeconomic theory, to identify a process that captures revisions to long-run expectations of innovation – an ‘innovation long-run risk component’. The results in this study depart from the predictions in Kung and Schmid (2015) only regarding the specific mechanics behind R&D shock propagation, which empirically does not appear to arise from the persistence of effective R&D itself, but rather from its interaction with external macroeconomic factors. Figure 1 displays the estimated effective R&D, along with the processes it is expected to drive, i.e., the components with half-lives between 8 and 16 years of consumption and productivity growth rates, whose comovement is apparent.

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<sup>1</sup>Applications include, among others, exchange rate dynamics (Colacito and Croce 2011), climate change asset pricing (Bansal et al. 2021), term structure models (Ai et al. 2018), and oil price dynamics (Ready 2018).

<sup>2</sup>Most notably Constantinides and Ghosh (2011), Beeler and Campbell (2012), and Epstein et al. (2014).



**Figure 1:** Consumption growth is US real total consumption per capita from BEA; ‘TFP’ is the utilization-adjusted, excluding R&D capital, TFP from Fernald (2012). Of both is plotted the 6<sup>th</sup> component of Ortú et al. (2013) decomposition, which filter the fluctuations with half-life between 8 and 16 years. Excess effective R&D is in levels, not growth rates.

Effective R&D expresses aggregate R&D in units of expected productivity growth, as prescribed by endogenous growth theory. It is a log-linear combination of aggregate R&D, the stock of ideas and a product variety measure, capturing the nonlinear impact of R&D on productivity growth. Its definition is formalized within a theoretical framework designed not to characterize optimal choices driving R&D dynamics, whose description is intentionally left to the econometric analysis, but to illustrate the minimal conditions linking effective R&D and asset prices. The framework relies primarily on a production function of ideas that accommodates both fully- and semi-endogenous growth mechanisms, ensuring flexibility to fit real data. This flexibility, together with closer alignment of the econometric approach with the underlying theory, allows for significant improvements over some undesirable statistical properties of the measure used by Kung and Schmid (2015), whose production function is encompassed as a special case. Another related measure is that of Kogan et al. (2017), which provides more granular information but focuses on the outcome of the innovation process – successful innovations – rather than the input, as is preferable for this work, following the spirit of Jinnai (2014).

The empirical identification of effective R&D relies on the widely supported assumption of productivity growth stationarity, which implies that the linear combination of trending variables defining it forms a cointegration relationship that can be estimated. For technical reasons related to the timing of the variables, this relationship is estimated using a single-equation approach (Phillips and Hansen 1990). For robustness, the cointegration model is estimated using productivity levels instead of the stock of ideas, thereby introducing

productivity drivers external to R&D into the error-correction term, which forms a ‘gross’ effective R&D measure. Identification of (net) effective R&D dynamics is pursued in several ways: (1) linearity of both the mapping from gross to net effective R&D and the VAR representing system dynamics ensures structural shocks are not distorted; (2) all estimates are performed on both the gross measure and a net measure, recovered using a recursive formula based on a one-step productivity forecast regression with robust controls that have been shown in previous work to capture productivity growth dynamics; (3) the dynamic implications from the VAR are tested and extended to consumption growth by employing the effective R&D structural shocks from the VAR in a local projection exercise (Jordà 2005; Montiel Olea and Plagborg-Møller 2021). A crucial result is that, although effective R&D is highly stationary, its shocks consistently affect productivity and consumption growth well beyond the business cycle, likely over horizons of ten years. These are significantly longer horizons compared with the evidence in Kung and Schmid (2015), while controlling for external factors, using methods more robust to small-sample bias, and allowing for richer multivariate dynamics. The persistence of effects from R&D fluctuations has also been studied by Anzoategui et al. (2019), who emphasized the role of gradual technology adoption in generating persistence, and many other studies which have leveraged it as a channel for propagating business cycle shocks.<sup>3</sup> Relative to these studies, this paper focuses on the financial implications while employing a novel methodology that assesses an R&D measure uniquely reflecting the time-varying efficiency of R&D to form a single risk factor.

The cross-sectional asset pricing tests rely on the effective R&D structural shocks in the macroeconomic analysis, which is orthogonalized to productivity growth shocks. This ensures that R&D shocks are isolated from the main confounding factor in these reduced-form tests. Combined with the procedure from Giglio and Xiu (2021), which exploits a wide cross-section of assets to mitigate concerns about omitted risk factor bias, this yields highly reliable estimates of the risk premia associated with effective R&D shocks. The premia are insignificant for contemporaneous shocks but highly significant and consistent for moving averages over multi-year horizons, yielding roughly 2% annually – consistent with investors’ underreaction to R&D news documented in Eberhart et al. (2004). Furthermore, a key feature of long-run risk models is that risk is transmitted through asset cash flows. This is tested following Bansal et al. (2005) using stock portfolios sorted by firm characteristics previously linked to R&D investment, as well as by industry portfolios. These results also provide descriptive evidence bridging the corporate finance literature on R&D investment and the asset pricing literature on firm-specific R&D risk premia. Beyond Kung and Schmid (2015), Hsu (2009) also linked aggregate R&D and financial markets. Relative to their work, this paper contributes by employing a theory-based R&D measure and providing explicit cross-sectional risk premium estimates.

From a technical perspective, the theoretical definition of effective R&D is grounded only in

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<sup>3</sup>For example, Benigno and Fornaro (2018) illustrate its role in propagating negative shocks, Antolin-Diaz and Surico (2025) for military spending shocks, Beqiraj et al. (2025) for monetary shocks, Aksoy et al. (2019) for demographic changes.

a definition of Total Factor Productivity (TFP) contributors and a ‘lab-equipment’ production function of ideas inspired by Jones (1999), making the results broadly applicable.<sup>4</sup> While the framework allows R&D efficiency in generating new ideas to be diluted by both decreasing returns to past ideas and an expanding variety of products, it does not explicitly assess their relative contribution to fitting the data, with product variety significance depending on which measure of R&D expenditure is employed. On the empirical side, cointegration models have been widely applied to study the relationship between R&D and technological progress in macroeconomic studies (Bottazzi and Peri 2007; Ha and Howitt 2007; Herzer 2022b; Kruse-Andersen 2023; Madsen 2008). However, these works mainly focus on foreign spillovers and the distinction between fully- and semi-endogenous economies, whereas this paper emphasizes the dynamic properties of R&D and its financial implications. Moreover, none of these studies employ a single-equation approach, which, on the other hand, is frequently used in the empirical macro-finance literature (e.g., Lettau and Ludvigson 2001; Melone 2021) and is adopted here.

The paper proceeds as follows. Section 2 outlines the theoretical framework, defining effective R&D and its key macroeconomic and financial predictions. Section 3 describes the econometric framework proposed to identify effective R&D and test the associated predictions. Section 4 presents the cointegration results and forecasting regressions that yield the effective R&D measures. Section 5 documents the impact of effective R&D on macroeconomic quantities, and Section 6 reports the cross-sectional asset pricing results. Section 7 concludes.

## 2 Theoretical framework

### 2.1 Persistent macroeconomic shocks and financial markets

In a discrete-time, arbitrage-free economy, the expected excess return of any asset  $i$  over the risk-free rate  $R_t^f$  is proportional to the covariance between its return  $R_t^i$  and the Stochastic Discount Factor (SDF)  $M_t$ .<sup>5</sup>

$$\mathbb{E}_t [R_{t+1}^i] - R_t^f = -R_t^f \cdot \text{Cov}_t [M_{t+1}, R_{t+1}^i] . \quad (1)$$

To discipline and better understand the dynamics of the SDF, asset pricing theory often relates the SDF to the intertemporal marginal rate of substitution (IMRS) of a representative agent with preferences over consumption streams. Through the IMRS, shocks to state variables that matter for investor welfare become the key drivers of asset valuations.

As illustrated by Bansal and Yaron (2004), persistent macroeconomic quantities strongly affect the IMRS and, consequently, asset valuations, when the representative agent has recursive preferences as in Epstein and Zin (1989). These preferences separate the intertemporal

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<sup>4</sup>The ‘lab-equipment’ class of models, introduced in Romer (1987), uses final output goods to produce ideas, in contrast to labor-based models à la Romer (1990).

<sup>5</sup>A standard reference is Cochrane (2005).

elasticity of substitution (IES) from risk aversion, and imply that the agent is sensitive both to contemporaneous consumption shocks

$$\varepsilon_{c,t+1} = \ln C_{t+1} - \mathbb{E}_t [\ln C_{t+1}] , \quad (2)$$

and to shocks to long-run consumption prospects

$$\varepsilon_{x,t+1} = \{\mathbb{E}_{t+1} - \mathbb{E}_t\} \sum_{j=1}^{\infty} (\kappa_x)^j \cdot \Delta \ln C_{t+1+j} , \quad (3)$$

as reflected in the log SDF,

$$\ln M_{t+1} = \mathbb{E}_t [\ln M_{t+1}] - b_c \varepsilon_{c,t+1} - b_x \varepsilon_{x,t+1} , \quad (4)$$

where  $\kappa_x \in (0, 1)$  is a function of the equilibrium consumption–wealth ratio, and  $b_c > 0$  and  $b_x > 0$  are the loadings on contemporaneous and long-run consumption shocks, respectively. The persistence of macroeconomic shocks plays a central role in this framework because the longer a shock affects consumption growth, the larger the fluctuations it generates in  $\varepsilon_{x,t+1}$ , and thus the stronger its impact on the IMRS.<sup>6</sup>

Assuming that  $\varepsilon_{c,t+1}$  and  $\varepsilon_{x,t+1}$  are also the key stochastic determinants of asset return dynamics,<sup>7</sup> the following reduced-form pricing equation holds:

$$\mathbb{E}_t [R_{t+1}^i] - R_t^f = \lambda_c \beta_c^i + \lambda_x \beta_x^i , \quad (5)$$

where each asset is fully characterized by two measures of risk – its sensitivities to the shocks,  $\beta_j^i$  for  $j \in \{c, x\}$ , and the market-wide prices of risk,  $\lambda_j$ , which represent the compensation per unit of exposure to each shock – the so-called ‘risk premium’. The economic interpretation is that the agent dislikes fluctuations not only in realized consumption streams but also in expectations of future consumption. Consequently, to hold any asset exposed to either type of shock, the agent requires compensation in the form of higher expected returns. A significant market price of long-run risk,  $\lambda_x$ , has important implications for pricing the entire cross-section of financial assets, and its magnitude crucially depends on the variance of the long-run shock, which also reflects how far into the future the current shocks influence consumption growth.

Naturally, consumption expectations may shift in response to a range of macroeconomic shocks, so long-run risks can stem from multiple economic sources. Among these, productivity growth has been shown to play a central role, as agents with sufficiently high IES optimally postpone consumption in response to positive news about future productivity, generating persistent fluctuations in expected consumption growth (Croce 2014; Kaltenbrunner and Lochstoer 2010; Ortu et al. 2013). Since productivity growth is itself shaped by the long-

<sup>6</sup>For instance, if consumption growth simply followed  $\Delta \ln C_{t+1} = \rho_c \Delta \ln C_t + \tilde{\varepsilon}_{t+1}$  with  $|\rho_c| < 1$  and  $\tilde{\varepsilon}_{t+1}$  i.i.d., then the long-run shock would amount to  $\varepsilon_{x,t+1} = \frac{1}{1-\kappa_x \rho_c} \tilde{\varepsilon}_{t+1}$ .

<sup>7</sup>One could explicitly model returns with a factor structure, e.g.,  $R_{t+1}^i = \bar{R}_t^i + \beta_c^i \varepsilon_{c,t+1} + \beta_x^i \varepsilon_{x,t+1} + e_{t+1}^i$ , although in the LRR framework, exposure arises specifically from assets’ cash-flow dynamics.

lasting effects of innovation, Kung and Schmid (2015) predicted that R&D dynamics would be a key source of long-run risk.

## 2.2 A flexible ‘innovation component’ of productivity growth

To study the role of innovation in generating long-run risks, consider a neoclassical production function for goods. Without loss of generality, assume that the aggregate productivity of rivalrous inputs at time  $t$ ,  $Z_t$ , is determined by the stock of ideas  $I_t$  and a stochastic factor  $a_t$ :

$$Z_t = I_t^\xi \cdot e^{a_t}, \quad (6)$$

for some positive value of  $\xi$ , capturing the degree of increasing returns to scale. Here, the intangible capital  $I_t$  embodies the technological frontier, as it is propelled by R&D expenditure  $S_t$ , according to the law of motion

$$I_t = (1 - \phi)I_{t-1} + \chi \cdot S_{t-1}^\eta I_{t-1}^\psi Q_{t-1}^{-\omega}, \quad (7)$$

where  $\phi \in [0, 1]$  represents the probability of ideas becoming obsolete,  $\chi > 0$  is a scale parameter,  $\eta \in (0, 1]$  controls the extent of duplication in R&D efforts,  $\psi \in (0, 1 - \xi\eta)$  sets the strength of spillovers from past ideas in the creation of new ones (net of fishing-out effects), and  $Q_t$  is a measure of goods variety, with dilution power of ideas  $\omega > 0$ . The process  $a_t$ , by contrast, captures all factors affecting productivity that are not direct by-products of R&D, such as misallocation, allowing their impact to be tracked transparently.

The law of motion of the stock of ideas is directly inspired by Jones (1999), but is more conveniently expressed in a ‘lab equipment’ form, as in Kruse-Andersen (2023), among others. This specification represents the reduced form of equilibrium conditions that can be derived from economies with different microfoundations, with their dynamic properties analyzed in depth by Sedgley and Elmslie (2013). The implied production function of new ideas is the most pivotal assumption of this theoretical framework. It dictates and displays how R&D pushes the technological frontier forward, which is mediated both by the extent to which current research can build on previous ideas and by how widely these new ideas spread into different applications, i.e. products. These two aspects are key to removing the strong scale effects of first-generation endogenous growth models like Romer (1990), which cause the models to show explosive behaviors when introducing population growth, making them unsuitable for empirical applications. The fully-endogenous approach, shown for example in Peretto (1998), focuses on the latter mechanism and implies that sustained higher growth can be obtained by increasing the share of resources devoted to R&D, while the semi-endogenous approach, reviewed in Jones (2005), pivots on the former mechanism, which makes spillovers from past R&D die out in the long-run, ultimately making growth rates a function of population growth only. (7) is flexible enough to accommodate both mechanisms,<sup>8</sup>

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<sup>8</sup>Kung and Schmid (2015), for example, can essentially be reproduced by setting  $\psi = 1 - \eta$  and  $\omega = 0$ .



even though the empirical analysis will not explicitly address the issue of which of the two mechanisms is more relevant for fitting the data.

The specification of productivity determinants in (6) and the law of motion for the stock of ideas in (7) provide enough structure to derive a meaningful characterization of productivity dynamics. Specifically, following a standard approach in the literature,<sup>9</sup> productivity growth can be written as

$$\Delta \ln Z_{t+1} \approx \gamma_0 + \gamma_1 \left( \ln S_t - \frac{1-\psi}{\eta} \ln I_t - \frac{\omega}{\eta} \ln Q_t \right) + \Delta a_{t+1}, \quad (8)$$

where  $\gamma_0$  and  $\gamma_1 > 0$  are composite parameters, with their expressions in terms of the structural parameters reported in Appendix A.1. In words, productivity growth is driven by a linear combination of R&D spending, the technological frontier, and product variety, as well as by shifts unrelated to R&D-fueled innovation,  $\Delta a_{t+1}$ . The term combining R&D expenditure, the technological frontier, and product variety

$$s_t \equiv \ln S_t - \frac{1-\psi}{\eta} \ln I_t - \frac{\omega}{\eta} \ln Q_t \quad (9)$$

arises from the log-linearization of the gross growth rate of ideas  $S_t^\eta / (I_t^{1-\psi} Q_t^\omega)$ . By capturing the contribution of R&D to the creation of new ideas while accounting for the effects of spillovers from past ideas and product proliferation,  $s_t$  is referred to as ‘effective R&D’ in this work. Indeed, even if absolute R&D investments are large, the economy may be so advanced that they are insufficient to keep up with the increasing difficulty of finding new ideas and offset expanding products variety, yielding relatively smaller, or even negative, productivity gains. This interpretation becomes clearer by rearranging (9) as a policy rule:

$$S_t = e^{s_t} \cdot \left( I_t^{1-\psi} Q_t^\omega \right)^{1/\eta}. \quad (10)$$

To sustain constant productivity growth, which requires constant  $s_t$ , the absolute level of R&D investments must grow with the economy as sized by its stock of ideas and product variety; any lower amount, even positive ones, implies a decrease in  $s_t$  and, consequently, a decrease in productivity growth. No alternative transformation of R&D expenditure – such as its growth rate or its ratio to GDP, commonly used in the literature – fully captures its effect on expected productivity growth, which depends on the contemporaneous dynamics of the stock of ideas and product variety. Crucially, this scaling is the only one that synthesizes the effective impact of R&D in a single variable without requiring additional information and regardless of whether the economy follows a fully- or semi-endogenous growth regime. By fully and uniquely capturing the innovation-driven part of productivity growth,  $s_t$  constitutes the *innovation component* of productivity growth – the central focus of this study.

Assuming stationarity of productivity growth, as is common in the literature and supported by the data, a literal interpretation of (8) implies that effective R&D must also be

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<sup>9</sup>E.g., Ha and Howitt (2007) and Kruse-Andersen (2023). These studies use annual data, whereas this analysis relies on quarterly observations, likely improving accuracy.



stationary, unless the external factor is integrated of order 2 or higher, in levels. For the sake of exposition, this section also adopts the common assumption that  $a_t$  is near- $I(1)$ , so that its first differences are close to white noise. Moreover, since in a non-degenerate economy sustained productivity growth leads to exponential growth in the stock of ideas, R&D expenditure, and product variety over time, their logarithms are predicted to be integrated of order one – a prediction strongly supported by empirical evidence for R&D expenditure and product variety proxies. Then, given that  $s_t$  is expected to be stationary and is defined as a linear combination of three  $I(1)$  variables, it follows that these three variables must be cointegrated, with  $s_t$  being the associated error correction term (ECT). Intuitively, this means that, while R&D makes ideas proliferate, it is expected not to systematically increase as much as the stock of ideas and product variety jointly grow. This feature has important implications for empirical applications. A crucial one is that the series  $s_t$  can be recovered as the residual from the regression

$$\ln S_t = \alpha_I \ln I_t + \alpha_Q \ln Q_t + s_t, \quad (11)$$

which has a straightforward mapping with the structural equation (9) and can, in principle, be estimated. Second, the unconditional mean of effective R&D,  $\bar{s}$ , exists and can be interpreted as the infinite-horizon equilibrium level around which  $s_t$  fluctuates. Deviations of effective R&D from this equilibrium level,  $\tilde{s}_t = s_t - \bar{s}$ , will be referred to as ‘excess effective R&D’ and drive the dynamics of conditional expectations of future productivity growth:

$$\mathbb{E}_t [\Delta \ln Z_{t+1}] \approx \mu + \gamma_1 \cdot \tilde{s}_t, \quad (12)$$

where  $\mu$  denotes the unconditional expectation of  $\Delta \ln Z_{t+1}$ .

### 2.3 The long-run risk from innovation

It should be noted that  $\tilde{s}_t$  plays the same role in shaping expectations of future productivity growth as the ‘long-run productivity risk component’ in Croce (2014). To illustrate the impact of the innovation component on long-term economic dynamics, this section follows the Long-Run Risk literature and assumes it follows a simple AR(1) process:

$$\tilde{s}_t = \rho_s \tilde{s}_{t-1} + \tilde{\varepsilon}_t, \quad \tilde{\varepsilon}_t \sim \mathcal{N}(0, \sigma_s^2),. \quad (13)$$

In this setting, the persistence of effective R&D alone determines how long its shocks influence productivity growth, making it straightforward to characterize the response of infinite-horizon productivity prospects to R&D shocks:

$$\mathbb{E}_{t+1} - \mathbb{E}_t \left( \sum_{j=0}^{\infty} \Delta \ln Z_{t+1+j} \right) = \frac{\rho_s}{1 - \rho_s} \tilde{\varepsilon}_{t+1},. \quad (14)$$

This underscores the significance of persistence in effective R&D, which Kung and Schmid (2015) showed can emerge endogenously,<sup>10</sup> making it a natural candidate for generating substantial long-run risk. With the simplifying assumption that consumption is a constant fraction of final goods produced, it is also immediately apparent that

$$\varepsilon_{x,t+1} \quad \text{is affine to} \quad \frac{\kappa_x \rho_s}{1 - \kappa_x \rho_s} \tilde{\varepsilon}_{t+1}, \quad (15)$$

whose combination with (4) clearly illustrates how shocks to effective R&D can affect the IMRS. From a financial perspective, the investor is expected to require higher returns for assets whose payoffs covary positively with R&D, since higher R&D provides an early signal of elevated future productivity and, consequently, consumption, which reduces marginal utility.

It should be noted that there is a well-known tension between the degree of persistence of a series and the difficulty of empirically distinguishing it from a non-stationary one.<sup>11</sup> Indeed, with a finite sample, it is possible both (1) for the data-generating process of effective R&D to be non-stationary while productivity growth appears stationary, due to substantial short-term exogenous fluctuations; and (2) for effective R&D to appear non-stationary despite being stationary but highly persistent. This can pose a challenge for the framework, since the stationarity of  $s_t$  is crucial for validation, to avoid spurious statistical results in standard empirical tests, while a high persistence of  $s_t$  is essential in making the long-run risk mechanism relevant in this univariate setting, as it amplifies the impact of its shocks on the economy – with the effects being the strongest precisely when approaching the unit root behavior. Ultimately, whether a stationary effective R&D best represents reality is an empirical question, with its key characteristic for theoretically qualifying as an Innovation Long-Run Risk Component being only that its shocks can forecast growth in productivity – and, consequently, in consumption – over long horizons. Importantly, in general, the persistence of the effects of R&D shocks does not depend solely on the intrinsic persistence of the innovation component itself. Indeed, it also arises from the way in which such shocks are transmitted and amplified by the interactions with the broader economic system. Even a transitory disturbance can generate lasting effects if its repercussions propagate across interconnected variables and feedback mechanisms.

### 3 Econometric framework

#### 3.1 Measuring effective R&D

##### An operational definition

To estimate (11), measures of R&D expenditure, the stock of ideas, and product variety are required. The first has straightforward counterparts in reality, while the latter two

<sup>10</sup>They referred to ‘effective R&D’ as ‘R&D intensity’.

<sup>11</sup>See, for example, Müller (2005).

are mapped into observable data following approaches previously adopted in the literature. Product variety is simply assumed to be proportional to labor input  $L_t$ .<sup>12</sup> The stock of ideas, instead, is replaced by the productivity level exploiting the definition of TFP in (6). This substitution allows one to bypass the challenging task of measuring the stock of ideas, which is significantly harder to identify than TFP in the data. A first issue concerns the data underlying most measures of ideas, namely patents, which numerous studies have argued do not well represent successful innovation.<sup>13</sup> Then, even with a reliable proxy for new ideas, the stock of ideas must be manually constructed. This requires specifying depreciation rates and aggregating foreign ideas, which would severely limit the sample's timespan and expose the measure to a significant risk of misspecification. On the other hand, TFP, measured as Solow residuals, is much easier to identify empirically. Its concept originates directly from the data, and its definition is common to many models, thereby enhancing the external validity of the analysis. Importantly, these benefits come at the cost of introducing the external component  $a_t$  into the definition of effective R&D. Indeed, rewriting effective R&D as

$$\tilde{s}_t = S_t - \frac{1-\psi}{\eta\xi}(\ln Z_t - a_t) - \frac{\omega}{\eta} \ln L_t - \bar{s} \quad (16)$$

prescribes a regression that depends only on observable data:

$$S_t = \alpha_0 + \alpha_Z \ln Z_t + \alpha_L \ln L_t + \hat{s}_t, \quad (17)$$

but the residuals of this regression no longer identify  $\tilde{s}_t$ , but rather a ‘gross effective R&D’

$$\hat{s}_t = \tilde{s}_t - \alpha_Z a_t, \quad (18)$$

so additional steps are required to recover  $\tilde{s}_t$  from the error correction term of (17).

### Single-equation cointegration estimation

The timing of the data involved in retrieving effective R&D informs the choice of method for estimating the cointegrating parameters in (17). Indeed, R&D expenditure is a flow variable, with its measure capturing the amount of resources devoted to R&D activities throughout the period, whereas TFP and employment levels, being stock variables, are only measured at the end of the period. One could realistically assume, as most models do, that R&D is either decided at the beginning of the period or chosen continuously throughout it, but the end-of-period stock levels are clearly not part of the information set underlying these decisions. Since intermediate values of stock variables are unavailable, and interpolating them would alter the statistical and dynamic properties of the series, the best approximation of the contemporaneous stock values is taken to be their value at the beginning of the period, i.e. the end of the period before. This adjustment implies that a standard Vector Error

<sup>12</sup>Product variety is generally assumed to be an exponential function of the  $L_t^\kappa$  type with  $0 < \kappa < 1$ , but  $\kappa$  has no impact on this analysis and would not be identified anyway, so for the sake of exposition it is fixed at 1.

<sup>13</sup>See, for example, Reeb and Zhao (2020) and Herzer (2022a).

Correction Model would effectively use R&D from time  $t - 1$  to  $t$  to forecast TFP growth over the same interval, which is not the predictive relation described by discrete-time endogenous growth theory. Therefore,  $\hat{s}_t$  is estimated by focusing solely on the long-run relation (17).

This relation is estimated using the Fully Modified Ordinary Least Squares (FM-OLS) method (Phillips and Hansen 1990), which corrects for endogeneity in cointegration regressions by adjusting the dependent variable to account for the long-run covariance with endogenous variables. FM-OLS is particularly suitable here because the error correction term is expected to be highly persistent. Therefore, by contrast, addressing endogeneity as in Dynamic OLS (Stock and Watson 1993), i.e., by including leads and lags of the differenced regressors, would consume many degrees of freedom and substantially reduce the effective sample size. For robustness, the Integrated Modified (IM) OLS of Vogelsang and Wagner (2014) is also considered, although it is expected to perform less efficiently than FM-OLS on a dataset of over 300 observations, as used in this work.

### Recovery of the innovation component

Endowed by  $\gamma_1$ , one can explicitly recover the whole time series of  $\tilde{s}_t$  from  $\Delta \hat{s}_t$  and  $\Delta \ln Z_t$ , through a simple recursive relation derived from (8) and (18) that can also be written as:

$$\tilde{s}_t = \alpha_Z \left( \sum_{j=0}^{t-1} \kappa_s^j (\Delta \ln Z_{t-j} - \mu) \right) + \sum_{j=0}^{t-1} \kappa_s^j \Delta \hat{s}_{t-j} + \kappa_s^t \tilde{s}_0, \quad (19)$$

where  $\kappa_s \equiv 1 - \alpha_Z \gamma_1$ . Clearly, as the initial value  $\tilde{s}_0$  is unknown, the retrievable values will consist of an approximation. Details on the accuracy and precision of the recovery are provided in Section A.3. Nonetheless, the impact of the initial condition is governed by the exponential decay of the weights  $\kappa_s^t$ , which do, in fact, diminish rapidly over time. Moreover, as illustrated below, the main analysis can effectively be carried out using either  $\hat{s}_t$  or  $\tilde{s}_t$ , ensuring robust findings through the use of both measures.

To obtain a reliable estimate of  $\gamma_1$ , two assumptions are made. First, it is assumed that a set of pervasive macroeconomic factors  $\mathbf{f}_t$  spans the non-innovation component of TFP growth, so that  $a_t = \mathbf{c}' \mathbf{f}_t$  for some vector  $\mathbf{c}$ . This assumption is supported by the extensive literature on the predictable part of TFP growth (Ai et al. 2018; Croce 2014), of which  $a_t$  represents the non-idea component; accordingly, it should already be captured by the information set of the predictors previously used. Second, the effects of the first lag of effective R&D on the external component  $a_t$ , later captured by the parameter  $\theta_s$ , are negligible in magnitude. This assumption is later validated by the study of the system's integrated dynamics, but it is also motivated by the observation that the external component is likely driven by a multitude of factors shaping aggregate economic conditions. Therefore, while feedback mechanisms may eventually amplify the contribution of effective R&D to the fluctuations of  $a_t$ , the immediate impact is expected to be negligible. Under these assumptions,  $\gamma_1$  is identified by  $b_s$  in the

estimation of (8) as

$$\Delta \ln Z_{t+1} = b_0 + b_s \hat{s}_t + \mathbf{b}'_f \mathbf{f}_t + u_{t+1} . \quad (20)$$

Since this estimation focuses solely on the parameter  $b_s$  rather than the full dynamics of the R&D impact, this forecasting regression is also estimated as a single equation rather than within a system. Relative to a multivariate approach, this method trades a modest increase in estimation variance for a substantial reduction in bias, incorporating numerous control variables in  $\mathbf{f}_t$ , including lagged values of the dependent variables, with lag lengths selected using standard information criteria.

An alternative approach to recover  $\tilde{s}$  is to estimate the cointegration between  $\ln S_t$ ,  $\ln Z_t$ ,  $\ln L_t$ , and the factors  $\mathbf{f}_t$  directly. However, this approach requires estimating a long-run covariance matrix with 144 elements using fewer than 280 observations, which is challenging and may lead to imprecise and unstable cointegrating parameter estimates.

### 3.2 Innovation shocks and long-run dynamics

The theoretical framework developed in Section 2 yields predictions that closely link the dynamics of productivity growth and effective R&D. Empirically, the dynamics of  $a_t$ ,  $\Delta \ln Z_t$ , and  $\tilde{s}_t$  (or  $\hat{s}_t$ ) are modeled jointly as a system to achieve two objectives. First, this approach enables an integrated assessment of the long-run impact of effective R&D, accounting for dynamic feedbacks and contemporaneous correlations that univariate models would overlook. Second, it allows identification of structural shocks to the innovation component. The identification strategy, detailed below, isolates shocks to innovation efforts that are orthogonal to fluctuations in other macroeconomic variables of the system, most importantly productivity growth. This separation is crucial to minimize contamination from other sources of risk in estimates of the risk premium from reduced-form asset pricing tests using effective R&D as a risk factor.

The stochastic processes from Section 2 are then extended to incorporate arbitrary persistence in  $a_t$  (controlled by  $\rho_a$ ) and feedback effects between  $a_t$  and  $\tilde{s}_t$  (governed by  $\theta_s$  and  $\theta_a$ ). Importantly, the shocks to effective R&D that are not determined by external factors,  $\varepsilon_{s,t}$ , are assumed to have no effect on the contemporaneous level of the non-idea component. This is a common assumption in the literature (see, for instance, Moran and Queralto (2018)), since the innovation process rarely has outcomes within such a short time frame to be considered contemporaneous.<sup>14</sup>

The resulting structural system is

$$a_{t+1} = \theta_s \tilde{s}_t + \rho_a a_t + b_{aa} \varepsilon_{a,t+1} \quad (21a)$$

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s) \tilde{s}_t + (\rho_a - 1) a_t + b_{aa} \varepsilon_{a,t+1} \quad (21b)$$

$$\tilde{s}_{t+1} = \rho_s \tilde{s}_t + \theta_a a_t + b_{as} \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1} , \quad (21c)$$

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<sup>14</sup>The implausibility of contemporaneous outcomes is further supported by the significant lag in the diffusion of new technologies, as argued in Rotemberg (2003) and Anzoategui et al. (2019).

where  $\varepsilon_{a,t+1}$  and  $\varepsilon_{s,t+1}$  are i.i.d. shocks from a standardized normal distribution, and  $b_{aa}$ ,  $b_{as}$ , and  $b_{ss}$  are free parameters controlling the volatility of the shocks and their cross-effects. A similar system can be written for  $\hat{s}_t$  by substituting  $\tilde{s}_t = \hat{s}_t + \alpha_Z a_t$  into the above equations. Notably, each variable continues to be driven by the same underlying structural shocks whether  $\tilde{s}$  or  $\hat{s}$  is used; only the reduced-form coefficients differ, allowing the same identification scheme to recover the same structural shocks. More details of the system are provided in Appendix A.2.

In this work, the estimation of (21) is approached by focusing on parsimonious 2-variable Vector Autoregression (VAR) models that approximate the VARMA systems obtained from substituting the external factor out of the 3-variable systems:

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s) \tilde{s}_t + \rho_a \Delta \ln Z_t - (\theta_s + \rho_a \gamma_1) \tilde{s}_{t-1} + b_{aa} \varepsilon_{a,t+1} - b_{aa} \varepsilon_{a,t} \quad (22a)$$

$$\begin{aligned} \tilde{s}_{t+1} = & \rho_s \tilde{s}_t - \frac{\theta_a \rho_a}{1 - \rho_a} \Delta \ln Z_t + \left( \theta_a \theta_s + \frac{\theta_a \rho_a (\gamma_1 + \theta_s)}{1 - \rho_a} \right) \tilde{s}_{t-1} + \\ & b_{as} \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1} + \frac{\theta_a b_{aa}}{1 - \rho_a} \varepsilon_{a,t}, \end{aligned} \quad (22b)$$

where the number of lags is chosen based on standard information criteria. A Cholesky decomposition of the reduced-form residuals' covariance matrix, with  $\tilde{s}_t$  ordered last, identifies the structural shocks to effective R&D,  $\varepsilon_{s,t}$ , from the estimates of (22). As anticipated, the same holds if the system is expressed in terms of  $\hat{s}_t$  instead of  $\tilde{s}_t$ , since only the coefficients change. Crucially, this approach leaves the external component unobserved, which may introduce serial correlation in the reduced-form residuals if its dynamics are poorly reflected in the two-variable system, potentially invalidating structural identification. However, the adequacy of this specification can be assessed ex post through standard diagnostic tests.

A natural way to incorporate a wider information set in the system could be approaching the system (21) with a Factor-Augmented VAR (FAVAR) in which the pervasive macroeconomic factors  $\mathbf{f}_t$  that have been previously argued to span the productivity external component were to be included among the endogenous variables in place of  $a_t$ . However, as with the cointegration problem, the rapidly increasing number of parameters in this approach leads to substantial costs in terms of estimation noise (11 endogenous variables imply 121 coefficients per lag in the VAR) and a high risk of overfitting.

Robustness of the impulse response functions (IRFs) is ensured by the use of recursive residual bootstrap standard errors of VAR estimates (Lütkepohl 2005), complemented with local projection (LP) estimates following Jordà (2005) and Montiel Olea and Plagborg-Møller (2021). LPs exploit lags of both the macroeconomic factors and the dependent variable, providing results that are generally more robust to misspecification though more volatile than those from the VAR. Following the standard approach, to analyze the dynamic responses of productivity and consumption growth rates to effective R&D shocks with local projections,

cumulative responses are estimated using the following specification:

$$\sum_{j=1}^h \Delta y_{t+j} = b_{y,h,0} + b_{y,h,s} \cdot \varepsilon_{s,t} + \sum_{l=0}^k (\mathbf{b}'_{y,h,f,l} \mathbf{f}_{t-l} + b_{yy,h,l} \cdot y_{t-l}). \quad (23)$$

Conveniently, the coefficients  $b_{y,h,s}$  precisely reflect the impact of R&D shocks on the dynamics of long-run expectations, truncated at horizon  $h$ ; that is, they indicate how strongly these shocks affect the long-run risk factor  $\varepsilon_{x,t}$ , as defined in (3).

### 3.3 Asset pricing tests

The key prediction from the theoretical framework in Section 2 is that if shocks to effective R&D influence the long-run dynamics of consumption growth (and agents have recursive preferences), then  $\lambda_x$  in (5) should be positive and significant. Although the covariance-based nature of asset pricing would, in principle, allow effective R&D to serve as the long-run risk factor in levels – as is common in the macro-finance literature, since estimation procedures net out predictable components – this analysis focuses on structural shocks to effective R&D as the risk factor, while also reporting results based on the levels. This choice provides a more stringent test of the theory and ensures consistency with the tests of the macroeconomic predictions.

The key concern in estimating factor models such as (5) is omitted variable bias, which arises when the estimation model fails to capture all priced sources of risk in the economy. This concern is particularly relevant here because the theoretical framework underlying this work, like most asset-pricing models, is deliberately stylized and does not explicitly account for all systematic risks. Recent work by Giglio and Xiu (2021) addresses this issue by proposing a methodology that improves the robustness of risk premia estimates through explicit control for omitted variables.

To further investigate the sources of innovation long-run risk premia, this study replicates the analysis of Bansal et al. (2005). Their methodology, specifically designed for the Long-Run Risks framework, focuses on stocks' cash-flow risks rather than total return variation, isolating the channel through which long-run risk factors theoretically generate equity risk premia. While this approach is less stringent than the Giglio and Xiu (2021) methodology, it provides complementary evidence that facilitates comparison with existing studies and contributes to broader discussions on the economics of R&D. The remainder of this section presents the two methodological approaches in greater detail, while details on the test assets are provided in the next sub-section.

#### A robust approach to risk premia estimation

In the context of a standard factor structure for returns such as

$$\mathbf{R}_t - R_{t-1}^f = \beta \boldsymbol{\lambda} + \beta \mathbf{v}_t + \mathbf{u}_t, \quad (24)$$



when the number of observations and test assets go to infinity, the ‘true’ risk factors in the economy  $\mathbf{v}_t$  can be recovered by the Principal Component Analysis up to an arbitrary rotation  $\hat{\mathbf{v}}_t = H\mathbf{v}_t$ , where  $H$  is a full-rank matrix. Then, Giglio and Xiu (2021) focus on an observable factor  $x_t$  of interest that is affine in the ‘true’ factors, with measurement error  $w_t$ ,

$$x_t = \zeta_0 + \zeta_v \mathbf{v}_t + w_t, \quad (25)$$

and show that the risk premia associated with it can be effectively estimated without bias. In this framework, the risk premium associated with  $x_t$  amounts to  $\zeta_v \boldsymbol{\lambda}$ , which corresponds to the expected excess return of an asset with a beta of one with respect to  $x_t$  and zero with respect to any other independent factor.

The key to its estimation is that  $\zeta_v H^{-1}$  can be obtained by regressing  $x_t$  on  $\hat{\mathbf{v}}_t$ , while  $H\boldsymbol{\lambda}$  can be obtained by regressing  $\mathbf{R}_t$  on  $\beta H^{-1}$ , the latter being estimated by regressing returns on the ‘true’ factors. This delivers all the necessary elements to recover  $\zeta_v \boldsymbol{\lambda}$ , since

$$\zeta_v H^{-1} H\boldsymbol{\lambda} = \zeta_v \boldsymbol{\lambda}. \quad (26)$$

In this setting, a crucial modeling choice concerns the number of principal components treated as the ‘true’ risk factors of the economy. This analysis considers multiple specifications for the number of factors, guided by the standard approach of Bai and Ng (2002) and the criteria proposed in Alessi et al. (2010).<sup>15</sup> Equally important is the breadth of the test assets: the wider the span of economic states they represent, the more robust the control for omitted risk factors will be. Moreover, to allow the information contained in the shocks to be incorporated into prices gradually (Eberhart et al. 2004), the innovation long-run risk factor is examined both as contemporaneous shocks to effective R&D  $\varepsilon_{s,t}$  and as rolling sums of these shocks. Specifically, results are reported for rolling sums with horizons of 1 quarter (i.e., contemporaneous shocks), two years (matching the analysis on cash flows), and four years (corresponding to the typical length of a business cycle).

### A traditional estimation approach

Bansal et al. (2005) applies the standard procedure of Fama and Macbeth (1973) with two modification. First, they ignore the risk associated with short-term fluctuations in consumption growth, based on the empirical finding that such fluctuations account for a negligible portion of the equity risk premium (Mehra and Prescott 1985). This observation motivated the focus on long-run risks, whose premia are predicted to be larger by orders of magnitude. Accordingly, they adopt the simpler cross-sectional pricing condition

$$\mathbb{E}_t [R_{t+1}^i] - R_t^f = \lambda_x \beta_x^i \quad (27)$$

as a reasonable approximation. Second, they measure asset risk by the sensitivity of cash-flow growth to the risk factors rather than by return sensitivities. This choice aligns more closely

<sup>15</sup>The latter consists of two criteria and is implemented by taking the median across 300 repetitions.

with the theoretical formulation of Long-Run Risk and other consumption-based models, in which return betas are endogenously determined by the sensitivity of cash flows to the risk factors. Operationally, this is implemented using the Campbell (1996) decomposition, which approximates return shocks as the sum of news about cash-flow growth and discount rates:

$$\ln R_{t+1}^i - \mathbb{E}_t [\ln R_{t+1}^i] \approx \delta_{D,t+1}^i - \delta_{R,t+1}^i \quad (28)$$

where

$$\delta_{D,t}^i = \{\mathbb{E}_t - \mathbb{E}_{t-1}\} \left[ \sum_{j=0}^{\infty} \bar{\kappa}^j \Delta \ln D_{t+j}^i \right], \quad \delta_{R,t}^i = \{\mathbb{E}_t - \mathbb{E}_{t-1}\} \left[ \sum_{j=1}^{\infty} \bar{\kappa}^j \ln R_{t+j}^i \right]. \quad (29)$$

This decomposition allows any return beta to be written approximately as the difference between a dividend-beta  $\beta_{x,D}^i$  and a discount-rate-beta  $\beta_{x,R}^i$ .<sup>16</sup>

$$\beta_x^i = \frac{\text{Cov} [R_t^i, \varepsilon_{x,t}]}{\text{Var} [\varepsilon_{x,t}]} \approx \frac{\text{Cov} [\delta_{D,t}^i, \varepsilon_{x,t}]}{\text{Var} [\varepsilon_{x,t}]} - \frac{\text{Cov} [\delta_{R,t}^i, \varepsilon_{x,t}]}{\text{Var} [\varepsilon_{x,t}]} = \beta_{x,D}^i - \beta_{x,R}^i, \quad (30)$$

Focusing on the risks stemming from assets' fundamentals, and ignoring the effects of risks originating from the discount rates channel, the analysis considers only the dividend-beta, yielding the final pricing equation

$$\mathbb{E}_t [R_{t+1}^i] - R_t^f = \lambda_x \beta_{x,D}^i. \quad (31)$$

Following Bansal et al. (2005), the dividend-beta  $\beta_{x,D}^i$  is estimated using the univariate time-series regression

$$\Delta \ln D_t^i = \hat{\beta}_{0,D}^i + \hat{\beta}_{x,D}^i \cdot \frac{1}{H} \sum_{l=1}^H \varepsilon_{s,t-l} + u_t^i, \quad (32)$$

which, as illustrated by Hodrick (1992), has inferential advantages in small samples, but is asymptotically equivalent to

$$\frac{1}{H} \sum_{l=1}^H \Delta \ln D_{t+l}^i = \check{\beta}_{0,D}^i + \hat{\beta}_{x,D}^i \varepsilon_{s,t} + \check{u}_{t+1}^i, \quad (33)$$

making clearer the mapping between  $\hat{\beta}_{x,D}^i$  and  $\beta_{x,D}^i$  from (30), as well as its interpretation as the 'long-lasting impact on cash-flow growth'. The premium  $\lambda_x$  is then estimated by regressing the dividend-betas on the assets' returns.

In Bansal et al. (2005), the raw series of consumption growth was used as the regressor, so the moving average also served to filter out high-frequency fluctuations and identify the shifts in long-run consumption prospects. In contrast, shocks to effective R&D, were the macroeconomic analysis to show that they have persistent effects on consumption growth,

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<sup>16</sup>The approximation is given both by (28) and  $R_t^i \approx 1 + \ln R_t^i$ . See Campbell and Vuolteenaho (2004) for a systematic application.

can capture changes in long-run consumption prospects without any filtering. Consequently, the sensitivity of the results to the horizon of aggregation is also examined, reporting outcomes both for the horizon traditionally employed in Bansal et al. (2005) ( $H = 8$  quarters) and for  $H = 1$  quarter.

### 3.4 Data

#### Macroeconomic data

The baseline measure of R&D in this study is the real US quarterly private R&D expenditures (chained 2017 dollars), consistent with closely related studies (Beqiraj et al. 2025; Kung and Schmid 2015; Moran and Queralto 2018). Private R&D reflects the profit-maximizing innovation decisions at the core of most endogenous growth models more directly than total R&D, since government expenditures operate through distinct institutional mechanisms, likely materializing in a fundamentally different knowledge production function. The total R&D series is used as a robustness check. Both series are provided by the Bureau of Economic Analysis (BEA) via the Federal Reserve Economic Data (FRED) online database and span 1947 Q1 to 2025 Q2.<sup>17</sup>

Total Factor Productivity is obtained from Fernald (2012). The baseline series is the quarterly TFP growth adjusted for utilization and excluding R&D from capital, while robustness checks use the raw TFP series. The utilization adjustment is preferred because removing cyclical utilization dynamics – like any non-idea-related factor – enhances the signal-to-noise ratio of the underlying technological component of productivity, thereby improving the precision of the estimates; the R&D capital is excluded because its construction through simple cumulation and depreciation of R&D flows is inconsistent with the knowledge production function studied in this work. Differences between the series mainly arise from the utilization adjustment, with minimal impact from the exclusion of R&D from capital. The series span 1947 Q2 to 2025 Q1, and levels are obtained by cumulating the growth rates.<sup>18</sup>

The labor force is measured by the total employment level, with non-farm employment used as a robustness check. Both series are provided monthly by the Bureau of Labor Statistics via FRED. The quarterly series is constructed by taking the last value of each quarter, spanning 1948 Q1 to 2025 Q2.<sup>19</sup>

The predicting factors consist of two distinct sets, previously employed to forecast TFP growth in Ai et al. (2018): (1) nine identified factors, extending those used in Bansal and Shaliastovich (2013); and (2) nine non-identified factors directly from Ludvigson and Ng (2009). These are referred to with the shorthands ‘BS’ and ‘LN’, respectively. The BS factors set originally comprised the US Cycle Adjusted Price Earnings (CAPE) ratio, the

<sup>17</sup>The real series is obtained by deflating the nominal R&D series Y006RC1Q027SBEA with the deflator Y006RG3Q086SBEA. The total series has ID Y694RX1Q020SBEA.

<sup>18</sup>The data are provided online by the author and also include the utilization adjustment and changes in capital excluding R&D.

<sup>19</sup>IDs: CE160V and LNS12035019.

3-month Treasury-bill yield, and the 3- and 5-year Treasury bond yields. Ai et al. (2018) later expanded this set to include the US stock market integrated daily volatility. This work additionally incorporates the 10-year Treasury bond yield, real US corporate profits, real US nonfinancial corporate liquid assets, and labor input growth, in order to better capture macroeconomic dynamics at longer horizons, as well as aspects related to financing conditions, profitability, and product proliferation — all known to influence productivity and R&D decisions. These controls span 1951 Q4 to 2025 Q1.<sup>20</sup> The LN factors set instead is formed by the principal components of a wide array of macroeconomic and financial variables. These series have monthly frequency and are aggregated as quarterly averages, yielding a time span from 1960 Q1 to 2025 Q2.<sup>21</sup> As illustrated in Appendix C, all BS variables appear to exhibit unit-root behaviour, whereas there is only weak evidence of non-stationarity among the LN factors. Therefore, while the LN factors are used in levels, the BS factors are included in first differences to mitigate the risk of spurious regression.

Finally, consumption is measured as real total personal consumption expenditures per capita, in chained 2017 US dollars. The series is provided by the BEA via FRED and span 1947 Q1 to 2025 Q2.<sup>22</sup>

More details on the data can be found in Appendix B.1.

## Test assets data

The selection of test assets for the robust risk premia estimation is guided by the need to cover as broad a portion of the economic state space as possible, ensuring that the resulting estimates are generalizable and robust. Expanding on the approach of Bryzgalova et al. (2025), this work employs 153 anomaly stock portfolios from Jensen et al. (2021), 17 industry-sorted stock portfolios from K. French’s database, and 13 bond portfolios. The bond portfolios are constructed from the zero-coupon yield data of Gürkaynak et al. (2007) by fitting Nelson-Siegel-Svensson curves and subtracting the return on a three-month Treasury bill. These portfolios span maturities of 6 months and 1, 2, 3, 4, 5, 6, 7, 10, 15, 20, 25, and 30 years. The final dataset covers the period from 1971 Q4 to 2024 Q4.

The test assets employed for the Bansal et al. (2005) exercise include only stock portfolios, as in the original study: 10 sorted by size, 10 by book-to-market equity, and 10 by past-year returns. This set is referred to as the ‘legacy pool’. It is expanded with 2-by-3 portfolios jointly sorted by size (big vs. small) and various firm characteristics related to R&D investment to form the ‘extended pool’, and further complemented by 17 industry portfolios to form the ‘wide pool’. The firm characteristics considered in the extended pool capture (i) the intensity of innovative efforts (*firm-specific* R&D ratio to market capitalization), (ii) financing capacity (leverage, turnover, and profitability), and (iii) growth opportunities (assets growth and Tobin’s  $q$ ). These dimensions have been associated with dispersion in cross-sectional risk

<sup>20</sup>CAPE is from R. Shiller’s website; bill and bond yields are from Finaeon until the first availability of DGS3M0, DGS3, DGS5, and DGS10 on FRED; daily stock market data is from CRSP. US corporate profits and liquid assets are the series CPRFIT and B0GZ1FL104001005Q on FRED, deflated by GDPDEF from FRED.

<sup>21</sup>Publicly available on S. Ludvigson’s website.

<sup>22</sup>ID: A794RX0Q048SBEA.

premium and different forms of sensitivity to innovation dynamics, therefore are likely to generate heterogeneity in exposure to the long-run risk carried by aggregate R&D. Specifically, variation in firms' R&D intensity affects the spillovers and 'fishing out' effects experienced by a firm, which Jiang et al. (2016) showed to be priced in financial markets, while financing capacity and growth opportunities interact with aggregate R&D investment by affecting firms' ability to react to innovation shocks (Aghion et al. 2012; Brown et al. 2009; Hall 2002; Hall et al. 2010; Li 2011; Maletic 2018; Zhang 2014). Their inclusion further provides descriptive statistics that contribute to the discussion on the cross-sectional variation in returns with firm-specific R&D intensity, which, since its first documentation in Chan et al. (2001), remains debated (Ahmed et al. 2025; Leung et al. 2020). The payout series is constructed following Bansal et al. (2005) and Hansen et al. (2005), with details provided in Appendix B.2. Monthly stock data come from CRSP, and annual accounting data from the Compustat Fundamentals dataset. Monthly returns are compounded to obtain quarterly figures and then deflated using the consumption deflator. The portfolio return and cash-flow growth rate series begin at different dates: the long-pool and industry-sorted portfolios start in 1967 Q1, while the others begin in 1975 Q1; all series end in 2022 Q4. Key statistics of the formed series are reported in Appendix B.2.

## 4 The empirical innovation component

### 4.1 The gross effective R&D

The estimation results for the long-run relation in (17) are shown in Table 1. The first column of the table shows the baseline specification, with the columns to the right substituting one variable at a time with the alternative robustness measure. The last column uses the baseline data but employs the IM-OLS method instead.

First, the  $\alpha_Z$  estimates have the expected sign and are always significantly different from zero. Simply put, this means that R&D expenditure and TFP levels increase together; that is, raw R&D rises with the scale of the economy, as expected. A similarly expected coefficient is that of labor,  $\alpha_L$ , which suggests some dilution in R&D's power to advance the technological frontier and implies a mediating effect on how R&D expenditure relates to the technological frontier to obtain a meaningful measure of effective R&D. The only exception occurs when total R&D is used, highlighting the possibility that public R&D may operate through a different production function than private R&D.<sup>23</sup> Further, the use of nonfarm employment does not result in discernible changes, while the use of raw TFP, although it does not materially affect the estimates, alters the short-term fluctuations in the resulting error correction term, as can be seen from the plots of all ECT time series in Appendix C (Figure 10). Visual inspection of the time series also reveals the considerable instability of the IM-OLS estimates, as reflected by the large condition number of the coefficients' covariance matrix  $\kappa$ , even though the estimates essentially confirm the baseline results.

<sup>23</sup>Estimates not reported in this paper are, in facts, significantly negative when only public R&D is used.

**Table 1:** Cointegration results. Standard errors in parentheses.  $T$  is the number of observations;  $\kappa$  is the condition number of the coefficients' covariance matrix. Statistics in the bottom part of the table refer to the error correction term  $\hat{s}$ :  $\sigma_{\hat{s}}$  is its standard deviation;  $tt$  and  $tt^2$  are the time trend and squared time trend coefficients (with HAC standard errors);  $ADF$  and  $KPSS$  are stationarity tests in levels;  $AR(1)$  is the coefficient from an AR(1) fit;  $HL$  are the lower and upper bounds, at 95% confidence, of the half-life implied by the AR(1) estimate, in years.

	Baseline	S: Tot. R&D	Z: Raw TFP	Q: N.F. Empl.	Est. Meth.: IM
$\alpha_Z$	3.526*** (0.439)	4.197*** (0.516)	3.655*** (0.490)	3.349*** (0.464)	2.821*** (0.552)
$\alpha_L$	0.909*** (0.336)	-0.354 (0.395)	0.956*** (0.356)	0.953*** (0.325)	1.387*** (0.398)
T	309	309	309	309	309
$\kappa$	$3.4 \times 10^6$	$3.4 \times 10^6$	$3.3 \times 10^6$	$3.5 \times 10^6$	$1.1 \times 10^8$
$\hat{s}_t$					
$\sigma_{\hat{s}}$	0.130	0.144	0.128	0.129	0.253
tt	0.00	0.00	0.00	0.00	0.00
tt <sup>2</sup>	0.00	0.00	0.00	0.00	0.00
ADF	-2.57**	-2.45**	-2.92***	-2.45**	-9.18***
KPSS	0.09	0.09	0.09	0.10	0.29
AR(1)	0.96	0.96	0.95	0.97	0.15
HL low	2.6	2.7	2.1	2.7	0.1
HL high	21.0	23.6	12.0	25.1	0.1

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01

The lower part of Table 1 reports descriptive statistics of the error correction term resulting from the estimation, i.e., the time series of  $\hat{s}_t$ . All estimated gross effective R&D series are found to be stationary according to both the ADF and KPSS tests, with none exhibiting a time trend or a squared time trend. The persistency of the series, as measured by an AR(1) fit, is perfectly in line with the persistent component of productivity growth that is transmitted to consumption growth, which Ortu et al. (2013) and Croce (2014) has shown having a half-life between 2 and 16 years. As shown in Appendix C (Table 10), correlations among ECTs from different specifications never drop below 86%, consistent with the close estimation results, except for the IM estimation.

## 4.2 The effective R&D

The estimated  $\hat{s}_t$  series allows for the estimation of equation (20), which yields  $\gamma_1$ , the missing parameter required to recover the effective R&D series. Information criteria (Appendix C, Figure 8) select one lag for specifications based on the adjusted TFP measure and two lags for those based on the raw TFP measure. The corresponding results are reported in Table 2.

The estimated R&D coefficient is consistently positive and statistically significant, confirming a strong empirical relationship between innovation intensity and productivity growth. Its magnitude closely matches the empirical estimates in Kung and Schmid (2015) and implies

**Table 2:** One-step productivity growth forecast results. HAC standard errors in parentheses.  $T$  is the number of observations;  $R^2$  is the goodness-of-fit;  $k$  is the number of control variables among the regressors;  $W(k)$  is the Wald statistic for their joint significance. Details on  $\kappa_s$  and its standard errors are in Section A.3. The lower panel reports statistics for the recovered time series  $\tilde{s}$  (see Section 3.1):  $\sigma_{\tilde{s}}$  is its standard deviation;  $tt$  and  $tt^2$  are the coefficients of the linear and quadratic time trends (with HAC significance levels);  $ADF$  and  $KPSS$  are stationarity tests in levels;  $AR(1)$  is the autoregressive coefficient from a first-order fit;  $HL$  are the 95% confidence bounds of the implied AR(1) half-life, in years.

	Baseline		S: Tot. R&D		Z: Raw TFP		Q: N.F. Empl.	
	$BS$	$LN$	$BS$	$LN$	$BS$	$LN$	$BS$	$LN$
$b_s$ (%)	1.558*** (0.429)	1.549*** (0.285)	1.066*** (0.318)	1.223*** (0.254)	0.997*** (0.355)	0.794** (0.337)	1.507*** (0.418)	1.520*** (0.289)
$T$	292	261	292	261	291	260	292	261
$R^2$ (%)	9.5	12.4	7.4	11.8	21.8	41.7	9.1	12.2
$k$	10	10	10	10	20	20	10	10
$W(k)$	79.97***	61.00***	64.56***	50.27***	287.53***	2775.10***	73.09***	61.99***
$\kappa_a$	0.964 (0.014)	0.971 (0.013)	0.950 (0.016)	0.949 (0.012)	0.945 (0.017)	0.945 (0.012)	0.955 (0.014)	0.949 (0.012)
$\tilde{s}_t$ ( $\kappa_a^t < 0.01$ )								
$T_{\tilde{s}}$	226	225	207	220	183	151	219	219
$\sigma_{\tilde{s}}$	0.058	0.057	0.068	0.065	0.060	0.062	0.055	0.055
$tt$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$tt^2$	0.00	0.00	0.00	0.00	0.00***	0.00***	0.00	0.00
ADF	-3.91***	-3.95***	-3.17***	-3.49***	-3.95***	-3.50***	-3.56***	-3.56***
KPSS	0.09	0.09	0.18	0.13	0.22	0.19	0.14	0.14
AR(1)	0.71	0.70	0.72	0.68	0.68	0.70	0.70	0.70
HL low	0.4	0.3	0.4	0.3	0.3	0.3	0.3	0.3
HL high	0.8	0.8	0.8	0.7	0.7	0.8	0.7	0.7

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01

an annualized increase of about 0.8% in TFP growth following a one-standard-deviation increase in  $\hat{s}_t$ . Control variables are always jointly significant, and specifications using LN-based controls consistently achieve higher explanatory power, as reflected in higher  $R^2$  values and lower information criteria.

Table 2 also reports the estimated implied  $\kappa_s$  and the recovered  $\tilde{s}_t$  series. Specifically,  $\tilde{s}_t$  is obtained by applying equation (19) for each  $t$  in the sample, using parameter estimates of  $\alpha_Z$  from Table 1 and  $b_s$  from Table 2. The series are trimmed at the beginning of the sample, up to the first  $t$  such that  $\kappa_s^t < 0.01$ , ensuring that the influence of the unobserved initial condition is negligible, as the omitted portion corresponds to only one-hundredth of  $\tilde{s}_0$ . Appendix A.3 provides a detailed discussion of the uncertainty in this recovery, arising both from the initial condition approximation and the estimation noise, and it also includes details on the computation of the reported standard errors. Figure 11 in Appendix C shows all recovered series with confidence intervals, illustrating that precision greatly varies across



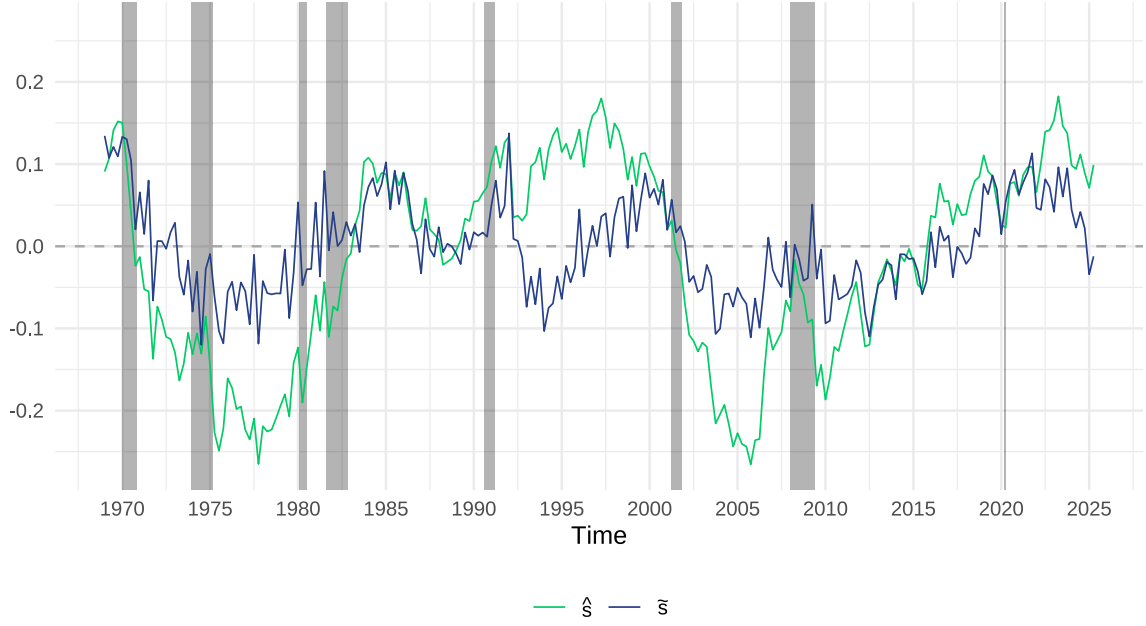


Figure 2: Baseline effective R&D measures. Shaded areas mark NBER recessions.

specifications. The series from the baseline specification, in particular, exhibit the smallest uncertainty, primarily reflecting the lower uncertainty in the estimates of  $b_s$ . Descriptive statistics reported in the lower panel of Table 2 indicate broadly consistent time series volatility across specifications. The recovered series display no trend, are stationary as confirmed by ADF and KPSS tests, and exhibit substantially lower persistence than the  $\hat{s}_t$  series. Notably, both the persistence of  $\tilde{s}$  and the magnitude of  $b_s$  are significantly lower than those assumed in the theoretical model of Kung and Schmid (2015). This discrepancy is not problematic, as the econometric framework developed in this work accounts for feedback effects between innovation and external components – a feature absent in that model but useful for capturing the more complex propagation of R&D shocks through the economy.

Figure 2 plots the baseline  $\hat{s}_t$  series alongside the  $\tilde{s}_t$  series corresponding to the baseline specification using controls based on LN factors, chosen for their superior explanatory power, though the series obtained from BS factors is virtually identical. This  $\tilde{s}_t$  series will serve as the baseline for subsequent analysis. Since the difference between  $\hat{s}_t$  and  $\tilde{s}_t$  is proportional to the external component  $a_t$ , the figure already highlights a strongly pro-cyclical behavior of innovation efforts, consistent with the predictions of Kung and Schmid (2015) and related contributions.

### 4.3 Previous evidence

By construction and purpose of use, the closest measure in the literature is Kung and Schmid (2015). They focused on a specification of effective R&D defined as the simple ratio  $S_t/I_t$ . The empirical counterpart was constructed as the ratio of U.S. annual private R&D expenditures reported by the National Science Foundation (measuring  $S_t$ ) to the R&D stock

series estimated by the U.S. Bureau of Labor Statistics (representing intangible capital  $I_t$ ). They showed that this measure of effective R&D fulfilled several theoretical predictions: it was highly persistent, co-moved at low frequencies with the price-dividend ratio, and univariately forecasted the growth rates of consumption, GDP, and TFP up to 5 years.

Their measure, however, presents a few shortcomings, documented in greater detail in Appendix C (Table 13).<sup>24</sup> Most notably, it exhibits extreme persistence, with a first-order annual autocorrelation of 0.995, with standard error 0.063. This estimate raises two potential concerns: the upper confidence bound indicates a significant risk of non-stationary behavior, while the lower bound implies persistence that may be excessively high for the productivity component it is intended to capture. Formal stationarity tests yield conflicting results: the ADF test rejects non-stationarity at the 10% level, while the KPSS test rejects stationarity at 1%, with visual inspection of the series more consistent with the latter result. While non-stationarity would not undermine the theoretical validity of the measure and the underlying theory, it would pose serious challenges for empirical applications due to the heightened risk of spurious regression results. Even disregarding stationarity concerns, an implied half-life exceeding 40 years raises questions about its economic interpretation. This persistence far exceeds that of the productivity LRR component documented in Croce (2014) and Ortu et al. (2013), which, as noted earlier, never exceeds 20 years. Although this level of persistence aligns with the consumption-based LRR calibration in Bansal and Yaron (2004), it appears too long-lived to accurately reflect the productivity channel of long-run risk. These findings cast doubt on the suitability of this effective R&D specification for identifying the productivity LRR component within this empirical framework.

The problematic dynamics of the effective R&D used by Kung and Schmid (2015) may stem from the data employed, as the measure of the stock of ideas they use is constructed through simple accumulation and depreciation of R&D expenditures, deviating from the law of motion assumed in the model. To address this inconsistency, one could construct an alternative effective R&D measure by substituting TFP for the stock of ideas (as previously argued), maintaining the assumption of labor-augmenting technology, and calibrating it using standard labor share values from the literature, as well as employing the longer datasets used in this work. However, the results exhibit similar, if not more pronounced, issues (see Table 13). The root cause likely lies in the lack of flexibility in the strength of knowledge spillovers from past innovations in the Kung and Schmid (2015) framework, a limitation that recent work, such as Bloom et al. (2020), has highlighted as crucial for achieving a good empirical fit to the data.

Another closely related measure is proposed by Kogan et al. (2017), who link changes in market valuations to patent announcements to assess the private value of successful innovations. Whereas their measure captures the outcome of the innovation process, effective R&D reflects its input side. The two measures thus offer complementary perspectives on innovation. For the purposes of this paper, however – namely, constructing a process

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<sup>24</sup>It should be noted that the R&D stock series has been updated by the provider and now covers a slightly different time period.

**Table 3:** VAR estimation diagnostics.  $N. Obs.$  and  $N. Lags$  denote the number of observations and VAR lags;  $R_{\Delta Z}^2$  is the fit of the TFP growth equation;  $\max |roots|$  is the largest root of the companion matrix;  $\kappa$  is the condition number of the residual covariance matrix.  $H-LM$  are 1-year horizon heteroskedasticity tests for TFP growth and effective R&D;  $AC-LM$  are heteroskedasticity-robust autocorrelation tests at different lags;  $F-GC(s)$  is the F-test for Granger causality with respect to effective R&D.

	Baseline	S: Tot. R&D	Z: Raw TFP	Q: N.F. Empl.	$\tilde{s}$
N. Obs.	305	305	306	305	223
N. Lags	3	3	2	3	2
$R_{\Delta Z}^2$ (%)	5.3	4.4	4.8	5.3	2.8
$\max  roots $	0.92	0.90	0.93	0.92	0.93
$\kappa$	$2.2 \times 10^3$	$5.7 \times 10^3$	$2.7 \times 10^3$	$2.2 \times 10^3$	$2.8 \times 10^3$
H-LM( $\Delta Z, 4$ )	3.2	2.3	22.6***	3.3	4.9
H-LM( $s, 4$ )	30.2***	27.0***	33.2***	29.4***	6.4
AC-LM(1)	5.8	6.3	6.2	5.1	7.2
AC-LM(8)	29.4	37.9	41.9	26.7	37.5
AC-LM(16)	69.6	68.6	69.3	69.6	69.1
AC-LM(40)	169.4	155.7	166.9	165.9	154.7
GC-F(s)	5.3***	6.5***	6.1***	5.5***	1.7

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

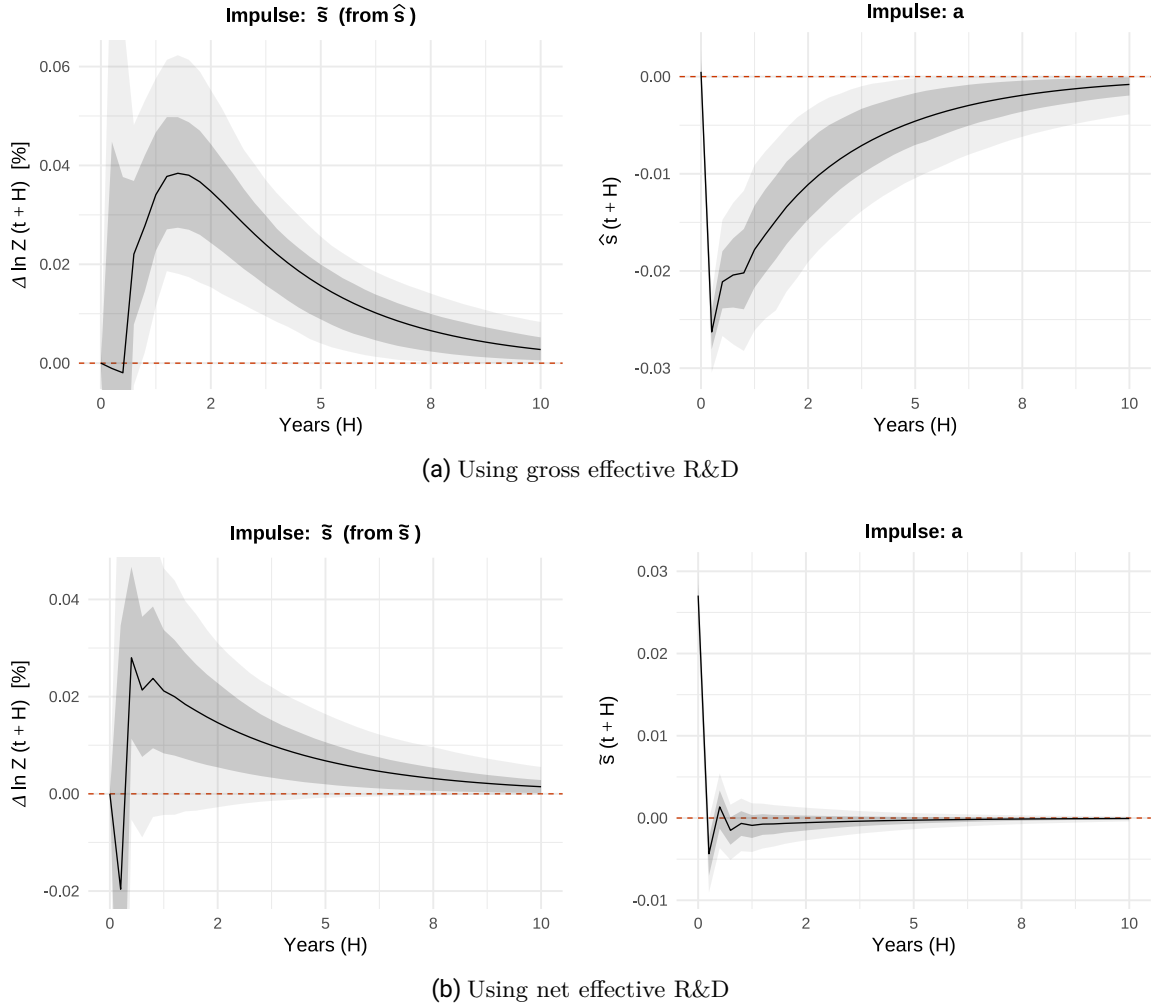
that tracks expectations of future innovation and productivity growth – effective R&D is particularly suitable. This is further supported by the results in Appendix C (Table 14), which show that effective R&D Granger-causes the innovation measure of Kogan et al. (2017), but not vice versa.

## 5 The long-run impact of effective R&D shocks

Table 3 reports the key statistics from the estimation of (22), for different specifications of  $\hat{s}$  and, in the last column, for the baseline estimate of  $\tilde{s}$ . The maximum number of lags considered is 10, with the Akaike, Hannan–Quinn, and Bayesian information criteria generally agreeing on the optimal lag length, except for the specification using raw TFP, for which the most parsimonious lag order indicated by the criteria is applied. The predictability of TFP growth, as measured by the equation  $R^2$ , is comparable to those estimates in Croce (2014) that are based on samples of similar length. The system and its estimates appear reliable: the moduli of the companion matrix roots lie well within the unit circle, and the condition number of the residual covariance matrix is moderate.

Tests on the VAR residuals, reported in the middle panel of Table 3, indicate significant heteroskedasticity in the effective R&D residuals for all specifications except that using  $\tilde{s}$ , and no significant autocorrelation at any horizon up to 10 years (based on heteroskedasticity-robust wild-bootstrap tests as in Ahlgren and Catani (2017)).

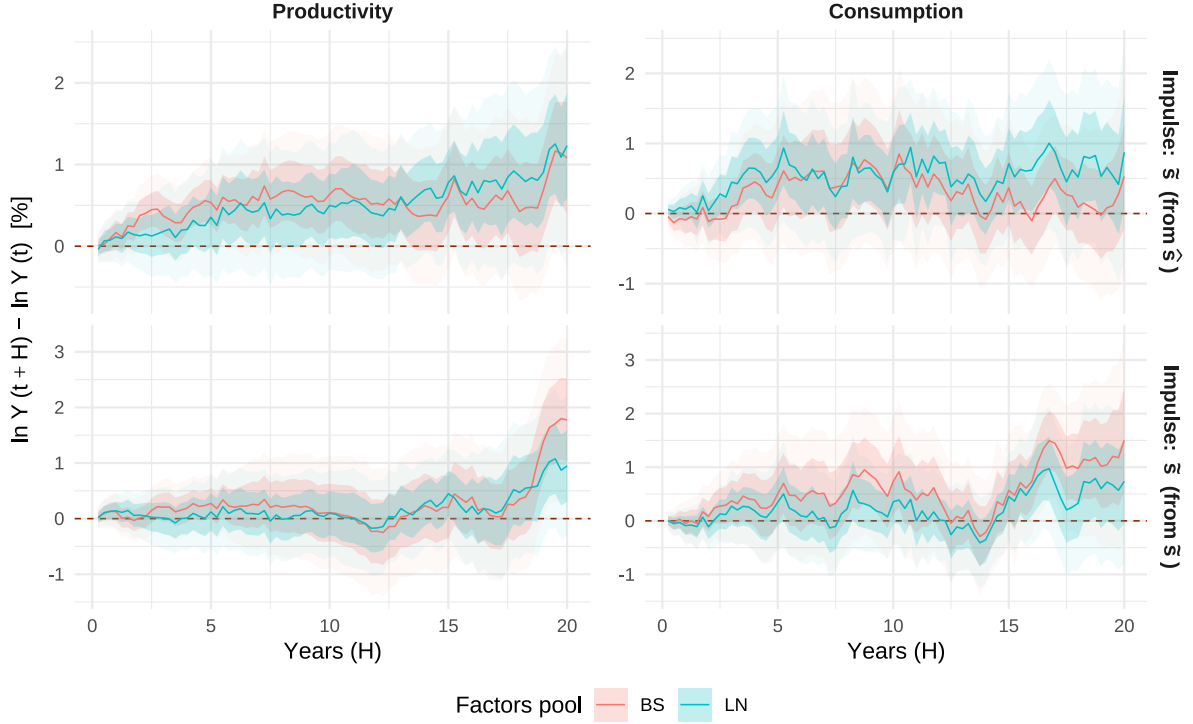
Turning to system dynamics, the Granger causality Wald test (based on a HAC covariance



**Figure 3:** VAR impulse response functions of productivity growth ( $\Delta \ln Z$ ) and effective R&D to structural shocks. Panel (a) shows estimates using the gross effective R&D measure  $\hat{s}$ , while panel (b) shows estimates using the net effective R&D measure  $\tilde{s}$ . Shaded areas indicate 95% confidence intervals based on recursive residual bootstrap standard errors. The horizon  $H$  is expressed in years.

matrix) for effective R&D is always highly significant, except for the specification using  $\tilde{s}$ , whose p-value (18%) still provides some evidence of predictive content. This weaker result is likely influenced by the shorter sample length and greater measurement error, both of which can substantially limit test power.

IRFs for the two key specifications – the baseline models using  $\hat{s}$  and  $\tilde{s}$  – are displayed in Figure 3. Structural shocks to effective R&D are always highly persistent: for the  $\hat{s}$ -based estimates, the 95% confidence interval includes zero only at horizons approaching 10 years. As expected, the  $\tilde{s}$ -based estimates are noisier, producing wider confidence intervals, but display broadly comparable dynamics, with the 68% confidence interval reaching zero only close to the 10-year horizon. Both specifications support the hypothesis of a null immediate effect of effective R&D on the external factor, assumed in Section 3.1: the response of TFP growth becomes significantly different from zero only after about one year. The systems differ in their response to external productivity shocks: gross effective R&D decreases on



**Figure 4:** Local projection cumulative impulse response functions of productivity growth ( $\Delta \ln Z$ ) and consumption growth ( $\Delta \ln C$ ) to effective R&D shocks. Top panels show responses to gross effective R&D shocks ( $\hat{s}$ ), while bottom panels show responses to net effective R&D shocks ( $\tilde{s}$ ). Shaded areas indicate 68% and 95% confidence intervals based on Montiel Olea and Plagborg-Møller (2021). BS and LN refer to different factor sets used as controls. Goodness of fit measures ( $R^2$ ) are shown in Figure 9. The horizon  $H$  is expressed in years.

impact, while net effective R&D reacts positively. The difference stems from  $\hat{s}$  incorporating the external component negatively, whereas  $\tilde{s}$  excludes it, thereby confirming the commonly assumed procyclicality of R&D investment.

The cumulative IRFs to the structural shocks identified in the VAR estimated via local projections are shown in Figure 4 (corresponding  $R^2$  values are reported in Appendix C, Figure 9). Since the aim of the local projection exercise is to provide more robust evidence on the dynamic impact of R&D shocks, these projections include five lags of both the external factor and the dependent variable (in levels), chosen to exceed the annual data frequency. With effective R&D shocks from  $\hat{s}$ , both productivity and consumption cumulative growth show significant positive effects at the 10-year horizon, and, in the case of productivity, an even larger effect at the 20-year horizon. Consumption responds significantly at horizons of 15-20 years only when LN controls are used, which also produce a higher  $R^2$  than the BS factors (Figure 9). Shocks from  $\tilde{s}$  yield weaker effects at the 10-year horizon but stronger effects between 15 and 20 years. Overall, shocks to effective R&D orthogonalized to TFP growth shocks appear to have a significant influence on long-run prospects for productivity and consumption.

## 6 The cross-sectional risk premium

### 6.1 Risk premia estimates

The optimal number of factors in the cross-section of the 183 test assets used for the robust estimation of risk premia is estimated at 6 and 14 under the two criteria of Alessi et al. (2010), while the three criteria of Bai and Ng (2002) suggest 39, 22, and one diverging estimate. Since all values from Bai and Ng (2002) are substantially higher than those from Alessi et al. (2010), which was specifically proposed as an improvement on the former, only the minimum estimate from Bai and Ng (2002) is retained. The first six principal components explain 35.4% of the variance in returns, the first fourteen account for 51.1%, and the first twenty-two for 60.4%. Scree plots of the principal component analysis are shown in Figure 13, Appendix C. A more relevant criterion for identifying the factors closest to the ‘true’ ones, however, is their ability to price the cross-section of test assets. This depends on their associated market-wide risk premia, which, combined with the test assets’ betas, yield predictions for expected returns. From this perspective, the first six factors explain 47.0% of the cross-sectional variance, the first fourteen account for 70.7%, and the first twenty-two reach 83.0% (values for all factors are shown in Figure 14). Notably, factors 7 through 14 account for only 15% of the time-series variation in returns, yet explain 24% of the cross-sectional variation. This suggests that their economic relevance in this application is likely under-estimated by the first Alessi et al. (2010) criterion.

Table 4 reports the estimated risk premia associated with the effective R&D structural shocks, for each optimal number of factors identified by the selection criteria. The first panel, where contemporaneous shocks are used, shows no premia significantly different from zero. By contrast, the second and third panels, where the factor is constructed using moving averages of the shocks at 2-year and 4-year horizons, display sizable and significant premia linked to innovation long-run risk. An exception arises only with the lowest number of test-asset factors: in that case, the premia are not statistically significant, although most t-statistics remain above 1, suggesting some evidence of priced risk. As discussed earlier, this pattern may reflect measurement error that is averaged out over time as well as investors’ underreaction to R&D news, consistent with Eberhart et al. (2004). The estimated premia are fairly stable across specifications, at about 2% per year. Overall, the results support the prediction that fluctuations in effective R&D are positively priced by investors.

### 6.2 The cash-flow channel

Table 5 reports the estimated dividend-betas for the additional portfolios in the extended pool relative to the legacy pool. Appendix C.1 reports the sensitivities for the other test assets employed. Regarding effective R&D, the results refer to the baseline structural shock and the baseline levels of (net) effective R&D,  $\tilde{s}$ .

Consumption sensitivities are predominantly positive, whereas exposures to other risks are often negative, particularly with respect to effective R&D levels. Across horizons,

**Table 4:** Risk premia estimation following Giglio and Xiu (2021). Each column reports the risk premia associated with the respective specification of effective R&D structural shocks, based on the corresponding estimations in Table 3. t-statistics are reported in square brackets. The test assets are 183 portfolios spanning 1971 Q4 to 2023 Q4. The number of factors (6, 14, and 22) corresponds to optimal selections per Alessi et al. (2010) and Bai and Ng (2002), with 22 being the smallest optimal number from the latter method.

	Baseline	S: Tot. R&D	Z: Raw TFP	Q: N.F. Empl.	$\tilde{s}$
<i>Horizon: 1 quarter</i>					
<i>6 Factors</i>	0.01 [0.93]	0.02 [0.90]	0.02 [1.22]	0.02 [1.03]	0.02 [1.28]
<i>14 Factors</i>	0.04 [1.32]	0.03 [0.74]	0.05 [1.35]	0.04 [1.12]	0.04 [1.08]
<i>22 Factors</i>	−0.01 [−0.21]	−0.09 [−1.30]	0.01 [0.09]	−0.02 [−0.38]	−0.04 [−0.55]
<i>Horizon: 2 years</i>					
<i>6 Factors</i>	0.06 [1.63]	0.04 [0.91]	0.08* [1.87]	0.06 [1.63]	0.10 [1.44]
<i>14 Factors</i>	0.22** [2.35]	0.12 [1.24]	0.27*** [2.92]	0.19** [2.05]	0.29* [1.86]
<i>22 Factors</i>	0.15 [1.12]	0.11 [0.73]	0.23* [1.81]	0.10 [0.74]	0.18 [0.84]
<i>Horizon: 4 years</i>					
<i>6 Factors</i>	0.08 [1.33]	0.07 [1.11]	0.09 [1.33]	0.08 [1.36]	0.11 [0.97]
<i>14 Factors</i>	0.48*** [3.28]	0.34** [2.50]	0.52*** [3.52]	0.45*** [3.11]	0.69*** [2.75]
<i>22 Factors</i>	0.54*** [2.80]	0.43** [2.23]	0.61*** [3.17]	0.48** [2.52]	0.80** [2.28]
Num.Obs.	213	213	213	213	213

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01

dividend-betas with respect to effective R&D, both structural shocks and levels, are stable. Consumption sensitivities are likewise stable, except for the RD (3-small) portfolio, which exhibits a significant sign reversal. By contrast, dividend-betas with respect to TFP vary sharply, especially in the adjusted specification, suggesting that differences in the moving-average horizon lead the regressor processes to capture different risks.

Regarding the portfolio sorting, several regularities emerge for innovation long-run risk. First, bigger firms consistently show smaller sensitivity in payout growth rates across all sortings, a pattern that extends to other systemic long-run risks as well. For innovation long-run risk specifically, these sensitivities are all negative. Second, dividend-betas are negative across most firm-specific R&D-intensity levels. The exception is small, highly R&D-intensive firms, which exhibit a distinctive response depending on the nature of aggregate



**Table 5:** Dividend betas for additional test assets from the extended pool at a 1-quarter and 2-year horizons (1975 Q1–2022 Q4). Stocks are double-sorted into  $2 \times 3$  portfolios by size (NYSE median) and accounting characteristics: *RD* (R&D/market cap), *To* (sales/assets), *Prof* (gross profits/assets), *Lvg* (debt/assets), *AG* (asset growth), and *TQ* (Tobin’s *Q*). Risk factors: Cons. (consumption growth), Raw/Adj. TFP (raw/adjusted total factor productivity),  $\tilde{s}$ : shock/level (effective R&D shock/level).

Portfolio	Cons.		Raw TFP		Adj. TFP		$\tilde{s}$ : shock		$\tilde{s}$ : level	
<i>Horizon</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>
RD(1-small)	0.09	0.18	0.05	0.39	−0.07	0.03	0.01	0.00	−0.59	−0.58
RD(2-small)	0.06	0.04	0.02	0.46	−0.11	0.19	0.04	−0.02	−1.16	−0.73
RD(3-small)	0.75	−0.68	0.59	1.17	−0.35	0.45	0.54	1.09	−1.55	−3.37
RD(1-big)	0.01	0.03	0.00	0.08	−0.02	−0.01	0.00	−0.03	−0.27	−0.29
RD(2-big)	0.05	0.12	0.01	0.23	−0.03	0.00	0.03	−0.07	−0.36	−0.28
RD(3-big)	0.03	0.09	−0.01	0.24	−0.07	−0.09	−0.02	−0.17	−1.20	−1.20
To(1-small)	0.05	0.13	0.05	0.27	−0.01	0.03	0.02	0.06	−0.25	−0.76
To(2-small)	0.10	0.29	−0.01	0.81	−0.13	0.22	0.01	0.28	0.20	0.99
To(3-small)	0.38	1.06	0.23	1.85	−0.15	0.08	0.12	0.75	2.64	3.53
To(1-big)	0.01	0.06	−0.01	0.08	−0.02	−0.02	−0.01	−0.05	−0.31	−0.40
To(2-big)	0.03	0.09	0.00	0.17	−0.03	−0.03	0.00	−0.07	−0.45	−0.32
To(3-big)	0.04	0.11	0.03	0.29	−0.05	0.02	0.03	0.02	−0.21	−0.24
Prof(1-small)	0.00	−0.01	−0.02	0.20	−0.07	0.11	0.01	−0.18	−1.15	−0.82
Prof(2-small)	0.23	0.58	0.11	0.97	−0.13	−0.12	0.06	0.42	1.00	0.56
Prof(3-small)	0.38	1.34	0.19	2.29	−0.15	0.35	0.09	0.71	3.98	6.16
Prof(1-big)	0.01	0.05	0.00	0.09	−0.02	−0.02	−0.01	−0.02	−0.25	−0.22
Prof(2-big)	0.03	0.08	0.00	0.16	−0.03	−0.09	0.00	−0.12	−0.64	−0.67
Prof(3-big)	0.05	0.13	0.02	0.34	−0.06	0.14	0.03	−0.05	−0.41	−0.07
Lvg(1-small)	0.01	0.15	−0.01	0.20	−0.05	−0.05	0.02	−0.09	−0.73	−0.68
Lvg(2-small)	0.18	0.47	0.08	1.03	−0.19	0.22	0.06	0.17	−0.86	0.00
Lvg(3-small)	0.10	0.30	0.04	0.75	−0.06	0.07	0.01	0.24	1.21	1.54
Lvg(1-big)	0.03	0.09	0.01	0.19	−0.04	−0.01	0.00	−0.07	−0.61	−0.52
Lvg(2-big)	0.02	0.08	0.00	0.14	−0.03	−0.06	0.00	−0.08	−0.36	−0.41
Lvg(3-big)	0.02	0.04	0.00	0.10	−0.02	0.02	0.00	−0.03	−0.19	−0.08
AG(1-small)	0.19	0.82	0.01	1.66	−0.13	0.18	0.04	0.67	2.84	3.12
AG(2-small)	0.18	0.43	0.08	1.02	−0.20	0.16	0.05	−0.07	−1.57	−0.27
AG(3-small)	0.09	0.19	0.05	0.38	−0.05	0.04	0.03	0.09	0.29	0.47
AG(1-big)	0.06	0.14	0.00	0.29	−0.09	−0.05	0.01	−0.14	−1.02	−0.84
AG(2-big)	0.02	0.05	0.01	0.21	−0.01	0.01	0.00	−0.06	−0.30	−0.49
AG(3-big)	0.01	0.07	0.00	0.08	−0.03	−0.02	0.00	−0.04	−0.29	−0.01
TQ(1-small)	0.35	0.87	0.05	2.43	−0.50	0.78	0.18	0.27	−1.51	1.92
TQ(2-small)	0.14	0.65	0.01	1.10	−0.12	−0.15	0.06	0.20	0.36	0.63
TQ(3-small)	0.06	0.14	0.05	0.24	−0.01	0.00	−0.01	−0.06	−0.13	−0.37
TQ(1-big)	0.03	0.15	−0.01	0.25	−0.06	−0.09	−0.02	−0.06	−0.51	−0.47
TQ(2-big)	0.01	0.09	−0.01	0.15	−0.03	−0.07	0.01	−0.05	−0.43	−0.52
TQ(3-big)	0.03	0.03	0.03	0.14	−0.03	0.10	0.01	−0.07	−0.35	0.03

R&D changes: their payouts raise when increases are unexpected, but fall when predictable components are included (i.e. with respect to overall effective R&D changes). Third, among small firms, variables related to financing capacity – turnover, profitability, and leverage – correlate positively with sensitivities, whereas those capturing investment opportunities show the opposite pattern, with Tobin’s  $q$  exhibiting a particularly strong negative relation with payout betas.

A full structural interpretation of the observed patterns in dividend-betas is beyond the scope of this work, but the evidence appears broadly consistent with: (i) firms benefiting from peers’ higher R&D investment, unless they simultaneously raise their own R&D investment in response to predictable aggregate R&D increases; (ii) a greater ability to generate internal cash flows – higher turnover and profitability – improving the ability to react to aggregate innovation news, particularly in smaller, typically more constrained firms, although evidence from leverage-sorted portfolios is ambiguous;<sup>25</sup> (iii) aggregate innovation tends to reduce payout growth of ‘leading’ firms, i.e. the largest and the fastest-growing ones.

Resulting estimates of risk premia from the cross-sectional step are reported in Table 6. Notably, the premia associated with consumption cash-flow risk differ markedly across horizons: they are highly significant at the 1-quarter horizon but only barely significant in the wide pool at the 2-year horizon. This decline is even more apparent in the cross-sectional  $R^2$ , which falls from roughly 20–30% to a range of 2–50% across pools. The magnitude of the premia, at the horizon common to Bansal et al. (2005), exceeds theirs but remains well within the confidence intervals.

Risk premia associated with productivity long-run risk, as measured based on moving averages of raw TFP, are much more consistent: premia are significant for two of the three test-asset pools at both horizons and explanatory power increases at the 2-year horizon. By contrast, estimates based on adjusted TFP are less stable across horizons, exhibiting negative premia at the 1-quarter horizon and positive premia at the 2-year horizon, with  $R^2$  comparable to those for raw TFP, except in the legacy pool, where  $R^2$  drops by over 50%.

Like productivity, the premia associated with innovation long-run risk, based on the structural shocks, are significant for the two widest of the three test-asset pools and remain so across horizons. By contrast, forming the risk factor from effective R&D levels yields premia that are smaller in magnitude and never significant at the 5% level, highlighting the substantial role of the predictable component of effective R&D in pricing. Nonetheless, three of the six premia estimated for effective R&D in levels have  $t$ -statistics above 1.2, indicating that some risk is still captured. Overall, these results support the notion that a substantial portion of the premia for holding long-run risk derives from cash-flow risk, consistent with the standard long-run risk framework.

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<sup>25</sup>In general, higher leverage implies reduced financial slack or even distress. This is difficult to reconcile with the finding that high-leverage portfolios do not exhibit the strongest consumption sensitivities. A more consistent interpretation is that leverage partly proxies for better access to external finance rather than distress, possibly reflecting omitted firm characteristics correlated with leverage—an issue likely exacerbated by the coarse two-by-three sorting used here.

**Table 6:** Cash-flow risk premia.  $t$ -statistics in square brackets. Risk factors: Cons. (consumption growth), Raw/Adj. TFP (raw/adjusted total factor productivity),  $\tilde{s}$ : shock/level (effective R&D shock/level). The legacy pool comprises 16 test assets (224 observations, 1967 Q1–2022 Q4); the extended pool, 51 test assets (192 observations, 1975 Q1–2022 Q4); and the wide pool, 68 test assets (192 observations, 1975 Q1–2022 Q4).

	Cons.	Raw TFP	Adj. TFP	$\tilde{s}$ : shock	$\tilde{s}$ : level
<i>Horizon: 1 quarter</i>					
<i>Legacy pool</i>	0.68	0.18	−1.47	1.16	0.02
	[1.60]	[0.84]	[−1.54]	[1.34]	[0.66]
R <sup>2</sup> (%)	30.99	0.87	58.96	38.69	19.84
MAPE (%)	0.19	0.25	0.12	0.18	0.23
<i>Ext. pool</i>	1.72**	1.97***	−2.47**	2.28**	0.06*
	[2.58]	[3.14]	[−2.12]	[2.31]	[1.68]
R <sup>2</sup> (%)	24.85	20.44	17.95	16.77	4.89
MAPE (%)	0.41	0.44	0.43	0.46	0.48
<i>Wide pool</i>	1.45***	1.38**	−1.09***	2.00**	0.03
	[3.11]	[2.39]	[−3.48]	[2.51]	[0.97]
R <sup>2</sup> (%)	18.05	14.16	4.38	14.97	4.06
MAPE (%)	0.45	0.47	0.49	0.47	0.48
<i>Horizon: 2 years</i>					
<i>Legacy pool</i>	0.26	0.20	0.27	0.35	0.01
	[1.42]	[1.48]	[0.67]	[1.40]	[0.70]
R <sup>2</sup> (%)	54.21	59.62	6.35	55.46	21.37
MAPE (%)	0.15	0.12	0.25	0.15	0.23
<i>Ext. pool</i>	0.32	0.40**	1.17**	0.71**	0.04
	[1.65]	[2.15]	[2.15]	[2.14]	[1.63]
R <sup>2</sup> (%)	3.06	23.66	29.24	20.32	4.58
MAPE (%)	0.48	0.41	0.41	0.44	0.48
<i>Wide pool</i>	0.28*	0.36**	0.42*	0.60*	0.03
	[1.93]	[2.53]	[1.71]	[1.92]	[1.26]
R <sup>2</sup> (%)	2.17	18.61	12.23	17.33	4.96
MAPE (%)	0.49	0.45	0.47	0.46	0.48

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

## 7 Conclusion

This paper focuses on a theoretical measure of aggregate R&D that captures the mediating effects of idea spillovers and product proliferation on R&D's impact on productivity growth, consistent with both fully- and semi-endogenous growth mechanisms. This measure – termed ‘effective R&D’ or the ‘innovation component’ – is designed to reflect the contribution of R&D investments to productivity growth dynamics.

A univariate empirical framework is introduced to recover fluctuations in two versions of this measure: a gross effective R&D series, derived from the cointegration relationship among R&D, TFP, and labor force; and a net measure, constructed recursively relying on a one-period TFP growth forecast. Both series are stationary in quarterly U.S. data, though they differ markedly in persistence: the gross measure exhibits half-lives of 3 to 21 years, while the net measure displays a half-life of less than one year.

Embedding either series in a VAR with productivity growth shows that innovation shocks generate persistent movements in productivity growth, propagating over horizons of a decade. Structural identification ensures that shocks to effective R&D are orthogonal to contemporaneous productivity growth, while local projection exercises confirm these dynamics and extend them to consumption growth, which responds to innovation shocks at horizons well beyond the business cycle, possibly up to 15 years.

The paper's primary contribution is demonstrating that shocks to the innovation component constitute a significant cross-sectional risk factor, consistent with long-run risk asset pricing theories, associated to a substantial premium, in the order of 2% annually. This finding is particularly robust given that recent estimation techniques control for omitted risk factors and the structural VAR identification rules out spurious results due to correlations with other productivity-related factors.

The analysis further highlights the importance of the cash-flow channel in innovation long-run risk and reveals heterogeneous exposures across firm characteristics linked to R&D. In particular, payouts of small, R&D-intensive firms increase with aggregate R&D shocks, while those of other R&D-sorted portfolios decline. Measures of internal financing capacity (turnover, profitability) correlate positively with payout sensitivities, whereas proxies for investment opportunities (asset growth, Tobin's  $q$ ) correlate negatively.

Taken together, these findings establish aggregate innovation as a fundamental macroeconomic risk factor with distinct asset pricing implications. Beyond this contribution, the empirical methodology developed here provides a platform for future work exploring international evidence, firm-level responses, and the differential roles of alternative types of R&D, among others.

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## References

- Aghion, Philippe et al. (2012). ‘CREDIT CONSTRAINTS AND THE CYCLICALITY OF R&D INVESTMENT: EVIDENCE FROM FRANCE: Aghion et al. Credit Constraints and the Cyclicity of R&D Investment’. In: *Journal of the European Economic Association* 10.5, pp. 1001–1024.
- Ahlgren, Niklas and Paul Catani (2017). ‘Wild bootstrap tests for autocorrelation in vector autoregressive models’. In: *Statistical Papers* 58.4, pp. 1189–1216.
- Ahmed, Shamim, Ziwen Bu, and Xiaoxia Ye (2025). ‘Illiquidity, R&D Investment, and Stock Returns’. In: *Journal of Money, Credit and Banking* 57.4, pp. 981–1022.
- Ai, Hengjie et al. (2018). ‘News Shocks and the Production-Based Term Structure of Equity Returns’. In: *The Review of Financial Studies* 31 (7), pp. 2423–2467.
- Aksoy, Yunus et al. (1, 2019). ‘Demographic Structure and Macroeconomic Trends’. In: *American Economic Journal: Macroeconomics* 11.1, pp. 193–222.
- Alessi, Lucia, Matteo Barigozzi, and Marco Capasso (1, 2010). ‘Improved penalization for determining the number of factors in approximate factor models’. In: *Statistics & Probability Letters* 80.23, pp. 1806–1813.
- Antolin-Diaz, Juan and Paolo Surico (1, 2025). ‘The Long-Run Effects of Government Spending’. In: *American Economic Review* 115.7, pp. 2376–2413.
- Anzoategui, Diego et al. (1, 2019). ‘Endogenous Technology Adoption and R&D as Sources of Business Cycle Persistence’. In: *American Economic Journal: Macroeconomics* 11.3, pp. 67–110.
- Bai, Jushan and Serena Ng (2002). ‘Determining the Number of Factors in Approximate Factor Models’. In: *Econometrica* 70.1, pp. 191–221.
- Bansal, Ravi, Robert F. Dittmar, and Christian T. Lundblad (2005). ‘Consumption, Dividends, and the Cross Section of Equity Returns’. In: *The Journal of Finance* 60 (4), pp. 1639–1672.
- Bansal, Ravi, Marcelo Ochoa, and Dana Kiku (15, 2021). *Climate Change Risk*. Rochester, NY.
- Bansal, Ravi and Ivan Shaliastovich (2013). ‘A Long-Run Risks Explanation of Predictability Puzzles in Bond and Currency Markets’. In: *Review of Financial Studies* 26 (1), pp. 1–33.
- Bansal, Ravi and Amir Yaron (2004). ‘Risks for the Long Run: A Potential Resolution of Asset Pricing Puzzles’. In: *The Journal of Finance* 59 (4), pp. 1481–1509.

- Beeler, Jason and John Y. Campbell (1, 2012). ‘The Long-Run Risks Model and Aggregate Asset Prices: An Empirical Assessment’. In: *Critical Finance Review* 1.1, pp. 141–182.
- Benigno, Gianluca and Luca Fornaro (1, 2018). ‘Stagnation Traps’. In: *The Review of Economic Studies* 85.3, pp. 1425–1470.
- Beqiraj, Elton et al. (2025). ‘Persistent slumps: Innovation and the credit channel of monetary policy’. In: *European Economic Review* 172, p. 104946.
- Bhandari, Laxmi Chand (1988). ‘Debt/Equity Ratio and Expected Common Stock Returns: Empirical Evidence’. In: *The Journal of Finance* 43.2, pp. 507–528.
- Bloom, Nicholas et al. (2020). ‘Are Ideas Getting Harder to Find?’ In: *American Economic Review* 110 (4), pp. 1104–1144.
- Bottazzi, Laura and Giovanni Peri (2007). ‘The International Dynamics of R&D and Innovation in the Long Run and in the Short Run’. In: *The Economic Journal* 117 (518), pp. 486–511.
- Brown, James R., Steven M. Fazzari, and Bruce C. Petersen (2009). ‘Financing Innovation and Growth: Cash Flow, External Equity, and the 1990s R&D Boom’. In: *The Journal of Finance* 64.1, pp. 151–185.
- Bryzgalova, Svetlana, Christian Julliard, and Jiantao Huang (2025). ‘Consumption in Asset Returns’. In: *SSRN Electronic Journal*.
- Bureau of Economic Analysis (2024). ‘Chapter 4: Estimating Methods’. In: *NIPA Handbook: Concepts and Methods of the U.S. National Income and Product Accounts*. U.S. Department of Commerce, Bureau of Economic Analysis. Chap. 4.
- Campbell, John Y. (1996). ‘Understanding Risk and Return’. In: *Journal of Political Economy* 104 (2), pp. 298–345.
- Campbell, John Y. and Tuomo Vuolteenaho (1, 2004). ‘Bad Beta, Good Beta’. In: *American Economic Review* 94.5, pp. 1249–1275.
- Chan, Louis K.C., Josef Lakonishok, and Theodore Sougiannis (2001). ‘The stock market valuation of research and development expenditures’. In: *Journal of Finance* 56 (6), pp. 2431–2456.
- Chung, Kee H. and Stephen W. Pruitt (1994). ‘A Simple Approximation of Tobin’s  $q$ ’. In: *Financial Management* 23.3, p. 70.
- Cochrane, John H. (2005). *Asset pricing*. Rev. ed. Princeton, N.J: Princeton University Press. 533 pp. ISBN: 978-0-691-12137-6.
- Colacito, Riccardo and Mariano Massimiliano Croce (2011). ‘Risks for the Long Run and the Real Exchange Rate’. In: *Journal of Political Economy* 119.1, pp. 153–181.
- Comin, Diego and Mark Gertler (1, 2006). ‘Medium-Term Business Cycles’. In: *American Economic Review* 96.3, pp. 523–551.
- Constantinides, George M. and Anisha Ghosh (2011). ‘Asset Pricing Tests with Long-run Risks in Consumption Growth’. In: *Review of Asset Pricing Studies* 1.1, pp. 96–136.
- Cooper, Michael J., Huseyin Gulen, and Michael J. Schill (2008). ‘Asset Growth and the Cross-Section of Stock Returns’. In: *The Journal of Finance* 63.4, pp. 1609–1651.

- Croce, Mariano Massimiliano (2014). ‘Long-run productivity risk: A new hope for production-based asset pricing?’ In: *Journal of Monetary Economics* 66, pp. 13–31.
- Dew-Becker, Ian and Stefano Giglio (2016). ‘Asset Pricing in the Frequency Domain: Theory and Empirics’. In: *Review of Financial Studies* 29.8, pp. 2029–2068.
- Eberhart, Allan C., William F. Maxwell, and Akhtar R. Siddique (2004). ‘An Examination of Long-Term Abnormal Stock Returns and Operating Performance Following R&D Increases’. In: *The Journal of Finance* 59.2, pp. 623–650.
- Epstein, Larry G., Emmanuel Farhi, and Tomasz Strzalecki (2014). ‘How Much Would You Pay to Resolve Long-Run Risk?’ In: *American Economic Review* 104.9, pp. 2680–2697.
- Epstein, Larry G. and Stanley E. Zin (1989). ‘Substitution, Risk Aversion, and the Temporal Behavior of Consumption and Asset Returns: A Theoretical Framework’. In: *Econometrica* 57 (4), p. 937.
- Evans, George W., Seppo Honkapohja, and Paul Romer (1998). ‘Growth Cycles’. In: *The American Economic Review* 88.3, pp. 495–515.
- Fama, Eugene F. and Kenneth R. French (2015). ‘A five-factor asset pricing model’. In: *Journal of Financial Economics* 116.1, pp. 1–22.
- Fama, Eugene F. and James D. Macbeth (1973). ‘Risk, Return, and Equilibrium: Empirical Tests’. In: *Journal of Political Economy* 81 (3), pp. 607–636.
- Fernald, John G. (2012). ‘A Quarterly, Utilization-Adjusted Series on Total Factor Productivity’. In: *Federal Reserve Bank of San Francisco, Working Paper Series*, pp. 01–28.
- Giglio, Stefano and Dacheng Xiu (1, 2021). ‘Asset Pricing with Omitted Factors’. In: *Journal of Political Economy* 129.7, pp. 1947–1990.
- Gourieroux, Christian and Joann Jasiak (30, 2024). ‘Long-run risk in stationary vector autoregressive models’. In: *Journal of Econometrics*, p. 105905.
- Gürkaynak, Refet S., Brian Sack, and Jonathan H. Wright (2007). ‘The U.S. Treasury yield curve: 1961 to the present’. In: *Journal of Monetary Economics* 54.8, pp. 2291–2304.
- Ha, Joonkyung and Peter Howitt (2007). ‘Accounting for Trends in Productivity and R&D: A Schumpeterian Critique of Semi-Endogenous Growth Theory’. In: *Journal of Money, Credit and Banking* 39 (4), pp. 733–774.
- Hall, B. H. (1, 2002). ‘The Financing of Research and Development’. In: *Oxford Review of Economic Policy* 18.1, pp. 35–51.
- Hall, Bronwyn H., Jacques Mairesse, and Pierre Mohnen (2010). ‘Measuring the Returns to R&D’. In: *Handbook of the Economics of Innovation*. Vol. 2. Elsevier, pp. 1033–1082. ISBN: 978-0-444-53609-9.
- Hansen, Lars Peter, John C. Heaton, and Nan Li (2005). *Intangible Risk*.
- Haugen, Robert A. and Nardin L. Baker (1996). ‘Commonality in the determinants of expected stock returns’. In: *Journal of Financial Economics* 41.3, pp. 401–439.
- Herzer, Dierk (1, 2022a). ‘Semi-endogenous Versus Schumpeterian Growth Models: A Critical Review of the Literature and New Evidence’. In: *Review of Economics* 73.1, pp. 1–55.



- Herzer, Dierk (1, 2022b). ‘The impact of domestic and foreign R&D on TFP in developing countries’. In: *World Development* 151, p. 105754.
- Hodrick, Robert J. (1992). ‘Dividend Yields and Expected Stock Returns: Alternative Procedures for Inference and Measurement’. In: *Review of Financial Studies* 5 (3), pp. 357–386.
- Hou, Kewei, Chen Xue, and Lu Zhang (2015). ‘Digesting Anomalies: An Investment Approach’. In: *Review of Financial Studies* 28.3, pp. 650–705.
- Hsu, Po-Hsuan (2009). ‘Technological innovations and aggregate risk premiums’. In: *Journal of Financial Economics* 94.2, pp. 264–279.
- Jensen, Theis Ingerslev, Bryan T. Kelly, and Lasse Heje Pedersen (2021). ‘Is There a Replication Crisis in Finance?’ In: *SSRN Electronic Journal*.
- Jiang, Yi, Yiming Qian, and Tong Yao (2016). ‘R&D Spillover and Predictable Returns\*’. In: *Review of Finance* 20 (5), pp. 1769–1797.
- Jinnai, Ryo (2014). ‘R&D Shocks and News Shocks’. In: *Journal of Money, Credit and Banking* 46.7, pp. 1457–1478.
- Jones, Charles I (1, 1999). ‘Growth: With or Without Scale Effects?’ In: *American Economic Review* 89.2, pp. 139–144.
- (2005). ‘Growth and Ideas’. In: *Handbook of Economic Growth*. Vol. 1, pp. 1063–1111. ISBN: 978-0-444-52043-2.
- Jordà, Òscar (1, 2005). ‘Estimation and Inference of Impulse Responses by Local Projections’. In: *American Economic Review* 95.1, pp. 161–182.
- Kaltenbrunner, Georg and Lars A. Lochstoer (2010). ‘Long-Run Risk through Consumption Smoothing’. In: *Review of Financial Studies* 23 (8), pp. 3190–3224.
- Kogan, Leonid et al. (1, 2017). ‘Technological Innovation, Resource Allocation, and Growth\*’. In: *The Quarterly Journal of Economics* 132.2, pp. 665–712.
- Kruse-Andersen, Peter K. (2023). ‘Testing R&D-Based Endogenous Growth Models\*’. In: *Oxford Bulletin of Economics and Statistics* n/a (n/a).
- Kung, Howard and Lukas Schmid (2015). ‘Innovation, Growth, and Asset Prices’. In: *The Journal of Finance* 70 (3), pp. 1001–1037.
- Lettau, Martin and Sydney C. Ludvigson (2001). ‘Consumption, Aggregate Wealth, and Expected Stock Returns’. In: *The Journal of Finance* 56 (3), pp. 815–849.
- Leung, Woon Sau, Kevin P. Evans, and Khelifa Mazouz (2020). ‘The R&D anomaly: Risk or mispricing?’ In: *Journal of Banking & Finance* 115, p. 105815.
- Li, Dongmei (2011). ‘Financial Constraints, R&D Investment, and Stock Returns’. In: *Review of Financial Studies* 24.9, pp. 2974–3007.
- Lin, Xiaoji (2011). ‘Endogenous technological progress and the cross-section of stock returns \$’. In.
- Liu, Yukun and Ben Matthies (1, 2022). ‘Long-Run Risk: Is It There?’ In: *The Journal of Finance* 77.3, pp. 1587–1633.
- Ludvigson, Sydney C. and Serena Ng (2009). ‘Macro Factors in Bond Risk Premia’. In: *Review of Financial Studies* 22 (12), pp. 5027–5067.

- Lütkepohl, Helmut (2005). *New Introduction to Multiple Time Series Analysis*. Berlin, Heidelberg: Springer Berlin Heidelberg. ISBN: 978-3-540-40172-8 978-3-540-27752-1.
- Madsen, Jakob B. (2008). ‘Semi-endogenous versus Schumpeterian growth models: testing the knowledge production function using international data’. In: *Journal of Economic Growth* 13.1, pp. 1–26.
- Maletic, Matjaz (2018). ‘Profitability, R&D Investments and the Cross-Section of Stock Returns’. In: *SSRN Electronic Journal*.
- Mehra, Rajnish and Edward C. Prescott (1985). ‘The equity premium: A puzzle’. In: *Journal of Monetary Economics* 15.2, pp. 145–161.
- Melone, Alessandro (2021). ‘Consumption Disconnect Redux’. In: *SSRN Electronic Journal*.
- Montiel Olea, José Luis and Mikkel Plagborg-Møller (2021). ‘Local Projection Inference Is Simpler and More Robust Than You Think’. In: *Econometrica* 89.4, pp. 1789–1823.
- Moran, Patrick and Albert Queralto (2018). ‘Innovation, productivity, and monetary policy’. In: *Journal of Monetary Economics* 93, pp. 24–41.
- Müller, Ulrich K. (1, 2005). ‘Size and power of tests of stationarity in highly autocorrelated time series’. In: *Journal of Econometrics* 128.2, pp. 195–213.
- Novy-Marx, Robert (2013). ‘The other side of value: The gross profitability premium’. In: *Journal of Financial Economics* 108.1, pp. 1–28.
- Ortu, Fulvio, Andrea Tamoni, and Claudio Tebaldi (2013). ‘Long-Run Risk and the Persistence of Consumption Shocks’. In: *Review of Financial Studies* 26 (11), pp. 2876–2915.
- Peretto, Pietro F. (1998). ‘Technological Change and Population Growth’. In: *Journal of Economic Growth* 3.4, pp. 283–311.
- Phillips, Peter C. B. and Bruce E. Hansen (1990). ‘Statistical Inference in Instrumental Variables Regression with I(1) Processes’. In: *The Review of Economic Studies* 57.1, p. 99.
- Rajan, Raghuram G. and Luigi Zingales (1995). ‘What Do We Know about Capital Structure? Some Evidence from International Data’. In: *The Journal of Finance* 50.5, pp. 1421–1460.
- Ready, Robert C (2018). ‘Oil consumption, economic growth, and oil futures: The impact of long-run oil supply uncertainty on asset prices’. In: *Journal of Monetary Economics* 94, pp. 1–26.
- Reeb, David M. and Wanli Zhao (2020). ‘Patents do not measure innovation success’. In: *Critical Finance Review* 9.1, pp. 157–199.
- Romer, Paul M. (1987). ‘Growth Based on Increasing Returns Due to Specialization’. In: *The American Economic Review* 77.2, pp. 56–62.
- (1990). ‘Endogenous Technological Change’. In: *Journal of Political Economy* 98.5, S71–S102.
- Rotemberg, Julio J (1, 2003). ‘Stochastic Technical Progress, Smooth Trends, and Nearly Distinct Business Cycles’. In: *American Economic Review* 93.5, pp. 1543–1559.
- Schorfheide, Frank, Dongho Song, and Amir Yaron (2018). ‘Identifying Long-Run Risks: A Bayesian Mixed-Frequency Approach’. In: *Econometrica* 86.2, pp. 617–654.
- Sedgley, Norman and Bruce Elmslie (11, 2013). ‘THE DYNAMIC PROPERTIES OF ENDOGENOUS GROWTH MODELS’. In: *Macroeconomic Dynamics* 17.5, pp. 1118–1134.

- Stock, James H. and Mark W Watson (1993). ‘A Simple Estimator of Cointegrating Vectors in Higher Order Integrated Systems’. In: *Econometrica* 61 (4), p. 783.
- Vogelsang, Timothy J. and Martin Wagner (2014). ‘Integrated modified OLS estimation and fixed- inference for cointegrating regressions’. In: *Journal of Econometrics* 178.2, pp. 741–760.
- Zhang, Wei (12, 2014). ‘R&D investment and distress risk’. In: *Journal of Empirical Finance* 32, pp. 94–114.

## A Additional derivations

### A.1 A simple full model

#### Model Closure

To characterize a Balanced Growth Path (BGP) in an economy featuring conditions (6) and (7) from Section 2, first assume the production function

$$Y_t = e^{a_t} I_t^\xi L_t, \quad (34)$$

where output only depends on the labor employed  $L_t$  and some elements scaling its productivity,  $e^{a_t} I_t^\xi$ , which constitute the so-called Total Factor Productivity (TFP) level. Next, consider the resource constraint of the economy

$$Y_t = C_t + S_t, \quad (35)$$

where  $C_t$  is consumption. Next, in the spirit of Jones (2005), assume a stochastic rule of thumb as a policy rule for resources allocation:

$$S_t = e^{\tilde{s}_t} Y_t. \quad (36)$$

Lastly, assume an exogenous non-degenerate growth rate for the labor force,  $\Delta \ln L_t$ .

#### The approximately linear law of motion of ideas

From (6) it follows that

$$\ln Z_t = a_t + \xi \ln I_t, \quad (37)$$

while from (7) it follows that

$$\Delta \ln I_{t+1} = \ln \left\{ 1 - \phi + \chi \cdot S_t^\eta I_t^{-(1-\psi)} Q_t^{-\omega} \right\}, \quad (38)$$

which for small values can be well approximated by

$$\Delta \ln I_{t+1} \cong -\phi + \chi \cdot S_t^\eta I_t^{-(1-\psi)} Q_t^{-\omega}. \quad (39)$$

The shorter the time steps, the more accurate the approximation is. For small values of  $S_t^\eta I_t^{-(1-\psi)} Q_t^{-\omega}$ , this can be further approximated as

$$\exp \left\{ \ln \left[ S_t^\eta I_t^{-(1-\psi)} Q_t^{-\omega} \right] \right\} = \exp \{ \eta \ln S_t - (1-\psi) \ln I_t - \omega \ln Q_t \} \quad (40)$$

$$\cong 1 + \eta \ln S_t - (1-\psi) \ln I_t - \omega \ln Q_t, \quad (41)$$

which leads to

$$\Delta \ln I_{t+1} \cong -\phi + \chi (1 + \eta \ln S_t - (1-\psi) \ln I_t - \omega \ln Q_t). \quad (42)$$

This can be more succinctly written as

$$\Delta \ln I_{t+1} \cong (\chi - \phi) + \chi \eta \left( \ln S_t - \left( \frac{1-\psi}{\eta} \right) \ln I_t - \left( \frac{\omega}{\eta} \right) \ln Q_t \right). \quad (43)$$

Plugging  $\ln I_t$ , and the implied  $\Delta \ln I_t$ , from (37), one gets

$$\frac{1}{\xi} (\Delta \ln Z_{t+1} - \Delta a_{t+1}) \cong (\chi - \phi) + \chi \eta \left( \ln S_t - \left( \frac{1-\psi}{\eta} \right) \frac{1}{\xi} (\ln Z_t - a_t) - \left( \frac{\omega}{\eta} \right) \ln Q_t \right). \quad (44)$$

Rearranging:

$$\Delta \ln Z_{t+1} \cong \xi (\chi - \phi) + \xi \chi \eta \left( \ln S_t - \left( \frac{1-\psi}{\eta \xi} \right) (\ln Z_t - a_t) - \left( \frac{\omega}{\eta} \right) \ln Q_t \right) + \Delta a_{t+1}. \quad (45)$$

It is clear that bringing (45) to the data as illustrated in the main text does not allow to identify the structural parameters. Thus, assuming  $\kappa \neq 1$  in  $Q_t = L_t^\kappa$  does not affect the interpretation of empirical results. Therefore, I will maintain this assumption in the theoretical analysis of this appendix.

### The Balanced Growth Path

Assuming that the consumption share of output is not integrated of order 2 or higher, implies

$$\mathbb{E} [\Delta \tilde{s}_t] = \mu_s. \quad (46)$$

Then,

$$\mathbb{E} [\Delta \ln S_t] = \mu_s + \mathbb{E} [\Delta \ln Y_t] \quad (47)$$

$$= \mu_s + \mathbb{E} [\Delta a_t + \xi \Delta \ln I_t + \Delta \ln L_t]. \quad (48)$$

From stationarity of TFP growth and of the first differences of the external component  $a_t$ ,  $\Delta \ln I_t$  is implied to be stationary too, making its unconditional expectation a finite value. Therefore, differencing both sides of (43), substituting  $L_t$  for  $Q_t$ , and taking expectations of

them returns

$$\mathbb{E} \left[ \Delta \ln S_t - \frac{1-\psi}{\eta} \Delta \ln I_t - \frac{\omega}{\eta} \Delta \ln L_t \right] = 0. \quad (49)$$

Subtracting (49) from (48), one gets an expression for the unconditional expectation of the growth rate of ideas' stock that is only function of structural variables:

$$\mathbb{E} [\Delta \ln I_t] = \frac{\eta - \omega}{1 - \psi - \xi \eta} \cdot \mathbb{E} [\Delta \ln L_t] + \frac{\mathbb{E} [\Delta a_t]}{1 - \psi - \xi \eta} + \frac{\mu_s \eta}{1 - \psi - \xi \eta}. \quad (50)$$

Clearly, the order of integration of  $a_t$  does not need to be 0, but cannot be integrated or order 2 or higher either, in this theoretical framework. (50) shows the basis for the domain restriction on  $\psi$  stated in the main text, while the positivity of  $\eta$ ,  $\psi$ ,  $\xi$ , and  $\omega$  is taken as given, since R&D increasing productive inputs' productivity and past ideas increasing R&D impact are the conceptual foundations of the endogenous growth theory. It should be noted that products' variety can impact final goods productivity, but this channel is not explicitly considered here, although in principle it is captured by  $a_t$ . Finally, leveraging the definition of excess effective R&D and rewriting (38) as  $\mathbb{E} [\Delta \ln I_t] = \gamma'_0 + \gamma'_1(\bar{s} + \tilde{s}_t)$ , an expression determining the BGP value of  $\bar{s}$  can be derived from

$$\bar{s} = \frac{\mathbb{E} [\Delta \ln I_t] - \gamma'_0}{\gamma'_1}. \quad (51)$$

## A.2 The derivation of the structural systems

### The structural system with gross effective R&D

Considering  $\tilde{s}_t = \hat{s}_t + \alpha_Z a_t$ , (21) can be rewritten as

$$a_{t+1} = \theta_s(\hat{s}_t + \alpha_Z a_t) + \rho_a a_t + b_{aa} \varepsilon_{a,t+1} \quad (52a)$$

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s)(\hat{s}_t + \alpha_Z a_t) + (\rho_a - 1)a_t + b_{aa} \varepsilon_{a,t+1} \quad (52b)$$

$$\hat{s}_{t+1} + \alpha_Z a_{t+1} = \rho_s(\hat{s}_t + \alpha_Z a_t) + \theta_a a_t + b_{as} \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1}, \quad (52c)$$

from which follows then

$$a_{t+1} = \theta_s \hat{s}_t + (\rho_a + \theta_s \alpha_Z) a_t + b_{aa} \varepsilon_{a,t+1} \quad (53a)$$

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s) \hat{s}_t + (\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1) a_t + b_{aa} \varepsilon_{a,t+1} \quad (53b)$$

$$\begin{aligned} \hat{s}_{t+1} &= (\rho_s - \alpha_Z \theta_s) \hat{s}_t + [\theta_a + \alpha_Z(\rho_s - \rho_a - \alpha_Z \theta_s)] a_t + \\ &\quad (b_{as} - \alpha_Z b_{aa}) \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1}. \end{aligned} \quad (53c)$$

Note also that if  $a_t$  is I(1), then the system (21) could be rewritten as

$$\Delta a_{t+1} = \theta_s \tilde{s}_t + b_{aa} \varepsilon_{a,t+1} \quad (54a)$$

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s) \tilde{s}_t + b_{aa} \varepsilon_{a,t+1} \quad (54b)$$

$$\tilde{s}_{t+1} = \rho_s \tilde{s}_t + \theta_a a_t + b_{as} \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1} . \quad (54c)$$

and (53) would become

$$a_{t+1} = \theta_s \hat{s}_t + (\theta_s \alpha_Z + 1) a_t + b_{aa} \varepsilon_{a,t+1} \quad (55a)$$

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s) \hat{s}_t + \alpha_Z (\gamma_1 + \theta_s) a_t + b_{aa} \varepsilon_{a,t+1} \quad (55b)$$

$$\begin{aligned} \hat{s}_{t+1} = & (\rho_s - \alpha_Z \theta_s) \hat{s}_t + [\theta_a + \alpha_Z (\rho_s - (1 + \theta_s \alpha_Z))] a_t + \\ & (b_{as} - \alpha_Z b_{aa}) \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1} . \end{aligned} \quad (55c)$$

As both  $\Delta \ln Z_{t+1}$  and  $\hat{s}_t$  are strongly supported to be stationary empirically, (55b) implies that  $a_t$  must likewise be  $I(0)$ , except under the strict condition  $\theta_s = -\gamma_1$ . Note that if  $\theta_s = -\gamma_1$ ,  $\hat{s}_t$  would have no impact on productivity growth at all. This restriction is rejected by all the tests in this study; however, this does not constitute conclusive evidence against unit root behavior in  $a_t$ , since such behavior would also alter the inferential theory underlying the tests. Anyway, such a possibility would correspond to external factors perfectly offsetting the effect of R&D on TFP growth, thereby canceling any role of R&D, a conclusion at odds with the entire literature on endogenous growth.

## 2-variable systems

From (21b),

$$a_t = \frac{1}{\rho_a - 1} [\Delta \ln Z_{t+1} - (\gamma_1 + \theta_s) \tilde{s}_t - b_{aa} \varepsilon_{a,t+1}] , \quad (56)$$

so (21a) can be rewritten as

$$a_{t+1} = \frac{\rho_a}{\rho_a - 1} \Delta \ln Z_{t+1} + \left[ \theta_s + \frac{\rho_a (\gamma_1 + \theta_s)}{1 - \rho_a} \right] \tilde{s}_t + \frac{b_{aa}}{1 - \rho_a} \varepsilon_{a,t+1} . \quad (57)$$

This allows to rewrite the system in (21) as

$$\Delta \ln Z_{t+1} = (\gamma_1 + \theta_s) \tilde{s}_t + \rho_a \Delta \ln Z_t - (\theta_s + \rho_a \gamma_1) \tilde{s}_{t-1} + b_{aa} \varepsilon_{a,t+1} - b_{aa} \varepsilon_{a,t} \quad (58)$$

$$\begin{aligned} \tilde{s}_{t+1} = & \rho_s \tilde{s}_t - \frac{\theta_a \rho_a}{1 - \rho_a} \Delta \ln Z_t + \left( \theta_a \theta_s + \frac{\theta_a \rho_a (\gamma_1 + \theta_s)}{1 - \rho_a} \right) \tilde{s}_{t-1} + \\ & b_{as} \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1} + \frac{\theta_a b_{aa}}{1 - \rho_a} \varepsilon_{a,t} , \end{aligned} \quad (59)$$

Similarly, from system (62),

$$a_t = \frac{1}{\alpha_Z (\gamma_1 + \theta_s) + \rho_a - 1} [\Delta \ln Z_{t+1} - (\gamma_1 + \theta_s) \hat{s}_t - b_{aa} \varepsilon_{a,t+1}] , \quad (60)$$

so

$$a_{t+1} = \frac{\rho_a + \theta_s \alpha_Z}{\alpha_Z (\gamma_1 + \theta_s) + \rho_a - 1} \Delta \ln Z_{t+1} +$$

$$\begin{aligned} & \left( \theta_s - (\gamma_1 + \theta_s) \frac{\rho_a + \theta_s \alpha_Z}{\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1} \right) \hat{s}_t + \\ & b_{aa} \left( \frac{\alpha_Z \gamma_1 - 1}{\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1} \right) \varepsilon_{a,t+1}, \end{aligned} \quad (61)$$

resulting in

$$\begin{aligned} \Delta \ln Z_{t+1} &= (\gamma_1 + \theta_s) \hat{s}_t + (\rho_a + \theta_s \alpha_Z) \Delta \ln Z_t + \\ & [\theta_s (\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1) - (\gamma_1 + \theta_s)(\rho_a + \theta_s \alpha_Z)] \hat{s}_{t-1} + \\ & b_{aa} \varepsilon_{a,t+1} + (b_{aa} \alpha_Z \gamma_1 - 1) \varepsilon_{a,t} \end{aligned} \quad (62)$$

$$\begin{aligned} \hat{s}_{t+1} &= (\rho_s - \alpha_Z \theta_s) \hat{s}_t + \frac{[\theta_a + \alpha_Z(\rho_s - \rho_a - \alpha_Z \theta_s)](\rho_a + \theta_s \alpha_Z)}{\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1} \Delta \ln Z_t + \\ & [\theta_a + \alpha_Z(\rho_s - \rho_a - \alpha_Z \theta_s)] \left( \theta_s - \frac{(\gamma_1 + \theta_s)(\rho_a + \theta_s \alpha_Z)}{\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1} \right) \hat{s}_{t-1} + \\ & (b_{as} - \alpha_Z b_{aa}) \varepsilon_{a,t+1} + b_{ss} \varepsilon_{s,t+1} + \\ & b_{aa} \left( \frac{[\theta_a + \alpha_Z(\rho_s - \rho_a - \alpha_Z \theta_s)](\alpha_Z \gamma_1 - 1)}{\alpha_Z(\gamma_1 + \theta_s) + \rho_a - 1} \right) \varepsilon_{a,t}. \end{aligned} \quad (63)$$

### A.3 The recursive recovery of effective R&D

After rewriting (18) as

$$a_t = \frac{1}{\alpha_Z} (\tilde{s}_t - \hat{s}_t), \quad (64)$$

and (8) as

$$\overline{\Delta \ln Z_{t+1}} \equiv \Delta \ln Z_{t+1} - \mu = \gamma_1 \tilde{s}_t + \frac{1}{\alpha_Z} (\tilde{s}_{t+1} - \hat{s}_{t+1}), \quad (65)$$

straightforward rearrangement yields

$$\tilde{s}_{t+1} = \alpha_Z \overline{\Delta \ln Z_{t+1}} + \Delta \hat{s}_{t+1} + (1 - \alpha_Z \gamma_1) \tilde{s}_t. \quad (66)$$

Recursive substitution of  $\tilde{s}$  on the right-hand side of (66) leads to (19).

The decay rate of  $\kappa_s^t$  determines the impact of the unobservable component in (19), and hence the accuracy of its approximation based on observable variables. Figure 5 displays the series of  $\kappa_s^t$  across all specifications and  $t$  in the sample, constructed from the empirical estimates of  $\alpha_Z$  and  $b_s$ .

The precision of the  $\kappa_s$  estimate can be assessed by approximating its variance from the standard errors of the parameters composing it, via the Delta method. By definition,  $\kappa_s = 1 - \alpha_Z b_s$ , so

$$\text{Var}[\kappa_s] \approx \begin{bmatrix} -b_s & -\alpha_Z \end{bmatrix} \begin{bmatrix} \sigma_{\alpha_Z}^2 & \sigma_{\alpha_Z, b_s} \\ \sigma_{\alpha_Z, b_s} & \sigma_{b_s}^2 \end{bmatrix} \begin{bmatrix} -b_s \\ -\alpha_Z \end{bmatrix} \quad (67)$$



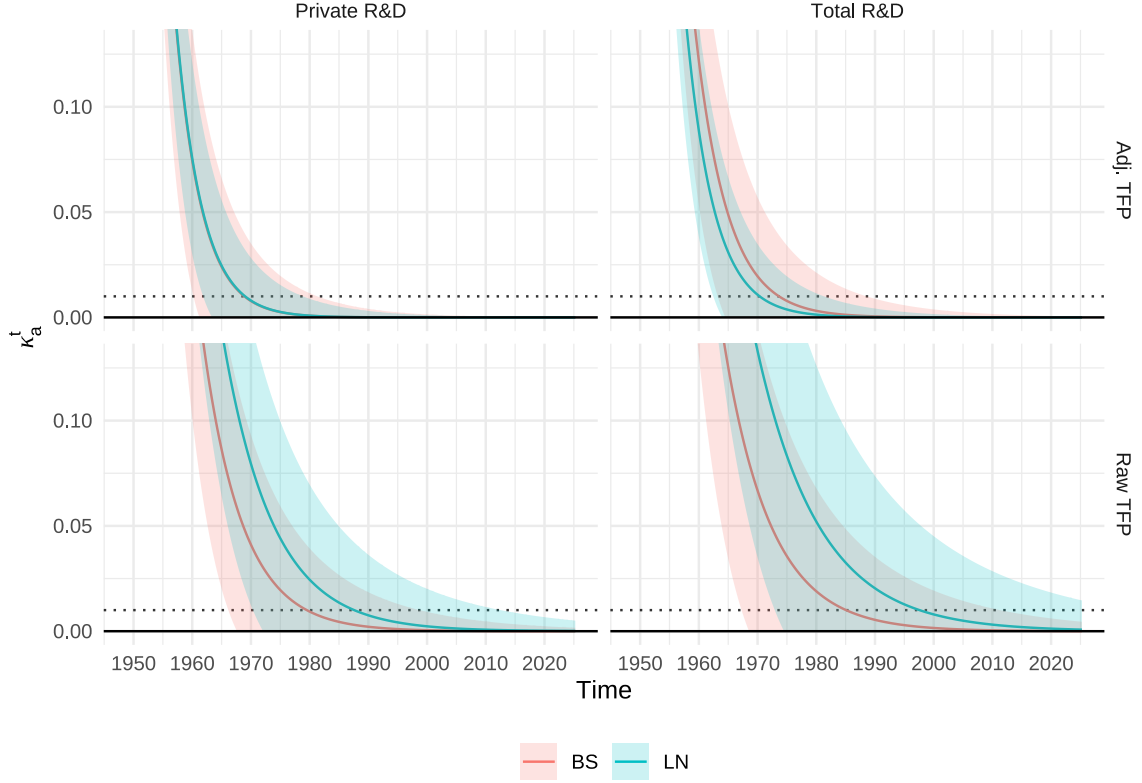


Figure 5:  $\kappa_a^t$  from all the specifications tested in Table 2.

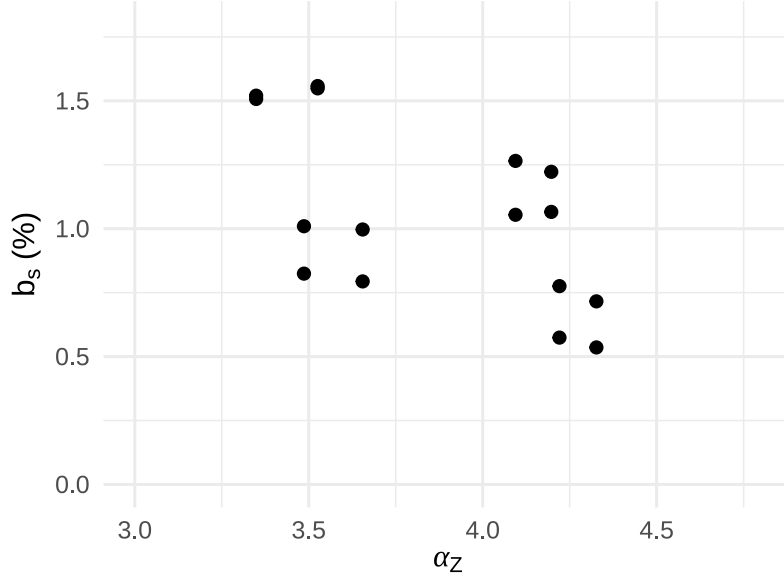
$$= b_s^2 \sigma_{\alpha_Z}^2 + \alpha_Z^2 \sigma_{b_s}^2 + 2b_s \alpha_Z \sigma_{\alpha_Z, b_s}. \quad (68)$$

Across the 16 specifications considered in this study, the correlation between empirical estimates of  $\alpha_Z$  and  $b_s$  is significantly negative (Figure 6). Heuristically, this implies that omitting the covariance term yields an upper bound for the standard error of  $\kappa_s$ :  $\sqrt{b_s^2 \sigma_{\alpha_Z}^2 + \alpha_Z^2 \sigma_{b_s}^2}$ . Using this upper bound provides a conservative measure of parameter uncertainty in  $\kappa_s$ , which can be safely used in subsequent calculations. Building on this, the variance of  $\text{Var}[\kappa_s^t] \approx t \cdot \kappa_s^{t-1} \text{Var}[\kappa_s]$ , which decreases in  $t$  once  $t > \frac{\kappa_s}{1-\kappa_s}$ . For instance, with the largest estimated value  $\kappa_s = 0.972$ ,  $t \cdot \kappa_s^{t-1}$  is strictly decreasing for  $t$  exceeding 34 quarters (approximately 9 years).

The effects of parameter uncertainty on the precision of the recovered series can be assessed at each time  $t$  in a similar manner, treating data as given. Specifically, the variance of the observable component of  $\tilde{s}_t$ , i.e.  $\alpha_Z \sum_{j=0}^{t-1} \kappa_s^j \Delta \ln \bar{Z}_{t-j} + \sum_{j=0}^{t-1} \kappa_s^j \hat{s}_{t-j}$ , can be approximated by

$$\tilde{\sigma}_{\tilde{s},t}^2 = \nabla \tilde{s}_t(\alpha_Z, b_s)^\top \begin{bmatrix} \sigma_{\alpha_Z}^2 & \sigma_{\alpha_Z, b_s} \\ \sigma_{\alpha_Z, b_s} & \sigma_{b_s}^2 \end{bmatrix} \nabla \tilde{s}_t(\alpha_Z, b_s), \quad (69)$$

where, with slight abuse of notation,  $\alpha_Z$ ,  $b_s$ , and  $\kappa_s$  in the gradient represent their respective



**Figure 6:** values of  $\alpha_Z$  and  $b_s$  across the 16 specifications studied; a linear regression fit yields a slope of  $-0.55$ , with a heteroskedasticity-robust p-value of 1.5%.

point estimates:

$$\nabla \tilde{s}_t(\alpha_Z, b_s) = \begin{bmatrix} \sum_{j=0}^{t-1} \kappa_s^{j-1} \left( [1 - \alpha_Z b_s(j+1)] \cdot \overline{\Delta \ln Z_{t-j}} - j \cdot b_s \cdot \Delta \hat{s}_{t-j} \right) \\ -\alpha_Z \left( \sum_{j=0}^{t-1} j \cdot \kappa_s^{j-1} (\alpha_Z \cdot \overline{\Delta \ln Z_{t-j}} + \Delta \hat{s}_{t-j}) \right) \end{bmatrix}. \quad (70)$$

Moreover, assuming that estimates of  $\kappa_s$  are independent of the true  $\tilde{s}$ , the uncertainty from the unobservability of  $\tilde{s}_0$  can also be accounted for, provided the recovered series yields consistent variance estimates. Indeed, exploiting  $\mathbb{E}[\tilde{s}_t] = 0$ , which holds by definition, stationarity of  $\tilde{s}_t$ , and the law of total variance:

$$\text{Var}[\kappa_s^t \tilde{s}_0] \approx \left( \mathbb{E}[\kappa_s]^2 + t(2t-1)\mathbb{E}[\kappa_s]^{2(t-1)} \cdot \text{Var}[\kappa_s] \right) \cdot \text{Var}[\tilde{s}_t] \quad (71)$$

where the approximation comes from a second-order approximation of  $\mathbb{E}[\kappa_s^{2t}]$ , and stationarity allows substituting  $\text{Var}[\tilde{s}_t]$  for  $\text{Var}[\tilde{s}_0]$ . The total variance of the recovered series, conditional on the observed data, is therefore given by:

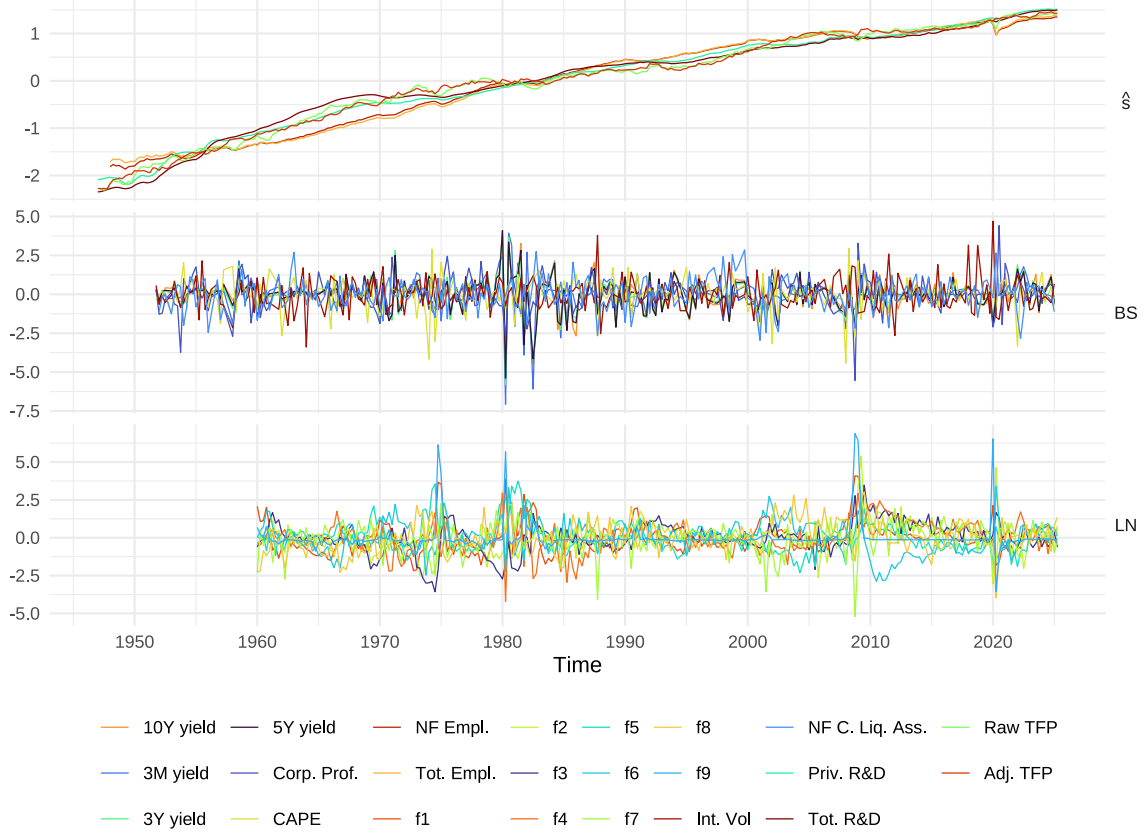
$$\text{Var} \left[ \tilde{s}_t \middle| \{ \overline{\Delta \ln Z_i}, \hat{s}_i \}_{i=1}^T \right] = \tilde{\sigma}_{\tilde{s},t}^2 + \text{Var}[\kappa_s^t \tilde{s}_0], \quad (72)$$

which is used to quantift the uncertainty of the recovered time series.

## B Details on the data

### B.1 Macroeconomic data

This section presents the macroeconomic data, showing the series and descriptive statistics.



**Figure 7:** Raw macroeconomic data.  $\hat{s}$  denotes the panel showing data used to estimate effective R&D, while  $BS$  and  $LN$  indicate the respective factor sets.

**Table 7:** Descriptive statistics: effective R&D data.  $N. Obs.$  is the number of observations.  $tt$  and  $tt^2$  are the time trend and squared time trend coefficients (with HAC standard errors);  $ADF$  and  $KPSS$  are stationarity tests in levels;  $AR(1)$  is the coefficient from an AR(1) fit.

	Priv. R&D	Tot. R&D	Raw TFP	Adj. TFP	Tot. Empl.	N.F. Empl.
$tt$	0.017***	0.019**	0.018***	0.018***	0.018***	0.017***
$tt^2$	0.000	0.000	0.000***	0.000	0.000***	0.000***
AR(1)	1.000***	1.000***	1.000***	1.000***	1.000***	1.000***
ADF	-1.482	-2.027**	-2.346**	-2.891***	-1.353	-0.948
KPSS	2.004***	1.924***	1.976***	1.978***	2.001***	2.011***
N. Obs.	314	314	314	314	310	310

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

**Table 8:** Descriptive statistics: BS factors. *N. Obs.* is the number of observations. *tt* and *tt*<sup>2</sup> are the time trend and squared time trend coefficients (with HAC standard errors); *ADF* and *KPSS* are stationarity tests in levels; *AR(1)* is the coefficient from an AR(1) fit.

	CAPE	10Y yield	3M yield	3Y yield	5Y yield	Int. Vol	Corp. Profits	N.F. Liq. Assets
<i>tt</i>	−0.001	−0.004*	−0.003	−0.004*	−0.004*	0.002	0.002	0.005*
<i>tt</i> <sup>2</sup>	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
AR(1)	−0.334***	−0.053	−0.187***	−0.117*	−0.102*	−0.297***	0.031	0.068
ADF	−13.638***	−11.188***	−13.206***	−11.844***	−11.734***	−15.514***	−10.569***	−10.688***
KPSS	0.078*	0.184*	0.099*	0.144*	0.170*	0.259*	0.052*	0.097*
N. Obs.	270	270	270	270	270	270	270	269

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01

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**Table 9:** Descriptive statistics: LN factors. *N. Obs.* is the number of observations. *tt* and *tt*<sup>2</sup> are the time trend and squared time trend coefficients (with HAC standard errors); *ADF* and *KPSS* are stationarity tests in levels; *AR(1)* is the coefficient from an AR(1) fit.

	f1	f2	f3	f4	f5	f6	f7	f8	f9
<i>tt</i>	0.005	0.005	0.002	−0.004	−0.001	0.006	−0.001	0.017***	0.003
<i>tt</i> <sup>2</sup>	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000***	0.000
AR(1)	0.725***	0.360***	0.749***	0.426***	0.703***	0.620***	0.138**	0.513***	0.329***
ADF	−6.467***	−7.252***	−4.577***	−6.929***	−4.911***	−5.758***	−10.204***	−7.415***	−9.526***
KPSS	0.324*	0.514**	0.525**	0.373*	0.224*	0.278*	0.190*	0.603**	0.062*
N. Obs.	262	262	262	262	262	262	262	262	262

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01

## B.2 Financial data

### Cash-flow growth rates

First, a measure  $h_{i,t}$  of capital gain is computed for each stock by adjusting CRSP ex-dividend returns  $RET_X$  for share repurchases as

$$h_{i,t} = \left( \frac{P_{i,t+1}}{P_{i,t}} \right) \cdot \min \left( \frac{n_{i,t+1}}{n_{i,t}}, 1 \right). \quad (73)$$

For each portfolio, these stock-level measures are aggregated using market-capitalization weights to obtain a portfolio capital gain series  $h_{p,t}$ . From each portfolio series, the value of one dollar invested at the beginning of the sample is computed recursively as  $V_{p,t+1} = h_{p,t+1} V_{p,t}$  with  $V_{p,0} = 1$ . Payouts are then given by  $D_{p,t+1} = y_{p,t+1} V_{p,t}$ , where  $y_{p,t+1}$  is the portfolio dividend yield, obtained from  $R_{p,t} = h_{p,t} + y_{p,t}$ . Capital gains are less than proportional to price appreciation when equivalent shares outstanding decline, typically due to share repurchases, which are a form of payout not recorded in dividend data. Quarterly dividend series are obtained by summing monthly values and deflating them with the implicit price deflator for nondurable and services consumption, constructed as in Bureau of Economic Analysis (2024). The series are log-transformed and, following Bansal et al. (2005), de-seasoned with a 4-quarter rolling mean to remove residual seasonality. Finally, cash-flow growth rates are computed as first differences of the log-transformed, de-seasoned real quarterly payouts.

### Portfolio Formation

To mitigate liquidity concerns, the sample is restricted to common stocks with market capitalization above the 1st percentile of the monthly NYSE distribution and share prices above \$2, removing less than 0.4% of total market capitalization. Firms must also have at least twelve consecutive monthly observations to enter the final sample. Portfolio construction follows standard methodology: portfolios are formed at the end of June, value-weighted, and held until the following June. Sorting variables are Market capitalization (Size), Book-to-Market (BM), Momentum (Mom), firm-specific R&D intensity (RD), Turnover (To), Profitability (Prof), Leverage (Lvg), Asset growth (AG), Tobin's Q (TQ), and Industry (Ind). Most variables are sorted using a 2×3 framework, where stocks are first split by whether market capitalization is above or below the NYSE median and then divided into terciles within each size group. Exceptions are Size, BM, and Mom, which follow univariate sorts as in Bansal et al. (2005), and Industry, which is directly classified. All portfolios exhibit patterns consistent with established literature.

**Size portfolios** All firms are assigned to quintiles based on market capitalization relative to NYSE breakpoints. Both returns and cash-flow growth decrease with size.

**BM portfolios** All non-financial firms (SIC outside 6000–6999) are assigned to quintiles based on book equity in fiscal year  $t - 1$  to market capitalization at end of calendar year  $t - 1$ , relative to NYSE breakpoints. Both returns and cash-flow growth increase with the B/M ratio.

**Mom portfolios** All firms are assigned to quintiles based on cumulative returns from month  $t - 12$  to month  $t - 1$ . Both returns and cash-flows increase with momentum.

**RD portfolios** See Chan et al. (2001) and Lin (2011). All non-financial and non-utility firms (SIC outside 4000–4999, 6000–6999) are ranked by R&D expenditures from the previous fiscal year to market capitalization at end of calendar year  $t - 1$ . Returns and cash-flow growth increase with with R&D intensity in both small and big portfolio.

**To portfolios** See Haugen and Baker (1996). All firms are assigned to quintiles based on the sales-to-assets ratio from the previous fiscal year. Returns and cash-flow growth increase with turnover for both small and large portfolios.

**Prof portfolios** See Fama and French (2015), Hou et al. (2015), and Novy-Marx (2013). All non-financial and non-utility firms are sorted on gross profits over assets. Returns and cash-flow growth increase with profitability for both small and large portfolios, with stronger effects among small portfolios.

**Lvg portfolios** See Bhandari (1988). All non-financial firms are sorted on debt-to-assets ratio, used instead of debt-to-market capitalization for consistency with corporate finance literature (e.g. Rajan and Zingales 1995) and with other sorts related to financing capabilities in this study. Returns and cash-flow growth increase with leverage among small portfolios, while cash-flow growth decreases among large portfolios, with returns showing no clear pattern.

**AG portfolios** See Cooper et al. (2008) and Hou et al. (2015). All non-financial and non-utility firms are sorted on asset growth (first difference of assets over lagged value). Both cash-flow growth and returns decrease with asset growth for small and large portfolios.

**TQ portfolios** See Hou et al. (2015). All firms are sorted on Tobin’s Q, defined as (assets - book equity + market capitalization) / assets as in Chung and Pruitt (1994). Cash-flow growth and returns clearly decrease with Tobin’s Q for small portfolios, with no evident pattern for large portfolios.

## C Additional tables and figures

### C.1 Tables

This subsection presents supplementary tables on correlations, R&D measures, and test asset portfolio statistics.

**Table 10:** Correlation among error correction terms from the specifications in Table 1.

	Baseline	$S$ : Tot. R&D	$Z$ : Raw TFP	$Q$ : N.F. Empl.
$S$ : Tot. R&D	0.880	.	.	.
$Z$ : Raw TFP	0.855	0.721	.	.
$Q$ : N.F. Empl.	0.997	0.858	0.859	.
Est. Meth.: IM	0.511	0.504	0.377	0.503

**Table 11:** Correlation among estimates of  $\tilde{s}_t$  from the specifications in Table 2.

Specification	Baseline		$S$ : Tot. R&D		$Z$ : Raw TFP		$Q$ : N.F. Empl.	
	BS	LN	BS	LN	BS	LN	BS	LN
Baseline-LN	1.000	.	.	.	.	.	.	.
$S$ : Tot. R&D-BS	0.777	0.777	.	.	.	.	.	.
$S$ : Tot. R&D-LN	0.806	0.806	0.996	.	.	.	.	.
$Z$ : Raw TFP-BS	0.858	0.859	0.640	0.641	.	.	.	.
$Z$ : Raw TFP-LN	0.853	0.853	0.644	0.636	0.994	.	.	.
$Q$ : N.F. Empl.-BS	0.998	0.998	0.752	0.781	0.868	0.862	.	.
$Q$ : N.F. Empl.-LN	0.998	0.998	0.752	0.781	0.868	0.861	1.000	.

**Table 12:** Correlation among estimates of structural shocks from the VAR specifications in Table 3.

	Baseline	$S$ : Tot. R&D	$Z$ : Raw TFP	$Q$ : N.F. Empl.
$S$ : Tot. R&D	0.690	.	.	.
$Z$ : Raw TFP	0.915	0.630	.	.
$Q$ : N.F. Empl.	0.991	0.699	0.901	.
$\tilde{s}$	0.926	0.646	0.837	0.929

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

**Table 13:** Summary statistics of the (updated) Kung and Schmid (2015) R&D intensity measure. Column 1 reports yearly R&D expenditure ( $S$ , NSF) and R&D stock ( $I$ , BLS) for 1963-2020 (yearly observations from 1986 onward); columns 2-3 show data from the baseline specifications in the main analysis.  $\xi$  corresponds to commonly used labor-share values, following the original paper.  $T$  denotes the number of observations;  $\sigma$ , the standard deviation;  $tt$  and  $tt^2$ , linear and quadratic time trends;  $ADF$  and  $KPSS$ , respective stationarity tests;  $AR(1)$ , the first-order autoregressive coefficient; and  $HL$ , the implied half-life based on  $AR(1)$ .

$\tilde{s}_t :$	$(\ln S_t - \ln I_t)$	$(\ln S_t - \frac{1}{\xi} \ln Z_t)$	
$1 - \xi :$	—	0.35	0.3
$T$	62	314	314
$\sigma$	0.321	0.864	0.835
$tt$	−0.043	0.01	0.01
$tt^2$	0.000	−0.00	−0.00
$ADF$	−2.82*	3.80	3.72
$KPSS$	1.29***	0.82***	0.79***
$AR(1)$	0.995***	1.000***	1.000***
	(0.063)	(0.000)	(0.000)
HL low	40.2	$\infty$	$\infty$
HL high	$\infty$	$\infty$	$\infty$

\*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$

**Table 14:** Granger causality F-test  $p$ -values from a VAR of effective R&D ( $s$ ) and the aggregated innovation measure of Kogan et al. (2017) ( $KPSS$ ), both included as structural shocks orthogonal to productivity growth, estimated from a first-step bivariate VAR with productivity growth (as in Table 3). VAR lags are selected by Hannan–Quinn information criterion (max 10);  $k$  denotes second-step VAR lags. Results are shown using standard, HC, and HAC covariance estimators.

	Baseline	$S$ : Tot. R&D	$Z$ : Raw TFP	$Q$ : N.F. Empl.	$\tilde{s}$
$k$	1	1	2	1	1
N. Obs.	298	298	298	298	216
GC( $s$ ) p.v.	0.072	0.926	0.095	0.074	0.073
GC( $KPSS$ ) p.v.	0.786	0.395	0.667	0.662	0.154
GC( $s$ ) HC p.v.	0.069	0.934	0.131	0.072	0.066
GC( $KPSS$ ) HC p.v.	0.838	0.436	0.699	0.745	0.345
GC( $s$ ) HAC p.v.	0.011	0.921	0.013	0.008	0.031
GC( $KPSS$ ) HAC p.v.	0.824	0.497	0.636	0.719	0.288

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$



**Table 15:** Descriptive statistics of the legacy pool test assets used in Section 3.3. Quarterly returns and cash-flow growth rates are reported from 1967 Q1 to 2022 Q1; summary statistics include mean and standard deviation.

<b>Portfolio</b>	<b>CF Growth Mean</b>	<b>CF Growth SD</b>	<b>Returns Mean</b>	<b>Returns SD</b>
Size(1)	134.68	604.09	2.47	13.20
Size(2)	68.34	373.78	2.31	11.83
Size(3)	36.33	193.21	2.18	10.77
Size(4)	29.38	161.65	2.14	10.06
Size(5)	6.38	36.26	1.59	8.34
BM(1)	3.09	16.54	1.72	9.76
BM(2)	2.31	21.74	1.78	8.86
BM(3)	1.49	17.17	1.67	8.22
BM(4)	3.47	36.58	1.96	8.65
BM(5)	8.70	69.61	2.41	9.37
Mom(1)	1.11	20.96	1.47	12.61
Mom(2)	7.44	74.50	1.75	9.31
Mom(3)	8.34	58.26	1.78	8.47
Mom(4)	17.24	107.76	1.85	8.77
Mom(5)	34.09	280.68	1.98	11.66

**Table 16:** Descriptive statistics of the additional test assets in the extended pool used in Section 3.3. Quarterly returns and cash-flow growth rates are reported from 1975 Q1 to 2022 Q1; summary statistics include mean and standard deviation.

Portfolio	CF Growth Mean	CF Growth SD	Returns Mean	Returns SD
RD(1-small)	5.23	44.17	2.58	12.32
RD(2-small)	4.53	67.45	2.84	13.13
RD(3-small)	20.34	314.97	4.04	15.79
RD(1-big)	0.97	9.79	1.72	8.42
RD(2-big)	5.90	35.87	2.39	9.02
RD(3-big)	4.04	34.68	2.60	9.69
To(1-small)	3.69	27.70	2.29	10.46
To(2-small)	13.36	73.27	3.01	12.29
To(3-small)	32.86	157.91	3.41	11.99
To(1-big)	0.72	9.65	1.78	8.75
To(2-big)	3.08	18.27	2.08	8.64
To(3-big)	4.88	23.34	2.40	8.62
Prof(1-small)	1.90	42.75	2.29	13.44
Prof(2-small)	15.08	82.61	3.06	12.50
Prof(3-small)	39.22	189.22	3.57	12.47
Prof(1-big)	0.98	10.70	1.75	9.26
Prof(2-big)	3.10	18.54	2.29	8.78
Prof(3-big)	6.87	36.63	2.31	8.70
Lvg(1-small)	4.16	46.37	2.63	12.97
Lvg(2-small)	11.64	87.41	2.97	11.91
Lvg(3-small)	14.02	66.32	3.02	11.99
Lvg(1-big)	2.46	16.73	2.10	9.63
Lvg(2-big)	2.79	17.32	2.15	8.17
Lvg(3-big)	1.70	11.32	2.09	7.92
AG(1-small)	25.67	144.45	3.43	13.38
AG(2-small)	12.67	99.21	2.97	12.37
AG(3-small)	6.93	40.81	2.73	12.37
AG(1-big)	4.67	31.69	2.41	9.08
AG(2-big)	3.33	18.94	2.22	8.18
AG(3-big)	1.47	14.16	1.87	9.25
TQ(1-small)	29.50	248.34	3.45	13.17
TQ(2-small)	16.36	91.69	3.12	12.02
TQ(3-small)	3.18	29.12	2.56	13.60
TQ(1-big)	3.18	26.42	2.18	8.53
TQ(2-big)	2.42	15.68	2.29	8.31
TQ(3-big)	3.05	17.48	1.99	9.94

**Table 17:** Descriptive statistics of the additional test assets in the wide pool used in Section 3.3. Quarterly returns and cash-flow growth rates are reported from 1967 Q1 to 2022 Q1; summary statistics include mean and standard deviation.

Portfolio	CF Growth Mean	CF Growth SD	Returns Mean	Returns SD
Ind(Cars)	3.71	106.84	2.11	13.17
Ind(Chems)	22.46	433.41	1.87	10.62
Ind(Clths)	6.30	58.46	2.32	13.02
Ind(Cnstr)	26.06	209.55	2.28	11.84
Ind(Cnsum)	28.52	248.93	2.23	8.49
Ind(Durbl)	2.83	62.31	1.17	11.33
Ind(FabPr)	9.56	144.51	1.95	10.75
Ind(Finan)	6.38	49.55	2.03	10.68
Ind(Food)	13.22	113.91	2.18	8.32
Ind(Machn)	49.53	450.87	2.14	12.97
Ind(Mines)	1.46	32.69	1.46	13.13
Ind(Oil)	22.92	186.66	2.09	11.28
Ind(Other)	9.51	50.02	1.78	9.35
Ind(Rtail)	27.08	275.63	2.24	10.67
Ind(Steel)	2.21	48.84	1.50	14.83
Ind(Trans)	3.91	77.20	1.80	10.51
Ind(Utils)	1.51	13.95	1.50	7.51

**Table 18:** Dividend betas for the test assets in the legacy pool at a 1-quarter and 2-year horizons (1967 Q1–2022 Q4). Stocks are double-sorted into  $2 \times 3$  portfolios by size (NYSE median) and accounting characteristics: *RD* (R&D/market cap), *To* (sales/assets), *Prof* (gross profits/assets), *Lvg* (debt/assets), *AG* (asset growth), and *TQ* (Tobin’s *Q*). Risk factors: Cons. (consumption growth), Raw/Adj. TFP (raw/adjusted total factor productivity),  $\tilde{s}$ : shock/level (effective R&D shock/level).

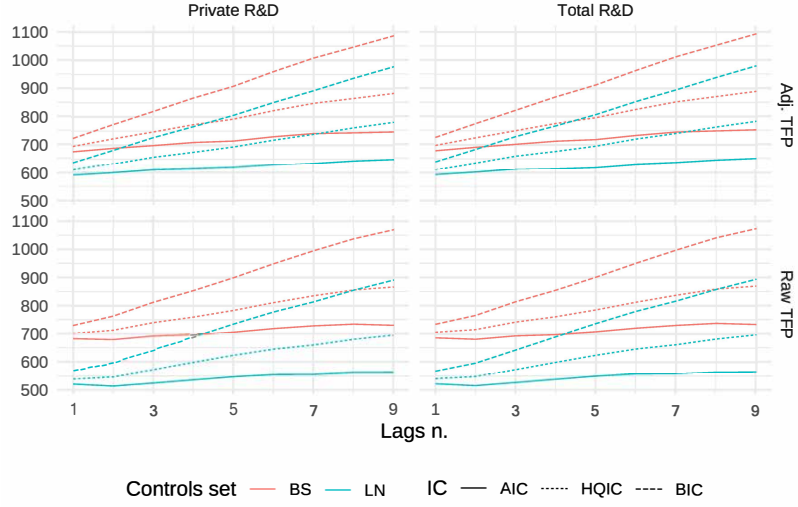
<b>Portfolio</b>	<b>Cons.</b>		<b>Raw TFP</b>		<b>Adj. TFP</b>		<b><math>\tilde{s}</math>: shock</b>		<b><math>\tilde{s}</math>: level</b>	
<i>Horizon</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>
Size(1)	0.23	3.27	−0.24	3.75	−0.49	0.55	0.58	1.85	14.20	24.02
Size(2)	1.00	1.64	0.54	3.20	−0.42	−0.07	0.21	1.63	0.61	−0.69
Size(3)	0.37	1.08	0.09	1.98	−0.39	−0.14	0.12	0.66	−1.97	−1.16
Size(4)	0.18	0.98	−0.10	1.40	−0.32	−0.22	0.06	0.48	−1.75	−0.39
Size(5)	0.06	0.21	0.01	0.36	−0.06	−0.06	0.00	−0.12	−0.98	−1.02
BM(1)	0.03	0.04	0.02	0.09	−0.02	0.04	0.02	−0.02	−0.23	−0.13
BM(2)	0.01	0.07	−0.01	0.14	−0.04	−0.04	0.00	−0.07	−0.57	−0.45
BM(3)	0.02	0.08	−0.01	0.12	−0.03	−0.08	−0.01	−0.02	−0.36	−0.55
BM(4)	0.03	0.13	0.00	0.23	−0.07	−0.10	0.01	−0.08	−0.73	−0.62
BM(5)	0.11	0.30	0.01	0.53	−0.09	0.07	−0.02	0.27	0.19	0.71
Mom(1)	0.03	0.02	0.02	0.14	−0.02	0.07	−0.02	−0.02	−0.14	−0.08
Mom(2)	0.07	0.41	−0.05	0.44	−0.15	−0.35	0.00	−0.22	−2.62	−3.76
Mom(3)	0.08	0.31	0.01	0.41	−0.09	−0.03	0.03	0.10	−0.92	−1.27
Mom(4)	0.10	0.35	0.06	0.52	−0.11	−0.36	−0.02	−0.18	−1.29	−1.64
Mom(5)	0.26	0.67	0.01	1.14	−0.11	−0.77	0.27	−0.31	−2.10	−3.27

**Table 19:** Dividend betas for the additional test assets of the wide pool at a 1-quarter and 2-year horizons (1967 Q1–2022 Q4). Stocks are double-sorted into  $2 \times 3$  portfolios by size (NYSE median) and accounting characteristics: *RD* (R&D/market cap), *To* (sales/assets), *Prof* (gross profits/assets), *Lvg* (debt/assets), *AG* (asset growth), and *TQ* (Tobin’s *Q*). Risk factors: Cons. (consumption growth), Raw/Adj. TFP (raw/adjusted total factor productivity),  $\tilde{s}$ : shock/level (effective R&D shock/level).

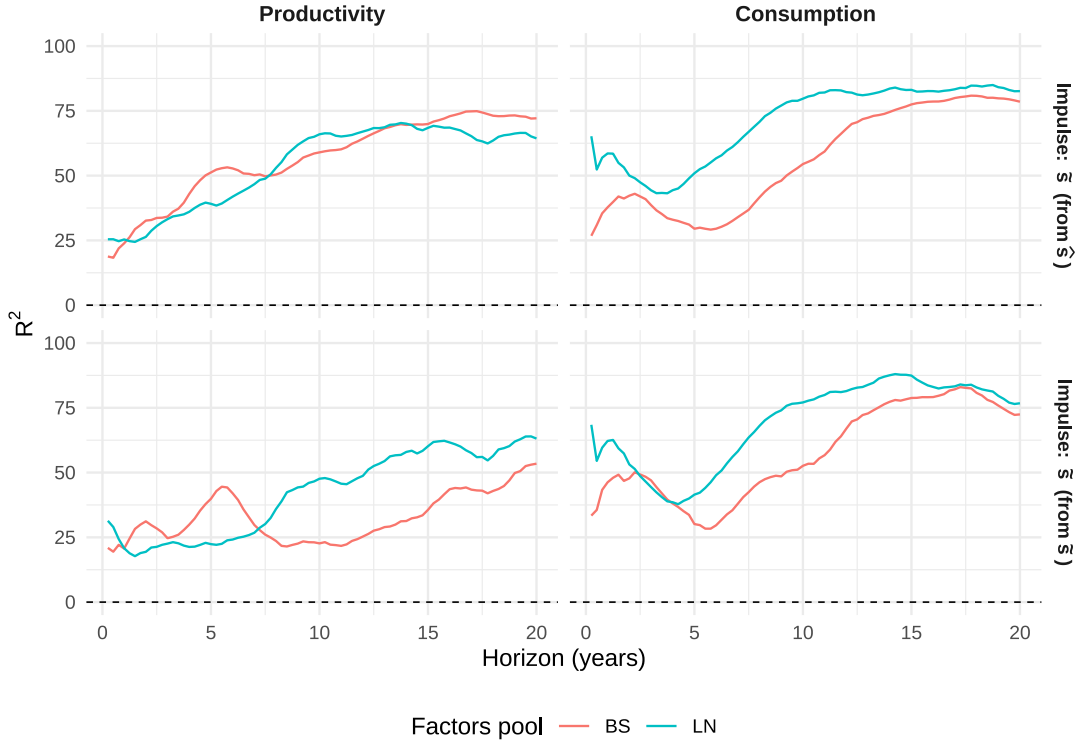
<b>Portfolio</b>	<b>Cons.</b>		<b>Raw TFP</b>		<b>Adj. TFP</b>		<b><math>\tilde{s}</math>: shock</b>		<b><math>\tilde{s}</math>: level</b>	
<i>Horizon</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>	<i>1</i>	<i>8</i>
Ind(Cars)	0.16	0.40	0.05	0.60	−0.12	−0.21	0.02	0.35	−0.80	−1.03
Ind(Chems)	0.40	0.93	−0.47	1.38	−0.86	−1.15	−0.02	0.48	−7.24	−3.46
Ind(Clths)	−0.01	0.26	−0.09	0.25	−0.12	−0.19	0.04	0.13	−0.78	−0.41
Ind(Cnstr)	0.37	0.37	0.21	1.34	−0.28	0.67	0.14	0.33	−0.79	2.65
Ind(Cnsum)	−0.12	0.19	−0.28	0.09	−0.25	−0.38	−0.03	−1.10	−3.76	−2.34
Ind(Durbl)	0.04	0.14	0.04	0.30	−0.06	−0.04	0.02	−0.07	−0.94	−0.86
Ind(FabPr)	0.03	0.26	0.01	0.79	−0.03	0.01	−0.05	−0.01	0.35	−0.32
Ind(Finan)	0.05	0.33	0.00	0.41	−0.04	−0.04	−0.01	0.01	−0.51	−0.99
Ind(Food)	0.11	0.09	0.13	0.59	0.01	0.42	−0.11	−0.15	−0.80	−1.20
Ind(Machn)	0.54	1.95	0.09	2.66	−0.74	−1.57	0.16	−0.53	−12.11	−10.32
Ind(Mines)	0.01	0.08	0.01	0.11	−0.02	−0.03	−0.02	−0.15	−0.40	0.19
Ind(Oil)	0.09	1.60	−0.16	1.76	−0.19	−0.65	0.03	0.38	1.29	0.86
Ind(Other)	0.07	0.11	0.05	0.38	−0.03	0.07	0.03	−0.17	−0.90	−1.11
Ind(Rtail)	0.48	0.44	0.20	1.52	−0.50	0.12	0.42	0.13	−5.32	−4.26
Ind(Steel)	0.03	0.16	0.03	0.19	−0.04	−0.18	0.00	0.11	0.00	−0.16
Ind(Trans)	0.03	0.24	−0.02	0.24	−0.09	−0.18	−0.04	−0.17	−1.17	−0.54
Ind(Utils)	0.01	0.03	0.01	0.07	−0.01	−0.01	0.00	0.00	−0.07	−0.21

## C.2 Figures

These figures complement the main text by showing key diagnostics, estimated quantities, and the variance explained by principal components of test assets.



**Figure 8:** Information criteria from regressions on the largest sample common to all specifications, using baseline employment, were used to select the regressions reported in Table 2. Results using nonfarm employment are visually indistinguishable.



**Figure 9:**  $R^2$  of local projection regressions over forecast horizons for productivity and consumption, corresponding to the cumulative impulse responses shown in Figure 4.

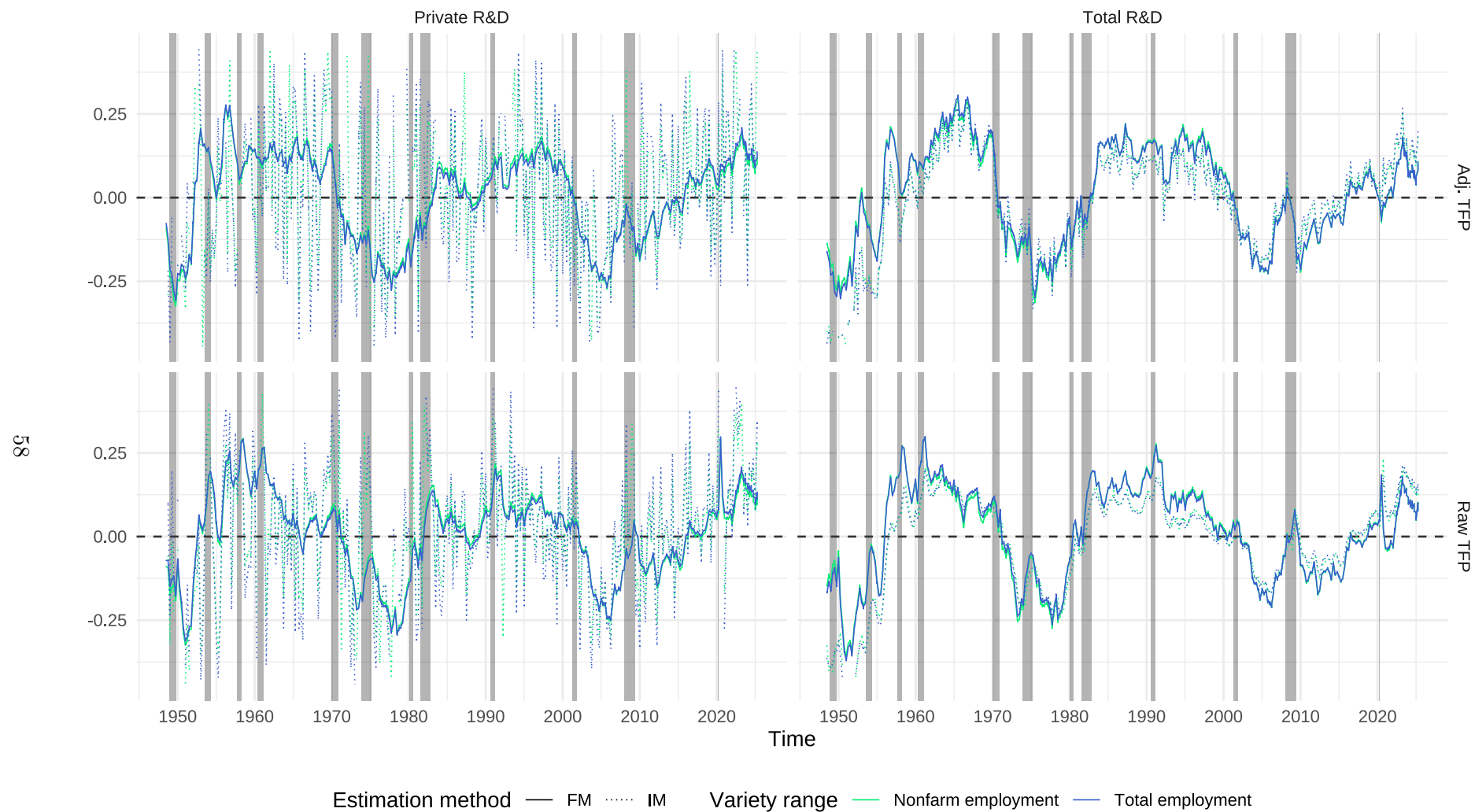


Figure 10: Error correction terms from all tested cointegrations; selected estimates are reported in Table 1. Shaded areas indicate NBER recessions.



**Figure 11:**  $\tilde{s}_t$  from all specifications tested. Bands show 95% confidence intervals assuming normality, with variance computed as in (72). Shaded areas indicate NBER recessions.



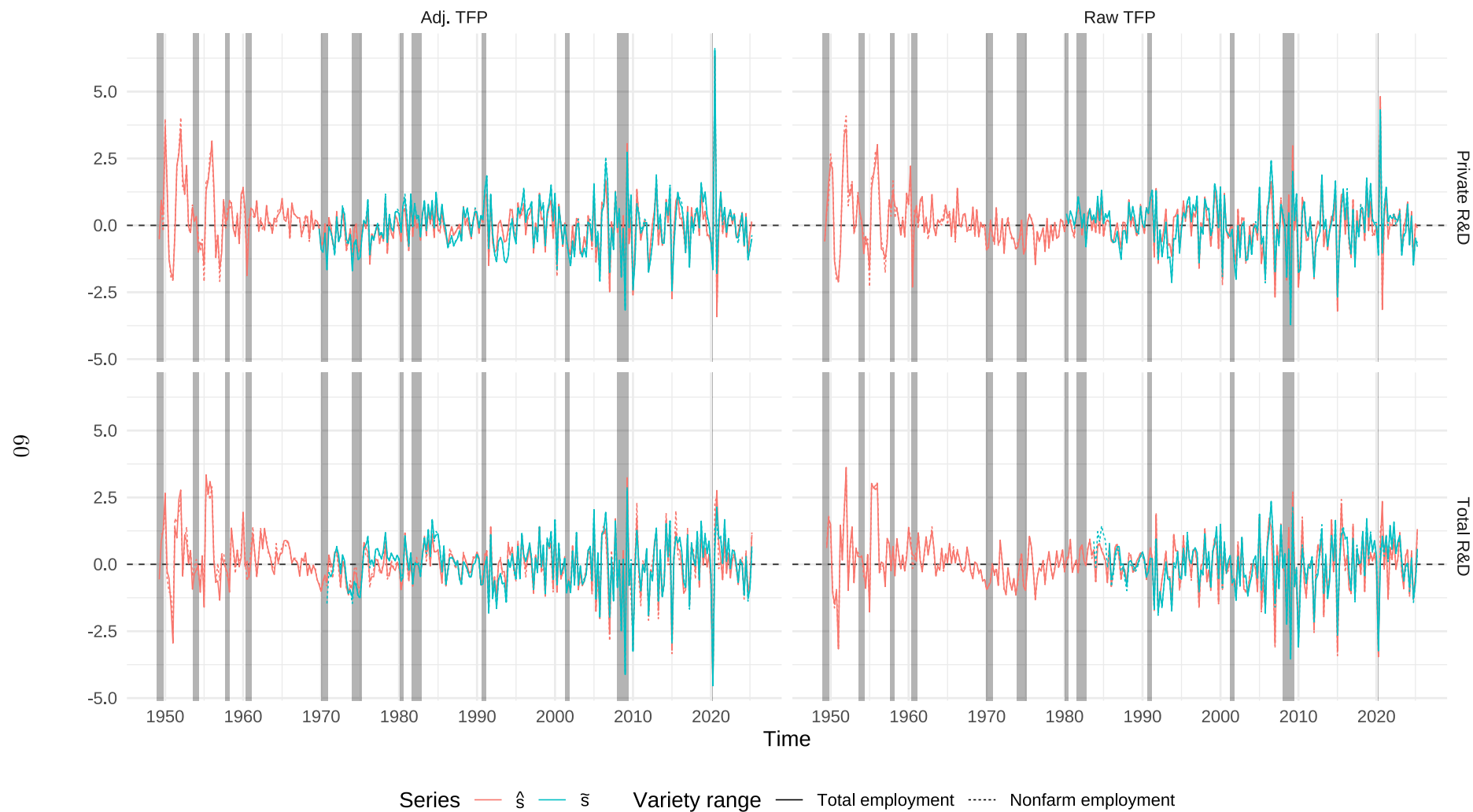
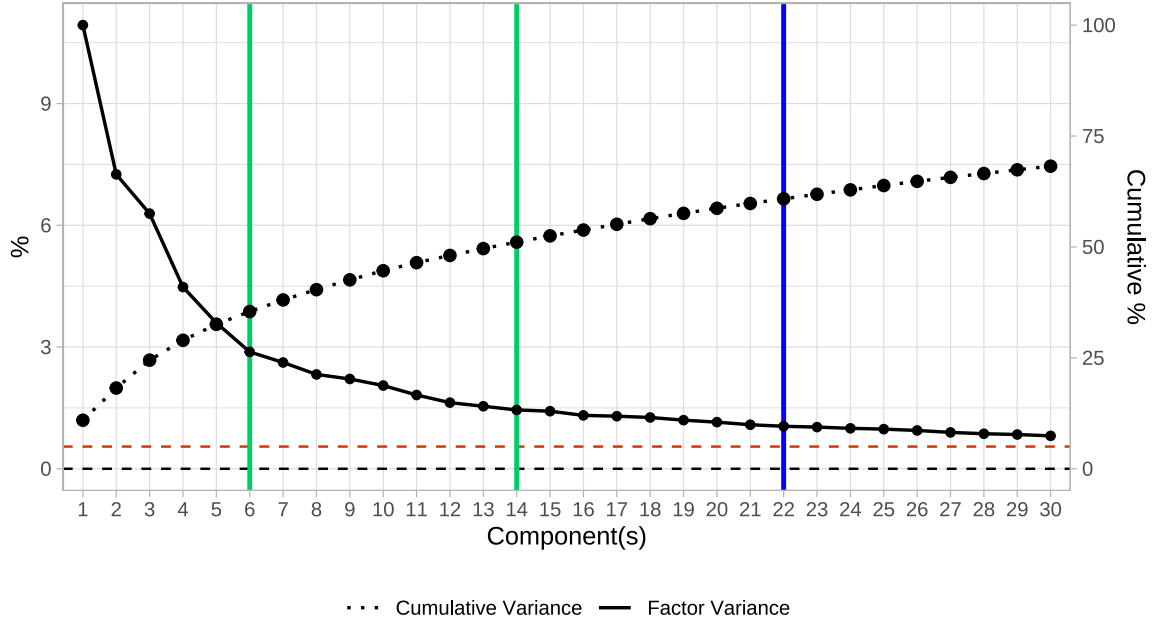
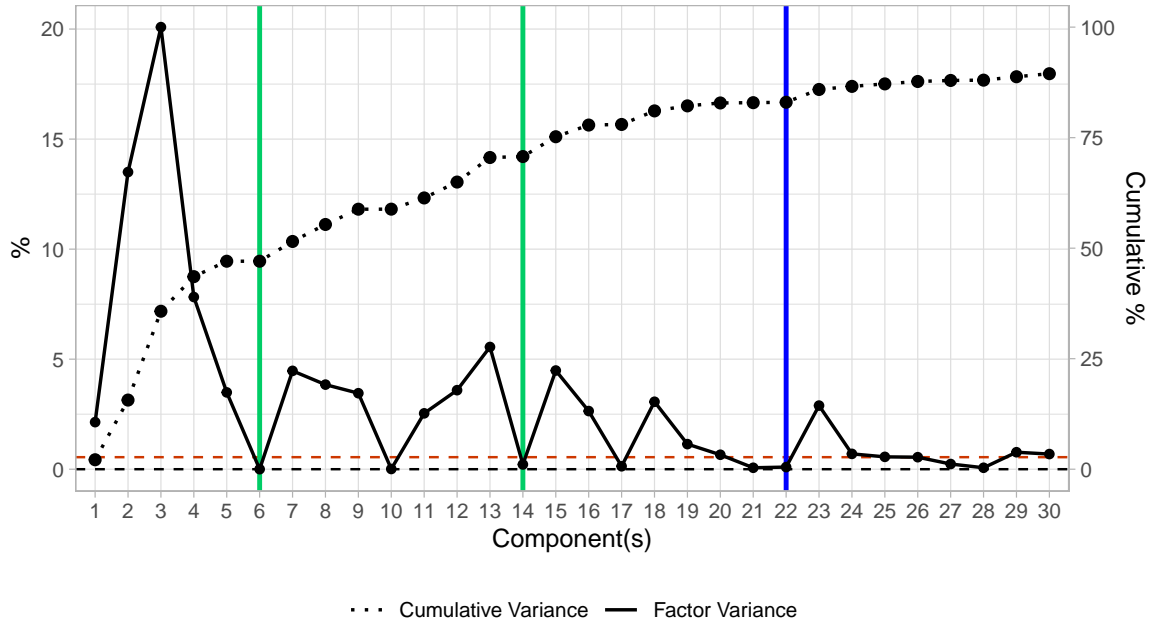


Figure 12: Structural shocks from VAR estimations; selected results are reported in Table 3. Shaded areas indicate NBER recessions.



**Figure 13:** Principal component scree plots of the test assets in Section 3.3. The left y-axis shows the variance explained by each factor (solid line), and the right y-axis shows the cumulative variance explained (dotted line). Vertical green lines indicate the optimal number of factors according to Alessi et al. (2010), while the vertical blue line marks the minimum optimal number of factors as in Bai and Ng (2002). The horizontal red line corresponds to the reciprocal of the number of test assets.



**Figure 14:** Cross-sectional average returns: variance explained by the principal components used as risk factors in Section 3.3. The left y-axis shows the variance explained by each factor (solid line), and the right y-axis shows the cumulative variance explained (dotted line). Vertical green lines indicate the optimal number of factors according to Alessi et al. (2010), while the vertical blue line marks the minimum optimal number of factors as in Bai and Ng (2002). The horizontal red line corresponds to the reciprocal of the number of test assets.