An Epidemiological Extension of the El Farol Bar Problem

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2 ABSTRACT

- 3 This paper presents an epidemiological extension of the El Farol Bar problem, where both a
- 4 social and an epidemiological dimension are present. In the model, individual agents making
- 5 binary decisions—to visit a bar or stay home—amidst a non-fatal epidemic. The extension of
- 6 the classic social dilemma is implemented as an agent-based model, and it is later explored by
- 7 sampling the parameter space and observing the resulting behavior. The results of this analysis
- 8 suggest that the infection could be contained by increasing the information available in the
- 9 underlying social system and adjusting its structure.
- 10 Keywords: Agent-based modelling, El Farol bar problem, Social dilemma, Epidemiological modelling, Simulation, Computational Social
- 11 Science

1 INTRODUCTION

- 12 The appearance of Covid-19 pandemic brought a greater interest on the spread of epidemics in social
- 13 systems, which has ascended as a research imperative (Squazzoni et al., 2020). The pandemic has especially
- 14 highlighted the presence of an interplay between disease dynamics and socio-behavioral patterns (Kreulen
- 15 et al., 2022). Consequently, understanding and strategizing against the spread of epidemics in interconnected
- 16 social systems have become paramount to safeguarding global health and socio-economic stability (Maharaj
- 17 and Kleczkowski, 2012).
- Mathematical models (Kermack and McKendrick, 1927), and subsequently, simulation models (Bagni
- 19 et al., 2002), have long been pivotal tools in epidemic management, offering the capacity to predict
- 20 (Colizza et al., 2006), analyze (Colizza et al., 2007), and strategize (Ibarra-Vega, 2020) against the spread
- 21 of infectious diseases (Ferreri et al., 2014). The computational implementation of an epidemiological
- 22 model enables the analysis of disease transmission dynamics (Rahmandad and Sterman, 2008) through
- 23 the systematic examination of epidemiological variables, even when they are not analytically tractable
- 24 (Bobashev et al., 2007). In this perspective, simulations can serve two main interrelated goals, although a
- 25 more precise taxonomy can be defined (Epstein, 2008; Edmonds et al., 2019). First, by incorporating real-
- 26 world data and multifaceted parameters, simulations provide a computational platform to assess possible
- 27 outcomes and interventions in real-world systems (Bertolotti and Roman, 2024). Second, simulations can
- 28 be employed to assess the reliability of hypotheses and to refine the objectives of empirical studies and
- 29 treatments (Georgescu, 2012).

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The El Farol Bar problem (Arthur, 1994), a seminal example in complexity science (Casti, 1996), exemplifies the use of toy models to study the unpredictability of the dynamics of seemingly simple social systems (Lorenz, 1963). In the original form of the problem, multiple agents all face the same binary decision, that each of them has to make without the possibility to agree or to share information with the others: either to visit a bar with limited capacity or to stay home, where a threshold is set and known to all agents above which they no longer find it enjoyable to visit the bar. The binary outcome – either the visit was enjoyable if the bar was not too crowded or viceversa – is known to each attending agent after the event, and the time series of the outcomes of repeated events is the basis for predicting the next outcome and a decision of each accordingly.

In this paper, the dilemma has been modified and enrich with a new epidemiological dimension. Individuals must decide whether or not to engage in social activities amidst a contagious disease outbreak, as it happened during the Covid-19 pandemic (Kluwe-Schiavon et al., 2021). To the best of the authors' knowledge, interactions between the underlying mechanisms of social decision-making and the epidemiological dynamics in such scenarios are largely unexplored (Pullano et al., 2020), and the El Farol bar problem was never investigated from an epidemiological perspective.

The El Farol Bar problem extension has been implemented into an agent-based model (Bonabeau, 2002). This specific methodology embodies a bottom-up approach, allowing for the representation of heterogeneous behaviors and leading to the emergence of complex system-wide phenomena (Siegenfeld and Bar-Yam, 2020), and it is widely employed across multiple fields, including ecology (Goodman et al., 2023), economics (Arthur, 2006), social sciences (Marwal and Silva, 2023), and epidemiology (Squazzoni et al., 2020). The computational implementation was needed to generate simulated data, with the purpose of contributing to the understanding of the entangled nature of socio-epidemiological systems.

The results suggest that epidemic survival rate is strongly dependent on the experimental configuration, given that with the specific parameters' space employed only a small fraction of simulations resulting in persistent infections. This indicates that system dynamics are governed more by the setup of the configuration space than by external environmental factors. Parameters affecting infection survival display varied behaviors, monotonic and non-monotonic. Environmental co-effects highlight regions of increased infection persistence, particularly in configurations with higher population densities and prolonged infection durations. The results emphasizes the role of information flow and the structural dynamics of social systems, where short-term memory and agent presence significantly affect infection survival probabilities.

This paper is structured as follows: The agent-based model is first introduced and a detailed description of its components provided. The model exploration process is then outlined, emphasizing the methodology employed to generate the results. Finally, we present and discuss the outcomes and draw conclusions from our research.

2 RELATED WORKS

Social dilemmas exist with the purpose of improving our understanding of how people interact in a resourcebounded environment (Van Lange et al., 2013), especially were there is a conflict between bounded rational entities which are metabolically dependent from a shared environment (Valentinov and Chatalova, 2016). At the best of our knowledge, (Dawes, 1980) was the first to introduce the concept of social dilemma, describing it as a scenario where individual decision-makers possess a dominant strategy that leads to non-cooperation and, if everyone adopt this dominant strategy, the outcome would be universally poorer, leading to a suboptimal equilibrium. The final rate of cooperation usually depends on the payoff structure

71 (Rand et al., 2012); even then, it is an approximation and usually requires a certain number of iterations to 52 be reached (Capraro, 2013).

73 The concept of the social dilemma is not confined to a single field of study. In economics, they encompass 74 a range of perspectives and findings, such as investigating the difference between rational behaviour and 75 social norm (Weber et al., 2004; Biel and Thøgersen, 2007). Also, social norms have been employed for 76 addressing environmental policies (Cerutti, 2017), conflict management strategies (Sitkin and Bies, 1993), 77 social learning (Mobius and Rosenblat, 2014), and knowledge sharing (Razmerita et al., 2016). Ecology has 78 a long tradition of using social dilemmas as well (Eshel and Motro, 1988; Woodall et al., 2000), especially 79 in light of the pervasive presence of cooperation in natural species (Gokhale and Hauert, 2016). These 80 settings can help in understanding the origin of sociality (Purcell et al., 2012) or group foraging strategies (Bach et al., 2006). Also, social dilemmas have been employed as the border between ecology and social 81 82 sciences, to study how success in species conservation depends as much on individuals can collaborate to a 83 common purpose (Di Chio et al., 2008; Cumming, 2018) and to use classic economic concepts such as 84 signaling and contract theory to interpret evolutionary biology (Archetti et al., 2011).

85 While El Farol Bar problem (Arthur, 1994) is a classic example of social dilemma with decisionmaking under uncertainty, it already presents several extensions. Statistical approaches have been used to 86 improve agents' decision-making strategies, particularly in dynamic environments with evolving population 87 behaviors (Challet and Zhang, 1997). Also, many approaches have been proposed to model the prediction 88 89 mechanisms and agent behaviors in contexts such as resource allocation (Challet and Zhang, 1997) and market dynamics (Johnson et al., 1998). A variant of the El Farol bar problem has recently been used to 90 91 examine the fairness of social distancing measures introduced during the Covid-19 pandemic (Schosser, 2022). However, this analysis did not consider the potential for agents to become infected. 92

Although the fields of epidemiology and social dilemmas have not traditionally intersected extensively, 93 recent years have seen a burgeoning interest in the interplay between these disciplines, particularly highlighted by global health crises such as the COVID-19 pandemic (Tanimoto and Tanimoto, 2018). The 95 application of social dilemma frameworks has proven insightful for examining the relationship between 96 individual behaviors and collective outcomes, notably in the context of vaccination rates within populations 97 (Tanimoto, 2021). These analyses utilize various models to illuminate the impact of factors such as 98 replicator dynamics (Kabir, 2021), social efficiency (Kabir, 2021; Khan and Tanimoto, 2023), and diffusion 99 structures (Wei et al., 2019) on vaccination uptake. Human behavior has been indicated as critical in 100 shaping epidemic trajectories, emphasizing how deviations from optimal behavior can lead to suboptimal 101 public health outcomes (Meloni et al., 2011) or how different cooperation styles affect the achievement 102 of herd immunity (Gharakhanlou and Hooshangi, 2020). Furthermore, empirical studies highlight how 103 cooperative behaviors may be amplified by the accelerated transmission of disease (Rychlowska et al., 104 2022). Additionally, the exploration of oscillatory behaviors within social dilemmas reveals how perceived 105 infection risks can drive a collective shift towards more cautious approaches to social interaction, such as 106 increased adherence to social distancing measures (Glaubitz and Fu, 2020). 107

3 MATERIAL AND METHODS

108 This section presents a description of the model of an epidemiological version of the El Farol Bar and the 109 exploration methodology employed to generate results.

3.1 Agent-based model description 110

- In this section an agent-based model of an epidemiological version of the El Farol Bar problem is 111
- described and the method employed to explore the model is presented. 112
- In addressing how epidemics affects the social dynamics in the El Farol Bar problem, agent-based 113
- modeling serves for two compelling reasons: as an approach traditionally employed to address social 114
- dilemmas, it is an effective means of communication within the scientific community; and it is particularly 115
- well-suited for capturing individual behaviors and their effects on an overall epidemic spread. This enables 116
- to get insights from the global co-effect of individual (i.e., agent-related) epidemic and social variables.
- At each time step t, the model implements a sequence of actions, as depicted in the flowchart (see 118
- Figure 1). "The first concerns the decision-making process regarding bar attendance: evaluating agents' 119
- memory of past attendance, estimating the expected crowd level, and making a decision accordingly. The 120
- second is about the dynamics of infection as induced by the interactions among the agents given their
- health states, where an infectious pathogen could be transmitted to those who decide to attend the bar, 122
- influenced by the density of the crowd and the duration of exposure. 123
- Together, these two sets of actions capture a dual aspect of agent behavior: social decision making 124
- influenced by past experiences and the epidemiological implications of these social choices. The model 125
- thus provides a framework for examining the interplay between individual decision making based on 126
- memory of previous states and the collective outcomes in terms of disease transmission, offering insights 127
- into how individual behaviors aggregate to impact public health. 128

3.1.1 Social dilemma 129

- 130 The proposed model includes a single kind of agents, representing the individuals that could decide to
- attend the bar in any given week (the time step of the model) and thus possibly be infectious. The agents' 131
- behavior is modeled according to the hypotheses of the original El Farol Bar problem. First, the only 132
- decision each agent can make each week is whether to attend the bar, and the decision is always executed. 133
- Second, agents like to attend the bar, if it is not too crowded, and do it as much as they can: hence, each 134
- agent decides each week whether to attend the bar depending upon its expectation of the total number of 135
- agents who will attend. Third, agents interact with each other only at the bar, and therefore when their 136
- decision to attend has been already made. 137
- The model introduced by this paper incorporates several hypotheses concerning agents' behavior. First, 138
- agents make a binary decision, as they can either choose to attend a bar or not; no other actions are included 139
- in the model, to focus on a specific aspect of social behavior. Second, agents inherently enjoy attending 140
- the bar and will do so as much as they can, but their preference is tempered by the bar's occupancy; 141
- agents are averse to overcrowding. Therefore, the decision to attend the event is influenced by their 142
- expectations regarding how crowded the bar will be. In time, this introduces a feedback loop where the 143
- average attendance of the bar inversely affects its attractiveness while it is directly influenced by it; a 144
- dynamic seen in many real-world social scenarios. Third, agents' interaction is solely defined by the shared 145
- presence in the crowded space of the bar, and there are no interpersonal communications or relationships 146
- affecting their attending decision.
- 148 The information about past attendance plays a crucial role in shaping agents' expectations, as it is used
- to estimate the number of agents likely to attend the bar in the subsequent week, as follows. For agents 149
- attending the event, the new value is the actual number of agents at the bar, while for agents that did not 150

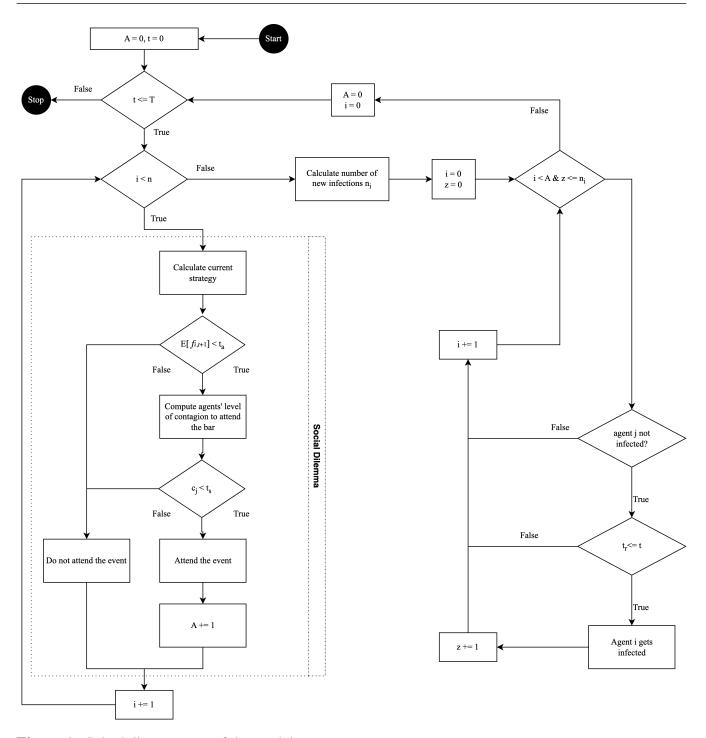


Figure 1. Scheduling process of the model.

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attend the new element of the memory is a random value, which stands for an educated guess made by agents which can not communicate with each other.

The agent's decision whether to attend the event or not is taken comparing an attendance threshold and the expectation regarding the future attendance. The attendance threshold t_a is a parameter of the model that depicts venue saturation level above which agents would consider unpleasant to be in the bar, consequently not attending the event.

Each agent i (where i goes from 1 to n, the total number of agents) generates an expectation regarding 157 how many agents will attend the bar at the next time step memorizing the number of agents present at the 158 bar during the last m times it attended the bar, with m being the memory length, and and assigning weights 159 to generate a prediction. In cases where the agent does not attend the bar, the value saved in memory is the 160 one hypothesized by the agent, namely, the one generated with the 'expected attendance'. Let $s_{i,k}$ be the 161 k-th element of the memory of agent i (with $k \in \{0, 1, ..., t\}$) and w the list of weight w_k used to the define 162 importance of each memory element, which increases with k. So, the attendance – which is the number the 163 agent i expects to be at the event at time t + 1 – is therefore given by: 164

$$E_i[\sum_{j=1}^m a_{j,t+1}] = \sum_{k=1}^m s_{i,k} w_k \tag{1}$$

where a_j is the participation of the agent j to the event at time t+1, $\sum_{j=1}^m a_{j,t+1}$ is the total attendance at time t+1 and $E_i[\sum_{j=1}^m a_{j,t+1}]$ is the expectation of the total attendance from agent i at time t+1. Consequently, from the expected attendance is possible to determine also the expected filling f of the venue at the time t+1

$$E_i[f_{t+1}] = \frac{E_i[\sum_{j=1}^m a_{j,t+1}]}{C_{max}}$$
 (2)

where C_{max} is the maximum capacity of the venue. Given the expected filling, at each time step an agent i attends the event whenever $E_i[f_{i,t+1}] < t_a$.

171 3.1.2 Epidemiological transmission

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In epidemiological models, each agent is typically (but not necessarily) in one of three states: susceptible, infectious, or recovered. These class of models accounts for the possibility of waning immunity after an infection, and eventually become susceptible again, modelling diseases where immunity, either natural or vaccine-induced, can be acquired and diminishes over time.

The epidemiological dimension of this model is based on several key modeling hypotheses. Firstly, the contagion process is assumed to be uniform across all agents, characterized by a consistent duration and an initially uniform level of infectiousness. This simplification negates individual variations in disease progression and response to infection. Secondly, the model posits that the disease in question is non-lethal; agents cannot die as a result of contracting the illness. This assumption is critical as it focuses the model on the dynamics of disease spread rather than mortality rates, and the overall number of individual in the system remains the same. Despite the absence of mortality and the maintenance of agent numbers over time, a disease that infects multiple agents has the potential to reduce the number of agents available for social interaction at any given time. Furthermore, the model assumes the absence of long-term physical or psychological effects post-infection. Recovered agents are not hindered in their ability to participate in normal activities, such as attending a bar, indicating that the disease does not cause lasting health impacts. Psychologically, the model assumes that agents do not experience fear or behavioral changes as a result of the infection. They continue to frequent the events without any alteration in their behavior due to the experience of being infected. The sole variable that the agent takes into account when determining whether or not to attend the bar is their own contagion level. Indeed, should an agent's c_i be too high, they may elect not to attend the bar due to the symptoms of the disease. Finally, a crucial aspect of this model is the agents' ignorance of the epidemic. Agents lack information about the total number of infected individuals

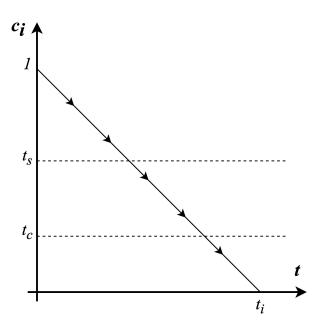


Figure 2. Dynamics of contagious level for each agent

and do not consider the risk of infection in their decision-making process. This implies a lack of adaptive behavior in response to the epidemic, which significantly influences the model's predictions about disease spread. By ignoring potential changes in social behavior and risk assessment, the model strictly focuses on the deterministic spread of the disease under constant behavioral patterns. This approach simplifies the modeling process but may overlook important dynamics present in real-world scenarios where awareness and behavioral adaptations play a crucial role in disease transmission.

Agents can get infected only by participating in an event. So, the epidemic transmission happens solely at the bar, and only if at least one infectious is attending. The number of new infected agents i_t at time t is

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$$i_t \propto \left\lfloor \alpha \frac{\sum_{j=1}^{n_i} c_j S_t}{C_{max}} \right\rfloor$$

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where c_i is the level of contagion of each agent attending the bar (which is 0 when agents are not infectious), S_t the number of agents in susceptible state attending the bar at time t, and α is the level of contagiousness of the infection. Notable, the contagious level is taken into account only for the n_i agents which are contagious enough, which is $c_j > t_c$.

In the proposed model, social relationships among agents are not considered, leading to a uniform infection probability for all individuals attending the bar at time t. Consequently, the selection of new i_t infected agents at each time step is randomized from those present, not considering individual interactions or relationships.

Whenever, an agent becomes infected, the infection follows this dynamics. Initially, the contagion level of the newly infected agent i is set to $c_i = 1$. Given an infection duration d_i , the contagiousity of agents decreases linearly by $1/d_i$ at each time step.

In the progression of the disease modeled, two critical thresholds, t_s and t_c , play pivotal roles in influencing agent behavior and the spread of the infection. The first threshold, t_s , represents the infection level at which an agent exhibits sufficient symptoms to deter them from attending the bar. The second, t_c , indicates the infection level beyond which agents can spread the infection The spread of the infection is

- most influenced by the agents with $t_c < c_i < t_s$, so with a contagious level between these two thresholds.
- 218 This is because it encapsulates the period when agents are infectious but may not have anymore the level
- 219 of symptom severity or self-awareness to avoid social gatherings, thereby contributing to the disease
- 220 transmission dynamics.

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- In the modeled scenario, infected agents undergo a recovery process after a duration of t_i time steps.
- 222 Upon recovery, these agents are conferred a temporary immunity lasting t_r time steps. However, this
- 223 immunity is not permanent; after the elapse of t_r time steps, the agents once again become susceptible
- 224 to infection. In this model, the transition from immune to susceptible is unambiguous; thus, an immune
- 225 agent will invariably possess a null probability of becoming infected. This cyclical pattern of recovery and
- 226 renewed susceptibility underscores the transient nature of immunity within the model.

3.2 Model exploration settings

The results from the simulation model were generated by means of a grid sampling exploration of the parameter space, to collect the model outputs from different parameters' combination j2013applying. Grid sampling from a parameter space involves systematically selecting a finite subset of parameter values that aims at comprehensively represent the entire parameter space. The idea underlying the use of this technique is to facilitate the exploration of system behavior across distinct parameter combinations, especially in cases where not a specific behaviour is expected or researched. Table 1 presents the parameters tested in the simulation and their explored ranges. Each parameter has been sampled from a uniform distribution. The data are collected by simulating the agent-based model 100'000 times. A preliminary analysis was conducted to assess the sensitivity to seed variation with specific parameter combinations (Bertolotti et al., 2020). It was observed that the variability of the metrics due to seed changes was practically zero, indicating that the mean or the presence of interesting behaviour in the time series was not dependent on the random number generator. Consequently, multiple experiments were not conducted for each random seed.

Table 1. Description of model parameters

Parameter	Description
$\overline{}$	Threshold of share of expected agents above which an agent does not attend the event
$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$	Duration of the infection
$\overline{t_p}$	Threshold of infection above which the infected agents have symptoms and do not attend the bar
α	Level of contagiousness of the disease
$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$	Threshold of infection below which an agent can not transmit the disease anymore
\overline{m}	Weight of the last memory in the decision-making process of agents
t_r	Duration of the immunity
n	Number of agents in the simulation

Even if the model is stochastic, each simulation was initialized with a specific random seed, that was stored as well. Consequently, the results were reproducible at a later stage, and the time series for each configuration of interest was observable. Furthermore, the initial number of infected is not fixed; rather, it is 10% of the population. This ensures that the infection will commence, and that any subsequent extinction will not be contingent on the initial number being insufficient. Additionally, a specific formula

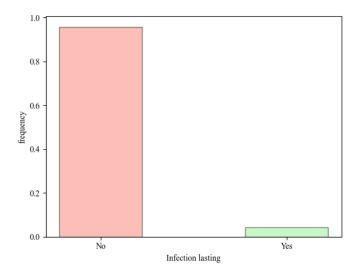


Figure 3. Share of runs where I(t=200)>0, i.e. where the infection lasted until the end of the simulation

was contemplated for identifying the minimum number of agents for which the contagion would be nonzero in the subsequent time step. However, to enhance replicability and explicability, the 10% method was ultimately selected.

From each simulation run, two time-series were collected: A, which is the number of attending agent at each time-step t, and I, the number of infected agents at each step of the simulation. From each time-series two output were extracted: the mean value of the series E[A] and E[I], which are used to assess the overall status of the system in time.

The model, the exploration code and the data analysis are all implemented in Python 3.11.

4 EXPERIMENTAL RESULTS

As illustrated in Figure 3, the epidemic did not persist until the conclusion of the simulation in the majority of instances when the specific experimental configuration was employed. The specific configuration of the model exploration plays a more significant role than the specific features of the model or the specific environmental parameters in determining the outcome. The percentage of surviving infections is highly dependent on the experimental configuration. Although it could be adjusted to achieve higher survival rates, the primary objective was to study the behaviour of the system under the current conditions. Keeping specific configurations that increase the likelihood of infection survival would limit the study of dynamics and introduce bias by artificially inflating survival rates.

One might be surprised that only a small proportion of runs result in a lasting infection, and thus conclude that the existence of infection in social systems is merely coincidental. This line of reasoning fails to consider the potential for biological specimens to adapt, which could result in the emergence of new infectious diseases. Such adaptations may occur through evolutionary processes, resulting in the evolution of new pathogens that are better equipped to survive and disseminate within a given environment. An alternative hypothesis is that these adaptations could either result in the evolution of a more resilient pathogen or in the extinction of the pathogen. In a scenario where the infecting entity is not adapting, the observed consequences are the result of a previous adaptation. Therefore, the parameters configuration in Table 2 should be considered in this context, particularly with regard to the epidemiological elements.

It is then possible to label of the simulation outcomes into two distinct groups based on their characteristics and behaviors;: S_a , which includes all the simulation results, serving as a comprehensive dataset to which to make confrontations; and S_i , containing those simulations where the epidemiological output I(t = 200) > 0. Table 2 provides a detailed comparison between two scenarios

Parameter	$\int E[par S_a]$	$E[par S_i]$	$\frac{E[par S_i] - E[par S_a]}{E[par S_a]}$
t_a	0.50	0.58	0.17
t_i	0.50	0.17	-0.66
d_i	5.51	6.91	0.26
\overline{m}	0.50	0.39	-0.22
t_p	0.50	0.56	0.13
$\overline{t_r}$	5.01	4.20	-0.16
α	0.26	0.32	0.23
c_p	0.75	0.77	0.02
\overline{n}	2252.35	2704.81	0.20

Table 2. The following table presents the results of the simulation. The second and third columns indicate the mean value of each analysed parameter for the S_a and S_i scenario, respectively. The final column shows the relative difference between the two scenarios, with the values normalised by the base scenario.

Figure 3 shows the effect of each parameter to the infection surviving, illustrating the distribution of each parameter exclusively for simulation runs for S_i . Given that each parameter has been sampled from a uniform distribution, the presence of diverse shapes suggests that there is an actual effect of each parameters upon the infection continuation, and that this effect may vary. It confirms the finding from Table 2.

For instance, the infection duration (d_i) , contagiousness of the infection (α) , and the number of agents in the simulation (n) all exert a growing monotonic influence on the infection's ability to survive. While the effect of d_i and α is intuitive, the impact of an increasing number of individuals is less clear, especially given that the capacity is not fixed but depends on n. This observation could depend on increased opportunities for interactions between agents, the potential for delayed saturation, and the presence of a buffer for randomness. Conversely, the significance of the most recently encoded event in the decision-making process of the agents (m) is univocally monotonically decreasing, indicating that a more rapid reaction time could diminish the probability of an infection's survival, even when considering solely the overall attendance and the absence of knowledge regarding the number of infected agents.

The remaining four parameters exhibit non-monotonic behaviour. The threshold of contagion below which the infection is not spread (t_i) or not perceived (t_p) plays a role only for specific values, functioning as enabling factors. Finally, it can be observed that the attendance threshold, t_a , and the recovery time, t_r , exhibit a non-symmetric "bell" shape. In the first case, the dependence may be attributed to the fact that insufficient attendance does not result in the establishment of a critical mass at the bar, thereby preventing the constant dissemination of the epidemic. Conversely, when the value is excessively high, the epidemic rapidly eliminates all susceptible individuals, leading to extinction following a primary surge. With regard to the recovery time, it is evident that the proportion of surviving infections declines as this variable increases. However, it is counterintuitive that, at low values of this variable, there is an increase in the proportion of surviving infections. It may be the case that this is due to the fact that it reduces the size of the infection waves by reducing infection synchronisation, thus allowing them to persist for longer without being extinguished due to the absence of non-infected agents.

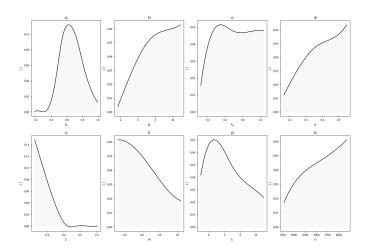


Figure 4. Distribution of experimental parameters for S_i

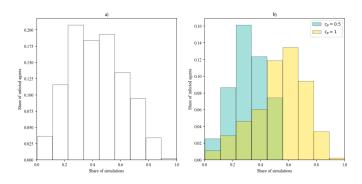


Figure 5. The distribution of the share of infected agents at the conclusion of the simulation I(t = 200) for S_i , aggregated (on the left) and divided by the percentage capacity of the venue relative to the total number of agents c_p (on the right).

In Figure 5, histogram on the left depicts the mean number of agents infected over the course of a simulation in which the infection was sustained, while the one on the right decomposes the data as a function of the percentage capacity of the bar, which can be only $c_p = 0.5$ or $c_p = 1$. The symmetrical shape of the histogram (a) could suggest a relatively balanced distribution of infection rates, with few extreme cases of very low or very high infection levels, but histogram (b) reveals that it depends strongly from the bar capacity, given that it is the combination of two distribution ranging from 0 to 1 with respectively a left and a right tail.

It is evident that there is a co-effect between the environmental parameters, which can be visualised in Figure 6. The gradient of the simulation in the top-left part of Figure 6 exhibits a pronounced clustering of elevated values in the top right quadrant, with a gradual decline in the lower left. This suggests that, within the confines of this experimental configuration, it is highly improbable to observe a simulation characterised by low population density and minimal infection duration. Analogously, the top-right subfigure illustrates that, for a given configuration of infection threshold (t_i) and attendance threshold (t_a) , the probability of infection survival is higher when the majority of runs occur at a specific point.

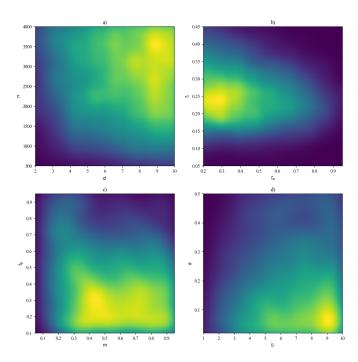


Figure 6. The number of simulations conducted for a configuration of parameters in S_i .

5 DISCUSSIONS AND CONCLUSIONS

This paper introduces a modified version of the El Farol Bar social dilemma with an added epidemiological dimension, where individuals must choose whether to engage in social activities during a disease outbreak. The simulation results indicate two key messages. The first is the importance of the rate of information available in the social system, which can be observed in the role of short-term memories and personal awareness regarding the infective status. This is not unexpected when the model is viewed as a decision-making context, and there is a long tradition of research exploring how an entity's capacity to gather and process information affects their actions. The second element is the need for taking explicitly into account social system structure, which in this case derives from agents' numerosity and dynamics. From a topological perspective, an agent can be situated in one of two states: present or absent from the event. Agents that are present are interconnected, at least potentially, while those that are absent are not. This situation undergoes change at each time step. These elements can change in accordance with both social and epidemic features, which in turn give rise to a diversification of the system structure and, consequently, an increase in the probability of an infection lasting.

Also, the results indicate a positive effect between population size and infection surviving. Given than, by design, the model is a structured representation of a closed systems, this finding suggets that an efficient strategy could be involve sectoral management by dividing larger systems into smaller, manageable units. Such an approach would facilitate easier control and monitoring of these smaller systems.

The most negative effect on infection spread is linked to the infectiousness threshold. This is consistent with the expectation that when an infective specimen falls in the area where can be perceived longer than it can be widespread, it has less chances to survive. Furthermore, this underscores again the critical role of information. More informed agents, who are thus more aware of the risks, and so have an higher perception threshold, are more likely to make decisions that would spread the infection, thereby influencing the overall dynamics of disease spread.

- A limitation of this study is the homogeneity of agents' behavior. Future research could explore how the system behaves when agents exhibit diverse behaviors. However, it was deemed unnecessary to include this aspect in the initial analysis. Intuitively, increasing the number of agents would likely result in behavioral heterogeneity being averaged out in a mean-field approximation, which guided the decision to use the current configuration. Nonetheless, this represents a limitation and a potential avenue for future research aimed at validating the results under more heterogeneous scenarios.
- More broadly, the main limitation of this study is that the analyses were conducted within the framework of a social dilemma, rather than on an empirically validated model. While the insights and results derived from this approach are valid, they should be viewed as preliminary suggestions for empirical researchers conducting field experiments. The findings provide a theoretical foundation that can guide future empirical work, but further validation through real-world data is necessary to confirm their applicability.
- 347 Future developments can take multiple directions. First, the time-series dynamics of the model could 348 be studied to identify whether specific dynamic equilibria or limit cycles emerge, which could be highly 349 relevant for public decision-makers. Second, an extension to the model could be make, introducing a policy-maker agent that could employ actions for epidemic containment. The results from the synthetic 350 351 decision-makers' actions could be compared to real-world policy decisions made during the Covid-19 pandemic. Third, an analysis could be conducted to quantify the amount of information (in bits) required 352 by each agent to make informed decisions in such contexts. Finally, a potential extension could explore 353 long-term infections not tied to short-term events like a night out, but where the socio-epidemiological 354 co-dynamics remain critical, such as in diseases like AIDS. 355

CONFLICT OF INTEREST STATEMENT

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

AUTHOR CONTRIBUTIONS

F.B. contributes in the conceptualization, formal analysis, investigation, methodology, project administration, software, validation, visualization and writing of the paper. N.K and L.P. contributes in the software, visualization and writing the original draft of the paper. L.M. contributes in supervision and review and editing the draft.

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DATA AVAILABILITY STATEMENT

- 364 The model used to generate the data, the generated data and the notebook used to treat 365 the data and generate the results and the figures is available at the following repository:
- 366 https://anonymous.4open.science/r/epielfarol-D880/

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