

# Planning for Temporally Extended Goals in Pure-Past Linear Temporal Logic



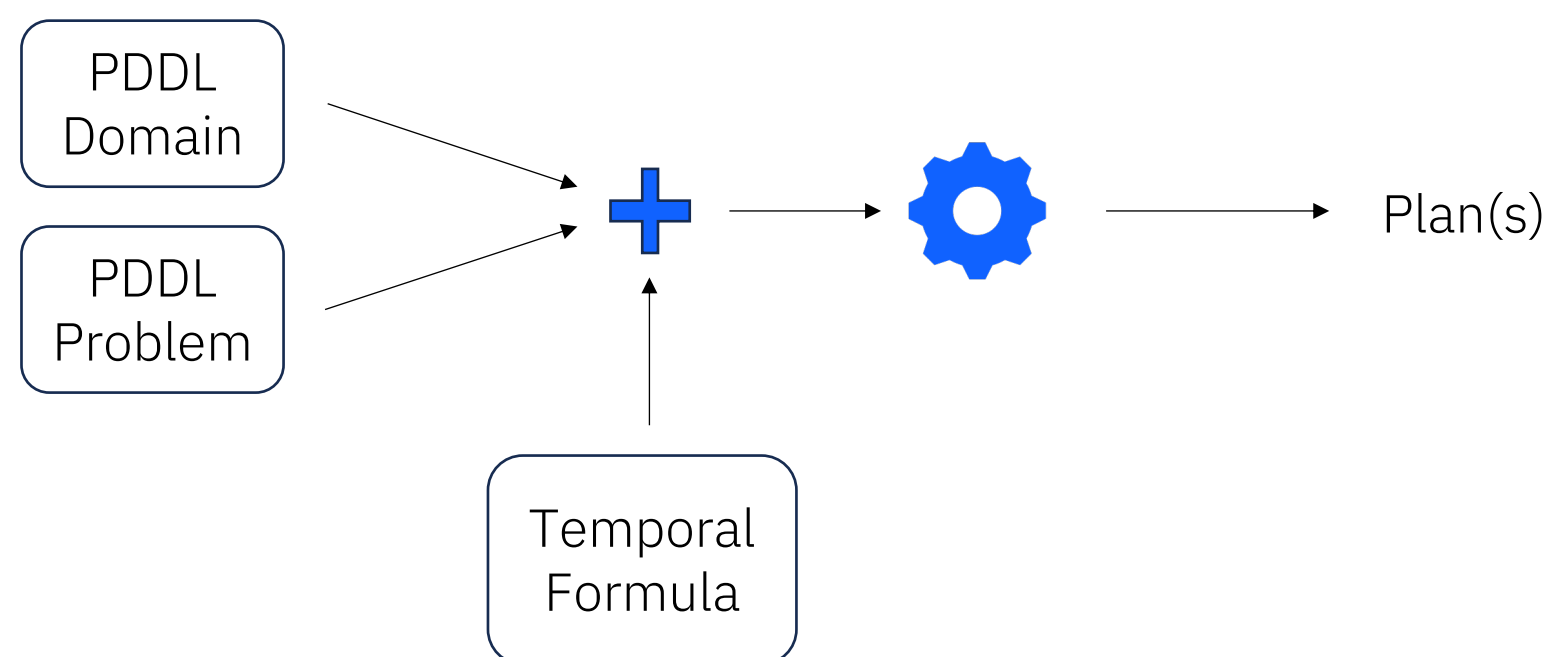
Best Student  
Paper Award

Luigi Bonassi, Giuseppe De Giacomo, Marco Favorito, [Francesco Fuggitti](#), Alfonso E. Gerevini, Enrico Scala

Contact: [francesco.fuggitti@gmail.com](mailto:francesco.fuggitti@gmail.com)

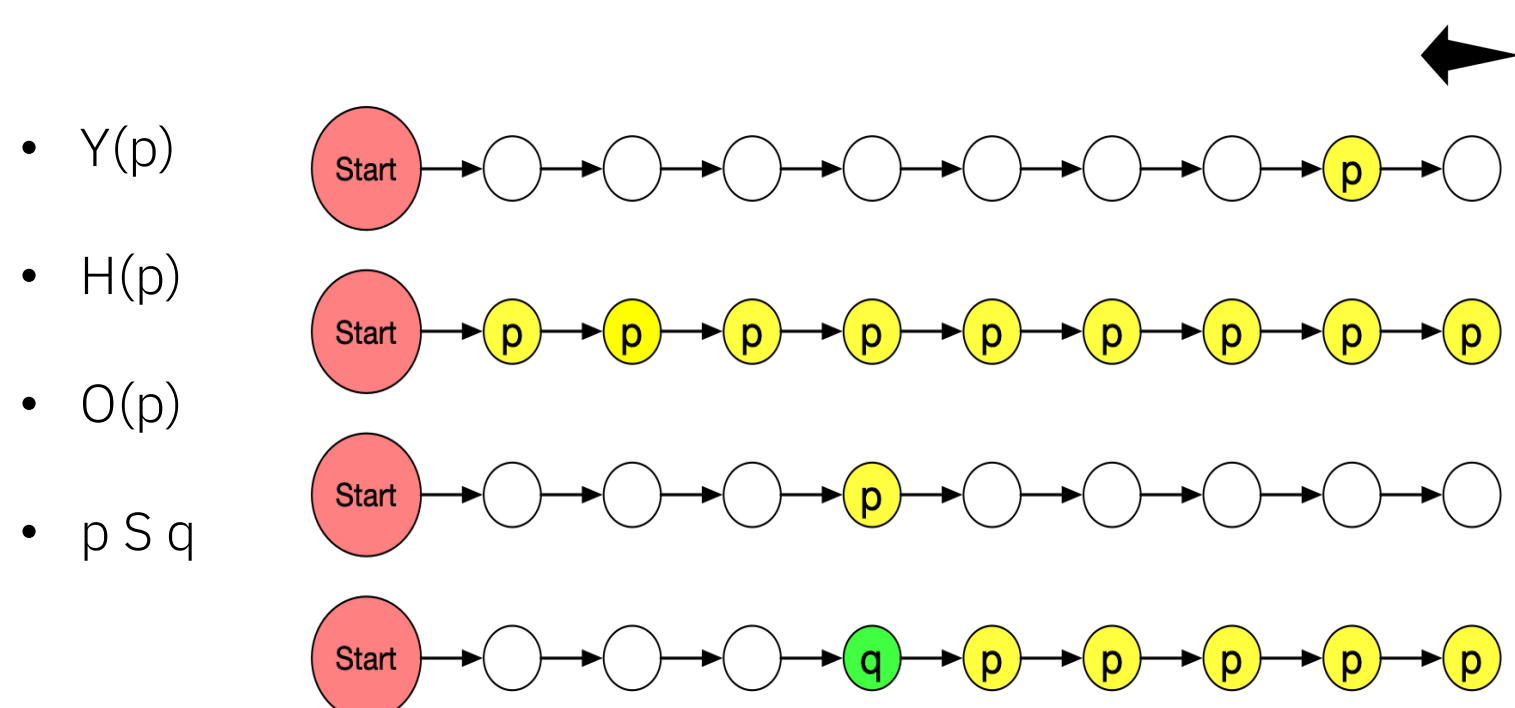
## Context

Restrict the way the planner achieves the goal



## Pure-Past Linear-time Temporal Logic

- Talks about properties of the world with past temporal operators only: (Y)esterday, (H)istorically, (O)nce, (S)ince
- PPLTL looks at the trace backward, and evaluates formulas on the last instant of the trace (i.e., the current instant)



## Useful PPLTL Patterns

DECLARE Template	Equivalent PPLTL Formula	Equivalent LTL <sub>f</sub> Formula
init( <i>a</i> )	$O(a \wedge \neg Y(true))$	$a$
existence( <i>a</i> )	$O(a)$	$F(a)$
absence( <i>a</i> )	$\neg O(a)$	$\neg F(a)$
absence2( <i>a</i> )	$H(a \rightarrow WYH(\neg a))$	$\neg(Fa \wedge XF(a))$
choice( <i>a</i> , <i>b</i> )	$O(a) \vee O(b)$	$F(a) \vee F(b)$
exclusive-choice( <i>a</i> , <i>b</i> )	$(O(a) \vee O(b)) \wedge \neg(O(a) \wedge O(b))$	$(F(a) \vee F(b)) \wedge \neg(F(a) \wedge F(b))$
co-existence( <i>a</i> , <i>b</i> )	$H(\neg a) \leftrightarrow H(\neg b)$	$F(a) \leftrightarrow F(b)$
responded-existence( <i>a</i> , <i>b</i> )	$O(a) \rightarrow O(b)$	$F(a) \rightarrow F(b)$
response( <i>a</i> , <i>b</i> )	$(\neg a S b) \vee H(\neg a)$	$G(a \rightarrow F(b))$
precedence( <i>a</i> , <i>b</i> )	$H(b \rightarrow O(a))$	$(\neg b U a) \vee G(\neg b)$
succession( <i>a</i> , <i>b</i> )	$\text{response}(a, b) \wedge \text{precedence}(a, b)$	
chain-response( <i>a</i> , <i>b</i> )	$H(Y(a) \rightarrow b) \wedge \neg a$	$G(a \rightarrow X(b))$
chain-precedence( <i>a</i> , <i>b</i> )	$H(b \rightarrow Y(a))$	$G(X(b) \rightarrow a) \wedge \neg b$
chain-succession( <i>a</i> , <i>b</i> )	$(H(Y(a) \rightarrow b) \wedge \neg a) \wedge H(Y(\neg a) \rightarrow \neg b)$	$G(a \leftrightarrow X(b))$
not-co-existence( <i>a</i> , <i>b</i> )	$O(a) \rightarrow \neg O(b)$	$F(a) \rightarrow \neg F(b)$
not-succession( <i>a</i> , <i>b</i> )	$H(b \rightarrow \neg O(a))$	$G(a \rightarrow \neg F(b))$
not-chain-succession( <i>a</i> , <i>b</i> )	$H(b \rightarrow \neg Y(a))$	$G(a \rightarrow \neg X(b))$

PDDL3 Operator	Equivalent PPLTL Formula	Equivalent LTL <sub>f</sub> Formula
(at-end $\theta$ )	$\theta$	$F(\theta \wedge \text{final})$
(always $\theta$ )	$H(\theta)$	$G(\theta)$
(sometime $\theta$ )	$O(\theta)$	$F(\theta)$
(sometime-after $\theta_1 \theta_2$ )	$(\neg \theta_1 S \theta_2) \vee H(\neg \theta_1)$	$G(\theta_1 \rightarrow F(\theta_2))$
(sometime-before $\theta_1 \theta_2$ )	$H(\theta_1 \rightarrow Y(O(\theta_2)))$	$\theta_2 R \neg \theta_1$
(at-most-once $\theta$ )	$H(\theta \rightarrow (\theta S (H(\neg \theta) \vee \text{start})))$	$G(\theta \rightarrow (\theta U (G(\neg \theta) \vee \text{final})))$
(hold-during $n_1 n_2 \theta$ )	$\bigvee_{0 \leq i \leq n_1} (\theta \wedge Y^i(\text{start})) \vee \bigwedge_{n_1 < i \leq n_2} H(\theta \vee WY^i(Y(true)))$	$\bigvee_{0 \leq i \leq n_1} X^i(\theta \wedge \text{final}) \vee \bigwedge_{n_1 < i \leq n_2} WX^i(\theta)$
* (hold-after $n \theta$ )	$\bigvee_{0 \leq i \leq n} (\theta \wedge Y^i(\text{start})) \vee O(\theta \wedge Y^{n+1}(O(\text{start})))$	$\bigvee_{0 \leq i \leq n} X^i(\theta \wedge \text{final}) \vee X^{n+1}(F(\theta))$

## Contribution

In our work, using PPLTL goals, we introduce a **linear** encoding of classical planning for PPLTL goals into classical planning that **preserves** plan length

- Due to the LTLf nature, state-of-the-art encodings for LTLf are
  - Exponential**, but **preserves** the plan length [Baier & McIlraith, 2006]
  - Polynomial**, but **increases** the plan length [Torres & Baier, 2015]

## Handling PPLTL Goals

**Intuition:** given the prefix of a trace, while LTLf must consider all possible extensions, PPLTL can simply be evaluated on the prefix (i.e., the history produced so far)

$$\text{pnf}(p) = p;$$

$$\text{pnf}(Y\phi) = \boxed{Y\phi};$$

$$\text{pnf}(\phi_1 S \phi_2) = \text{pnf}(\phi_2) \vee (\text{pnf}(\phi_1) \wedge \boxed{Y(\phi_1 S \phi_2)});$$

$$\text{pnf}(\phi_1 \wedge \phi_2) = \text{pnf}(\phi_1) \wedge \text{pnf}(\phi_2);$$

$$\text{pnf}(\neg\phi) = \neg\text{pnf}(\phi).$$

How?

Exploit the “**fixpoint characterization**” of temporal formulas [Gabbay et al., 1980; Manna 1982; Barringer et al., 1989; Emerson 1990]

To evaluate a PPLTL formula, we only need to keep track of the truth value of *some* of its subformulas!!!

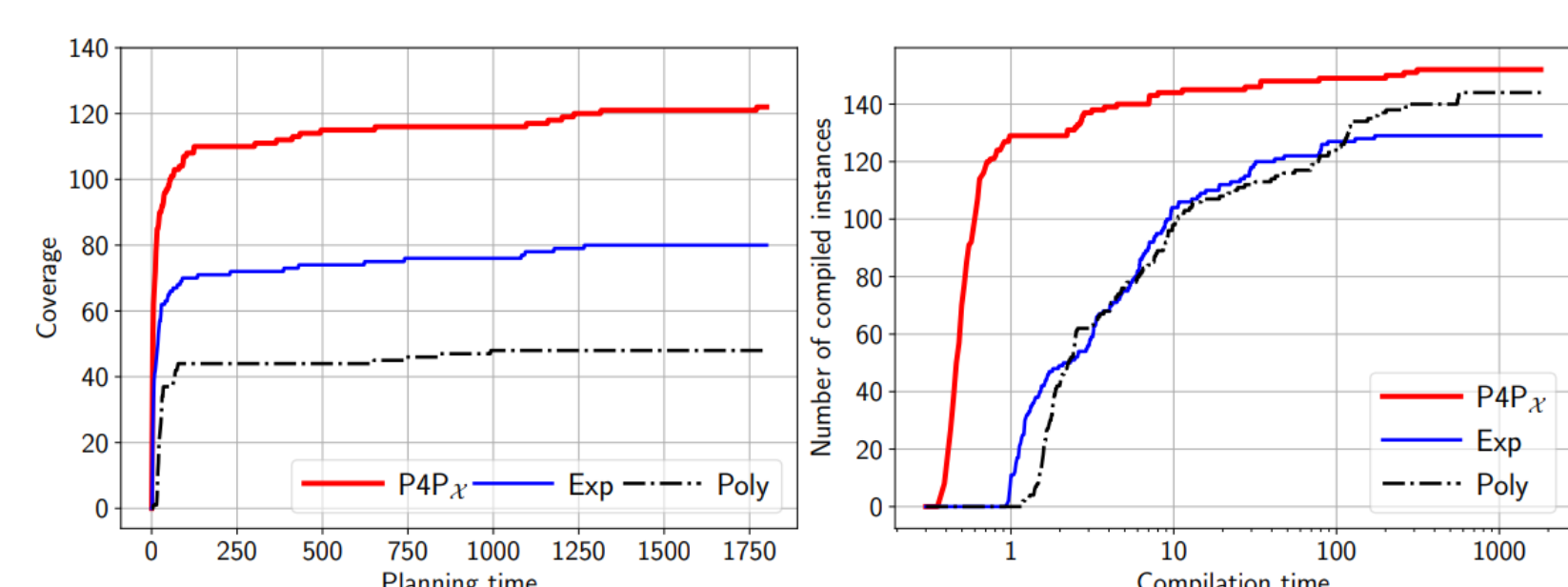
## Evaluating PPLTL Goals

Sound and complete approach to symbolically encode PPLTL goal formulas in planning domains that is **polynomial** in the size of the domain specification and **linear** in the size of the PPLTL goal

Components	Encoding										
Fluents $\mathcal{F}'$	$\mathcal{F}' := \mathcal{F} \cup \Sigma_\varphi$										
Derived Predicates $\mathcal{F}'_{der}$	$\mathcal{F}'_{der} := \mathcal{F}_{der} \cup \{\text{val}_\phi \mid \phi \in \text{sub}(\varphi)\}$										
Axioms $\mathcal{A}'$	$\mathcal{A}' := \mathcal{A} \cup \{x_\phi \mid \phi \in \text{sub}(\varphi)\}$ where $x_\phi$ is <table> <tr> <td><math>\text{val}_p \leftarrow p</math></td><td><math>(\phi = p)</math></td></tr> <tr> <td><math>\text{val}_{Y\phi'} \leftarrow \neg Y\phi'</math></td><td><math>(\phi = Y\phi')</math></td></tr> <tr> <td><math>\text{val}_{\phi_1 S \phi_2} \leftarrow (\text{val}_{\phi_2} \vee (\text{val}_{\phi_1} \wedge \neg Y(\phi_1 S \phi_2)))</math></td><td><math>(\phi = \phi_1 S \phi_2)</math></td></tr> <tr> <td><math>\text{val}_{\phi_1 \wedge \phi_2} \leftarrow (\text{val}_{\phi_1} \wedge \text{val}_{\phi_2})</math></td><td><math>(\phi = \phi_1 \wedge \phi_2)</math></td></tr> <tr> <td><math>\text{val}_{\neg\phi'} \leftarrow \neg \text{val}_{\phi'}</math></td><td><math>(\phi = \neg\phi')</math></td></tr> </table>	$\text{val}_p \leftarrow p$	$(\phi = p)$	$\text{val}_{Y\phi'} \leftarrow \neg Y\phi'$	$(\phi = Y\phi')$	$\text{val}_{\phi_1 S \phi_2} \leftarrow (\text{val}_{\phi_2} \vee (\text{val}_{\phi_1} \wedge \neg Y(\phi_1 S \phi_2)))$	$(\phi = \phi_1 S \phi_2)$	$\text{val}_{\phi_1 \wedge \phi_2} \leftarrow (\text{val}_{\phi_1} \wedge \text{val}_{\phi_2})$	$(\phi = \phi_1 \wedge \phi_2)$	$\text{val}_{\neg\phi'} \leftarrow \neg \text{val}_{\phi'}$	$(\phi = \neg\phi')$
$\text{val}_p \leftarrow p$	$(\phi = p)$										
$\text{val}_{Y\phi'} \leftarrow \neg Y\phi'$	$(\phi = Y\phi')$										
$\text{val}_{\phi_1 S \phi_2} \leftarrow (\text{val}_{\phi_2} \vee (\text{val}_{\phi_1} \wedge \neg Y(\phi_1 S \phi_2)))$	$(\phi = \phi_1 S \phi_2)$										
$\text{val}_{\phi_1 \wedge \phi_2} \leftarrow (\text{val}_{\phi_1} \wedge \text{val}_{\phi_2})$	$(\phi = \phi_1 \wedge \phi_2)$										
$\text{val}_{\neg\phi'} \leftarrow \neg \text{val}_{\phi'}$	$(\phi = \neg\phi')$										
Action Labels $A$	$A := A$ , i.e., unchanged										
Preconditions $pre$	$pre(a) := pre(a)$ for every $a \in A$ , i.e., unchanged										
Effects $eff'$	$eff'(a) := eff(a) \cup eff_{val}$ , where $eff_{val} = \{\text{val}_\phi \triangleright \neg Y\phi' \mid \neg Y\phi' \in \Sigma_\varphi\}$										
Initial State $s'_0$	$s'_0 := \sigma_0 \cup s_0$										
Goal $G'$	$G' := \text{val}_\varphi$										

## Experimental Results

- Introduce the [Plan4Past<sup>1</sup>](#) (P4P) system ([github.com/whitemech/Plan4Past](https://github.com/whitemech/Plan4Past))
- IPC domains: BLOCKS, ELEVATOR, OPENSTACKS, ROVERS
- P4P + LAMA, Exp + LAMA Poly + LAMA



Domain	I	Coverage			Avg RT			Avg PL		
		P4P	Poly	Exp	P4P	Poly	Exp	P4P	Poly	Exp
ROVERS	TB 7	<b>7</b>	<b>7</b>	6	<b>1.43</b>	21.11	1.98	<b>5.33</b>	5.67 (74.50)	<b>5.33</b>
	BF 40	<b>33</b>	6	22	35.36	—	<b>24.24</b>	43.68	—	<b>43.50</b>
BLOCKSWORLD	TB 15	<b>15</b>	<b>15</b>	8	<b>1.41</b>	20.43	13.13	7.50	7.88 (132.88)	<b>7.25</b>
	BF 21	<b>21</b>	1	1	—	—	—	—	—	—
OPENSTACKS	TB 10	<b>10</b>	<b>10</b>	6	<b>6.11</b>	31.66	8.75	22.00	<b>21.67</b> (349.00)	22.00
	BF 30	7	5	8	<b>11.88</b>	68.86	19.50	<b>24.00</b>	<b>24.00</b> (841.00)	<b>24.00</b>
ELEVATOR	BF 29	<b>29</b>	4	<b>29</b>	231.83	—	<b>228.09</b>	<b>75.48</b>	—	<b>75.48</b>
Total		<b>122</b>	48	80						