

# Concepts of Program Design — Assignment 1

## An evaluator for MinHs

Version 1.0

Due date: **Friday, 13th of December, 23:59**

### History

27/11/2019 Initial spec released

### Overview

In this assignment you will implement an interpreter for MinHs, a small functional language similar to ML and Haskell. It is fully typed, with types specified by the programmer. The assignment consists of a base component, worth 60%, and five additional components, each worth 8%.

- **Task 1 (70%)**  
Implement an interpreter for the MinHs language presented in the lectures, using an environment semantics, including support for recursion and closures.
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- **Task 2 (8%)**  
Extend the interpreter to support partially applied prim-ops.
  - **Task 3 (8%)**  
Extend the interpreter to support n-ary functions
  - **Task 4 (8%)**  
Extend the interpreter to support multiple bindings in the one `let` form.
  - **Task 5 (8%)**  
Extend the interpreter to support `let` bindings that take parameters, defining non-recursive functions.
  - **Task 6 (8%)**  
Extend the interpreter to support mutually recursive bindings.

Each of these parts is explained in detail below.

The front end of the interpreter (lexer, parser, type checker) is provided for you, along with the type of the `evaluate` function (found in the file `Evaluator.hs`).

The function `evaluate` returns an object of type `Value`. You may modify the constructors for `Value` if you wish, but not the type for `evaluate`. The return value of `evaluate` is used to check the correctness of your assignment.

You must provide an implementation of `evaluate`, in `Evaluator.hs`. It is this file you will submit for Task 1. No other files can be modified.

You can assume the typechecker has done its job and will only give you correct programs to evaluate. The type checker will, in general, rule out invalid programs, so the interpreter does not have to consider them.

**Email Ron `r.g.f.p.vanderfeesten@uu.nl` in case you have questions about this assignment (or ask after the lecture or during the exercises).**

## 1 Task 1

This is the core part of the assignment. You are to implement an interpreter for MinHs. The following expressions must be handled:

- variables. `v, u`
- integer constants. `1, 2, . .`
- boolean constants. `True, False`
- some primitive arithmetic and boolean operations. `+, *, <, <=, . .`
- constructors for lists. `Nil, Cons`
- destructors for lists. `head, tail`
- inspectors for lists. `null`
- function application. `f x`
- `if e then e1 else e2`
- `let x :: τx = e1; y :: τy = e2; ... in e2`
- `recfun f :: (τ1 → τ2) x = e` expressions

These cases are explained in detail below. The abstract syntax defining these syntactic entities is in `Syntax.hs`. You should understand the data type `Exp` and `Bind` well.

Your implementation is to follow the dynamic semantics described in the lectures, and this document. You are *not* to use substitution as the evaluation strategy, but must use an environment/heap semantics. If a runtime error occurs, which is possible, you should use Haskell's `error :: String -> a` function to emit a suitable error message (the error code returned by `error` is non-zero, which is what will be checked for – the actual error message is not important).

## 1.1 Program structure

A program in MinHs may evaluate to either an integer, a list of integers, or a boolean, depending on the type assigned to the `main` function. The `main` function is always defined (this is checked by the implementation). In Task 1 programs, you need only consider the case of a single top-level binding for `main`, like so:

```
main :: Int = 1 + 2;
```

or

```
main :: Bool
= let x :: Int = 1;
  in if x + ((recfun f :: (Int -> Int) y = y * y) 2) == 0
      then True
      else False;
```

## 1.2 Variables, Literals and Constants

MinHs is a spartan language. We only have to consider 4 types:

```
Int
Bool
t1 -> t2
[Int]
```

The only literals you will encounter are integers. The only non-literal constructors are `True` and `False` for the `Bool` type, and `Nil` and `Cons` for the `[Int]` type.

## 1.3 Function application

MinHs is, by virtue of its Haskell implementation, a non-strict language. An argument to a function is only evaluated when needed — when the function tries to inspect its value. This does not add a great deal of complexity to your implementation — it will occur naturally as you will be writing the interpreter in Haskell, which is also a non-strict language.

*The result of a function application may in turn be a function.*

## 1.4 Primitive operations

You need to implement the following primitive operations:

```
+      :: Int -> Int -> Int
-      :: Int -> Int -> Int
*      :: Int -> Int -> Int
/      :: Int -> Int -> Int

negate  :: Int -> Int

>      :: Int -> Int -> Bool
>=     :: Int -> Int -> Bool
<      :: Int -> Int -> Bool
```

```

<=      :: Int -> Int -> Bool

==      :: Int -> Int -> Bool
/=      :: Int -> Int -> Bool

head :: [Int] -> Int
tail :: [Int] -> [Int]
null  :: [Int] -> Bool

```

These operations are defined over `Ints`, `[Int]`s, and `Bools`, as usual. `negate` is the primop representation of the unary negation function, i.e. `-1`. The abstract syntax for primops is defined in `Syntax.hs`.

## 1.5 if - then - else

`MinHs` has an `if  $e$  then  $e_1$  else  $e_2$`  construct. The types of  $e_1$  and  $e_2$  are the same. The type of  $e$  is `Bool`.

## 1.6 let

For the first task you only need to handle simple `let` expressions of the kind we have discussed in the lectures. Like these:

```

main :: Int
  = let
      x :: Int = 1 + 2;
    in x;

```

or

```

main :: Int
  = let f :: (Int -> Int)
      = recfun f :: (Int -> Int) x = x + x;
    in f 3;

```

For the base component of the assignment, you do not need to handle `let` bindings of more than one variable at a time (as is possible in Haskell). Remember, a `let` may bind a recursive function defined with `recfun`.

## 1.7 recfun

The `recfun` expression introduces a new, named function value. It has the form:

```
(recfun f :: (Int -> Bool) x = x + x)
```

A `recfun` value is a first-class value, and may be bound to a variable with `let`. The value ‘`f`’ is bound in the body of the function, so it is possible to write recursive functions:

```

recfun f :: (Int -> Int) x =
  if x < 10 then f (x+1) else x

```

Be very careful when implementing this construct, as there can be problems when using environments in a language allowing functions to be returned by functions.

## 1.8 Evaluation strategy

We have seen in the lecture how it is possible to evaluate expressions via substitution. This is an extremely inefficient way to run a program. In this assignment you are to use an environment instead. You will be penalised for an interpreter that operates via substitution. The module `Env.hs` provides a data type suitable for most uses. Consult the lecture notes on how environments are to be used in dynamic semantics. The strategy is to bind variables to values in the environment, and look them up when required.

In general, you will need to use: `empty`, `lookup` and `addAll` to begin with an empty environment, lookup the environment, or to add a binding to the environment, respectively. As these functions clash with functions in the `Prelude`, a good idea is to import the module `Env` qualified:

```
import qualified Env
```

This makes the functions accessible as `Env.empty` and `Env.lookup`, to disambiguate from the `Prelude` versions.

## 2 Dynamic Semantics of MinHs

### Big-step semantics

We define a relation  $\Downarrow$  which relates an environment mapping variables to values<sup>1</sup>  $\Gamma$  and an expression  $E$  to the resultant value of that expression  $V$ . Our value set for  $V$  will, to start with, consist of:

- *Machine integers*
- *Boolean values*
- *Lists of integers*

We will also need to add *closures*, or *function values* to our value set to deal with the `recfun` construct in a sound way. See the section on Function Values for details.

### Environment

The environment  $\Gamma$  maps variables to values, and is used in place of substitution. It is specified as follows:

$$\Gamma ::= \cdot \mid \Gamma, x = v$$

Values bound in the environment are closed – they contain no free variables. This requirement creates a problem with function values created with `recfun` whose bodies contain variables bound in an outer scope. We must bundle them with their associated environment as a *closure*.

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<sup>1</sup>Or, possibly, to an unevaluated computation of the value, but in Haskell these two things are indistinguishable.

## Constants and Boolean Constructors

$$\frac{}{\Gamma \vdash \text{Num } n \Downarrow n} \quad \frac{}{\Gamma \vdash \text{Con True} \Downarrow \text{True}} \quad \frac{}{\Gamma \vdash \text{Con False} \Downarrow \text{False}}$$

## Primitive operations

$$\frac{\Gamma \vdash e_1 \Downarrow v_1 \quad e_2 \Downarrow v_2}{\Gamma \vdash \text{Plus } e_1 \ e_2 \Downarrow v_1 + v_2}$$

Similarly for the other arithmetic and comparison operations (as for the language of arithmetic expressions, and in chapters 7,8 of Harper [2].).

Note that division by zero should cause your interpreter to throw an error using Haskell's `error` function.

The abstract syntax of the interpreter re-uses function application to represent application of primitive operations, so `Plus e1 e2` is actually represented as:

$$\text{App (App (Prim Plus } e_1) \ e_2)$$

For this first part of the assignment, you may assume that prim-ops are never partially applied — that is, they are fully saturated with arguments, so the term `App (Prim Plus e1)` will never occur in isolation.

## Evaluation of *if*-expression

$$\frac{\Gamma \vdash e_1 \Downarrow \text{True} \quad \Gamma \vdash e_2 \Downarrow x}{\Gamma \vdash \text{If } e_1 \ e_2 \ e_3 \Downarrow x}$$

$$\frac{\Gamma \vdash e_1 \Downarrow \text{False} \quad \Gamma \vdash e_3 \Downarrow x}{\Gamma \vdash \text{If } e_1 \ e_2 \ e_3 \Downarrow x}$$

## Variables

$$\frac{\Gamma(x) = v}{\Gamma \vdash \text{Var } x \Downarrow v}$$

## List constructors and primops

$$\frac{}{\Gamma \vdash \text{Nil} \Downarrow []} \quad \frac{\Gamma \vdash x \Downarrow v_x \quad \Gamma \vdash xs \Downarrow v_{xs}}{\Gamma \vdash \text{Cons } x \ xs \Downarrow v_x : v_{xs}}$$

$$\frac{\Gamma \vdash x \Downarrow v : vs}{\Gamma \vdash \text{head } x \Downarrow v} \quad \frac{\Gamma \vdash x \Downarrow v : vs}{\Gamma \vdash \text{tail } x \Downarrow vs} \quad \frac{\Gamma \vdash x \Downarrow v : vs}{\Gamma \vdash \text{null } x \Downarrow \text{False}}$$

$$\frac{\Gamma \vdash x \Downarrow []}{\Gamma \vdash \text{head } x \Downarrow \text{error}} \quad \frac{\Gamma \vdash x \Downarrow []}{\Gamma \vdash \text{tail } x \Downarrow \text{error}} \quad \frac{\Gamma \vdash x \Downarrow []}{\Gamma \vdash \text{null } x \Downarrow \text{True}}$$

For the first part of the assignment, you may assume that `Cons` is also never partially applied, as with `prim-ops`.

### Variable Bindings with Let

$$\frac{\Gamma \vdash e_1 \Downarrow v_1 \quad \Gamma, x=v_1 \vdash e_2 \Downarrow v_2}{\Gamma \vdash \text{Let } e_1 (x.e_2) \Downarrow v_2}$$

### Function values

To maintain soundness with function values, we need to pair a function with its environment, forming a *closure*. We introduce the following syntax for function values: (the types are included for completeness, but are not required at runtime):

$$\langle\langle\Gamma; \text{Recfun } \tau_1 \tau_2 f.x.e\rangle\rangle$$

You will need to decide on a suitable representation of closures as a Haskell data type.

Now we can specify how to introduce closed function values:

$$\frac{}{\Gamma \vdash \text{Recfun } \tau_1 \tau_2 f.x.e_1 \Downarrow \langle\langle\Gamma; \text{Recfun } \tau_1 \tau_2 f.x.e_1\rangle\rangle}$$

We also re-use the `recfun` syntax, only without arguments, to construct infinite structures like infinite lists. Here, the recursive reference is provided but no function value is necessary:

$$\frac{\Gamma, f = v \vdash e \Downarrow v}{\Gamma \vdash \text{Recfun } \tau f.e \Downarrow v}$$

### Function Application

$$\frac{\Gamma \vdash e_1 \Downarrow v_1 \quad v_1 = \langle\langle\Gamma'; \text{Recfun } \tau_1 \tau_2 f.x.e_f\rangle\rangle \quad \Gamma \vdash e_2 \Downarrow v_2 \quad \Gamma', f=v_1, x=v_2 \vdash e_f \Downarrow r}{\Gamma \vdash \text{App } e_1 e_2 \Downarrow r}$$

## 3 Advanced Tasks

### 3.1 Task 2: Partial Primops

In the base part of the assignment, you are allowed to assume that all primitive operations (and the constructor `Cons`) are fully saturated with arguments. In this task you are to implement *partial* application of primitive operations (and `Cons`), which removes this assumption. For example:

```

main :: Int
  = let inc :: (Int -> Int)
      = recfun inc :: (Int -> Int) = (+) 1;
      in inc 2;  -- returns 3

```

Note that the expression `(+) 1` partially applies the primop `Plus` to 1, returning a *function* from `Int` to `Int`.

You will need to develop a suitable dynamic semantics for such expressions and implement it in your evaluator. The parser and type checker are already capable of dealing with expressions of this form.

### 3.2 Task 3: *n*-ary functions

In this task you are to implement *n*-ary functions. In other words, you should modify the interpreter to handle bindings of functions of more than 1 argument.

```

main :: Bool
  = let eq :: (Int -> Int -> Bool)
      = recfun eq :: (Int -> Int -> Bool) x y = x == y;
      in eq 3 4;

```

We haven't discussed the semantics of such functions in the lectures so you will need to work out a reasonable dynamic semantics for *n*-ary functions on your own, based on the semantics for unary functions. The parser and type checker are once again already capable of handling expressions of this form, so the only extension necessary is in the evaluator component.

Hint: Is the following example semantically different to the previous?

```

main :: Bool
  = let eq :: (Int -> Int -> Bool)
      = recfun eq :: (Int -> Int -> Bool) x =
          recfun eq2 :: (Int -> Bool) y = x == y;
      in eq 3 4;

```

### 3.3 Task 4: Multiple bindings in `let`

In the base part of the assignment, we specify that `let` expressions contain only one binding. In this task, you are to extend the interpreter so that `let` expressions with multiple bindings, like:

```

main :: Int
  = let a :: Int = 3;
      b :: Int = 2;
      in a + b;

```

are evaluated the same way as multiple nested `let` expressions:

```

main :: Int
  = let a :: Int = 3;
      in let b :: Int = 2;
          in a + b;

```

Once again the only place where extensions need to be made are in the evaluator, as the type checker and parser are already capable of handling multiple `let` bindings.



### 3.4 Task 5: `let` bindings declare functions

In this task you are to extend the `let` construct further so that `let` bindings can take parameters — defining *non-recursive* functions. This makes programming in MinHs much less verbose, as `recfun` is only necessary for defining recursive functions. For example:

```
main :: Int
  = let y :: Int = 3;
      in let f :: (Int -> Int) x = x + 1;
          in f y;  -- returns 4
```

Note that these bindings are *non-recursive*, so `let x = x` is a scope error, as the `x` in the binding is not in scope.

### 3.5 Task 6: Mutually recursive bindings

Currently bindings must be specified in dependency order. However, in Haskell, the order of declarations is irrelevant, which allows *mutually recursive* bindings. Implement Haskell-style mutually recursive bindings, like so:

```
main :: Int
  = letrec a :: Int = b;
           b :: Int = c;
           c :: Int = 7;
      in c + a;
```

Syntax for `letrec` bindings is already defined, typechecked, and parsed by the provided code. To implement this part, you simply need to implement the evaluator portion.

## 4 Testing

Your assignments will be tested *very* rigorously. You are encouraged to test yourself. `minhs` comes with a regress tester script, and you should add your own tests to this. Simply add test programs names `prgname.mhs` and a corresponding file with the expected result `prgname.out` anywhere in the `tests` subdirectory, and the testscript will find it and run it.

The tests that come with this assignment tarball cover the *base part* (the first 60%) of the assignment only. You are responsible for testing the other parts adequately.

## 5 Building `minhs`

`minhs` (the compiler/interpreter) is written in Haskell, and requires GHC 7.4 or higher, and the `cabal` build tool included in the Haskell Platform, or alternatively the `stack` tool.

## 5.1 Building with cabal

To install the necessary libraries for compiling MinHS, please type (assuming GHC and cabal are in your PATH, and you are connected to the Internet):

```
$ cd /path/to/my/assignment01
$ cabal update
$ cabal install --only-dependencies
```

In addition to the `base` and `containers` libraries which come with GHC, and the `parsec` library which comes with the Haskell platform, MinHS requires two utility libraries (`optparse-applicative` and `ansi-wl-pprint`), which will be fetched by the above command and installed into your system's Haskell platform.

Assuming all libraries are available, MinHS can be built with:

- `cabal configure` to set up the build environment
- `cabal build` to build the compiler
- `./dist/build/minhs-1/minhs-1 --help` will help you find any useful debugging options.

To run the interpreter:

```
$ ./dist/build/minhs-1/minhs-1 foo.mhs
```

You may wish to experiment with some of the debugging options to see, for example, how your program is parsed, and what abstract syntax is generated.

To get, for example, the parser output for `file.mhs`, type

```
./dist/build/minhs-1/minhs-1 --dump parser-raw file.mhs
```

To run the test driver, a short shell script is provided. For usage information, type:

```
$ ./run-tests.sh --help
```

## 5.2 Building with stack

You should be able to build the compiler by simply invoking:

```
$ stack build
```

To see the debugging options, run (after building):

```
$ stack exec minhs-1
```

To get, for example, the parser output for a `file.mhs`, type

```
stack exec -- minhs-1 --dump parser-raw file.mhs
```

To run the compiler with a particular file, run:

```
$ stack exec minhs-1 foo.mhs
```

And to run all of our tests, type:

```
$ ./run_tests_stack.sh
```

## 6 Late Penalty

Unless otherwise stated if you wish to submit an assignment late, you may do so, but a late penalty reducing the maximum available mark applies to every late assignment. The maximum available mark is reduced by 10% if the assignment is one day late, by 25% if it is 2 days late and by 50% if it is 3 days late. Assignments that are late 4 days or more will be awarded zero marks. So if your assignment is worth 88% and you submit it one day late you still get 88%, but if you submit it two days late you get 75%, three days late 50%, and four days late zero.

Assignment extensions are only awarded for serious and unforeseeable events. Therefore aim to complete your assignments well before the due date in case of last minute illness, and make regular backups of your work.

## 7 Plagiarism

This assignment is an individual assignment. All work submitted for assessment must be entirely your own work. We regard unacknowledged copying of material, in whole or part, as an extremely serious offence.

If you haven't done so yet, please read the plagiarism policy of the university.

In this course submission plagiarism includes any work derived from another person, or solely or jointly written by and or with someone else, without clear and explicit acknowledgement. Note this includes including unreferenced work from books, the internet, etc.

Do not provide or show your assessable work to any other person. If you knowingly provide or show your assessment work to another person for any reason, and work derived from it is subsequently submitted you will be penalized, even if the work was submitted without your knowledge or consent. This will apply even if your work is submitted by a third party unknown to you. You should keep your work private until submissions have closed.

If you are unsure about whether certain activities would constitute plagiarism ask us before engaging in them!

## References

- [1] *Report on the Programming Language Haskell 98*, eds. Simon Peyton Jones, John Hughes, (1999) <http://www.haskell.org/onlinereport/>
- [2] Robert Harper, *Programming Languages: Theory and Practice*, (Draft of Jan 2003), <http://www-2.cs.cmu.edu/~rwh/plbook/>.
- [3] *The Implementation of Functional Programming Languages*, Simon Peyton Jones, published by Prentice Hall, 1987. Full text online (as jpg page images).
- [4] Simon Peyton-Jones, *Implementing Functional Languages : a tutorial*, 2000.

## A Lexical Structure

The lexical structure of MinHS is an small subset of Haskell98. See section 2.2 of the Haskell98 report [1]. The lexical conventions are implemented by the Parsec parser library, which we use for our Parser implementation.

## B Concrete syntax

The concrete syntax is based firstly on Haskell. It provides the usual arithmetic and boolean primitive operations (most of the Int-type primitive operations of GHC). It has conventional `let` bindings. At the outermost scope, the `let` is optional. As a result, multiple outer-level bindings are treated as nested `let` bindings down the page. It is required that a distinguished `main` function, of atomic type, exist. There is an `if-then-else` conditional expression. The primitive types of MinHS are `Int`, `Bool` and `[Int]`. MinHS also implements, at least partially, a number of extensions to MinML: inline comments,  $n$ -ary functions, infix notation, more primitive numerical operations and a non-mutually recursive, simultaneous `let` declaration (treated as a nested-`let`). Function values may be specified with `recfun`.

The concrete syntax is described and implemented in the `Parser.hs` module, a grammar specified using the Parser combinator library Parsec.

Features of Haskell we do not provide:

- No nested comments
- No layout rule. Thus, semi-colons are required to terminate certain expressions. Consult the grammar.

## C Abstract syntax

The (first-order) abstract syntax is based closely on the MinHs syntax introduced in the lectures. It is implemented in the file `Syntax.hs`. Extensions to the MinHs abstract syntax take their cue from the Haskell kernel language. Presented below is the abstract syntax, with smatterings of concrete syntax for clarity.

## D Static semantics

The static semantics are based on those of the lecture, and of and MinML, from Bob Harper's book. They are implemented by the module `TypeChecker.hs`.

### D.1 $n$ -ary functions

Functions may be declared to take more than 1 argument at a time.

## E Environments

*Environments* are required by typechecker and possibly by the interpreter. The type-checker needs to map variables to types, and the interpreter might need to map variables to functions or values (like a heap). This latter structure is used to provide a fast alternative to substitution.

Types	$\tau$	$\rightarrow$	$\text{Int} \mid \text{Bool} \mid \tau \rightarrow \tau$
Literals	$n$	$\rightarrow$	$\dots \mid 0 \mid 1 \mid 2 \mid \dots$
	$b$	$\rightarrow$	$\text{True} \mid \text{False}$
Primops	$o$	$\rightarrow$	$+ \mid - \mid * \mid / \mid$ $> \mid >= \mid == \mid /= \mid < \mid <=$
Expressions	$exp$	$\rightarrow$	$\text{Var } x$ $\mid \text{Lit } n$ $\mid \text{Con } b$ $\mid \text{Apply } e_1 e_2$ $\mid \text{Let } decl \ exp$ $\mid \text{Recfun } decl$ $\mid \text{If } exp \ exp_1 \ exp_2$
Decl	$decl$	$\rightarrow$	$\text{Fun } f \ \tau \ [arg] \ e$ $\mid \text{Val } v \ \tau \ e$

Figure 1: The expression abstract syntax of MinHS

We provide a general environment module, keyed by identifiers, in `Env.hs`.

Environments are generally simpler in MinHS than in real Haskell. We still need to bind variables to partially evaluated functions, however.

## F Dynamic semantics

The dynamic semantics are described in this document, the lectures, and resemble that of Harper [2]. Implemented in the module `Evaluator.hs`.

### F.1 Interpreter

The interpreter is the backend that runs by default. It should implement the dynamic semantics of MinHS.

## G Interfaces

The basic types are found in `Syntax.hs`, which contains definitions for the structure of terms, types, primOps, and others.

### Printing

Most structures in MinHS need to be printed at some point. The easiest way to do this is to make that type an instance of class `Pretty`. See `Pretty.hs` for an example.

## Testing

`./run-tests.sh`

Check directories may have an optional 'Flag' file, containing flags you wish to pass to minhs in that directory, or the magic flag, 'expect-fail', which inverts the sense in which success is defined by the driver.