

UNIVERSITÀ DEGLI STUDI DI PARMA
FACOLTÀ DI INGEGNERIA

CORSO DI LAUREA IN INGEGNERIA INFORMATICA

L11 - Image Segmentation

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K-Means Clustering

- Initialization:
 - choose k cluster centers
- Repeat:
 - **assignment step:**
 - For every point find its closest center
 - **update step:**
 - Update every center as the mean of its points
- Until:
 - The maximum number of iterations is reached, or
 - No changes during the assignment step, or
 - The average distortion per point drops very little

[Lloyd, 1957]

K-Means Clustering

- **Input:** N examples $\{\mathbf{x}_1, \dots, \mathbf{x}_N\}$ ($\mathbf{x}_n \in \mathbb{R}^D$); the number of partitions K
- **Initialize:** K cluster centers μ_1, \dots, μ_K . Several initialization options:
 - Randomly initialized anywhere in \mathbb{R}^D
 - Choose any K examples as the cluster centers
- **Iterate:**
 - Assign each of example \mathbf{x}_n to its closest cluster center

$$\mathcal{C}_k = \{n : k = \arg \min_k ||\mathbf{x}_n - \mu_k||^2\}$$

(\mathcal{C}_k is the set of examples closest to μ_k)

- **Recompute** the new cluster centers μ_k (mean/centroid of the set \mathcal{C}_k)

$$\mu_k = \frac{1}{|\mathcal{C}_k|} \sum_{n \in \mathcal{C}_k} \mathbf{x}_n$$

- **Repeat** while not converged

K-Means Clustering

The K -means objective function

- Let μ_1, \dots, μ_K be the K cluster centroids (means)
- Let $r_{nk} \in \{0, 1\}$ be **indicator** denoting whether point \mathbf{x}_n belongs to cluster k
- K -means objective minimizes the total **distortion** (sum of distances of points from their cluster centers)

$$J(\mu, r) = \sum_{n=1}^N \sum_{k=1}^K r_{nk} \|\mathbf{x}_n - \mu_k\|^2$$

- Note: **Exact optimization** of the K -means objective is **NP-hard**
- The K -means algorithm is a **heuristic** that converges to a local optimum [1]

[1] [L. Bottou and Y. Bengio. Convergence properties of the kmeans algorithm. NIPS, 1995.](#)

Esercizio #1

- Implementare K-Means utilizzando come feature il **tono di grigio** dell'immagine [0-255]
- Scelta iniziale dei centri:
 - Equidistribuiti su 0-255
 - Random su 0-255

Esercizio #2

- Scelta dei centri in base all'istogramma:
 - Calcolare l'istogramma dei toni di grigio
 - Prendere un centro cluster per ogni **massimo locale** dell'istogramma

Esercizio #3

- Implementare K-Means utilizzando come feature i **3 canali di colore RGB**
 - Modificare opportunamente funzione distanza e costo

Esercizio #4

- Implementare K-Means utilizzando come feature il **tono di grigio** più la posizione riga-colonna:
 - $(L, u, v,) \rightarrow [0 - 255][0 - (\text{rows}-1)][0 - (\text{cols}-1)]$
 - Modificare opportunamente le funzioni distanza e costo

Supapixel

SLIC Superpixels:

- Feature space → **intensity + position**
 - L.a.b. color space
 - *limited region* (window $2*S$)

$$[l_k, a_k, b_k, x_k, y_k]$$

- Distance metric:

$$d_c = \sqrt{(l_j - l_i)^2 + (a_j - a_i)^2 + (b_j - b_i)^2}$$

$$d_s = \sqrt{(x_j - x_i)^2 + (y_j - y_i)^2}$$

$$D' = \sqrt{\left(\frac{d_c}{N_c}\right)^2 + \left(\frac{d_s}{N_s}\right)^2}$$

- Initialization:
 - Spatial grid (grid step = S)
- Iterate over centers and not points

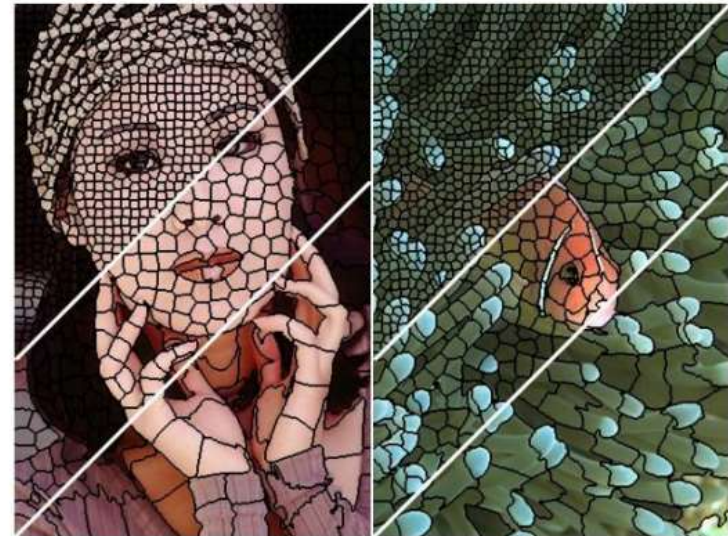


Fig. 1: Images segmented using SLIC into superpixels of size 64, 256, and 1024 pixels (approximately).

