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3.49

$$\sum_{j=1}^N (X_j - 1)^2 = \sum_{j=1}^N X_j^2 - 2 \left(\sum_{j=1}^N X_j \right) + N$$

To show the equality of the equation above, we can use the **inductive method**.

First, let's get the inductive form of our equation.

$$\sum_{j=1}^N (X_j - 1)^2$$

inductive method

$$\begin{aligned} \sum_{j=1}^{N+1} (X_j - 1)^2 &= \sum_{j=1}^N (X_j - 1)^2 + (X_{N+1} - 1)^2 \\ &= \sum_{j=1}^N X_j^2 - 2 \left(\sum_{j=1}^N X_j \right) + N + (X_{N+1} - 1)^2 \end{aligned}$$

Now, let's get the inductive form our right hand equation.

$$\sum_{j=1}^N X_j^2 - 2 \left(\sum_{j=1}^N X_j \right) + N$$

inductive method

$$\begin{aligned} &= \sum_{j=1}^N X_j^2 - 2 \left(\sum_{j=1}^N X_j \right) + N + 1 \\ &= \sum_{j=1}^N X_j^2 - 2 \left(\sum_{j=1}^N X_j \right) + N + (X_{N+1}^2 - 2X_{N+1} + (X_{N+1} - 1)^2) \\ &= \sum_{j=1}^N X_j^2 - 2 \left(\sum_{j=1}^N X_j \right) + N + (X_{N+1} - 1)^2 \end{aligned}$$

We have then shown that the equation

$$\sum_{j=1}^N (X_j^2 - 1)^2 = X_j^2 - 2X_j + N$$

Is indeed equal for its inductive form. QED

3.50 (a-g)

$$\begin{aligned}
 a.) \sum UV &= \sum_{n=1}^3 (U_n V_n) \\
 &= (3 \cdot (-4)) + (-2 \cdot (-1)) + (5 \cdot 6) \\
 &= -12 + 2 + 30 \\
 &= \boxed{20}
 \end{aligned}$$

a.) 20

$$\begin{aligned}
 b.) \sum (U+3)(V-4) &= \sum_{n=1}^3 (U_n + 3)(V_n - 4) \\
 &= (3+3)(-4-4) + (-2+3)(-1-4) + (5+3)(6-4) \\
 &= (6)(-8) + (1)(-5) + (8)(2) \\
 &= -48 + (-5) + 16 \\
 &= \boxed{-37}
 \end{aligned}$$

b.) -37

$$\begin{aligned}
 c.) \sum V^2 &= \sum_{n=1}^3 (V_n)^2 \\
 &= (-4)^2 + (-1)^2 + (6)^2 \\
 &= 16 + 1 + 36 \\
 &= \boxed{53}
 \end{aligned}$$

a.) 53

$$\begin{aligned}
 d.) (\sum U)(\sum V)^2 &= \sum_{n=1}^3 U_n \cdot \left(\sum_{n=1}^3 V_n \right)^2 \\
 &= \left[\sum_{n=1}^3 U_n = (3 + (-2) + 5) \right] \left[\sum_{n=1}^3 V^2 = (-4 + -1 + 6)^2 \right] \\
 &= (6)(1)^2 \\
 &= (6)(1) \\
 &= \boxed{6}
 \end{aligned}$$

d.) 6

$$\begin{aligned}
 e.) \quad & \sum_{n=1}^3 uv^2 \\
 &= 3(-4)^2 + (-2)(-1)^2 + (5)(6)^2 \\
 &= (3)(16) + (-2)(1) + (5)(36) \\
 &= 48 + 2 + 180 \\
 &= 230
 \end{aligned}$$

e.) 230

$$\begin{aligned}
 f.) \quad & \sum_{n=1}^3 (u^2 - 2(v^2) + 2) \\
 &= ((3)^2 - 2(4)^2 + 2) + ((-2)^2 - 2(-1)^2 + 2) + ((5)^2 - 2(6)^2 + 2) \\
 &= ((9) - 2(16) + 2) + (4 - 2(1) + 2) + (25 - 2(36) + 2) \\
 &= 62
 \end{aligned}$$

f.) 62

$$\begin{aligned}
 g.) \quad & \sum_{n=1}^3 \left(\frac{u}{v} \right) \\
 &= \frac{3}{-4} + \frac{-2}{-1} + \frac{5}{6} \\
 &= \frac{25}{12}
 \end{aligned}$$

g.) $\frac{25}{12}$

3.90 a

In [1]:

```
a_SET= [3, 5, 8, 3, 7, 2]
a_SET

a_SET_length= len(a_SET)
a_SET_length

prod_a_SET=1

for i in a_SET:
    prod_a_SET *= i

print("Product of set:", prod_a_SET)
Geomean_a_SET= ((prod_a_SET)**(1/a_SET_length))
Geomean_a_SET
print("Geometric Mean:", Geomean_a_SET)
```

Product of set: 5040
Geometric Mean: 4.140680833465288

In [2]:

```
sum_a_SET=0

for i in a_SET:
    sum_a_SET += i

Arithmean_a_SET= (((1/a_SET_length)*(sum_a_SET)))
print("Arithmetic Mean:", Arithmean_a_SET)
```

Arithmetic Mean: 4.666666666666666

3.90 b

In [3]:

```
b_SET= [28.5, 73.6, 47.2, 31.5, 64.8]
b_SET

b_SET_length= len(b_SET)
b_SET_length

prod_b_SET=1

for i in b_SET:
    prod_b_SET *= i

print("Product of set:", prod_b_SET)
Geomean_b_SET= ((prod_b_SET)**(1/b_SET_length))
print("Geometric Mean:", Geomean_b_SET)
```

Product of set: 202092516.864
Geometric Mean: 45.82579906814073

In [4]:

```
sum_b_SET=0

for i in b_SET:
    sum_b_SET += i

Arithmean_b_SET= (((1/b_SET_length)*(sum_b_SET)))

print("Arithmetic Mean:", Arithmean_b_SET)
```

Arithmetic Mean: 49.120000000000005