

# PROGRAMACIÓN USANDO INVARIANTES DE CICLO

30 de mayo de 2018

# EJERCICIO 1

```
proc factorial (in  $n: \mathbb{Z}$ , out  $res: \mathbb{Z}$ ) {  
  Pre  $\{n \geq 2\}$   
  Post  $\{res = \prod_{i=2}^n i\}$   
}
```

$$l_1 \equiv 1 \leq i \leq n \wedge_L res = \prod_{j=2}^i j$$

$$l_2 \equiv 2 \leq i \leq n \wedge_L res = \prod_{j=2}^i j$$

$$l_3 \equiv 2 \leq i \leq n + 1 \wedge_L res = \prod_{j=i}^n j$$

## EJERCICIO 2

```
proc swap (inout I: seq( $\mathbb{Z}$ )) {  
  Pre { $|I| \bmod 2 = 0 \wedge I = L_0$ }  
  Post { $|I| = |L_0| \wedge_L (\forall i : \mathbb{Z})( (0 \leq i < |I| \wedge i \bmod 2 = 0) \rightarrow_L$   
     $I[i] = L_0[i + 1] ) \wedge (\forall i : \mathbb{Z})( (0 \leq i < |I| \wedge i \bmod 2 =$   
     $1) \rightarrow_L I[i] = L_0[i - 1] )$ }  
}
```

$$\begin{aligned} I \equiv & |I| = |L_0| \wedge -1 \leq i \leq |I| - 1 \wedge_L i \bmod 2 = 1 \\ & \wedge (\forall j : \mathbb{Z})( 0 \leq j \leq i \rightarrow_L I[j] = L_0[j] ) \\ & \wedge (\forall j : \mathbb{Z})( (i < j < |I| \wedge j \bmod 2 = 0) \rightarrow_L I[i] = L_0[i + 1] ) \\ & \wedge (\forall j : \mathbb{Z})( (i < j < |I| \wedge j \bmod 2 = 1) \rightarrow_L I[j] = L_0[j - 1] ) \end{aligned}$$