

Dafny



Boogie translation

Dafny:

```
method Main() {  
  TestAdd(3, 180);  
  TestAdd(3, -180);  
  TestAdd(0, 1);  
  [...]
```

Boogie:

```
implementation [...].Main()  
returns ($_reverifyPost: bool) {  
  var $_Frame:  
    <beta>[ref,Field beta]bool;  
  var x##i (0..8): int;  
  x##0 := LitInt(3);  
  y##0 := LitInt(180);  
  call Intra[...]TestAdd(x##0, y##0);  
  [...]
```

Boogie translation

method Add(x: int, y: int) returns (r:
int)

ensures r == x+y;

procedure Impl[...]AddAdd(
x#0: int, y#0: int)

r#0: int, y#0: int)

returns (
r#0: int, \$_reverifyPost: bool);

Boogie translation

method Add [...]

{

 r := x;

 if (y < 0) {

 var n := y;

 while (n != 0)

 invariant r == x+y-n && 0 <= -n;

 {

 r := r - 1;

 n := n + 1;

 }

 } else [...]

implementation Impl[...]Add[...] {

 r#0 := x#0;

 if (y#0 < 0)

 {

 n#0_0 := y#0;

 \$PreLoopHeap\$loop#0_0 := \$Heap;

 \$decr_init\$loop#0_00 := (if n#0_0 <= LitInt
 (0) then 0 - n#0_0 else n#0_0 - 0);

 havoc \$w\$loop#0_0;

 while (true)

Boogie translation

```
method Add [...]
```

```
{
```

```
  r := x;
```

```
  if (y < 0) {
```

```
    var n := y;
```

```
    while (n != 0)
```

```
      invariant r == x+y-n && 0 <= -n;
```

```
      {
```

```
        r := r - 1;
```

```
        n := n + 1;
```

```
      }
```

```
  } else [...]
```

```
while (true)
```

```
  free invariant $w$loop#0_0 ==> r#0 == x#0  
  + y#0 - n#0_0 ==> true;
```

```
  invariant $w$loop#0_0 ==> r#0 == x#0 +  
  y#0 - n#0_0;
```

```
  invariant $w$loop#0_0 ==> LitInt(0) <= 0 -  
  n#0_0;
```

```
  free invariant (if n#0_0 <= LitInt(0) then 0 -  
  n#0_0 else n#0_0 - 0) <= $decr_init$loop#0_00
```

```
  free invariant [heap related];
```

Boogie translation

method Add [...]

```
{  
  r := x;  
  if (y < 0) {  
    var n := y;  
    while (n != 0)  
      invariant r == x+y-n && 0 <= -n;  
    {  
      r := r - 1;  
      n := n + 1;  
    }  
  } else [...]
```

```
if (!w$loop#0_0) { [...] assume false; }  
if (n#0_0 == 0) { break; }  
$decr$loop#0_00 := (if n#0_0 <= LitInt(0) then 0  
- n#0_0 else n#0_0 - 0);  
r#0 := r#0 - 1;  
n#0_0 := n#0_0 + 1;  
assert 0 <= $decr$loop#0_00 || (if n#0_0 <=  
LitInt(0) then 0 - n#0_0 else n#0_0 - 0) ==  
$decr$loop#0_00;  
assert (if n#0_0 <= LitInt(0) then 0 - n#0_0 else  
n#0_0 - 0) < $decr$loop#0_00;
```

Control Flow

```
implementation Impl[...]Add[...] {
```

```
  r#0 := x#0;
```

```
  if (y#0 < 0)
```

```
    {
```

```
      n#0_0 := y#0;
```

```
      $PreLoopHeap$loop#0_0 := $Heap;
```

```
      $decr_init$loop#0_00 := (if n#0_0 <= LitInt(0) then 0 - n#0_0 else n#0_0 - 0);
```

```
      havoc $w$loop#0_0;
```

```
      while (true)
```

```
implementation Impl[...]Add[...] {
```

```
  anon0:
```

```
    r#0 := x#0;
```

```
    goto anon23_Then, anon23_Else;
```

```
  anon23_Then:
```

```
    n#0_0 := y#0;
```

```
    $PreLoopHeap$loop#0_0 := $Heap;
```

```
    $decr_init$loop#0_00 := (if [...]);
```

```
    havoc $w$loop#0_0;
```

```
    goto anon24_LoopHead;
```

Control Flow

while (true)

free invariant $\$w\$loop\#0_0 \implies r\#0 == x\#0 + y\#0 - n\#0_0 \implies \text{true};$

invariant $\$w\$loop\#0_0 \implies r\#0 == x\#0 + y\#0 - n\#0_0;$
invariant $\$w\$loop\#0_0 \implies \text{LitInt}(0) \leq 0 - n\#0_0;$

free invariant (if $n\#0_0 \leq \text{LitInt}(0)$ then $0 - n\#0_0$ else $n\#0_0 - 0$) $\leq \$decr_init\$loop\#0_00$
free invariant [heap related];

anon24_LoopHead:

assume $\$w\$loop\#0_0 \implies \text{rasdf}\#0 == x\#0 + y\#0 - n\#0_0 \implies \text{true};$

assert $\$w\$loop\#0_0 \implies \text{rasdf}\#0 == x\#0 + y\#0 - n\#0_0;$
assert $\$w\$loop\#0_0 \implies \text{LitInt}(0) \leq 0 - n\#0_0;$

assume (if $n\#0_0 \leq \text{LitInt}(0)$ then $0 - n\#0_0$ else $n\#0_0 - 0$) $\leq \$decr_init\$loop\#0_00$
assume [heap related];

goto anon24_LoopDone, anon24_LoopBody;

Control Flow

```
if (!$w$loop#0_0)
```

```
{ [...] assume false; }
```

```
if (n#0_0 == 0) { break; }
```

```
$decr$loop#0_00 := (if n#0_0 <= LitInt(0) then 0 -  
n#0_0 else n#0_0 - 0);
```

```
r#0 := r#0 - 1;
```

```
n#0_0 := n#0_0 + 1;
```

```
assert 0 <= $decr$loop#0_00 || (if n#0_0 <= LitInt  
(0) then 0 - n#0_0 else n#0_0 - 0) ==  
$decr$loop#0_00;
```

```
assert (if n#0_0 <= LitInt(0) then 0 - n#0_0 else  
n#0_0 - 0) < $decr$loop#0_00;
```

```
anon24_LoopBody:
```

```
assume true;
```

```
goto anon25_Then, anon25_Else;
```

```
anon25_Then:
```

```
assume {:partition} !$w$loop#0_0;
```

```
goto [...] (assume false);
```

```
anon25_Else:
```

```
assume {:partition} $w$loop#0_0;
```

```
goto anon28_Then, anon28_Else;
```

```
anon28_Then:
```

```
assume {:partition} n#0_0 == 0;
```

```
return;
```

Control Flow

```
if (!$w$loop#0_0) { [...] assume false; }
```

```
if (n#0_0 == 0) { break; }
```

```
$decr$loop#0_00 := (if n#0_0 <= LitInt(0) then 0 -  
n#0_0 else n#0_0 - 0);
```

```
r#0 := r#0 - 1;
```

```
n#0_0 := n#0_0 + 1;
```

```
assert 0 <= $decr$loop#0_00 || (if n#0_0 <=  
LitInt(0) then 0 - n#0_0 else n#0_0 - 0) ==  
$decr$loop#0_00;
```

```
assert (if n#0_0 <= LitInt(0) then 0 - n#0_0 else  
n#0_0 - 0) < $decr$loop#0_00;
```

```
anon28_Else:
```

```
  assume {:partition} n#0_0 != 0;
```

```
  goto anon11;
```

```
anon11:
```

```
  $decr$loop#0_00 := (if n#0_0 <= LitInt(0) then 0  
- n#0_0 else n#0_0 - 0);
```

```
[...]
```

```
goto anon24_LoopHead;
```

It's a kind of maaagic

```
(  
let ((anon28_Else_correct (=> (! (and %lbl%+11822 true) :lblpos +11822) (=> (and (and (not (= |n#0_0@0| 0)) (= |$decr$loop#0_00@1| (ite (<= |n#0_0@0| (LitInt 0)) (- 0 |n#0_0@0|) (- |n#0_0@0| 0)))) (and (= |rasdf#0@3| (- |rasdf#0@2| 1)) (= |n#0_0@1| (+ |n#0_0@0| 1)))) (and (! (or %lbl%@28679 (or (<= 0 |$decr$loop#0_00@1|) (= (ite (<= |n#0_0@1| (LitInt 0)) (- 0 |n#0_0@1|) (- |n#0_0@1| 0)) |$decr$loop#0_00@1|))) :lblneg @28679) (=> (or (<= 0 |$decr$loop#0_00@1|) (= (ite (<= |n#0_0@1| (LitInt 0)) (- 0 |n#0_0@1|) (- |n#0_0@1| 0)) |$decr$loop#0_00@1|))) (and (! (or %lbl%@28708 (< (ite (<= |n#0_0@1| (LitInt 0)) (- 0 |n#0_0@1|) (- |n#0_0@1| 0)) |$decr$loop#0_00@1|))) :lblneg @28708) (=> (< (ite (<= |n#0_0@1| (LitInt 0)) (- 0 |n#0_0@1|) (- |n#0_0@1| 0)) |$decr$loop#0_00@1|) (=> (=> (= |rasdf#0@3| (- (+ |x#0| |y#0|) |n#0_0@1|)) true) (and (! (or %lbl%@28746 (=> |$w$loop#0_0@0| (= |rasdf#0@3| (- (+ |x#0| |y#0|) |n#0_0@1|)))) :lblneg @28746) (=> (=> |$w$loop#0_0@0| (= |rasdf#0@3| (- (+ |x#0| |y#0|) |n#0_0@1|))) (! (or %lbl%@28761 (=> |$w$loop#0_0@0| (<= (LitInt 0) (- 0 |n#0_0@1|)))) :lblneg @28761))))))))))  
+50lines  
)
```

Heap

```
class C_A {  
  var X : int;  
  method Set(Y : int)  
    modifies this;  
    ensures X == Y;  
  {  
    X := Y;  
  }  
}
```

```
method Sum(X: C_A, Y: C_A) returns (sum: C_A)  
  requires X != null;  
  requires Y != null;  
  modifies X;  
  ensures fresh(sum);  
  ensures sum.X == old(X.X) + Y.X;  
  ensures X.X == Y.X;  
  {  
    sum := new C_A.Set(X.X + Y.X);  
    X.Set(Y.X);  
  }
```

Heap

```
method Sum(X: C_A, Y: C_A)
```

```
    returns (sum: C_A)
requires X != null;
requires Y != null;
modifies X;
ensures fresh(sum);
ensures sum.X == old(X.X) + Y.X;
ensures X.X == Y.X;
{
    sum := new C_A.Set(X.X + Y.X);
    X.Set(Y.X);
}
```

```
procedure Impl$$_module.__default.Sum(
    X#0: ref
    where
        $Is(X#0, Tclass._module.C__A()) &&
        $IsAlloc(
            X#0, Tclass._module.C__A(), $Heap),
    Y#0: ref
    where
        $Is(Y#0, Tclass._module.C__A()) &&
        $IsAlloc(
            Y#0, Tclass._module.C__A(), $Heap))
```

Heap

method Sum(X: C_A, Y: C_A)

returns (sum: C_A)

requires X != null;

requires Y != null;

modifies X;

ensures fresh(sum);

ensures sum.X == old(X.X) + Y.X;

ensures X.X == Y.X;

{

sum := new C_A.Set(X.X + Y.X);

X.Set(Y.X);

}

returns (

sum#0: ref

where

\$!s(sum#0, Tclass._module.C__A()) &&

\$!sAlloc(

sum#0, Tclass._module.C__A(), \$Heap),

\$_reverifyPost: bool);

Heap

method Sum(X: C_A, Y: C_A)
 returns (sum: C_A)

requires X != null;
requires Y != null;

modifies X;

ensures fresh(sum);
ensures sum.X == old(X.X) + Y.X;
ensures X.X == Y.X;
{
 sum := new C_A.Set(X.X + Y.X);
 X.Set(Y.X);
}

// user-defined preconditions

requires X#0 != null;

requires Y#0 != null;

modifies \$Heap, \$Tick;

// user-defined postconditions

ensures sum#0 != null && !read(old(\$Heap),
sum#0, alloc);

Heap

method Sum(X: C_A, Y: C_A)

returns (sum: C_A)

requires X != null;

requires Y != null;

modifies X;

ensures fresh(sum);

ensures sum.X == old(X.X) + Y.X;

ensures X.X == Y.X;

{

sum := new C_A.Set(X.X + Y.X);

X.Set(Y.X);

}

ensures

read(\$Heap, sum#0, _module.C__A.X)

== read(old(\$Heap), X#0, _module.C__A.X)

+ read(\$Heap, Y#0, _module.C__A.X);

ensures

read(\$Heap, X#0, _module.C__A.X) ==

read(\$Heap, Y#0, _module.C__A.X);

Heap

```
method Sum(X: C_A, Y: C_A)
  returns (sum: C_A)
  requires X != null;
  requires Y != null;
  modifies X;
  ensures fresh(sum);
  ensures sum.X == old(X.X) + Y.X;
  ensures X.X == Y.X;
{
  sum := new C_A.Set(X.X + Y.X);
  X.Set(Y.X);
}
```

```
// frame condition
  free ensures (forall<alpha> $o: ref, $f: Field
alpha ::
  { read($Heap, $o, $f) }
  $o != null && read(old($Heap), $o, alloc)
    ==> read($Heap, $o, $f) == read(old
($Heap), $o, $f)
  || $o == X#0);
```

Heap

method Sum(X: C_A, Y: C_A)

returns (sum: C_A)

requires X != null;

requires Y != null;

modifies X;

ensures fresh(sum);

ensures sum.X == old(X.X) + Y.X;

ensures X.X == Y.X;

{

sum := **new** C_A.Set(X.X + Y.X);

X.Set(Y.X);

}

implementation Impl\$\$_module.__default.Sum
(X#0: ref, Y#0: ref) returns (sum#0: ref,
\$_reverifyPost: bool)

{

var \$_Frame: <beta>[ref,Field beta]bool;

var \$nw: ref;

var Y##0: int;

var Y##1: int;

Heap

method Sum(X: C_A, Y: C_A) returns (sum: C_A)

requires X != null;

requires Y != null;

modifies X;

ensures fresh(sum);

ensures sum.X == old(X.X) + Y.X;

ensures X.X == Y.X;

{

sum := **new C_A**.Set(X.X + Y.X);

X.Set(Y.X);

}

\$_Frame := (lambda<alpha> \$o: ref, \$f: Field
alpha ::

\$o != null && read(\$Heap, \$o, alloc)

==> \$o == X#0);

\$_reverifyPost := false;

havoc \$nw;

assume

\$nw != null &&

!read(\$Heap, \$nw, alloc) &&

dtype(\$nw) == Tclass._module.C__A();

\$Heap := update(\$Heap, \$nw, alloc, true);

assume \$IsGoodHeap(\$Heap);

Heap

```
method Sum(X: C_A, Y: C_A) returns (sum: C_A)
requires X != null;
requires Y != null;
modifies X;
ensures fresh(sum);
ensures sum.X == old(X.X) + Y.X;
ensures X.X == Y.X;
{
  sum := new C_A.Set(X.X + Y.X);
  X.Set(Y.X);
}
```

Modifies Set <=
Modifies Sum



```
assert X#0 != null; assert Y#0 != null;
// TrCallStmt: Before ProcessCallStmt
```

```
Y##0 :=
  read($Heap, X#0, _module.C__A.X) +
  read($Heap, Y#0, _module.C__A.X);
```

```
// ProcessCallStmt: CheckSubrange
```

```
assert (forall<alpha> $o: ref, $f: Field alpha ::
  $o != null && read($Heap, $o, alloc) && $o ==
  $nw ==> $_Frame[$o, $f]);
```

```
// ProcessCallStmt: Make the call
call IntraModuleCall$_module.C__A.
  Set($nw, Y##0);
sum#0 := $nw;
```

Heap

```
method Sum(X: C_A, Y: C_A) returns (sum: C_A)
requires X != null;
requires Y != null;
modifies X;
ensures fresh(sum);
ensures sum.X == old(X.X) + Y.X;
ensures X.X == Y.X;
{
  sum := new C_A.Set(X.X + Y.X);
  X.Set(Y.X);
}
```

```
assert X#0 != null; assert Y#0 != null;
// TrCallStmt: Before ProcessCallStmt
Y##0 :=
  read($Heap, X#0, _module.C__A.X) +
  read($Heap, Y#0, _module.C__A.X);
// ProcessCallStmt: CheckSubrange
assert (forall<alpha> $o: ref, $f: Field alpha ::
  $o != null && read($Heap, $o, alloc) && $o ==
  $nw ==> $_Frame[$o, $f]);
// ProcessCallStmt: Make the call
```

call IntraModuleCall\$_module.C__A.
Set(\$nw, Y##0);

sum#0 := \$nw;

Set

sum :=

Heap

```
method Sum(X: C_A, Y: C_A) returns (sum: C_A)
requires X != null;
requires Y != null;
modifies X;
ensures fresh(sum);
ensures sum.X == old(X.X) + Y.X;
ensures X.X == Y.X;
{
  sum := new C_A.Set(X.X + Y.X);
  X.Set(Y.X);
}
```

```
assert X#0 != null; assert Y#0 != null;
    // ProcessCallStmt: CheckSubrange
Y##1 := read($Heap, Y#0, _module.C__A.X);
assert (forall<alpha> $o: ref, $f: Field alpha ::
  $o != null && read($Heap, $o, alloc) &&
  $o == X#0 ==> $_Frame[$o, $f];
    // ProcessCallStmt: Make the call
call IntraModuleCall$_module.C__A.
  Set(X#0, Y##1);
```

(40 lines +

```
($HeapSucc $Heap@1 $Heap@2))) (and (! (or %lbl%@24666 (and (not (= $nw@0 null)) (not (U_2_bool  
(MapType1Select $Heap@@@3 $nw@0 alloc)))))) :lblneg @24666) (=> (and (not (= $nw@0 null)) (not (U_2_bool  
(MapType1Select $Heap@@@3 $nw@0 alloc)))) (and (! (or %lbl%@24681 (= (U_2_int (MapType1Select $Heap@2  
$nw@0 _module.C__A.X)) (+ (U_2_int (MapType1Select $Heap@@@3 |X#0@@@2| _module.C__A.X)) (U_2_int  
(MapType1Select $Heap@2 |Y#0@@@1| _module.C__A.X)))))) :lblneg @24681) (=>
```

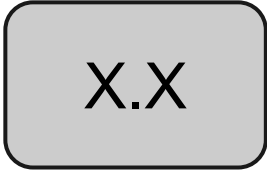
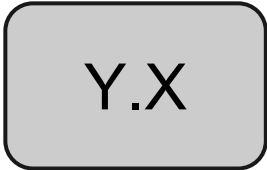
```
(= (U_2_int (MapType1Select $Heap@2 $nw@0 _module.C__A.X)) (+ (U_2_int (MapType1Select  
$Heap@@@3 |X#0@@@2| _module.C__A.X)) (U_2_int (MapType1Select $Heap@2 |Y#0@@@1|  
_module.C__A.X))))
```

```
(! (or %lbl%@24705 (= (U_2_int (MapType1Select $Heap@2 |X#0@@@2| _module.C__A.X)) (U_2_int  
(MapType1Select $Heap@2 |Y#0@@@1| _module.C__A.X)))) :lblneg @24705))))))))))))))))))))))))))
```

```
(let ((PreconditionGeneratedEntry_correct@@@2 (=> (! (and %lbl%+24092 true) :lblpos +24092) (=> ($IsGoodHeap  
$Heap@@@3) (=> (and ($Is |X#0@@@2| Tclass._module.C__A) ($IsAlloc |X#0@@@2| Tclass._module.C__A  
$Heap@@@3)) (=> (and (and (and ($Is |Y#0@@@1| Tclass._module.C__A) ($IsAlloc |Y#0@@@1| Tclass._module.C__A  
$Heap@@@3)) (and ($Is |sum#0@@@0| Tclass._module.C__A) ($IsAlloc |sum#0@@@0| Tclass._module.C__A  
$Heap@@@3))) (and (and (= 0 $ModuleContextHeight) (= 1 $FunctionContextHeight)) (and (not (= |X#0@@@2| null)) (not  
(= |Y#0@@@1| null)))))) anon0_correct@@@2)))))) PreconditionGeneratedEntry_correct@@@2))
```

```
(=  
  (U_2_int  
    (MapType1Select  
      $Heap@2 $nw@0 _module.C__A.X))
```

sum.X


```
(+  
  (U_2_int  
    (MapType1Select  X.X  
      $Heap@@@3 |X#0@@@2| _module.C__A.X))  
  (U_2_int  
    (MapType1Select  Y.X  
      $Heap@2 |Y#0@@@1| _module.C__A.X))))
```

Triggers

```
type Heap = <alpha>[ref,Field alpha]alpha;
```

```
axiom
```

```
  (forall<alpha>
```

```
    h: Heap, r: ref,
```

```
    f: Field alpha, x: alpha ::
```

```
  { update(h, r, f, x) }
```

```
  $IsGoodHeap(update(h, r, f, x))
```

```
    ==> $HeapSucc(h, update(h, r, f, x)));
```

Flags

```
dafny /print:boogie-output.bpl dafny-input.dfy
```

```
boogie
```

```
  /printInstrumented
```

```
  /print:boogie-output.bpl
```

```
  /prover-log:smt-output.txt
```

```
  boogie-input.dfy
```