STAT 203 PROBLEM SET 4

Due date: Thursday, March 5.

- (1) The O-rings in the booster rockets used in space launching play an important part in preventing rockets from exploding. Probabilities of O-ring failures are thought to be related to temperature. A detailed discussion of the background of the problem is found in the Flight of the Space Shuttle Challenger (pp. 33-35) in Chatterjee, Handcock, and Simonoff (1995). Each flight has six O-rings that could potentially be damaged in a particular flight. The data from 23 flights are given in the data file *Orings.txt*. For each flight, we have the number of O-rings damaged (out of 6) and the temperature of the launch.
 - (a) Fit a logistic regression connecting the probability of an O-ring failure with temperature. Interpret the coefficients.
 - (b) The data for Flight 18 that was launched when the launch temperature was 75 was thought to be problematic, and was deleted. Fit a logistic regression to the reduced data set, and interpret the coefficients.
 - (c) From the fitted model, find the probability of an O-ring failure when the temperature at launch was 31 degrees. This was the temperature forecast for the day of the launching of the fatal Challenger flight on Jan 20, 1986.
 - (d) Would you have advised the launching on that particular day?
- (2) Field-goal-kicking data for the entire American Football League (AFL) and National Football League (NFL) for the 1969 season are given in the data file NFL.txt. Let $\pi(X)$ denote the probability of kicking a field goal from a distance of X yards.
 - (a) For each of the leagues, fit the model

$$\pi(X) = \frac{e^{\beta_0 + \beta_1 X + \beta_2 X^2}}{1 + e^{\beta_0 + \beta_1 X + \beta_2 X^2}}.$$

(b) Let Z be an indicator variable representing the league, that is,

$$Z = \begin{cases} 1, & \text{for the AFL;} \\ 0, & \text{for the NFL.} \end{cases}$$

Fit a single model combining the data from both leagues by extending the model to include the indicator variable Z; that

is, fit

$$\pi(X,Z) = \frac{e^{\beta_0 + \beta_1 X + \beta_2 X^2 + \beta_3 Z}}{1 + e^{\beta_0 + \beta_1 X + \beta_2 X^2 + \beta_3 Z}}.$$

- (c) Does the quadratic term contribute significantly to the model?
- (d) Are the probabilities of scoring field goals from a given distance the same for each league?
- (3) A researcher in geriatrics designed a prospective study to investigate the effects of two interventions on the frequency of falls. One hundred subjects were randomly assigned to one of the two interventions: education only $(X_1 = 0)$ and education plus aerobic exercise training $(X_1 = 1)$. Subjects were at least 65 years of age and in reasonably good health. Three variables considered to be important as control variables were gender $(X_2 : 0 = \text{female}; 1 = \text{male})$, a balance index (X_3) , and a strength index (X_4) . The higher the balance index, the more stable is the subject; and the higher the strength index, the stronger the subject. Each subject kept a diary recording the number of falls (Y) during the six months of the study.
 - (a) Fit a Poisson regression model with the response function

$$\mu(X,\beta) = \exp(\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \beta_4 X_4).$$

State the estimated regression coefficients, their estimated standard deviations, and the estimated response function.

- (b) Obtain the model deviance and test the goodness of fit of the Poisson regression model at level $\alpha=0.05$. State the alternatives, decision rule, and conclusion.
- (c) Assuming that the fitted model is appropriate, use the relevant partial deviance to test whether gender (X_2) can be dropped from the model; control α at level 0.05. State the alternatives, decision rule and conclusion.