

# Strategic Concealment in Innovation Races

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- Innovations often build on existing knowledge.
- Access to knowledge is crucial in determining the direction of firms' innovation efforts.
- **General question:** How is knowledge acquired and disseminated in innovation races?

# Introduction

- Race paths are seldom unique.
  - COVID-19 Vaccine: mRNA or viral vector technologies.
  - Self-driving vehicles: LIDAR or radar technologies.
- Competitors must decide how to allocate resources (e.g. time, money) across the different paths.
- **Q1:** How do firms' decisions hinge on their competitors' choices and progress?

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  - Trade secrets.
  - Proprietary technology.
- This lack of access might introduce inefficiencies:
  - Duplication costs.
  - Suboptimal technology.
- **Q2:** What institutional arrangements drive firms to disclose and share their breakthroughs, and what is the effect on the overall pace of innovation?

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# What we do

- We study a model of innovation race in which
  - Multiple technologies can be used to win the race.
  - Using some technologies requires obtaining them first. (**firm-specific**).
  - Firms flexibly choose between
    - racing with already available technology.
    - try to obtain a better technology.
- We analyze the strategic behavior of firms in different information environments.
  - technological access is public or private information.
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- **Innovation Races:** Loury ('79); Lee, Wilde ('80);
  - **Patent vs. Secrecy:** Horstmann et al. ('85); Denicolo, Franzoni ('04); Anton, Yao ('04); Kultti et al. ('07); Zhang ('12); Kwon ('12)
  - **Multiple avenues to innovate:** Akcigit, Liu ('16); Brian, Lemus ('17); Das, Klein ('20); Hopenhayn, Squintani ('21)
  - **Multiple-stage innovation:** Scotchmer, Green ('90); Denicolo ('00)
- **Hail-Mary Attempts:** Carnehl, Schneider ('22); Kim ('22)

## Preview of results

- Without patents, firms do not disclose or share their technology. This entails inefficiencies that slow down innovation.
- When technology access is public information, patents are effective in inducing faster innovation.
  - Patents facilitate licensing, and firms are willing to share technologies with rivals for an adequate license fee.
- When technology access is private information, patents might be ineffective.
  - When stakes are sufficiently high, firms don't apply for patents to conceal their technology access.
  - True even when the patent holder has all the bargaining power in potential licensing negotiations.
  - Higher stakes might reduce the speed of innovation.

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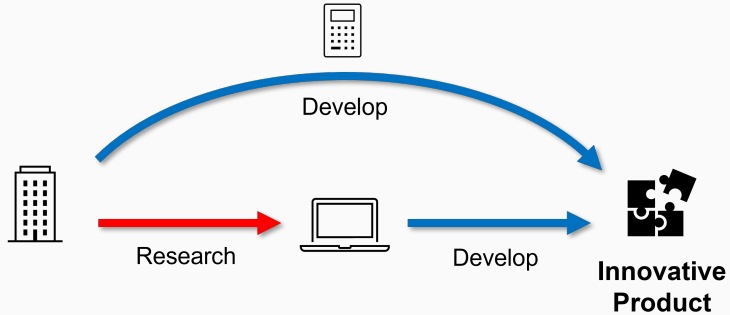
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# Preview of Framework



1. Model

2. Benchmark: Constant Development Rate

3. Public Information Setting

4. Private Information Setting

5. Patents and Licensing

## Model: Preliminaries

- Two risk-neutral firms  $i \in \{A, B\}$  race to develop an innovative product.
- Continuous and infinite time  $t \in [0, \infty)$
- Two technologies to develop the product:
  - An **old** technology  $L$
  - A **new** technology  $H$  (*not accessible at the beginning*)
- At  $t$ , each firm (w/o new technology) privately allocates a unit of resources to:
  - **Research**: trying to obtain the new technology.
  - **Development**: trying to win the race with the currently available technology.
- **Research progress** of a firm indicates whether they obtained the new technology.

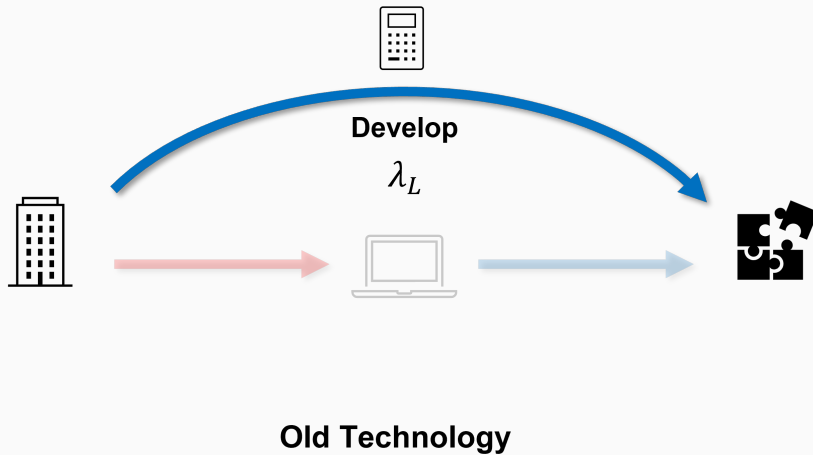
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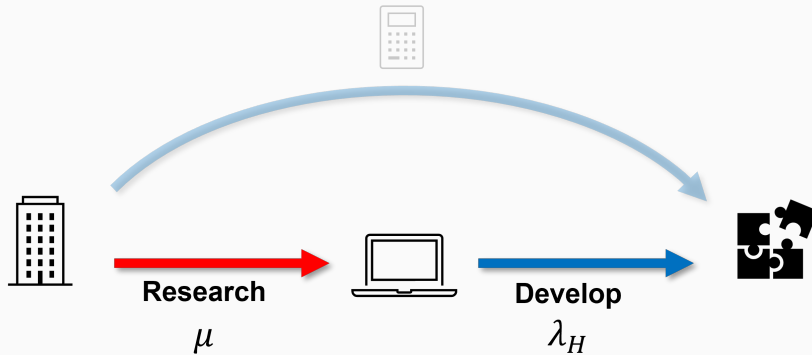
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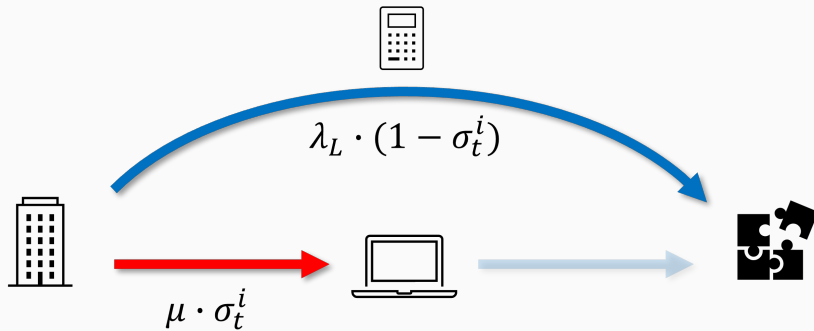
## Model: Technology Illustrations



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**Partial Allocation**



## Model: Payoffs

- The race ends when either firm develops the innovative product.
  - Winner obtains lump-sum prize  $\Pi$ .
  - Both firms pay a flow cost  $c$  throughout the race.
- Thus, the final payoff of Firm  $i$  is:

$$\mathbb{1}_{\{i \text{ is the winner}\}} \cdot \Pi - c \cdot T$$

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## Model: Parametric Assumptions

1. **A1:** The new technology path ( $R + D$ ) is (in expectation) faster than the old technology path:

$$\frac{1}{\lambda_L} > \frac{1}{\mu} + \frac{1}{\lambda_H}$$

2. **A2:** Developing with the old technology is profitable:

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## Model: Information

- Resource allocation is private information.
- Development of the innovative product is publicly observed.
- What about **research progress** of firms?
  - First part of the paper: we analyze **public** and **private**.
  - Second part of the paper: we extend the model to allow for voluntary disclosure through **patents**.

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## Benchmark: Constant Development Rate

- Suppose that the rival develops the innovative product at a constant rate  $\lambda$ .
  - Which path is optimal?

### Lemma

Suppose the rival's develops at a constant rate  $\lambda$ . There is a threshold  $\lambda_*$  such that

- (a) if  $\lambda < \lambda_*$ , it optimal to conduct research;
- (b) if  $\lambda > \lambda_*$ , it is optimal to develop with the old technology.

Moreover,

$$\lambda_* = \mu \cdot \lambda_H \left( \frac{1}{\lambda_L} - \frac{1}{\mu} - \frac{1}{\lambda_H} \right) > 0.$$

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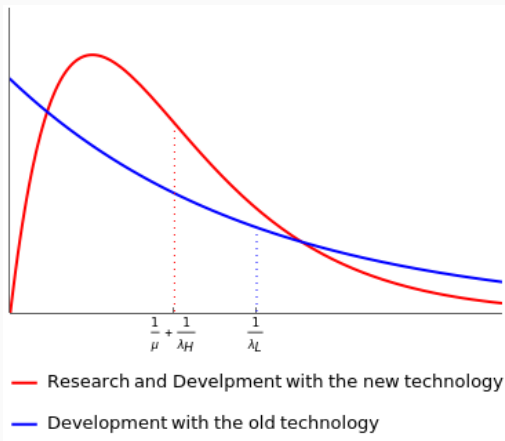
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# Development Times



PDF of the innovation time without race

## Long Run:

- By comparing the expected innovation time:

Research  $\succ$  Development

## Short Run:

- By comparing the prob. of innovation in the near future:

Research  $\prec$  Development

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- **Public information setting:** research progress of both firms is public information.
- **Strategy:** resource allocations contingent on entire history.
- **Markov strategy**
  - State variable: research progress of firms.
- **Observation:** A firm with the new technology conducts zero research.
  - It's only relevant to characterize what do firms do when they don't have the new technology.



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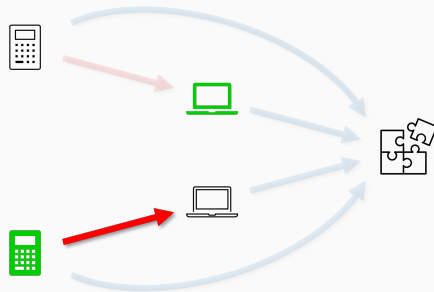
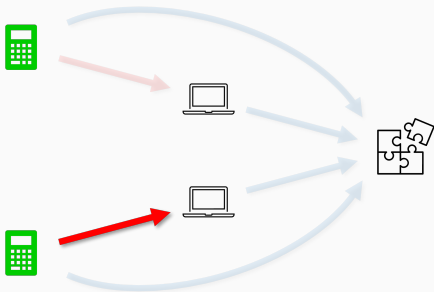
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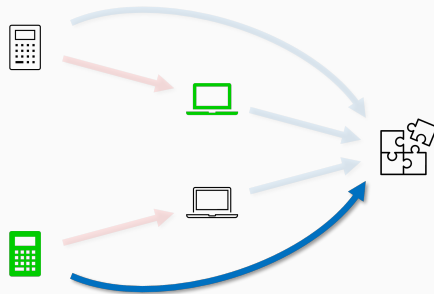
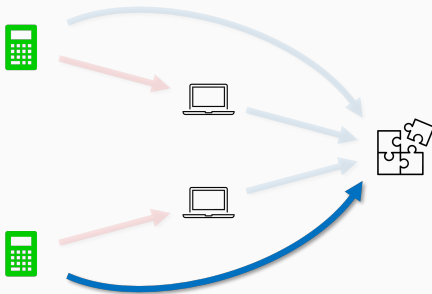
# Benchmark Strategy 1: Research Strategy

**Research Strategy:** Do research regardless of the rival's technology.



## Benchmark Strategy 2: Direct-Development Strategy

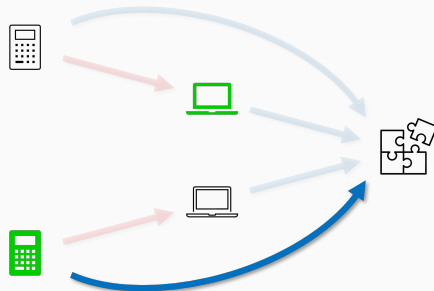
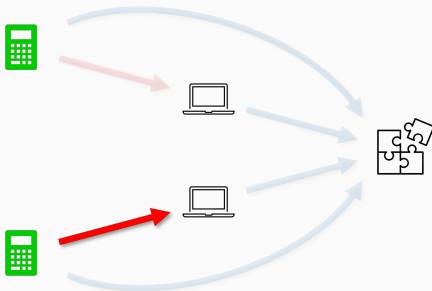
**Direct-Development Strategy:** Develop with old technology regardless of the rival's progress.



# Benchmark Strategy 3: Fall-Back Strategy

## Fall-Back Strategy

1. Do research if the rival does not possess the new technology;
2. Switch to developing with the old technology once the rival obtains the new tech.



### Theorem 1

Suppose that research progress is public information. The *unique* Markov perfect equilibrium is characterized as follows:

1. If  $\lambda_\star > \lambda_H$ , both firms play the research strategy;
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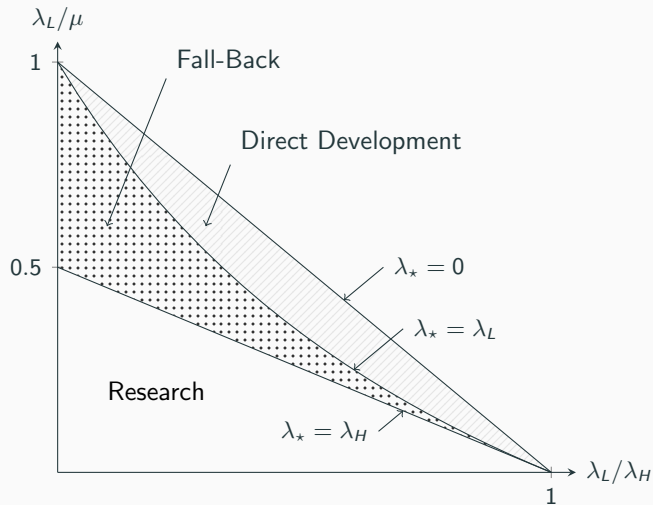
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- **Remark:** symmetry is obtained as a result.
- **Immediate part:**
  - $\lambda_\star < \lambda_H$  implies that firms develop with the old technology when opponent has the new one.
  - If  $\lambda_\star < \lambda_L$  there is an equilibrium in which both firms develop with the old technology.
- **Not-so-immediate part:**
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## Public Information: MPE Characterization



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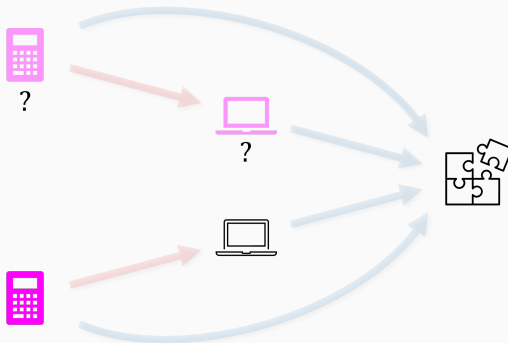
3. Public Information Setting

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# Private Information: Strategies

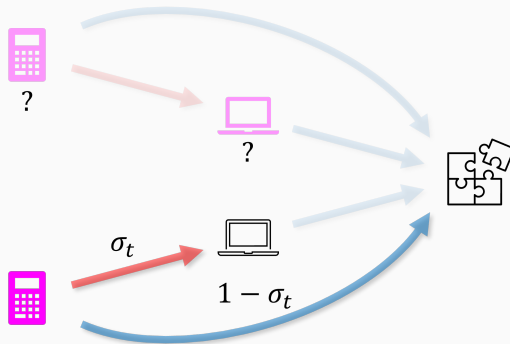
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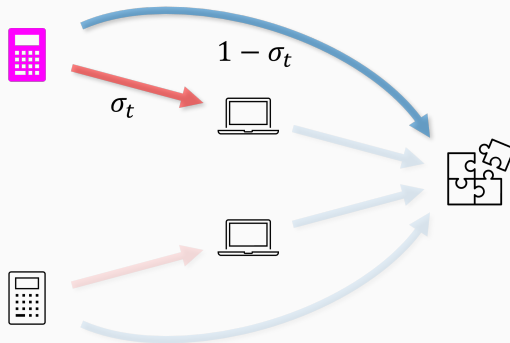


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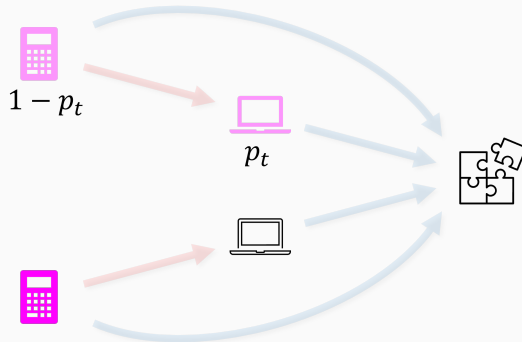
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## Private Information: Evolution of Beliefs

- $p_t$  : probability that a firm has the new technology at time  $t$  given no success in product development.

### Lemma: Evolution of Beliefs

Given allocation policy  $\sigma$ ,  $p_t$  is characterized by the initial condition  $p_0 = 0$  and

$$\dot{p}_t = \underbrace{\mu \cdot \sigma_t \cdot (1 - p_t)}_{\text{DE}} - \underbrace{[\lambda_H - (1 - \sigma_t)\lambda_L] \cdot p_t \cdot (1 - p_t)}_{\text{SRE}}.$$

- **Duration Effect (DE):** As more resources are allocated to research, it is more likely that the firm has the new technology.
- **Still-in-the-Race Effect (SRE):** Lack of success in product development indicates that it is less likely that the firm has the new technology.

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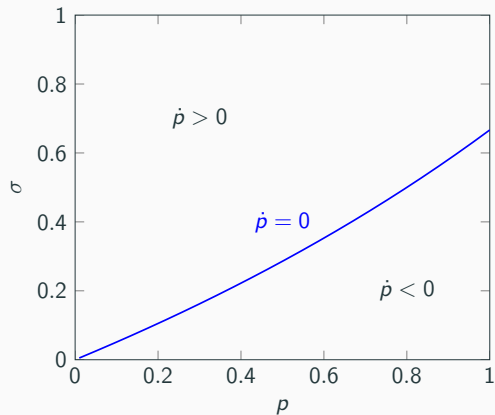
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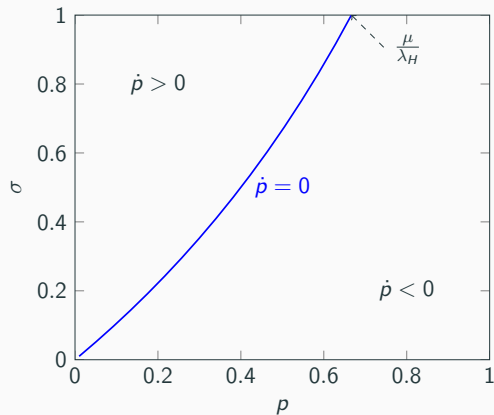
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## Private Information: Evolution of Beliefs



(a)  $\mu > \lambda_H$



(b)  $\mu < \lambda_H$

## Private Information: Equilibrium Concept

- $p_t^\sigma$ : prob. that a firm has the new tech. by time  $t$  when it employs  $\sigma$ .
- $h_t^\sigma$ : the associated development rate

$$h_t^\sigma = p_t^\sigma \cdot \lambda_H + (1 - p_t^\sigma) \cdot (1 - \sigma_t) \cdot \lambda_L$$

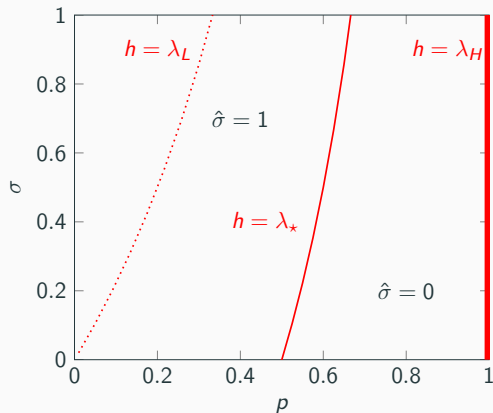
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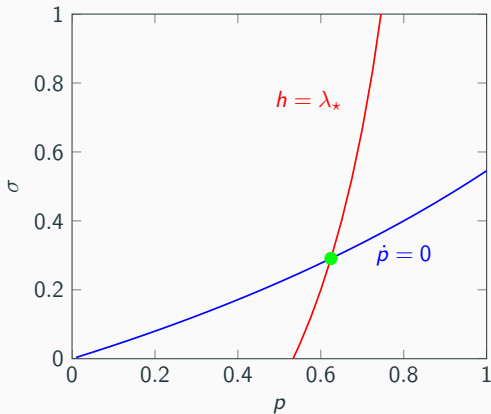
## Private Information: Iso-development-rate Curve and Best Responses



Iso-development curve and the best response when  $\lambda_* \in (\lambda_L, \lambda_H)$

$\hat{\sigma}$  is the best response for  $h$  constant.

## Private Information: Steady State

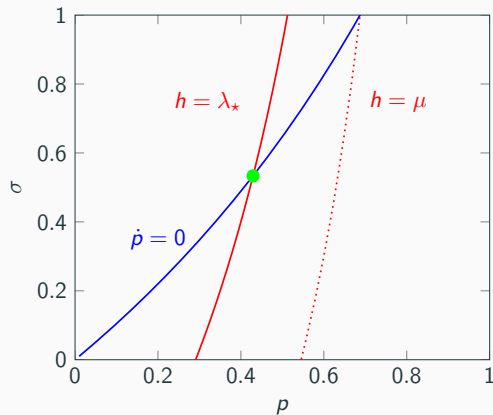


$$\mu > \lambda_H \text{ and } \lambda_H > \lambda_* > \lambda_L$$

A pair  $(p_*, \sigma_*)$  a *steady state* if  $\dot{p} = 0$  and  $h = \lambda_*$

**Lemma:** the steady state exists iff  $\lambda_* \in (\lambda_L, \min\{\mu, \lambda_H\})$ . Moreover, it is unique when it exists.

## Private Information: Steady State

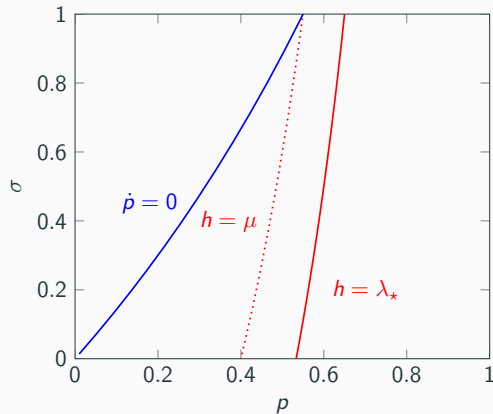


$$\lambda_H > \mu \text{ and } \mu > \lambda_* > \lambda_L$$

A pair  $(p_*, \sigma_*)$  a *steady state* if  $\dot{p} = 0$  and  $h = \lambda_*$

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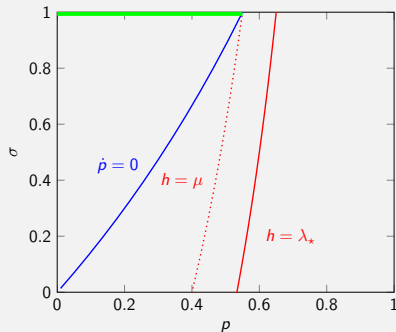
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## Theorem 2

When firms' research progress is private information, these are equilibria:

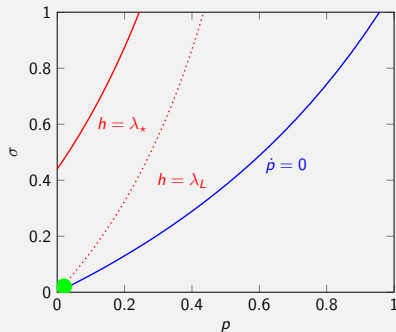


- (i) if  $\lambda_\star > \min\{\lambda_H, \mu\}$ ,  
the research equilibrium ( $\forall t, \sigma_t = 1$ );
- (ii) if  $\lambda_\star < \lambda_L$   
the direct-dev. equilibrium ( $\forall t, \sigma_t = 0$ );
- (iii) if  $\lambda_\star \in (\lambda_L, \min\{\lambda_H, \mu\})$ ,  
the stationary fall-back equilibrium  
( $\exists T$  s.th.  $\sigma_t = 1 \forall t < T$  &  $\sigma_t = \sigma_\star \forall t > T$ )

# Private Information: Nash Equilibrium with Monotone Development Rate

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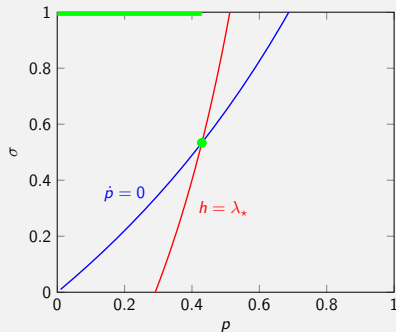


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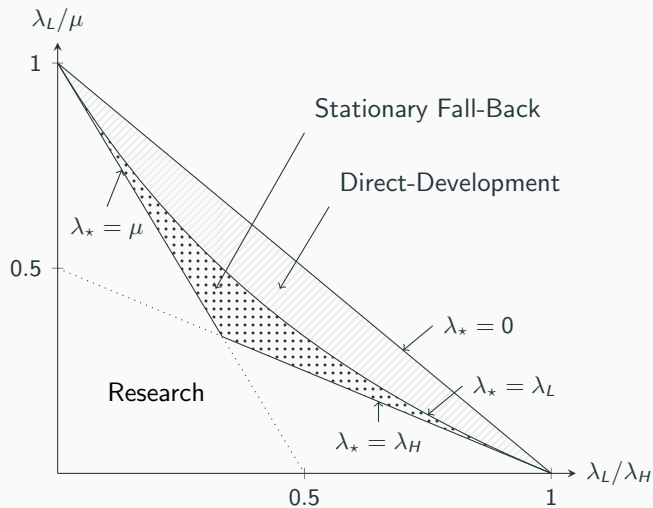


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- The equilibrium described in the previous theorem is the unique equilibrium:
  - with monotone development rates.
  - symmetric with monotone probabilities  $p$ .



## Private Information: Nash Equilibrium with Monotone Development Rate



1. Model

2. Benchmark: Constant Development Rate

3. Public Information Setting

4. Private Information Setting

5. Patents and Licensing

- We extend the model by allowing firms to patent & licensing of the new technology.
- Once a firm discovers the new technology, it can either
  1. apply for a patent (details will follow); or
  2. not apply for a patent.
- Patent applications are public information and granted:
  - With probability 1 if rival doesn't have the technology.
  - with probability  $\alpha \in [0, 1]$  if rival has new the technology.
- Patent gives the exclusive right to use the new technology and the right to license (TIOLI).

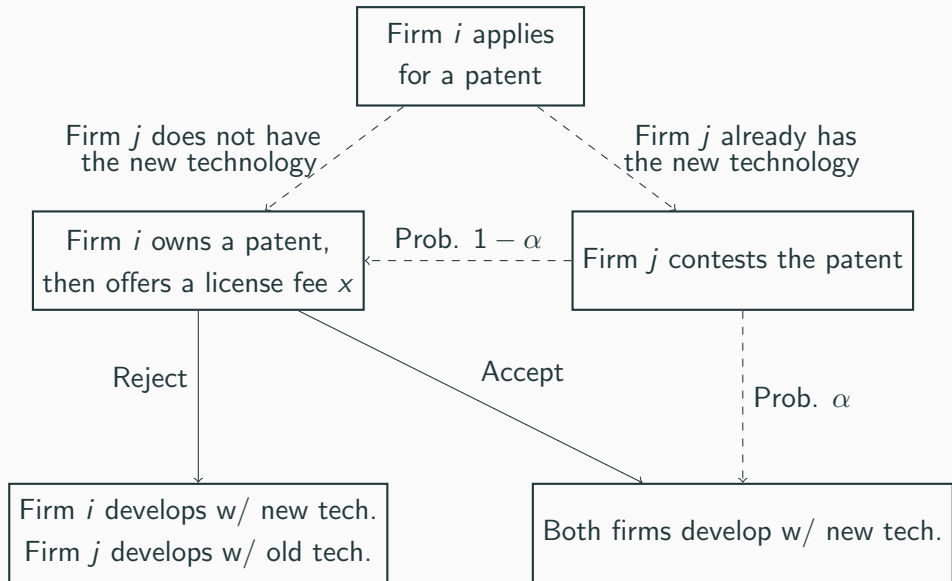
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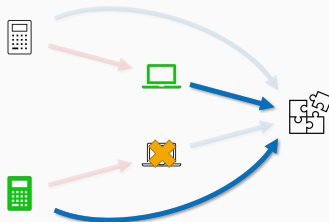
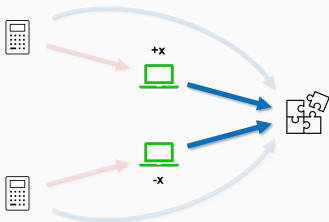


# Patents and Licensing: Optimal License Fee

## Proposition

Suppose that a firm has obtained the patent for the new technology. Then, the firm offers the following license fee to the rival:

$$x^* \equiv \frac{\lambda_H - \lambda_L}{\lambda_H + \lambda_L} \cdot \frac{\lambda_H \Pi + c}{2\lambda_H}$$





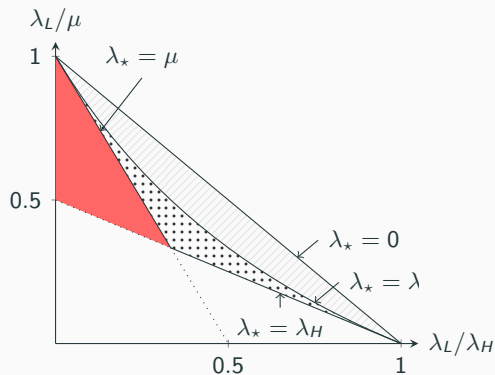
## Observation

- $V_C = \frac{\lambda_H \Pi - c}{2\lambda_H}$ : each firm's expected payoff when they race with the new tech.
- $\frac{x^*}{V_C} = \frac{\lambda_H - \lambda_L}{\lambda_H + \lambda_L} \cdot \frac{\lambda_H \Pi + c}{\lambda_H \Pi - c}$  is decreasing in  $\Pi$
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# Patents and Licensing: Equilibrium



- Focus on  $\lambda_H > \lambda_\star > \mu$
- Public info: fall-back strategy
- Private info: research strategy

- **Efficient Patent Equilibrium:** firms conduct research and apply for patents once they discover the new tech.
- **Concealment Equilibrium:** firms conduct research and do not apply for patents at all.

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## Proposition

The **efficient patent equilibrium** exists if

$$\frac{x^*}{V_C} > \frac{\lambda_H}{\lambda_H + \mu(2 - \alpha)} \quad (1)$$

## Necessary and sufficient conditions

- (i) if  $\alpha \leq \frac{2\lambda_*}{\lambda_H + \lambda_*}$ , (1) holds
- (ii) if  $\alpha > \frac{2\lambda_*}{\lambda_H + \lambda_*}$ , there exists  $\hat{\Pi}(\alpha)$  such that (1) holds iff  $\Pi < \hat{\Pi}(\alpha)$

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## Proposition

The **concealment equilibrium** exists if

$$\frac{x^*}{V_C} < \frac{\lambda_H(\lambda_H - \mu)}{(\lambda_H + \mu)(\lambda_H - \alpha\mu)} < \frac{\lambda_H}{\lambda_H + \mu(2 - \alpha)}. \quad (2)$$

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There exists  $\tilde{\Pi}(\alpha) > \hat{\Pi}(\alpha)$  such that (2) holds iff  $\alpha > \frac{2\lambda_*}{\lambda_H + \lambda_*}$  and  $\Pi > \tilde{\Pi}(\alpha)$ .

# Patent and Licensing: Concealment Equilibrium

## Proposition

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# Patents and Licensing: Takeaways

- Firms' patenting decisions crucially depend on the reward of winning the race ( $\Pi$ ) and the trade secret protection level ( $\alpha$ )
  - When  $\alpha$  is low or  $\Pi$  is *small*, the new technology is patented and licensed (Outcome is equivalent to the **First-Best** case)
  - When  $\alpha$  is high and  $\Pi$  is *high*, firms conceal their discoveries (Outcome is equivalent to the **Private Information** case)
- **Implications**
  - The first-best outcome can be achieved by lowering either  $\Pi$  or  $\alpha$  (e.g., imposing tax in the innovative product market; shifting the patent right from 'first-to-invent' to 'first-to-file')
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# Conclusion

- We study firms' strategic incentives to conceal their interim breakthroughs.
  - We introduce an innovation race model with multiple paths.
  - We characterize the equilibrium behaviors of firms when their research progress is public and private information.
  - We study firms' patenting behavior: Under a strong trade secret protection, Prize of winning the race  $\uparrow \Rightarrow$  Incentives to conceal  $\uparrow \Rightarrow$  Slower innovation.

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**Thank you!**