Efunctions.R

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```
### functions
update.tree <- function(tree,t_spe,t_ext){</pre>
 wt = tree$wt
 E = tree E
 ct = sum(wt)
 if(t_ext > ct){
   stop('Extinction beyond present!')
  if(t_ext < t_spe){</pre>
    stop('Speciation after extinction!')
  # speciation
 K = length(wt)
 k = length(wt[cumsum(wt) < t_spe])</pre>
  if((k+1)<K){
   lastbit = E[(k+1):(K-1)]
 }
  else{
   lastbit = NULL
 E = c(E[0:k],1,lastbit)
  # (this can be witten in one line, is convinent?)
  if(k==0){
    wt = c(t_spe, wt[1]-t_spe, wt[2:K])
  if(k > 0 & k < (K-1)){
    wt = c(wt[1:k], t_spe - sum(wt[1:k]), wt[k+1]-(t_spe - sum(wt[1:k])), wt[(k+2):K])
  if(k == (K-1)){
    wt = c(wt[1:(K-1)],t_spe-sum(wt[1:(K-1)]),ct-t_spe)
 }
  #extinction
 K = length(wt)
 k = length(wt[cumsum(wt) < t_ext])</pre>
  if((k+1)<K){
    lastbit = E[(k+1):(K-1)]
 else{
   lastbit = NULL
 E = c(E[0:k], 0, lastbit)
  # (this can be witten in one line, is convinent?)
  if(k==0){
    wt = c(t_ext, wt[1]-t_ext, wt[2:K])
 if(k > 0 & k < (K-1)){
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wt = c(wt[1:k], t_ext - sum(wt[1:k]), wt[k+1] - (t_ext - sum(wt[1:k])), wt[(k+2):K])
 }
  if(k == (K-1)){
   wt = c(wt[1:(K-1)], t_ext-sum(wt[1:(K-1)]), ct-t_ext)
 tree = list(wt=wt,E=E)
 return(tree)
sampprob <- function(t,s,mu,r){ ## equation (*)</pre>
 term1 = s*(1-exp(-mu*(r-t)))
  c = \exp(-(s/mu)*\exp(-mu*r))
 if(c==0){
   term2 = 0
  }else{
   term2 = c^{-exp(mu*t)+1}
 f = term1*exp(-s*t)*term2
 return(f)
}
# simulation of missing part [NEED TO CLEAN AND SIMPLIFY]
sim.extinct <- function(tree,pars,model='dd',seed=0, adjustment=FALSE){</pre>
  if(seed>0) set.seed(seed)
 wt = tree$wt
  ct = sum(wt)
 tree$E = rep(1,(length(wt)-1))
 lambda0=pars[1]
 mu0=pars[2]
 K=pars[3]
  limit = lambda0*K/(lambda0-mu0)
  rs = dim = length(wt)
  if (limit < (dim-1)){
   print('parameters do not make sense, observed tree implies negative rates')
  ms = NULL # missing species, for now we just add time. When we consider topology we do it with specie
  e.lims = NULL # limits on extinctions
  cbt = 0
  N = 2
  nm= 0 # number of missing species
  rprob = NULL # true probability of Missing/observed
  sprob = NULL # sampling probability of Missing/observed
  et = NULL # event type
 h = 1 # index to fill probabilities
  dif1 = vector(mode = 'numeric',length = dim)
  dif2 = vector(mode = 'numeric', length = dim)
 for(i in 1:dim){
   rs = rs-1 # this are the remaning speciations
   cwt = wt[i]
   cbt = sum(wt[0:(i-1)])
   key = 0
   last='nothing'
   while(key == 0){
      if(model == "dd"){ # diversity-dependence model
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lambda = \max(0, lambda0 - (lambda0-mu0)*N/K)
  mu = mu0
 lambda = rep(lambda, N)
if(model == 'cr'){ # constant-rate model
  lambda = rep(lambda0,N)
 mu = rep(mu0,N)
s = sum(lambda)
if (s == 0){
 t.spe = Inf
}
else{
  t.spe = rexp(1,s)
if (nm > 0) { # if there are missing species simulate extinction times
  t.ext = vector(mode = 'numeric',length = nm)
 for(j in 1:nm){
    t.ext[j] = truncdist::rtrunc(1,'exp',a=0,b=(e.lims[j]-cbt),rate=mu)
 extinctedone = which(t.ext == min(t.ext))
 t.ext = min(t.ext)
else{
 t.ext = Inf
if(t.ext ==Inf & t.spe == Inf){
 print('try another K!')
mint = min(t.spe, t.ext)
if(nm > 0){
 probs = vector(mode = 'numeric',length = nm)
 for(j in 1:nm){
    probs[j] = 1-truncdist::ptrunc(mint,'exp',a=0,b=(e.lims[j]-cbt),rate=mu)
 }
else\{probs = 1\}
if(mint < cwt){</pre>
  if(mint == t.spe & mint != t.ext){#speciation
    acep = runif(1)
    thre = pexp(ct-cbt,mu)
    if(acep < thre){</pre>
      ms = c(ms, cbt+t.spe)
      rprob[h] = dexp(x = t.spe, rate = (s+nm*mu))*(s/(s+nm*mu))
      sp = sampprob(t = mint,s = s,mu = mu,r = ct-cbt) #/integrate(sampprob,lower = 0, upper = ct-
      sprob[h] = prod(probs)*sp
      et[h] = 'speciation'
      h = h + 1
      nm = nm + 1 # number of missing species
      if((N + rs-1) < limit){
        e.lims = c(e.lims,ct)
      else{
```

```
e.lims = c(e.lims,sum(wt[1:(dim - (N+rs-floor(limit)-1))])) # cual es la interpretacion d
          }
          N = N+1
          #print(paste('at branching time',cbt+t.spe,'a missing species arises, resulting on',N,'curr
          last = 'speciation'
        else{last = 'nothing'}
        cwt = cwt - t.spe
        cbt = cbt + t.spe
      else{#extinction
       pickone = sample(1:nm,1)
        t spe = ms[pickone]
        t_{ext} = cbt + t.ext
        tree = update.tree(tree,t_spe=t_spe,t_ext=t_ext)
        rprob[h] = dexp(x = mint, rate = (s+nm*mu))*(mu/(s+nm*mu))
        et[h] = 'extinction'
        probs = probs[-extinctedone]
        sprob[h] = prod(probs)*truncdist::dtrunc(mint, 'exp', a=0, b=(e.lims[extinctedone]-cbt), rate=mu)
       ms = ms[-pickone]
        cwt = cwt - t.ext
        cbt = cbt + t.ext
       N = N-1
       h = h+1
        nm = nm - 1
       e.lims = e.lims[-extinctedone]
       last = 'extinction'
     }
    else{
      rprob[h] = pexp(q = cwt, rate = (s+nm*mu0),lower.tail = FALSE)
      et[h] = 'nothing'
      sprob[h] = prod(probs)*(1 - integrate(Vectorize(sampprob),lower = 0, upper = cwt,s=s,mu=mu,r=ct
     h = h+1
      dif1[i] = cwt/wt[i]
      dif2[i] = (mint - cwt)/wt[i]
      if(adjustment & cwt<(mint - cwt) & last=='speciation') { #Adjusting last speciation
        ms = ms[-length(ms)]
        e.lims = e.lims[-length(e.lims)]
       nm = nm - 1
        N = N-1
   }
 }
 N = N + 1
tree$rprob = rprob
tree$sprob = sprob
tree$et = et
tree$weight = prod(rprob)/prod(sprob)
logweight = log(rprob)-log(sprob)
tree$logweight = sum(logweight)
```

```
E = tree E
  n = c(2,2+cumsum(E)+cumsum(E-1))
  tree n = n
  return(tree)
#negative logLikelihood of a tree
nllik.tree = function(pars,tree){
  b = c(pars[1],(pars[1]-pars[2])/pars[3],pars[2])
  ldt = tree$wt[length(tree$wt)]
  dt = tree$wt[1:(length(tree$wt)-1)]
  E = tree E
  if(is.null(tree$n)){
    n = c(2,2+cumsum(E)+cumsum(E-1))
    tree n = n
  lastn = tree$n[length(tree$n)]
  n = tree$n[1:(length(tree$n)-1)]
  sigma = n*(b[1]-b[2]*n + b[3]) #n-dimentional
  lastsigma = lastn*(b[1]-b[2]*lastn + b[3])
  rho = pmax(b[1]*E-b[2]*n*E+b[3]*(1-E),0)
  1 = -(sum(-sigma*dt+log(rho))-lastsigma*ldt)
  if(min(b)<0)\{1 = Inf\}
  return(1)
}
# negative logLikelihood of a set of trees
nllik.st = function(pars, st){
  m = length(st$rec)
  1 = vector(mode = 'numeric',length = m)
  w = vector(mode = 'numeric',length = m)
  for(i in 1:m){
    s = st rec[[i]]
    w[i] = st$w[i]
    1[i] = nllik.tree(pars,tree=s)
  \#L = sum(l*w)/m
  w = w/sum(w)
  L = sum(1*w)
  return(L)
}
# relative likelihood
rel.llik <- function(S1,p0,p1){</pre>
  m = length(S1)
  f1 = vector(mode='numeric',length = m)
  f2 = vector(mode='numeric',length = m)
  d = vector(mode='numeric',length = m)
  for(i in 1:m){
    s = S1[[i]]
    f1[i] = nllik.tree(pars=p1,tree=s)
    f2[i] = nllik.tree(pars=p0,tree=s)
    d[i] = length(s$tree$wt)
    if(is.na(f1[i])) print(s)
  Delta = -log(sum(f1/f2)/m)
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return(Delta)
}
# MLE for a set of trees
mle.st <- function(S,init_par = c(0.5,0.5,100)){
  po = subplex(par = init_par, fn = nllik.st, st=S,hessian = TRUE)
  return(po)
# Monte-Carlo sampling / simulation of a set of complete trees
sim.sct <- function(tree,pars,m=10,printHistD=F,parallel=FALSE){</pre>
  if(parallel){
    no_cores <- detectCores()- 1</pre>
    cl <- makeCluster(no_cores)</pre>
    registerDoParallel(cl)
    trees <- foreach(i = 1:m, combine = list) %dopar% {</pre>
      ct = emphasis::sim.extinct(tree = tree,pars = pars) # complete tree
      lw = ct$logweight
      return(list(wt=ct$wt,E=ct$E,logweight=ct$logweight,lw=lw,n=ct$n))
    }
    lw = sapply(trees,function(list) list$lw)
    dim = sapply(trees,function(list) length(list$wt))
    stopCluster(cl)
    lw = lw - max(lw)
    w = exp(lw)
    Rec = trees #esta hay que sacarla
  else{
    Rec = vector(mode = 'list',length = m)
    d = vector(mode='numeric',length = m)
    lw = vector(mode='numeric',length = m)
    rp = vector(mode='numeric',length = m)
    sp = vector(mode='numeric',length = m)
    for(j in 1:m){
      rec = sim.extinct(tree = tree,pars = pars)
      Rec[[j]] = rec
      d[j] = length(rec$wt)
      lw[j] = rec$logweight
      rp[j] = prod(rec$rprob)
      sp[j] = prod(rec$sprob)
    }
    lw = lw - max(lw)
    w = \exp(lw)
  return(list(rec = Rec, w=w,dim=dim))
# Pilot study
pilot.study <- function(tree,epsilon,m1=10,printprocess=FALSE,init_par=c(1.2,0.3,60),11=20,parallel = T
  # pilot study suggested by Chan et. al
  pars = init_par
  M = matrix(ncol = 3, nrow = 11)
  H = matrix(ncol = 3, nrow = 11)
  for(i in 1:11){
    S = sim.sct(tree,pars,m=m1,printHistD = TRUE,parallel = parallel)
    mle = mle.st(S = S)
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```
pars = mle$par
   H[i,] = try(diag(solve(mle$hessian))/m1)
   M[i,] = pars
   print(paste('Q:',mle$value,'pars:',pars[1],pars[2],pars[3]))
  }
  1 = 10
 PM = M[1:(11-10),]
 PH = H[1:(11-10),]
 M = M[(11-9):11,]
 H = H[(11-9):11,]
  Q = vector(mode="numeric",length = (11-10))
 MLE = list()
  for(i in 1:10){
   Delta = vector(mode="numeric",length = 1)
   Me = matrix(ncol = 3, nrow = 1)
   if(printprocess) print(paste('iteration',i))
   for(j in 1:1){
      S = sim.sct(tree,M[i,],m=m1,parallel = parallel)
      mle = mle.st(S = S)
      pars = mle$par
     Me[j,] = pars
     Delta[j] = rel.llik(S1 = S$rec,p0 = M[i,], p1 = pars)
   MLE[[i]] = Me
   mD = mean(Delta)
   Q[i] = sum((Delta-mD)^2)
  s2 = sum(Q)/((1-1)*(11-10+1))
 s1 = sqrt(s2)
 m = m1*s1/epsilon
 m = floor(m) + 1
 return(list(m=m,p=M[10,],s1=s1,M=M,H=H,MLE=MLE,PM=PM,PH=PH))
}
#MCEM
mcem.tree <- function(tree,p,parallel=TRUE){</pre>
 m = p m
 s1 = p$s1
 sig = 100*s1/m
 tol = 2*sig*sqrt(1/5)
 D = Inf
 k = 1
 print("initializing mcem")
 pars = p$p
 PARS = pars
 H = c(NULL, NULL, NULL)
 Me = p$M
  while(abs(D)>tol){
   S = sim.sct(tree,pars,m = m,parallel = parallel)
   M = mle.st(S = S)
   mle = M$par
   h1 = try(diag(solve(M$hessian))/m)
   if(is.numeric(h1)) H = rbind(H,h1)
   D = rel.llik(S1 = S$rec,p0 = pars,p1 = mle)
```

```
PARS = rbind(PARS,mle)
   pars = mle
   print(paste("iteration",k,"Q: ",M$value, " lambda: ", pars[1]," mu: ", pars[2], "K:", pars[3]))
 PARS = data.frame(it=1:(dim(Me)[1]+dim(PARS)[1]),lambda = c(Me[,1],PARS[,1]),mu=c(Me[,2],PARS[,2]),K=
 return(list(pars=pars,PARS=PARS,H=H))
#############################
### Phylogenetic tree simulation
sim.tree <- function(ct=15, lambda0=0.8, mu0=0.1, K=40, model="dd", printEv=FALSE, seed=0){
  ## Set up
  if(seed>0){set.seed(seed)}
 key=0 # key to go out of the loop
  reboot2=0 # reboot in case that the tree is too small
  while(key==0){
   i = 1
   N = 2 # Starting number of species
   sigmas = NULL # vector with waiting times rates
   Tm = NULL # Waiting times
   E = NULL # vector with 0 if extinction and 1 if speciation
   n = NULL # vector with number of species at time t_i
   S = NULL # vector with species that went extinct/speciation # write this better
   sumt = 0 # time in simulation
   reboot = 0 # this is in case we want to check how many reboots the simulation had.
   newick = paste(sl[1],";",sep="") # Newick tree
   identf = data.frame(Spec="aa",Time=0) # Labels of species
   L = data.frame(spec='aa', spec_time=0, ext_time=-1, parent = '00') # is this working?
   while (sumt < ct){
      if(model == "dd"){  # diversity-dependence model
        lambda = \max(0, lambda0 - (lambda0-mu0)*N/K)
        mu = mu0
       lambda = rep(lambda, N)
       mu = rep(mu, N)
      if(model == 'cr'){ # constant-rate model
       lambda = rep(lambda0,N)
       mu = rep(mu0,N)
      s = sum(lambda) + sum(mu)
      sigmas = c(sigmas,s)
      if (s == 0)\{break\}
     tm = rexp(1,s) # waiting time of iteration i
      if(tm+sumt>ct){break}
      sumt = tm + sumt
      prob = c(lambda, mu)/s # Probability of extinctions and speciations
      BD = sample(2*N,1,prob=prob) # speciation/extinction & identification of the species.
     n[i] = N
      if(BD > N){
                    # Extinction
       E[i] = 0
        ## for newick output
        species = as.character(identf[BD-N,1])
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```
S[i] = species
      ind = regexpr(species,newick)[1] + 2
      atm = sumt-identf[which(identf[,1]==species),2]
      identf = identf[-(BD-N),]
      L[L$spec == species,]$ext_time = sumt #?
      newick = paste(substr(newick,1,ind),as.character(atm),substring(newick,ind+2),sep="")
     N = N-1
      if(printEv){print(paste("extinction in time", sumt, sep=" "))} # put it in a log file
    }else{ # Speciation
     E[i] = 1
      ## for newick output
      species = as.character(identf[BD,1])
     S[i] = species
      ind = regexpr(species,newick)[1]-1
      atm = sumt-identf[which(identf[,1]==species),2]
      newick = paste(substr(newick,1,ind),"(",substr(newick,ind+1,ind+4),",",",sl[i+1],"):",as.characte
      identf = rbind(identf,data.frame(Spec=substr(sl[i+1],1,2),Time=sumt))
      identf[identf$Spec == species,2] = sumt
      L = rbind(L,data.frame(spec=substr(sl[i+1],1,2), spec_time=sumt, ext_time=-1, parent=species))
     N = N+1
      if(printEv){print(paste("speciation in time", sumt, sep=" "))} # put it in a log file
    if (N==0){ # In case all species got extinct: restart
      reboot = reboot + 1
     N = 2 # Number of species
     i = 1
     Tm = NULL
      sumt = 0
     E = NULL # vector with 0 if extinction and 1 if speciation
      n = NULL # vector with number of species at time t_i
     newick = paste(sl[1],";",sep="") # Newick tree
      identf = data.frame(Spec="aa",Time=0)
      L = data.frame(spec='aa', spec_time=0, ext_time=-1, parent = '00')
    }else { # Otherwise, update values and go to next iteration
      Tm[i] = tm
      i < -i + 1
 }
  ####
  if(nchar(newick)<7){</pre>
   reboot2=reboot2+reboot+1
  }else{
   newick = compphyl(newi=newick,identf=identf,ct=ct) # set extant species to the present
   phy = read.tree(text=newick)
    dphy = drop.fossil(phy)
    if (Ntip(dphy)>2) { #check if the extant species tree is large enough
     key=1
   }else{
     reboot2=reboot2+reboot+1
 }
Tm[i] = ct-sum(Tm)
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```
n[i] = n[i-1] + E[i-1] - (1-E[i-1])
  newick.extant = drop.fossil(phy)
  newick.extant.p = phylo2vectors(newick.extant) # is it validated?
 reboot2 = reboot2 + reboot
  return(list(tree=list(wt=Tm, E=E, n=n, S=S, br = cumsum(Tm)), phylo = phy, tree.extant = newick.extan
extinction.processes <- function(u,inits,mu0){</pre>
 nm = length(u)
 t.ext = vector(mode='numeric',length=nm)
 if(nm > 0){
   for(i in 1:nm){
      t.ext[i] = inits[i] - log(1-u[i])/mu0 #Inverse of the intensity function for constant extinction
 }
 return(t.ext)
### simulation of extincted new version
sim.extinct2 <- function(brts,pars,model='dd',seed=0){</pre>
  if(seed>0) set.seed(seed)
  wt = -diff(c(brts, 0))
 ct = sum(wt)
 lambda0 = pars[1]
 mu0 = pars[2]
 K = pars[3]
 dim = length(wt)
 ms = NULL # missing speciations, for now we just add time. When we consider topology we do it with sp
 me = NULL # missing extinctions (in the uniform plane)
 bt = NULL
 to = NULL
  cbt = 0
 N = 2
  sprob = NULL # sampling probability of Missing/observed
  h = 1 # index to fill probabilities
  for(i in 1:dim){
    cwt = wt[i]
   cbt = sum(wt[0:(i-1)])
   key = 0
   gosttime = 0
    #last = 'nothing'
   while(key == 0){
      if(model == "dd"){  # diversity-dependence model
       lambda = max(1e-99, lambda0 - (lambda0-mu0)*N/K)
       mu = mu0
       s = N*lambda
      }else{print('Model not implemented yet, try dd')}
      t.spe = rexp(1,s)
      t.ext = extinction.processes(u=me,inits=ms,mu0=mu0)
      #sometimes parameters does not make sense. write a warning when that happens
      t_ext = ifelse(length(t.ext)>0,min(t.ext),Inf)-cbt # if is not empty gives the waiting time for
      mint = min(t.spe,t_ext)
      if(mint < cwt){</pre>
        if(mint == t.spe){#speciation
```

```
u = runif(1)
          if(u < pexp(ct-(cbt+t.spe),mu)){</pre>
            ms = c(ms, cbt+t.spe)
            me = c(me,u)
            bt = c(bt, cbt+t.spe)
            to = c(to,1)
            sprob[h] = sampprob(t = t.spe+gosttime, s = s, mu = mu, r = ct-(cbt-gosttime))
            h = h + 1
            N = N + 1
          }else{gosttime = t.spe + gosttime}
          cwt = cwt - t.spe
          cbt = cbt + t.spe
        else{#extinction
          extinctone = which(t.ext == min(t.ext))
          tspe = ms[extinctone]
          text = t.ext[extinctone]
          bt = c(bt, text)
          to = c(to,0)
          sprob[h] = truncdist::dtrunc(text-tspe,'exp',a=0,b=ct-tspe,rate=mu)*(1-integrate(sampprob,low
          ms = ms[-extinctone]
          me = me[-extinctone]
          cwt = cwt - mint
          cbt = cbt + mint
          N = N-1
         h = h+1
          gosttime = 0
       }
      else{
        sprob[h] = (1 - integrate(Vectorize(sampprob),lower = 0, upper = cwt+gosttime,s=s,mu=mu,r=ct-cb
       h = h+1
     }
   }
   N = N+1
  df = data.frame(bt = c(bt,15-brts),to = c(to,rep(2,length(wt))))
  df = df[order(df$bt),]
  n.tree = list(wt=c(diff(df$bt),ct-df$bt[length(df$bt)]),E=df$to[-length(df$to)])
  if(length(n.tree$E==1) != length(n.tree$E==0)) print('algo mal!!')
 n.tree$E[n.tree$E==2] = 1
 lrprob = -nllik.tree(pars,n.tree) #f
 lsprob = sum(log(sprob)) #g
  logweight = lrprob-lsprob
 n.tree$weight = exp(logweight)
 n.tree$logweight = logweight
 n.tree$f=lrprob
 n.tree$g=lsprob
 return(n.tree)
}
```

```
post.pro <-function(file,extrafile=NULL){</pre>
load(file)
#pars = DDD::dd_ML(brts = btdd, idparsopt = 1:3,soc=2,cond=0)
MLE = p$MLE
M = mcem$PARS
it = NULL
lambda = NULL
mu = NULL
K = NULL
for( i in 1:10){
 MM = MLE[[i]]
  it = c(it,rep(i+1,10))
 lambda = c(lambda,MM[,1])
 mu = c(mu, MM[,2])
 K = c(K, MM[,3])
};
col = rep('grey',length(lambda))
SD1 = rep(NaN,length(lambda))
SDm = rep(NaN,length(mu))
SDk = rep(NaN,length(K))
it = c(it, 1:dim(M)[1])
lambda = c(lambda, M[,2])
mu = c(mu, M[,3])
K = c(K,M[,4])
col = c(col,rep('blue',dim(M)[1]))
MCEMc = data.frame(it=it,lambda=lambda,mu=mu,K=K,col=col)
gamLambda = gam(lambda ~ s(it), data=MCEMc)
gamMu = gam(mu ~ s(it), data=MCEMc)
gamK = gam(K ~ s(it), data=MCEMc)
ex = dim(MCEMc)[1] - dim(mcem$H)[1] - 100
hessL = c(rep(NaN, ex), mcem$H[,1])
SD1 = c(SD1,sqrt(hessL+gamLambda$sig2))
hessM = c(rep(NaN, ex), mcem$H[,2])
SDm = c(SDm,sqrt(hessM+gamMu$sig2))
hessK = c(rep(NaN, ex), mcem$H[,3])
SDk = c(SDk,sqrt(hessK+gamK$sig2))
MCEMc\$SD1 = SD1
MCEMc\$SDm = SDm
MCEMc\$SDk = SDk
MCEM = rbind(MCEMc,data.frame(it=(-9:0),lambda=p$PM[,1],mu=p$PM[,2],K=p$PM[,3],col=rep('blue',10),SDl=r
gl=ggplot(MCEM) + geom_point(aes(it,lambda),colour=MCEM$col) + geom_errorbar(aes(x=it, y=lambda, ymin =
gm=ggplot(MCEM) + geom_point(aes(it,mu),colour=MCEM$col) + geom_errorbar(aes(x=it, y=mu, ymin = mu-1.96
gk=ggplot(MCEM) + geom_point(aes(it,K),colour=MCEM$col) + geom_errorbar(aes(x=it, y=K, ymin = K-1.96*SD
```

```
gLLmcem = ggplot(data=d)+geom_line(aes(x=it,y=llik))+geom_hline(yintercept = pars$loglik)
gLLmcem2 = ggplot(df, aes(lambda, mu))+ geom_contour(aes(z = llik,color=..level..),bins=100) +geom_poin
if(!is.null(extrafile)){
   load(extrafile)
   gLLmcem2 = gLLmcem2 + geom_point(data=mcem$PARS,aes(x=lambda,y=mu,size=it),col='red')
   gLLmcem = gLLmcem + geom_line(data=d,aes(x=it,y=llik),col='red')
}
return(list(gl=gl,gm=gm,gk=gk, gLLmcem=gLLmcem, gLLmcem3d=gLLmcem2))
}
```