

Graded Assignment I (part2)

1.

(a) Let θ be the parameter vector $\theta = (\theta_0 \theta_1 \dots \theta_n)^T$ and let the i -th data vector be: $x(i) = (x_0 \ x_1 \dots x_n)^T$ where $x_0 = 1$. What is the vectorial expression for the hypothesis function $h_{\theta}(x)$?

$$h = g(X\theta)$$

(b) What is the vectorized expression for the cost function: $J(\theta)$ (still using the explicit summation over all training examples)

$$J(\theta) = (1 / 2m) * (g(X\theta) - y^{\rightarrow})$$

(c) What is the vectorized expression for the gradient of the cost function, i.e. what is:

$$\partial J(\theta) / \partial \theta = (1 / m) * X^T (g(X\theta) - y^{\rightarrow})$$

Again the explicit summation over the data vectors from the learning set is allowed here.

(d) What is the vectorized expression for the θ update rule in the gradient descent procedure?

$$\theta = \theta - (1 / m) * X^T (g(X\theta) - y^{\rightarrow})$$

(e) (bonus points) Vectorization can be taken one step further. We can remove the explicit summation over the training samples by 'hiding' it in a matrix vector multiplication. Start by collecting all training samples in a data matrix X such that every row of X is a vector from the training set (with the augmented $x_0 = 1$ elements, i.e. the first column of X has elements equal to 1).

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2. Derive an equation that can be used to find the optimal value of the parameter θ_1 for univariate linear regression without doing gradient descent. This can be done by setting the value of the derivative equal to 0. You may assume that the value of θ_0 is fixed.

$$\partial J(\theta_1) / \partial \theta_1 = 0,$$

$$\theta_0 = \text{fixed (constant)}$$

??? //what am I taking the derivative of?