

0.1 Basic States

$$\begin{aligned}\Psi_1 &= -U_1 y & \Psi_2 &= -U_2 y \\ Q_1 &= (U_1 - U_2 + \beta)y & Q_2 &= (U_2 - U_1 + \beta)y\end{aligned}$$

0.2 New States and Perturbations

$$\begin{aligned}\psi_1 &= \Psi_1 + \psi'_1 & \psi_2 &= \Psi_2 + \psi'_2 \\ q'_1 &= \frac{1}{F_1} \nabla^2 \psi'_1 - (\psi'_1 - \psi'_2) & q'_2 &= \frac{1}{F_2} \nabla^2 \psi'_2 - (\psi'_2 - \psi'_1)\end{aligned}$$

0.3 QG Equations

$$\begin{aligned}0 &= \partial_t q'_1 + (u'_1 + U_1) \partial_x q'_1 + v'_1 \partial_y (q'_1 + Q_1) \\ 0 &= \partial_t q'_2 + (u'_2 + U_2) \partial_x q'_2 + v'_2 \partial_y (q'_2 + Q_2)\end{aligned}$$

0.4 Normal Modes

$$\begin{aligned}\hat{q}'_1 &= -\hat{\psi}'_1 \left(1 + \frac{K^2}{F_1}\right) + \hat{\psi}'_2 & \hat{q}'_2 &= \hat{\psi}'_1 - \hat{\psi}'_2 \left(1 + \frac{K^2}{F_2}\right) \\ \hat{\psi}'_1 &= \frac{\left(1 + \frac{K^2}{F_2}\right) \hat{q}'_1 + \hat{q}'_2}{1 - \left(1 + \frac{K^2}{F_1}\right) \left(1 + \frac{K^2}{F_2}\right)} & \hat{\psi}'_2 &= \frac{\hat{q}'_1 + \left(1 + \frac{K^2}{F_1}\right) \hat{q}'_2}{1 - \left(1 + \frac{K^2}{F_1}\right) \left(1 + \frac{K^2}{F_2}\right)} \\ \hat{u}'_1 &= -ik \hat{\psi}'_1 & \hat{u}'_2 &= -ik \hat{\psi}'_2 \\ \hat{u}'_1 &= -il \hat{\psi}'_1 & \hat{u}'_2 &= -il \hat{\psi}'_2 \\ K^2 &= k^2 + l^2\end{aligned}$$