$$\mathfrak{P}_n = \left\{ P \in \mathbb{R}^{n \times n} \text{ permutation matrix} \right\}$$