Solved selected problems of Lagrangian and Hamiltonian by Mann

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Solution. 1.1 Let us integrate the acceleration 2c to obtain the velocity $\dot{r}(t)$ as follows

$$\dot{r}(t) = \int 2c \ dt = 2ct + C$$

But at t = 0 we know that $\dot{r}(t) = b$ then C = b and hence

$$\dot{r}(t) = 2ct + b$$

Now, we integrate again to obtain the position r(t) as follows

$$r(t) = \int 2ct + b \ dt = ct^2 + bt + C$$

But at t = 0 we know that r(t) = a then C = a and hence

$$r(t) = ct^2 + bt + a$$