$$(u, \partial_t u) \in L^\infty(0, T; H^{1 + \frac{d}{4}} \times H^{\frac{d}{4}})$$