$$\dot{q} = -p - \frac{1}{N} \left(\mathbf{P}q - q \cdot \mathbf{P} \, \mathbf{1}_{N \times d} \right) + 2(v - \bar{v})$$