

## Problem H

# Duathlon

**Input:** standard input

**Output:** standard output

**Time Limit:** 15 seconds

A duathlon is a race that involves running  $r$  km and cycling  $k$  km.  $n$  contestants have entered the race; each contestant has different running and cycling speeds. One of the contestants has bribed the organizers to set  $r$  and  $k$  so that he can win by the maximum margin. You are to determine if this is possible and, if so, give  $r$  and  $k$ .

## Input

The input file contains several sets of input. The description of each set is given below:

The first line of each set contains an integer  $t$ , the total distance of the race, in km. That is,  $r + k = t$ . The next line contains an integer  $n$ , the number of competitors. For each contestant, a line follows with two real numbers giving the running and cycling speed for that contestant. The last line of input gives the running and cycling speed of the contestant who has bribed the organizers. You may assume  $t$  does not exceed 100 km/h and  $n$  does not exceed 20. Input is terminated by end of file. Two consecutive sets may or may not be separated by a blank line.

## Output

For each set of input produce one line of output. The output description for each set is given below:

If it is possible to fix the race as describe above, print a message giving  $r$  and  $k$ , and the amount by which the cheater will win the race, accurate to two decimal places as in the sample below. If it is not possible, print "The cheater cannot win." There is no blank line between outputs for two consecutive sets.

## Sample Input

```
100
3
10.0 40.0
20.0 30.0
15.0 35.0
```

```
100
3
10.0 40.0
20.0 30.0
15.0 25.0
```

## Sample Output

The cheater can win by 612 seconds with  $r = 14.29\text{km}$  and  $k = 85.71\text{km}$ .  
The cheater cannot win.

---

**(Regionals 2002 Warm-up Contest, Problem setter: Gordon V. Cormack)**