University of Technology Nuremberg Lecture: Introduction to Mobile Robotics Held at the Technical University of Munich Winter term 2022/23 Department of Engineering

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## Sheet 3

Topic: Bayes Rule

## Exercise 1: Bayes Rule

Suppose you are a witness to a nighttime hit-and-run accident involving a taxi in Athens. All taxi cars in Athens are blue or green. You swear under oath that the taxi was blue. Extensive testing shows that, under the dim lighting conditions, discrimination between blue and green is 75% reliable.

- (a) Given your statement as a witness and given that 9 out of 10 Athenian taxis are green, what is the probability of the taxi being blue?
- (b) Is there a significant change if 7 out of 10 Athenian taxis are green?
- (c) Suppose now that there is a second witness who swears that the taxi is green. Unfortunately he is color blind, so he has only a 50% chance of being right. How would this change the estimate from (b)?

## Exercise 2: Bayes Filter

A vacuum cleaning robot is equipped with a cleaning unit to clean the floor. Furthermore, the robot has a sensor to detect whether the floor is clean or dirty. Neither the cleaning unit nor the sensor are perfect.

From previous experience you know that the robot succeeds in cleaning a dirty floor with a probability of

$$p(x_{t+1} = \text{clean} \mid x_t = \text{dirty}, u_{t+1} = \text{vacuum-clean}) = 0.7,$$

where  $x_{t+1}$  is the state of the floor after having vacuum-cleaned,  $u_{t+1}$  is the control command, and  $x_t$  is the state of the floor before performing the action.

The probability that the sensor indicates that the floor is clean although it is dirty is given by  $p(z = \text{clean} \mid x = \text{dirty}) = 0.3$ , and the probability that the sensor correctly detects a clean floor is given by  $p(z = \text{clean} \mid x = \text{clean}) = 0.9$ .

Unfortunately, you have no knowledge about the current state of the floor. However, after cleaning the floor the sensor of the robot indicates that the floor is clean.

(a) Compute the probability that the floor is still dirty after the robot has vacuumcleaned it. Use an appropriate prior distribution and justify your choice.

(b) Which prior gives you a lower bound for that probability?					y?